

Optimum Hydraulic Oil Viscosity Based on Slipper Model Simulation for Swashplate Axial Piston Pumps/Motors

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Abstract: Viscosity of hydraulic oils decreases due to loss reduction and efficiency increase of fluid power systems. However, low viscosity is not always appropriate due to the induction of large leakage and small lubricity. Therefore, a detailed study on the optimum viscosity of hydraulic oils is necessary. In this study, based on the thermohydrodynamic lubrication theory, numerical simulation was conducted using the slipper model of swashplate-type axial piston pumps and motors. The viscosity grades' (VG) effects of oils on power losses are mainly discussed numerically in fluid film lubrication, including changes in temperature and viscosity. The simulation results reveal that the flow rate increases and the friction torque decreases as VG decreases. The film temperature and power loss were minimised for a specific oil with a VG. The minimum conditions regarding the temperature and loss were different and closed. Under various operating conditions, the film temperature and power loss were minimised, suggesting that an optimum hydraulic oil with a specific VG could be selected for given operating conditions of pressure and speed. Otherwise, a preferable operating condition must be established to determine a specific VG oil.

Nomenclature

a : recess radius ratio, $= R_1/R_2$
 B : pad thickness, m
 B_i : parameter, $= Bh_T/\lambda'$
 c_p : specific heat at constant pressure, J/(kg·K)
 E_c : parameter, $= (\omega R_2)^2/(c_p T_0)$
 H : representative clearance, m
 \bar{h} : clearance, $= h/H$
 \bar{h}_c : centre clearance, $= h_c/H$
 h_T : heat transfer coefficient, W/(m·K)
 \bar{L} : power loss, $= L/(\omega p_s R_2^3 S_o)$
 \bar{M} : moment, $= M/(p_s R_2^3 S_o)$
 Nu : parameter, $= Hh_T/\lambda$
 Pe' : parameter, $= PrRe'$
 Pr : parameter, $= \mu_0 c_p/\lambda$

p : pressure, $= p/(p_s S_o)$
 p_r : recess pressure, $= p_r/(p_s S_o)$
 p_s : supply pressure, Pa
 \bar{Q} : flow rate, $= Q/(\omega R_2^3)$
 Q_{out} : leakage flow rate, m³/s
 Re' : parameter, $= \rho \omega H^2/\mu_0$
 \bar{R}_0 : revolution radius, $= R_0/R_2$
 R_1 : recess radius, m
 R_2 : pad outer radius, m
 r, θ, z : cylindrical coordinates, $= r/R_2, \theta, z/H$
 r_w : load eccentricity, m
 S_o : parameter, $= 6\mu_0 \omega (R_2/H)^2/p_s$
 \bar{T} : temperature, $= T/T_0$
 \bar{T}_a : ambient temperature, $= T_a/T_0$
 \bar{T}_f : friction torque, $= T_f/(p_s R_2^3 S_o)$
 \bar{T}_r : recess temperature, $= T_r/T_0$
 \bar{T}_s : supply oil temperature, $= T_s/T_0$
 T_0 : reference temperature, K
 $\bar{u}, \bar{v}, \bar{w}$: velocities, $= u/(\omega R_2), v/(\omega R_2), w/(\omega H)$
 \bar{W} : load, $= W/(p_s R_2^2 S_o)$
 X, Y, Z : orthogonal coordinates on disk
 x, y, z : orthogonal coordinates on slipper
 $\bar{\alpha}$: pad inclination angle, $= \alpha R_2/H$
 λ : thermal conductivity of oil, W/(m·K)
 λ' : thermal conductivity of pad, W/(m·K)

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- μ : viscosity, $= \mu/\mu_0$
 ν : kinematic viscosity, m^2/s
 ρ : density, kg/m^3
 $\bar{\Phi}$: angle, $= \Phi R_2/H$
 ϕ : maximum pad azimuth, rad
 Ω : reference angular velocity, rad/s
 Ω' : sliding angular velocity, rad/s
 ω : pad angular velocity, rad/s

Subscripts

- 0: reference (high pressure period)

1. Introduction

Hydraulic systems are widely used in the construction, aviation and manufacturing industries because they can effectively transfer energy or power with high efficiency, responsiveness and flexibility¹. A large amount of power can be transmitted using hydraulic equipment with high pressure, linking the low efficiency of pumps and actuators to large losses².

