Nuclear Engineering and Technology 54 (2022) 462-468

Contents lists available at ScienceDirect

### Nuclear Engineering and Technology

journal homepage: www.elsevier.com/locate/net



Original article

# Evaluation of peak-fitting software for magnesium quantification through $k_0$ -instrumental neutron activation analysis



IUCLEAR NGINEERING AND ECHNOLOGY

Kishore B. Dasari <sup>a</sup>, Hana Cho <sup>b</sup>, Radojko Jaćimović <sup>c</sup>, Byung-Gun Park <sup>a</sup>, Gwang-Min Sun <sup>a, \*</sup>

<sup>a</sup> HANARO Utilization Division, Korea Atomic Energy Research Institute, Daejeon, 34057, Republic of Korea

<sup>b</sup> Division of Chemical and Biological Metrology, Korea Research Institute of Standards and Science, Daejeon, 34113, Republic of Korea

<sup>c</sup> Department of Environmental Sciences, Jožef Stefan Institute, 1000, Ljubljana, Slovenia

### ARTICLE INFO

Article history: Received 10 March 2021 Received in revised form 30 June 2021 Accepted 13 July 2021 Available online 14 July 2021

Keywords: HyperLab HyperGam KayWin® Magnesium Peak deconvolution Peak-fitting programs

### ABSTRACT

The selection and effective utilization of peak-fitting software for conventional gamma-ray spectrum analysis is significant for accurate determination of the mass fraction of elements, particularly in complex peak regions. Majority of the peak-fitting programs can derive similar peak characteristics for singlet peaks, but very few programs can deconvolute multi-peaks in a complex region. The deconvolution of multi-peaks requires special peak-fitting functions, such as left and right-skew distributions. In the this study, 843.76 keV (<sup>27</sup>Mg) peak area from the complex region (840 keV–850 keV) determined and compared using four different peak-fitting programs, namely, GammaVision, Genie2000, HyperLab, and HyperGam. The 843.76 keV peak interfered with 841.63 keV (<sup>152m</sup>Eu) and 846.81 keV (<sup>56</sup>Mn). The total Mg concentration was determined through *k*<sub>0</sub>-instrumental neutron activation analysis by applying the isotopic interference correction factor <sup>27</sup>Al(n,p)<sup>27</sup>Mg through the simultaneous determination of Al concentration. HyperLab and HyperGam peak-fitting programs reported consistent peak areas, and resultant concentrations agreed with the certified values of matrix-certified reference materials.

© 2021 Korean Nuclear Society, Published by Elsevier Korea LLC. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).

### 1. Introduction

Magnesium (Mg) is an essential nutrient element in human and plant biological systems. It helps in maintaining normal human body functions, such as the muscular, nervous, and immune systems, along with healthy plant growth [1]. Mg deficiency is linked to numerous diseases in the human body, such as hypertension [2]. Thus, the characterization of Mg-rich diets and the total mass fraction of Mg in various biological and environmental samples is important. Among the dry and wet chemistry analytical techniques, non-destructive methods are preferred in the analysis of aerosol particles and biological samples to avoid chemical contamination during the rigorous process of sample preparation.

Neutron activation analysis (NAA) is an outstanding technique that is non-destructive, highly sensitivity, and has a lower detection limit. The comparator INAA method is a unique primary calibration method with dry chemical analysis [3]. Apart from the comparator

INAA method, the  $k_0$ -based single comparator INAA ( $k_0$ -INAA) method has considerable characteristics for the determination of mass fraction of elements in various matrix samples and reference material development [4-6]. The  $k_0$ -INAA method also competes with other primary ratio methods for inorganic trace element quantification [4]. However, some elements (Mg, Sm, and Sr) cannot be determined accurate mass faction because of issues such as short half-life of activation products, gamma-ray, and isotopic interferences [7]. In INAA, total Mg content is determined using  $^{26}Mg(n,\gamma)^{27}Mg$  (843.76 keV and 1014.44 keV) reaction that is interfered with by gamma-rays of 841.63 keV (152mEu) and 846.81 keV (<sup>56</sup>Mn) to 843.76 keV gamma-line, and nuclear reaction interference from <sup>27</sup>Al(n,p)<sup>27</sup>Mg. Most of the environmental and biological samples contain Mg and interference elements such as Mn, Eu, and Al with high concentration. The complete avoidance of possible spectral and isotopic interference in the INAA method is impossible. The  $k_0$ -INAA method is preferred over the comparator

\* Corresponding author. E-mail address: gmsun@kaeri.re.kr (G.-M. Sun).

https://doi.org/10.1016/j.net.2021.07.016

<sup>1738-5733/© 2021</sup> Korean Nuclear Society, Published by Elsevier Korea LLC. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/ licenses/by-nc-nd/4.0/).