Selection of hydraulic oil with appropriate viscosity is a way of improving efficiency because viscosity dictates the physical properties of oils³, particularly in terms of lubrication and leakage that are directly related to mechanical and volumetric losses⁴. Generally, high viscosity causes mechanical loss, whereas, low viscosity causes volumetric loss. Since the total loss is the summation of mechanical and volumetric losses, an optimal viscosity may exist, e.g., the kinematic viscosity (ν) equivalent at 40°C is about 43–172 mm^2/s empirically for axial piston pumps⁵, although the preferable and optimum viscosity of hydraulic oils depends on pumps, motors, systems and operation.

Recently, the viscosity of hydraulic oils decreases owing to flow loss in pipes⁴ and churning loss in components. However, a low viscosity may not always be appropriate owing to the induction of less sealing effect and small hydrodynamic pressure, resulting in large leakage and solid contact and subsequently low volumetric efficiency and wear and seizure. Therefore, a detailed study of the optimum viscosity of hydraulic oils is necessary.

An appropriate oil with an optimum viscosity grade (VG) for a hydraulic system does not exist because a circuit of systems consists of several components including hydraulic pumps, valves, pipes, actuators and auxiliary components, having different flow behaviours and functions. Among them, hydraulic pumps and motors are the main components; thus, the losses in such components largely degrade their performances and the efficiency of a system⁶.

Hydraulic pumps and motors are positive displacement machines, whose performance depends on the tribological characteristics of sliding parts. For piston pumps and motors, prime parts are the interfaces between the pistons and cylinder bores⁷⁻⁸, the cylinder block and valve plate⁹⁻¹⁰ and the slippers and swashplate¹¹⁻¹². Precisely, the oil viscosity and the lubrication characteristics affect interface between slippers and a

swashplate because of the severe operating conditions of high load and speed. Sliding parts are heated by viscous dissipation in a thin fluid film, increasing oil temperature. Because viscosity varies with temperature, viscosity distribution becomes uneven owing to temperature variation. Since viscosity is determined by a reference ν at a specific temperature, e.g. 40°C (oil VG) and oil temperature (viscosity–temperature relation), accurate estimation of temperature distributions and appropriate selection of the oil VG are important.

The theoretical approach regarding thermal lubrication behaviour is the thermohydrodynamic lubrication (THL) theory¹³. Several theoretical and experimental studies of THL have been conducted mainly for hydrodynamic bearings rather than hydrostatic bearings¹⁴. Therefore, a model of hybrid (hydrostatic and hydrodynamic) thrust bearings, including the changes in physical properties of oils, was developed¹⁵. This model applies to a slipper installed in swashplate-type axial piston pumps and motors, suitable for thermal lubrication analysis of hydraulic equipment.

In this study, we investigate the thermal lubrication characteristics of a slipper relating to the oil VG and conduct a numerical simulation using the THL model between a slipper and a swashplate of axial piston pumps and motors¹⁶. Based on the optimum design of the components¹⁷, oil VG effects on the slipper characteristics including flow leakage, friction torque, film temperature and power losses in fluid film lubrication are discussed.

2. Theory

2.1 Theoretical model

The schematic of the THL slipper model is shown in Fig. 1¹⁴. The basic equations consisting mainly of the Reynolds, energy and heat conduction equations are given by

$$\begin{aligned}
 & \frac{1}{r} \frac{\partial}{\partial r} \left(\bar{F}_2 \bar{h}^3 r \frac{\partial p}{\partial r} \right) + \frac{1}{r^2} \frac{\partial}{\partial \theta} \left(\bar{F}_2 \bar{h}^3 \frac{\partial p}{\partial \theta} \right) \\
 & = \omega \frac{\partial}{\partial \theta} \left(\frac{\bar{F}_3 \bar{h}}{\bar{F}_0} \right) + \bar{\Omega} \bar{R}_0 \sin \theta \frac{\partial (\bar{F}_4 \bar{h})}{\partial r} \\
 & + \bar{\Omega} \left(\frac{\bar{R}_0}{r} \sin \theta + 1 \right) \frac{\partial (\bar{F}_4 \bar{h})}{\partial \theta}
 \end{aligned} \tag{1}$$

with

$$\begin{cases} \bar{F}_0 = \int_0^1 \frac{dz}{\mu} \\ \bar{F}_1 = \int_0^1 \frac{z dz}{\mu} \\ \bar{F}_2 = -6 \left(\int_0^1 \int_0^z \frac{dz}{\mu} dz - \bar{F}_1 \frac{\bar{F}_3}{\bar{F}_0} \right) \\ \bar{F}_3 = \int_0^1 \int_0^z \frac{dz}{\mu} dz \end{cases} \quad (2),$$

$$\begin{aligned} & \left[u \left(\frac{\partial \bar{T}}{\partial r} - m_r \frac{\partial \bar{T}}{\partial z} \right) + \frac{v}{r} \left(\frac{\partial \bar{T}}{\partial \theta} - m_\theta \frac{\partial \bar{T}}{\partial z} \right) + \frac{w}{\bar{h}} \frac{\partial \bar{T}}{\partial z} \right] \\ & = \frac{1}{Pe' \bar{h}^2} \frac{\partial}{\partial z} \left(\bar{\lambda} \frac{\partial \bar{T}}{\partial z} \right) + \frac{Ec}{Re'} \mu \varphi \end{aligned} \quad (3)$$

with

$$\begin{cases} m_r = \frac{z}{\bar{h}} \frac{\partial \bar{h}}{\partial r} \\ m_\theta = \frac{z}{\bar{h}} \frac{\partial \bar{h}}{\partial \theta} \end{cases} \quad (4)$$

and

$$\phi = \frac{1}{\bar{h}^2} \left[\left(\frac{\partial \bar{u}}{\partial z} \right)^2 + \left(\frac{\partial v}{\partial z} \right)^2 \right] \quad (5)$$

and

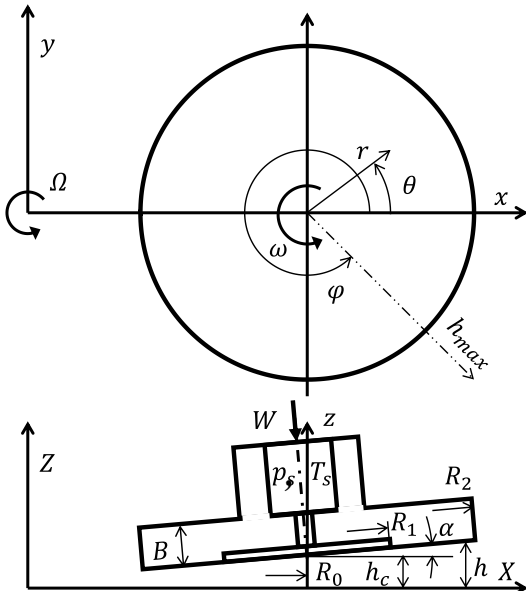


Fig. 1 Schematic of the slipper model

$$\begin{aligned} & \frac{1}{r'} \frac{\partial}{\partial r'} \left(r' \frac{\partial \bar{T}'}{\partial r'} \right) + \frac{1}{r'^2} \frac{\partial^2 \bar{T}'}{\partial \theta^2} \\ & + \left(\frac{R_2}{B} \right)^2 \frac{\partial^2 \bar{T}'}{\partial z'^2} = 0 \end{aligned} \quad (6).$$

In the following simulation, viscosity is treated as a function of temperature only although density, specific heat, thermal conductivity and viscosity are functions of temperature and pressure. Additionally, the thermal expansivity of oils is neglected in the energy equation.