INAA method for Mg quantification because the isotopic corrections can be calculated easily when both the analyte and interference elements are determined simultaneously [6].

Mg has three stable isotopes: Mg-24 (79%), Mg-25 (10%), and Mg-26 (11%).  $^{26}$ Mg has a (n, $\gamma$ ) cross-section ( $\sigma_0$ ) of 0.0364 b, and neutron-induced  $^{27}$ Mg has a short half-life of 9.46 m and emits three gamma-rays, 170.69 keV ( $\gamma_a$ : 0.8%), 843.76 keV ( $\gamma_a$ : 71.8%), and 1014.44 keV ( $\gamma_a$ : 28.0%) that, which are suitable for the calculation of the total Mg content through INAA. However, Mg quantification using 843.76 keV peak has two primary issues: gammaray interferences and isotopic interference. The Mg mass fraction is more than 10 times the interference elements (Eu and Mn) in most of the samples, although significant gamma-ray interference was caused by the relatively high thermal neutron cross section and abundance of gamma-rays of interference elements. Nuclear data was obtained from the radionuclide decay database online library for gamma and alpha emissions (http://www.nucleide.org/ Laraweb/index.php) and  $k_0$ -database [8]. <sup>27</sup>Mg emits another interference free gamma-ray at 1014.44 keV with only 30% of the 843.76 keV peak intensity and is subject to large uncertainty because of poor counting statistics. Thus, identifying suitable peakfitting software for two or more gamma-ray interference regions is necessary to obtain more reliable peak areas with corresponding uncertainties. In this study, both the peak areas of <sup>27</sup>Mg (843.76 keV and 1014.44 keV) were used to determine the total Mg mass fraction. In addition to gamma-ray interference, isotopic interference from the (n,p) threshold reaction in aluminum (Al) caused by the fast neutrons was also considered. If the sample contains high amounts of Al. Mg mass fraction likely bias because of isotopic interference from the  ${}^{27}$ Al(n,p) ${}^{27}$ Mg reaction [5,7]. Another isotopic threshold interference from  ${}^{30}\text{Si}(n,\alpha){}^{27}\text{Mg}$  did not significant contribute to the total Mg content because of the low abundance of silicon isotope (3.1%) and low  $(n,\alpha)$  cross-section (0.155 mb). These isotopic issues can be solved by introducing an isotopic correction factor such as the auto-correction option implemented in the revised version of the KayWin® software [6,9,10].

In 1995, the International Atomic Energy Agency (IAEA) conducted an inter-comparison study using synthetic gamma-ray spectra to identify a suitable peak-fitting program for gamma-ray spectrum analysis in terms of the number of peaks, peak position, peak position error, full width at half maximum (FWHM), peak area, peak-fitting error, and Chi-square [11]. Based on the findings, most of the programs were suitable for single-peak characterization and not recommended for complex peak region analysis, where there were two or more gamma-ray interferences [11]. Some programs such as Ganaas, Hypermet PC, GammaVision, Genie PC, and Span have shown consistent peak characterization in the complex region [11]. However, most of the peak-fitting programs are not compatible with personal computer (PC) versions, such as Windows 7 (issued in 2009) operating systems (OS) except GammaVision and Genie PC (updated as Genie2000), because they were not upgraded in a timely manner. Meanwhile, several programs have been developed, including HyperLab, HyperGam, and Gammalab that compatible with the present Windows OS. Some of these programs, such as HyperLab and HyperGam, were developed based on the Hypermet code [12,13]. In most software, FWHM calibration is used for deconvolution of the merged peaks. However, one peak may have high peak intensity while another closer peak on the left or right-side has a low peak intensity that will be considered as tails. To resolve this issue and identify the low peak intensity gamma-ray on the left or right-side of the high-intensity peak requires special peak-fitting functions such as left or rightskew functions. In recently developed programs also did not find satisfactory discussions on complex peak region analysis using IAEA synthetic or experimental gamma-ray spectra [12,14,15].

The aim of the present study is to identify suitable deconvolution capability of peak fitting program for the complex region using four software programs GammaVision, Genie2000, HyperLab, and HyperGam. Subsequently, the peak area was used for mass fraction determination in various matrix certified reference materials. Isotopic interference correction factor also calculated for the determination of Mg mass fraction accurately using  $k_0$ -INAA method. In the present study, four different matrix certified reference material (CRM) samples, urban particulate matter (NIST SRM 1648a), infant formula (KRISS CRM 108-02-004), peach leaves (NIST SRM 1547), and channel sediment (BCR-320R), were analyzed for the determination of total Mg and Al mass fractions simultaneously.

### 2. Theory

The software identifies the peaks on the basis of various functions such as peak type (Gaussian, FWHM, left-skew, and rightskew) and background type (polynomial, step, and tail) functions [16,17]. In this study, the peak type model functions required for the deconvolution of complex region gamma-rays are briefly discussed. The following peak functions are important for the analysis of complex region gamma-rays.

Gaussian peak function: The peak area of the Gaussian peak is calculated using Equation (1), which is a symmetry function (Fig. 1(a)). All peak-fitting programs consider this function to be important for singlet peak area calculations.

Gaussian peak function = 
$$\psi \cdot e^{-\left(\frac{x-x_0}{\delta}\right)^2}$$
, (1)

where x and  $x_0$  represent the channel number and centroid of the peak position, respectively,  $\psi$  represents the amplitude of the peak, and  $\delta$  represents the peak width parameter (FWHM/1.66).

*Left-skew function:* Some peaks appear as asymmetric shapes with an exponential decrease in the low-energy side from the



Fig. 1. Semi-empirical model functions of (a) Gaussian distribution, (b) Gaussian + left-skew, and (c) Gaussian + right-skew [17].

centroid of the Gaussian peak. This slope may be due to weak gamma peak energy (in terms of intensity) on the low-energy side (left-skew + Gaussian peak), as shown in Fig. 1(b). This low-energy peak can be easily resolved using the left-skew function (Equation (2)). In some cases, the asymmetric shape of the Gaussian peak may also be due to incomplete charge collection (tail background) in the detector. These two functions can be separated by a slope term. The tail background slope is 2.5–50, whereas the left-skew function slope ranges 0.3–2. Few software programs (e.g., HyperLab and Hypermet PC) consider this function for better deconvolution of merged peaks [16,17].

Left skew function = 
$$\psi \cdot \frac{\sqrt{\pi}}{2} \cdot \delta \cdot \alpha \cdot e^{\left(\left[\frac{\delta}{2\cdot a_1}\right]^2 + \frac{x - x_0}{a_1}\right) \cdot \operatorname{erfc}\left(\frac{\delta}{2\cdot a_1} + \frac{x - x_0}{\delta}\right)},$$
(2)

where  $\alpha$  denotes the left-skew amplitude relative to Gaussian,  $\alpha_1$  denotes the left-skew slope (0.3–0.2), and *erfc* denotes the standard complementary error function (erfc(x) =  $1 - \frac{2}{\sqrt{\pi}} \int_{0}^{x} e^{-t^2} dt$ ).

*Right-skew function:* The right-skew function is similar to the left-skew function form at the right side of the Gaussian peak, where they mirror each other. Fig. 1(c) shows a right-skewed function with at Gaussian peak. This high-energy peak with a low peak area can be resolved using the right-skewed function (Equation (3)). The Gaussian peak appears as an asymmetric shape with an exponential decrease in the right high-energy side from the centroid of the Gaussian peak. Similar to the left-skew function, this skewness function is also important for the deconvolution of complex regions. In some cases, right-skewness feature appears because of pile-up effect, particularly it is appearing in short-lived

radionuclide and high dead-time counting measurement. These two functions can be separated using a slope term as mentioned in the left-skew function. Based on the information given in the peak-fitting software manuals, this function was included in the recently developed peak-fitting programs such as HyperLab [17]. However, it was not considered in the original Hypermet PC code [16]. These three functions play an important role in the deconvolution of merged peaks along with the background functions [17]. Another suitable application of the right-skew function are <sup>85</sup>Sr (514.0 keV), it is right side of the annihilation peak (511.0 keV), and <sup>65</sup>Zn (1115.54 keV).

Right skew function = 
$$\psi \cdot \frac{\sqrt{\pi}}{2} \cdot \delta \cdot \beta \cdot e^{\left(\left[\frac{\delta}{2\cdot\beta_1}\right]^2 - \frac{x-x_0}{\beta_1}\right) \cdot \operatorname{erfc}\left(\frac{\delta}{2\cdot\beta_1} - \frac{x-x_0}{\delta}\right)}$$
,
  
(3)

where  $\beta$  denotes the right-skewed amplitude relative to Gaussian,  $\beta_1$  represents the right-skewed slope (0.3–0.2), and *erfc* denotes the standard complementary error function.

### 3. Experimental details

The samples were pressed into standard geometry pellets (ø 13 and 1 mm thicknesses) using a Whatman® cellulose filter paper to minimize the correction factors of neutron absorption, scattering, and gamma-ray attenuation. IRMM-530R Al-0.1%Au alloy foil (thickness: 0.1 mm) was used as the flux monitor and comparator. The samples and flux monitors were heat-sealed with polyethylene. Samples were irradiated with approximate thermal and epithermal neutron flux of  $1.1 \times 10^{12}$  cm<sup>-2</sup> s<sup>-1</sup> and  $3.6 \times 10^{10}$  cm<sup>-2</sup> s<sup>-1</sup>, respectively, at the TRIGA Mark II nuclear



Fig. 2. Deconvolution of the complex region containing 843.76 keV (<sup>27</sup>Mg) and 846.81 keV (<sup>56</sup>Mn) with HyperGam program (BCR-320R channel sediment).