The kinematic viscosity (ν) is estimated using the following Walther equation.

$$\log \log(\nu^\dagger + c) = -m \log T^\dagger + b \quad (7)$$

where ν^\dagger is the kinematic viscosity in mm^2/s , T^\dagger is the absolute temperature in K, b and m are specific constants depending on each oil and c is set at 0.7.

The boundary conditions of Eq. (1) for pressure and Eqs. (3) and (6) for temperature are given by

$$\begin{cases} p(a, \theta) = p_r \\ p(1, \theta) = p_a \end{cases} \quad (8)$$

and

$$\begin{cases} \bar{T}(r, \theta, 0) = \bar{T}_w \\ \bar{T}(a, \theta, z) = \bar{T}_r \\ \bar{T}'(a, \theta, z') = \bar{T}_r \\ \frac{\partial \bar{T}'(1, \theta, z')}{\partial r} = \frac{R_2}{B} Bi \left[\bar{T}'(1, \theta, z') - \bar{T}_a \right] \\ - \frac{\partial \bar{T}'(r, \theta, 1)}{\partial z'} = Bi \left[\bar{T}'(r, \theta, 1) - \bar{T}_a \right] \\ - \frac{\partial \bar{T}'(r, \theta, 0)}{\partial z'} = \frac{Bi}{Nu \bar{h}} \frac{\partial \bar{T}(r, \theta, 1)}{\partial z} \end{cases} \quad (9)$$

In Eq. (3) and the conditions of (9), Bi , Ec , Nu , Pe' and Re' are the Biot, Eckert, Nusselt, Péclet and Reynolds numbers, respectively, and $Pe' = PrRe'$, where Pr represents the Prandtl number.

The clearance between the slipper pad and the disk is

$$\bar{h} = \bar{h}_c + ar \cos(\theta - \phi) \quad (10)$$

The moment load-carrying capacities around the x and y axes (\bar{M}_{fx} and \bar{M}_{fy}) and the load-carrying capacity (\bar{W}_f) are calculated using

$$\begin{cases} \bar{M}_{fx} = \int_0^{2\pi} \int_a^1 pr^2 \sin \theta dr d\theta \\ \bar{M}_{fy} = - \int_0^{2\pi} \int_a^1 pr^2 \cos \theta dr d\theta \\ \bar{W}_f = \int_0^{2\pi} \int_a^1 pr dr d\theta + \pi a^2 p_r \end{cases} \quad (11)$$

The flow rates (\bar{Q}) in the slipper land at radius (r) and flow rate (\bar{Q}_r) through the capillary restrictor are given as

$$\bar{Q} = \frac{H}{R_2} r \int_0^{2\pi} \bar{h} \int_0^1 u dz d\theta \quad (12)$$

and

$$\bar{Q}_r = \pi \left(\frac{H}{R_2} \right) \frac{1}{\mu_s} \frac{p_s - p_r}{\beta} \quad (13),$$

respectively, where, μ_s is the viscosity at the restrictor and β is the recess parameter ($= 4H^3 l_c / (3r_c^4)$, where l_c and r_c are the length and radius of the restrictor, respectively). The leakage flow rate (\bar{Q}_{out}) can be obtained when $r = 1$ in Eq. (12).

The friction torque (\bar{T}_f) is computed using

$$\bar{T}_f = \frac{H}{6R_2} \times \int_0^{2\pi} \int_a^1 \frac{\mu}{\bar{h}} \left[\frac{\partial u}{\partial z} \Big|_{z=0} \sin(\theta - \theta) + \frac{\partial v}{\partial z} \Big|_{z=0} \cos(\theta - \theta) \right] \bar{R}' r dr d\theta \quad (14)$$

with

$$\begin{cases} \theta = \cos^{-1} \left(\frac{\bar{R}_0^2 + \bar{R}'^2 - r^2}{2\bar{R}_0 \bar{R}'} \right) \\ \bar{R}' = \sqrt{r^2 + \bar{R}_0^2 - 2r\bar{R}_0 \cos(\pi - \theta)} \end{cases} \quad (15)$$

The power loss (\bar{L}) can be estimated by summing the losses due to leakage (\bar{L}_Q) and friction (\bar{L}_T); thus,

$$\bar{L} = \bar{L}_Q + \bar{L}_T = p_s \bar{Q}_{out} + \bar{\Omega} \bar{T}_f \quad (16)$$

where $\bar{\Omega}$ is the sliding angular velocity of the disk.