Fig. 3. Deconvolution of the complex region containing 841.63 keV (152mEu), 843.76 keV (27Mg), and 846.81 keV (56Mn) with HyperLab program (BCR-320R channel sediment).

reactor, Jožef Stefan Institute, Ljubljana, Slovenia, for 30 s for determination of short-lived radionuclides. After an appropriate cooling time (<10 min), the samples were transferred to a radioactive laboratory for offline gamma-ray measurement using a highresolution HPGe detector (45% relative efficiency and 1.8 keV FWHM at 1332 keV) with <10% dead time. The short-lived radionuclide gamma-ray spectra were obtained at a distance of 20 cm from the detector and a 300 s time measurement using Maestro software with the zero dead time (ZDT) counting mode. The ZDT achieved a good performance for real-time correction in the peak area up to 30% dead time, including variable dead time during the short-lived radionuclide measurement [18]. Four different automatic peak-fitting programs, namely, HyperLab ver2014.1 [17], HyperGam ver1.3 [12,19], GammaVision ver6.01 [20], and Genie2000 ver3.1 [21] were used to analyze and compare the peak area of short-lived radionuclides (Mg and Al). The HyperLab peak report was used for concentration determination using the  $k_0$ -INAA method with KayWin® software [10]. More details on the experimental conditions, procedure, and calculations are provided in previous articles [5,22,23].

### 4. Results and discussion

## 4.1. Determination of peak areas using different peak-fitting software

The deconvolution of the merged peaks in the conventional gamma-ray spectrum using commercially available software was performed. All four software programs resolved the merged peak

areas along with uncertainties of the 843.76 keV (<sup>27</sup>Mg) and 846.81 keV (<sup>56</sup>Mn) gamma-rays except for GammaVision. GammaVision could not identify the 843.76 keV peak and merged it the 846.81 keV peak. Although the 843.76 keV peak area was determined through collectively peak evaluation process using interactive in viewed area mode instead of peak fitting. Screen shots of the peak-fitting analysis of the HyperGam and HyperLab programs for the BCR-320R channel sediment are presented in Figs. 2 and 3, respectively. As shown in Fig. 2 and 843.76 keV fitted slightly off with HyperGam to the original fitting because it cannot identify low-energy peaks at 841.63 keV (<sup>152m</sup>Eu). HyperLab can identify the third peak at 841.63 keV with a small peak area (Fig. 3) in the complex region, and this peak is not available in the HyperGam and Genie2000 programs. Along with complex region peak area analysis, singlet peak areas at 1014.44 keV (<sup>27</sup>Mg) and 1778.97 keV (<sup>28</sup>Al, half-life 2.24 m) were also determined for the quantification of Mg and Al. The capability of peak area determination was tested using statistical parameters, z-score, and percentage (%) deviation with respect to the reference peak report. In this study, the HyperLab peak report was considered as the reference spectra and peak areas that were used for total element concentration determination using  $k_0$ -INAA. The % deviation and z-score values were determined using Equations (4) and (5), respectively.

$$Dev. (\%) = \frac{x_i - x_j}{x_j} \cdot 100\%$$
 (4)

Sample	HyperLab			HyperG	m					Genie20	00					Gamma\	Vision				
		Control Control	0	<sup>27</sup> Mg,		<sup>27</sup> Mg,		<sup>28</sup> AI,		<sup>27</sup> Mg,		<sup>27</sup> Mg,		<sup>28</sup> Al,		<sup>27</sup> Mg,		<sup>27</sup> Mg,		<sup>28</sup> Al,	
	ivet peak art	a with munig		$E_{\gamma}(1)$		E <sub>7</sub> (2)		$E_{\gamma}(1)$		$E_{\gamma}(1)$		E <sub>7</sub> (2)		$E_{\gamma}(1)$		E <sub>γ</sub> (1)	. – 	E <sub>γ</sub> (2)		$E_{\gamma}(1)$	
	<sup>27</sup> Mg,	<sup>27</sup> Mg,	<sup>28</sup> AI,	% dev.	z	% dev.	z	% dev.	z	% dev.	z	% dev.	z	% dev.	z	% dev.	<b>N</b>	% dev.	z	% dev.	z
	E <sub>γ</sub> (1)	E <sub>γ</sub> (2)	E <sub>γ</sub> (1)																		
Urban PMs	2306(5.5%)	897(5.3%)	40,666(0.5%)	1.08	0.17	4.79	0.63	1.34	1.51	30.1	3.38	10.8	0.73	0.93	1.30	16.7	NC	5.94	0.41	0.68	0.94
Infant formula	1012(2.6%)	411(5.2%)	122(11.9%)	1.58	0.35	7.54	0.79	10.0	0.42	15.8	2.48	-6.08	-0.41	65.6	1.45	11.0	, NC	-6.57	-0.61	-20.5	-0.46
Peach leaves	8383(0.9%)	2834(1.5%)	9766(0.8%)	-2.09	-1.21	-1.27	-0.34	0.97	0.68	0.17	0.09	-1.27	-0.42	0.59	0.44	4.47	, NC	-1.06	-0.39	1.22	0.89
<b>Channel Sediment</b>	1258(5.5%)	520(7.2%)	42,182(0.5%)	7.23	1.02	3.85	0.34	-0.24	-0.31	36.0	4.17	0.38	0.04	0.18	0.21	4.61	, NC	-3.65	-0.34	0.12	0.16
NC: not calculated be	cause of Gamr	naVision prog	gram not generat	ed peak f	itting err	or (manu	ally fitted	deconvo	lution pe	aks); <sup>27</sup> N	Ag, $E_{\gamma}(1)$	= 843.7(	5 keV, <sup>27</sup>	Mg, $E_{\gamma}(2)$	= 1014	I.44 keV,	<sup>28</sup> Al, $E_{\gamma}$	(1) = 17	778.97 ke		

$$z = \frac{x_i - x_j}{\sqrt{\sigma_i^2 + \sigma_j^2}},\tag{5}$$

where  $x_i$  and  $x_j$  denote the peak areas reported by specific and reference software (HyperLab), and  $\sigma_i$  and  $\sigma_j$  represent peak-fitting errors reported by specific and reference software, respectively.

All selected programs yield the same fitting results of FWHM, peak position, and peak position uncertainty with  $\pm 2\%$  deviation, except for peak areas. The peak areas reported by the HyperLab and HyperGam programs are close values than those reported by the Genie2000 and GammaVision programs. The 1778.97 keV peak fitting error for infant formula is high because of the low peak area or low concentration. The % deviation and z-score of the peak area fitting calculated in HyperGam, Genie2000, and GammaVision with regard to HyperLab are summarized in Table 1. The % deviation and z-score values of HyperGam are within  $\pm 10\%$  and  $\leq \pm 2$ , respectively, which are close to the HyperLab values. The HyperGam and HyperLab programs were developed based on Hypermet-PC code. Thus, the peak search functions of these two programs were similar. Moreover, additional peak-fitting functions, such as the right-skew function, were included in HyperLab, which are not in the basic Hypermet-PC and HyperGam [16]. This right-skewed function is significant for the deconvolution of two or more peaks in the integrated region. The results from the other two programs, namely, Genie2000 and GammaVision, were inconsistent with HyperLab peak characteristics, and most of the peak area results had more than  $\pm 10\%$  deviation and were out of the  $\pm 2$  z-score range. In GammaVision, the z-score was not calculated for the 843.76 keV peak because fitting errors were not reported. The four selected peak fitting programs were arranged according to their deconvolution capability under the present experimental and measurement conditions: HyperLab, HyperGam, Genie2000, and GammaVision.

## 4.2. Determination of magnesium concentration through $k_0$ -based INAA

The simultaneous determination of Mg using two major gamma-ray peak areas (843.76 keV and 1014.44 keV) and Al in different matrix CRM samples was performed through  $k_0$ -INAA. In KayWin® software, the weighted mean mass fraction ( $\rho$ ) of the analyte (a) along with the observed (obs) and expected (exp) uncertainty are calculated using Equations (6)–(8) that provide more reliable information about the quality of the results [6,10]. In this software, the counting statistics of peak-fitting were not considered because the counting statistics of all peak areas were not reliable in all cases. A typical analyte mass fraction determination, including the isotopic interference correction factor calculation using Kay-Win® software ( $k_0$ -INAA), is shown in Fig. 4.

$$\rho_a = \frac{\sum_{i=1}^n \rho_i w_i}{\sum_{i=1}^n w_i},\tag{6}$$

$$\sigma_{i,obs} = \sqrt{\frac{\sum_{i=1}^{n} w_i (\rho - \rho_i)^2}{(n-1) \sum_{i=1}^{n} w_i}},$$
(7)

$$\sigma_{i,exp} = \sqrt{\frac{\sum_{i=1}^{n} (w_i \sigma_i)^2}{\left(\sum_{i=1}^{n} w_i\right)^2}},\tag{8}$$

where  $w_i = \frac{1}{\sigma_i^2}$  represents the weighting factor of a particular gamma-line (*i*), and  $\rho_i$  represents the weighted mean mass fraction