2.2 Calculation conditions

The Reynolds, energy and heat conduction equations were solved numerically along with pressure and temperature boundary conditions and viscosity-temperature relation of the Walther formula. The equations were discretized using the finite difference

method and were solved numerically. Additionally, the THL solutions were compared with the isothermal (ISO) solutions.

Table 1 lists the five hydraulic oil models designated as VG 22, 32, 46, 68 and 100 that are relatively used in general and distributed in the market. The table also includes the density (ρ) and ν of the oils. The specific heat at constant pressure and thermal conductivity of all oils were assumed as 2000 J/(kg·K) and 0.13 W/(m·K), respectively, although these properties must be somewhat different because of the VG dependency. Under these fluid models, the coefficients of the Walther equation, m and b , are specified using Table 1 as $m = 3.760, 3.729, 3.654, 3.615$ and 3.477 and $b = 9.521, 9.487, 9.341, 9.285$ and 8.985 for VG 22, 32, 46, 68 and 100, respectively.

Further, the representative geometrical and operating parameters are the pad radius (R_2), recess radius ratio (a) and pad thickness (B) of 10, 0.7 and 5 mm, respectively. The load eccentricity ratio (r_w/R_2), revolution radius ratio (R_0/R_2) and normalised load (hydrostatic balance ratio) (ζ)¹⁸⁾ are 0.1, 3 and 0.9, respectively. The thermal conductivity and heat transfer coefficient of the pad are 50 W/(m·K) and 50 W/(m²·K), respectively.

3. Results and discussion

3.1 Kinematic viscosity of the lubricant models

Figure 2 shows the temperature dependence of ν with VG 22–100 for the hydraulic oils. Owing to the viscosity-temperature relation, the ν of higher VG oils at high temperature is close to the ν of lower VG at low temperature. Thus, if ν at 40°C of VG 32 (32.6 mm²/s) is selected as the reference, the same ν for VG 22, 46, 68 and 100 are obtained at 31.6°C, 47.9°C, 56.7°C and 66.8°C, respectively.

Table 1 List of hydraulic fluid models

	ρ kg/m ³	ν m ² /s (40°C)	ν m ² /s (100°C)
VG 22	866	23.0 × 10 ⁻⁶	4.44 × 10 ⁻⁶
VG 32	869	32.6	5.49
VG 46	872	45.8	6.86
VG 68	875	68.0	8.73
VG 100	882	105.5	11.92