Eile Sam	o for Win	dows V3.3	37 (MyK	ey) History	Reports		Archiv	/e Tool	s Windo	w Help			
Crder	: JSISHO	RT Sampl	le : R221	7 (P:3;N;	E;I;dE0.65	; k0-201	5 : 18/0	8/2017)	, mindo	iii nop	- [		×
OK	Cancel	Print	Ext. Un	c. Report							Previous	Next	^
As	Br	In		I.	Ba	Eu		Dy	Tm	U	End	Check	
	Na	Mg !	AL !	CI	K	Ca	Ti	V	Cr	Mn	Cu	Zn	
Mg Mg-2	27 T 	Energy 11 84 10 hreshold Re	70.7 43.8 114.4 eaction In ference	(1) (1) (1) terference	<ul> <li>&lt;4.1714E</li> <li>12037.32</li> <li>11907.65</li> <li>s3713</li> </ul>	JSI +4 244 333	SHORT:2 <1.3989 -10827.1 -12453.1 371	9E+5 2749 3356 3.4265					
Si <	100%	Inter	ference	:	<1.250	000E+5	<1.2	5000E+5					
Cashi	Lalla 2	pi Thermal :	SelfAbso	rption Corr	rection		4.00	0					
Gept.	mg/mg-2 N	ι uclide Δver	90e		1.000		1.00	0					
Concentra Expected Observed	ation : StnDev % StnDev %	:	8295.4 2.903 0.446	605 35 68	8295.46 2.9035 0.4468	05 5 3	-	2	Witl	hout correctories	ction Mg co	onc.	
Extended	Uncer. % :		3.093	38	3.0938	3	-	$\langle$	🔵 Alt	o Mg conv	verted conc.	(n,p)	
LD	:		907.52	227	907.522	27	810.01	148	Cor	rected Mg	conc.		
LD elemen	nt :		907.5	227									

Fig. 4. Calculation of Mg concentration through auto correction of threshold reaction interferences using KayWin® software.

of a particular gamma-line.

The combined standard uncertainty with a coverage factor at k = 1 and expanded uncertainty (*U*) at k = 2 (95% confidence interval) of the final result was calculated using Equations (9) and (10).

$$u_{c,a} = \sqrt{u_{AREA,corr}^2 + u_{a,method}^2},\tag{9}$$

$$U_a = 2 \cdot u_{c,a},\tag{10}$$

where  $u_{AREA, corr}$  denotes the uncertainty of the corrected net peak area, and  $u_{method}$  represents the overall standard uncertainty of the  $k_0$ -INAA method (approximately 3.5%) that take into account the contribution from  $k_0$ -factors, f,  $\alpha$ ,  $Q_0$ ,  $\varepsilon_p$ , and true coincidence effects [6,10].

The results, which show the expanded uncertainties with a coverage factor of k = 2, are summarized in Table 2. The expanded uncertainty using a gamma-ray energy of 843.76 keV is within ±8% that is lower than the expanded uncertainty using 1014.44 keV (±12%). The Mg concentration with 843.76 keV is a more reliable value with a lower uncertainty than with 1014.44 keV. However, part of the Mg concentration was contributed by Al because of the fast neutron nuclear reaction <sup>27</sup>Al(n,p)<sup>27</sup>Mg. Approximately 11% Al was converted into Mg during sample irradiation in the irradiation channel (IC-40) of the 250 kW TRIGA Mark II reactor, where all irradiations were performed. The conversion factor for isotope interference nuclides depends on the fast neutron flux in the

irradiation position and it determined experimentally [24] using an Al-0.1%Au alloy (IRMM-530R) with approximately 99.9% of Al. The variation of the neutron flux in the sample irradiation position was monitored using an Al-0.1%Au alloy and irradiated along with the sample. Consequently, the determination of the accurate concentration of isotopic interference of Mg through the standard comparator INAA becomes difficult. This issue can be solved easily by the  $k_0$ -INAA method using KayWin® software that which includes an isotopic correction factor. However, it is possible only the analyte and interference elements analyzed simultaneously. The quality of laboratory values is compared with certified values through  $E_n$ -score that is calculated using Equation (11) [23].

$$E_n = \frac{X_{lab} - X_{ref}}{\sqrt{U_{lab}^2 + U_{ref}^2}},\tag{11}$$

where  $X_{lab}$  and  $X_{ref}$  denote the laboratory and reference values, and  $U_{lab}$  and  $U_{ref}$  represent the expanded uncertainties (k = 2) of the laboratory and reference values, respectively.

The experimental mass fraction values were consistent with the certified values, and the % deviations and  $E_n$ -scores were 6% and  $\leq 1$  with satisfactory results, respectively, except for Al in the infant formula sample. The concentration of Al in infant formula samples is low (<1 mg/kg) and, may be easily in-homogenized owing to contamination from the sample wrapping materials. The Mg mass fraction value was determined by 843.76 keV gamma-rays that were more consistent with the certified values compared with

#### Table 2

Results for Mg and Al mass fraction obtained through  $k_0$ -INAA in different CRMs. Results are given in mg/kg (dry mass basis) with associated expanded uncertainties (k = 2) along with % deviation and  $E_n$ -score.