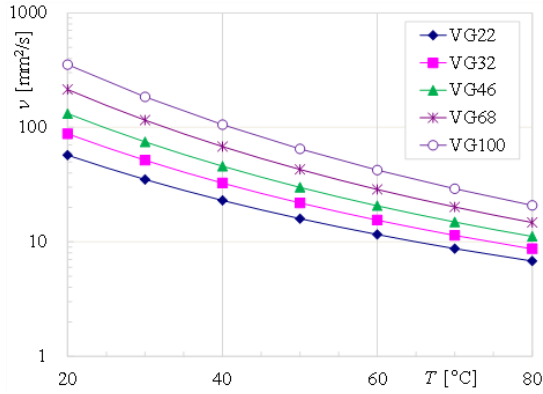


Fig. 2 Kinematic viscosity (ν) vs temperature (T) for oils with VG 22 - 100

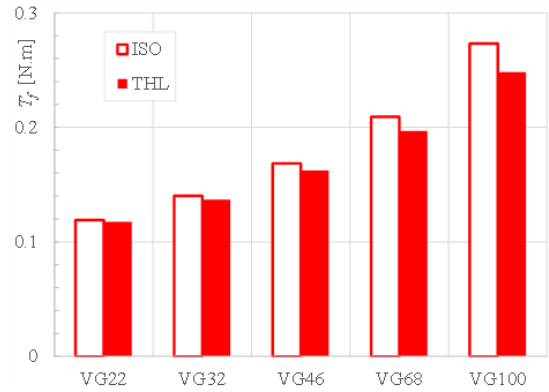


Fig. 4 VG effects on the friction torque (T_f) for VG 22-100 (1500 rpm and 21 MPa)

3.2 Comparison between ISO and THL solutions

Figures 3–6 present the VG effects on the leakage flow rate (Q_{out}), friction torque (T_f), power loss (L) and maximum temperature (T_{max}) in the film. These figures also include the differences between the ISO and THL solutions under a supply pressure of 21 MPa and a rotational speed of 1500 rpm (25 rps).

As VG decreases, Q_{out} increases and T_f decreases monotonously, mainly because of flow resistance and viscous friction, respectively (Figs. 3 and 4). In Figs. 5 and 6, L and T_{max} were minimised at the mid-VG because L in low and high VGs increased owing to the Q_{out} - and T_f -based losses, respectively.

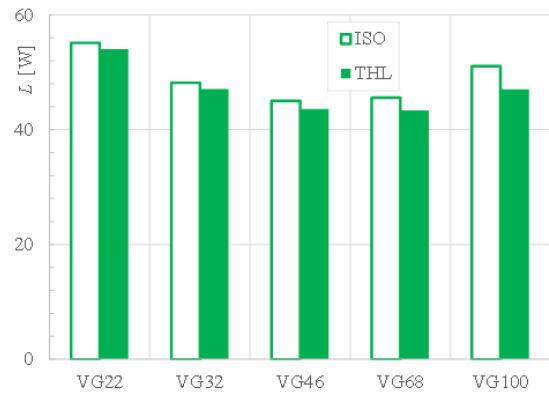


Fig. 5 VG effects on the power loss (L) for VG22 - VG100 (1500 rpm and 21 MPa)

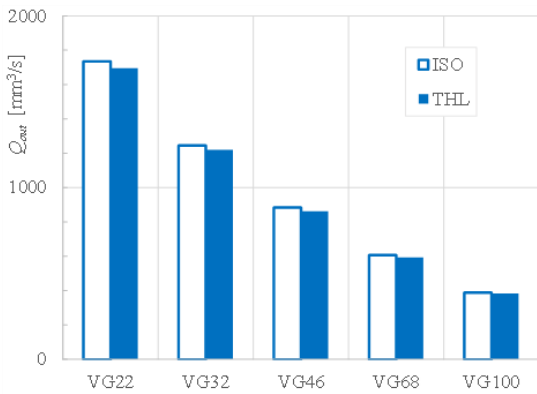


Fig. 3 VG effects on the leakage flow rate (Q_{out}) for VG 22 - 100 (1500 rpm and 21 MPa)

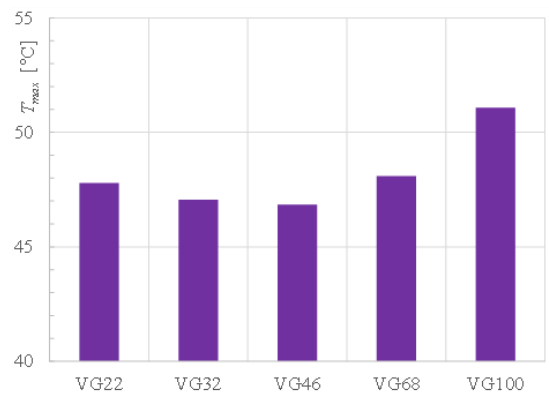


Fig. 6 VG effects on the maximum temperature (T_{max}) for VG 22 - 100 (1500 rpm and 21 MPa)

On comparing the ISO and THL solutions, Q , T_f and L of the ISO were larger than those of the THL. The minimum conditions for T_{max} and L were given at a mid-VG and the conditions were close; however, they were slightly different; T_{max} was minimised with VG 46, whereas, L of THL and ISO were minimised with VG 68 and VG 46, respectively. In any case, L was minimised at a specific VG oil because of the opposite tendency between leakage loss and friction loss against VG.