Sample	Certified value	Mg: <sup>27</sup> Mg, E	<sub>γ</sub> (1)		Mg: $^{27}$ Mg, E <sub><math>\gamma</math></sub> (	(2)		Mg: <sup>27</sup> Mg, E	$\gamma(1)$ and	E <sub>γ</sub> (2)	Certified value	Al: <sup>28</sup> Al, $E_{\gamma}(1)$		
	(Mg)	This work	% dev.	En	(Al)	% dev.	En	This work	% dev.	En		This work	% dev.	En
Urban PMs	8130 ± 120	8436 ± 791	3.76	0.38	8314 ± 1217	2.26	0.15	8415 ± 750	3.51	0.38	34,300 ± 1300	33,966 ± 2433	-0.97	-0.12
Infant formula	582.7 ± 8.1	$559 \pm 49$	-4.00	-0.47	$676 \pm 84$	15.9	1.11	577 ± 92	-1.03	-0.07	$0.79 \pm 0.28$	$3.30 \pm 0.82$	318	2.91
Peach leaves	$4320 \pm 150$	4546	5.23	0.63	$4579 \pm 347$	5.99	0.68	$4557\pm304$	5.49	0.70	$248.9 \pm 6.5$	$265 \pm 20$	6.36	0.77
		± 326												
Channel Sediment	NA	$6563 \pm 862$	NC	NC	$8182 \pm 1545$	NC	NC	$6869 \pm 965$	NC	NC	NA	$32,110 \pm 2259$	NC	NC

NC: not calculated; NA: not available;  ${}^{27}$ Mg,  $E_{\gamma}(1) = 843.76$  keV,  ${}^{27}$ Mg,  $E_{\gamma}(2) = 1014.44$  keV,  ${}^{28}$ Al,  $E_{\gamma}(1) = 1778.97$  keV.

1044.44 keV gamma-rays owing to the high weighted mean uncertainty. If the Mg concentration is high (~1%), then we can use both the gamma-ray peak areas. In contrast, in the case of low Mg content, using the 843.76 keV gamma peak area determined by HyperLab or HyperGam was recommended instead of 1014.44 keV. However, these findings depend on the intensity of the 846.81 keV (<sup>56</sup>Mn) peak next to it. Based on the present observation, the Mg peak area should be more than 5% with regard to the strongest peak at 846.81 keV.

### 5. Conclusions

In this study, the Mg mass fraction was determined accurately using 843.76 keV gamma-ray through  $k_0$ -INAA in different matrix samples. In nonlinear peak fitting functions, the Gaussian peak, left-skew, and right-skew functions are important for the deconvolution of the merged peaks. The four peak-fitting programs, namely, HyperLab, HyperGam, Genie2000, and GammaVision were used for complex region analysis and compared. The best peak area fitting program in the selected programs according to this study is as follows: HyperLab, HyperGam, Genie2000, and GammaVision. Among the programs, HyperLab and HyperGam exhibited better fitting characteristics of closely integrated peaks with low residuals. Moreover, the right-skew function included HyperLab program can extend also in complex cases of <sup>85</sup>Sr (514.00 keV) and <sup>65</sup>Zn (1115.54 keV), where these gamma lines are affected by the annihilation gamma-ray (511.0 keV) and <sup>152</sup>Eu (1112.08 keV), <sup>46</sup>Sc (1120.54 keV), respectively. The nuclear interference factor caused by  ${}^{27}Al(n,p){}^{27}Mg$  was considered to affect the total Mg content. The combination of HyperLab and KayWin $\mathbb{R}$  programs for  $k_0$ -INAA is recommended for the accurate quantification of elements with gamma-ray and isotopic interferences.

### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Acknowledgement

The authors from KAERI & KRISS thank Prof. Milena Horvat, Head of the Department of Environmental Sciences at JSI, for her support of the experimental work at JSI funded by the Slovenian Research Agency (ARRS) programme P1-0143 and the Metrology Institute of the Republic of Slovenia (MIRS), Slovenia contract No. C3212-10-000071 (6401-5/2009/27). This work was supported by KAERI, South Korea through the Korea Government project No. MSIT/1711078081, 2021. This work was also supported by KRISS, South Korea under the project, "Establishment of Measurement Standards for Inorganic Analysis" Grant No. 21011058, 2021.

### References

- [1] J.-D. Wilhelm, K. Markus, Magnesium basics, Clin. Kidney J. 5 (2012) i3–i14.
- [2] LJ. Dominguez, N. Veronese, M. Barbagallo, Magnesium and hypertension in old age, Nutrients 13 (2021) 139.
- [3] R.R. Greenberg, P. Bode, E.A. De Nadai Fernandes, Neutron activation analysis: a primary method of measurement, Spectrochim. Acta B 66 (3-4) (2011) 193-241.
- [4] R. Jaćimović, B. Smodiš, T. Bučar, P. Stegnar, k<sub>0</sub>-NAA quality assessment by analysis of different certified reference materials using the KAYZERO/SOLCOI software, J. Radioanal. Nucl. Chem. 257 (3) (2003) 659–663.
- [5] H. Cho, K.B. Dasari, R. Jaćimović, R. Zeisler, N.E. Sharp, S.-H. Kim, G.-M. Sun, Y.-H. Yim, Application of the INAA methods for KRISS infant formula CRM analysis: standardization of INAA at KRISS, J. Radioanal. Nucl. Chem. 322 (2019) 1537–1547.
- [6] F. De Corte, The K<sub>0</sub>-Standardization Method: a Move to the Optimization of Neutron Activation Analysis, Habilitation Thesis, University of Gent, Belgium, 1987.
- [7] G. Kennedy, J.-L. Galiniera, L. Zikovsky, Measurement of some primary nuclear interferences in neutron activation analysis with a SLOWPOKE reactor, Can. J. Chem. 64 (1986) 790–792.
- [8] k<sub>0</sub> Database, 2020. http://www.kayzero.com/k0naa/k0naaorg/Nuclear\_Data\_ SC/Entries/2020/8/24\_Update\_of\_k0-database\_I-128.html. Accessed 02 January 2021.
- [9] F. De Corte, A. Simonits, Vade Mecum for *K*<sub>0</sub>-Users, DSM Research, Geleen, 1994.
- [10] User's Manual for reactor neutron activation analysis (NAA) using the  $k_0$  standardization method, in: Kayzero for Windows (KayWin®) Version 3.30, 2017.
- [11] M. Blaauw, V. Osorio Fernandez, P. van Espen, G. Bernasconi, R. Capote Noy, H. Manh Dung, N.I. Molla, The 1995 IAEA intercomparison of γ-ray spectrum analysis software, Nucl. Instrum. Methods A 387 (1997) 416–432.
- [12] B.-G. Park, H.D. Choi, C.S. Park, New development of hyperGam and its test of performance for γ-ray spectrum analysis, Nucl. Eng. Technol. 44 (2012) 781–790.
- [13] A. Simonits, J. Östör, S. Kálvin, B. Fazekas, HyperLab: a new concept in gammaray spectrum analysis, J. Radioanal. Nucl. Chem. 257 (2003) 589–595.
- [14] J.M. Los Arcos, M. Blaauw, S. Fazinic, V.P. Kolotov, The 2002 IAEA test spectra for low-level γ-ray spectrometry software, Nucl. Instrum. Methods A 536 (2005) 189–195.
- [15] C.A. Kalfas, M. Axiotis, C. Tsabaris, SPECTRW: a software package for nuclear and atomic spectroscopy, Nucl. Instrum. Methods A 830 (2016) 265–274.
- [16] L. Szentmiklosi, Fitting special peak shapes of prompt gamma spectra, J. Radioanal. Nucl. Chem. 315 (2018) 663–670.
- [17] HyperLab User's Manual for Gamma Spectroscopy Software, 2014. http:// www.hlabsoft.com/web/hl2014/onlinedocs.php. accessed 15 February, 2021.
- [18] R. Acharya, K.B. Dasari, D. Chandra Shekhar, P.K. Pujari, Performance of digital gamma ray spectrometer for loss free counting and its application to NAA using short-lived radionuclides, J. Radioanal. Nucl. Chem. 302 (2014) 1333–1337.
- [19] C.S. Park, H.D. Choi, G.M. Sun, J.H. Whang, Status of developing HPGe γ-ray spectrum analysis code HYPERGAM, Prog. Nucl. Energy 50 (2008) 389–393.
- [20] GammaVision Gamma Spectroscopy Software User's Manual, 2016. https:// www.ortec-online.com/products/application-software/gammavision.
- [21] Genie2000 Basic Spectroscopy Software User's Manual, 2006. https://www3. nd.edu/~wzech/Genie%202000%20Operations%20Manual.pdf.
- [22] H. Cho, K.B. Dasari, M.C. Lim, G.M. Sun, R. Jaćimović, Y.-H. Yim, Application of k<sub>0</sub>-INAA method in preliminary characterization of KRISS urban airborne particulate matter certified reference material, Appl. Sci. 10 (19) (2020) 6649.
- [23] K.B. Dasari, H. Cho, R. Jaćimović, G.-M. Sun, Y.-H. Yim, Chemical composition of Asian dust in Daejeon, Korea, during the spring season, ACS Earth Space Chem. 4 (8) (2020) 1227–1236.
- [24] R. Jaćimović, A. Trkov, P. Stegnar, Error in k<sub>0</sub>-NAA measurement due to temporal variation in the neutron flux in TRIGA Mark II reactor, J. Radioanal. Nucl. Chem. 294 (1) (2012) 155–161.