Figure 7 depicts L in terms of rotational speeds of 900, 1500 and 2100 rpm (15, 25 and 35 rps). The pressure was constant at 21 MPa. VG is represented as ν_0 that is the kinematic viscosity at 40°C for each oil. Under these conditions, L was minimised at a specific ν_0 . As the speed increased, L increased and its minimum value shifted to a lower value of ν_0 because of the influence of viscous dissipation in the oil film.

3.3 Relationship with the operating parameter

Figures 8–10 respectively display L , T_{max} and the power loss ratio (L_Q/L) against the normalised operating parameter ($\mu N/p_s$, μ : viscosity = $\rho\nu_0$), corresponding to the operating conditions of $p_s = 7\text{--}35$ MPa and $N = 300\text{--}1500$ rpm (5–25 rps).

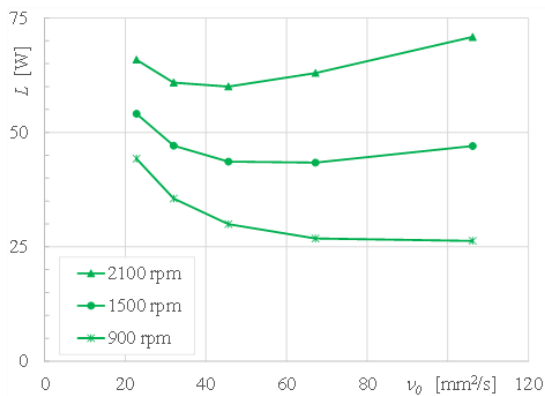


Fig. 7 VG effects on power loss (L) in terms of kinematic viscosity (ν_0) at 40°C (21 MPa)

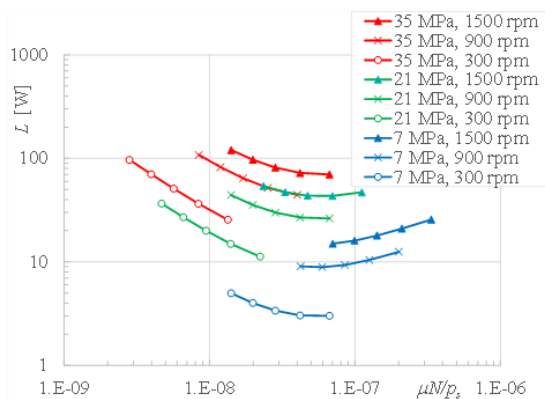


Fig. 8 Relationship between power loss (L) and operating parameter ($\mu N/p_s$)

Under the same μ , $\mu N/p_s$ would have the same value for the combination of $(p_s, N) = (7 \text{ MPa}, 300 \text{ rpm}), (14 \text{ MPa}, 600 \text{ rpm}), (21 \text{ MPa}, 900 \text{ rpm}), (28 \text{ MPa}, 1200 \text{ rpm})$ and $(35 \text{ MPa}, 1500 \text{ rpm})$. In Fig. 8, L is minimised at (21 MPa, 900 rpm) (additionally, (35 MPa, 1500 rpm), (21 MPa, 1500 rpm), (7 MPa, 900 rpm) and (7 MPa, 300 rpm)). Hence, L is minimised at $\mu N/p_s \approx (4\text{--}7) \times 10^{-8}$ over the various operating conditions, corresponding to VG 68–100.

Moreover, in Fig. 9, T_{max} is minimised at the specific conditions: (35 MPa, 1500 rpm) and (21 MPa, 1500 rpm); additionally, (7 MPa, 900 rpm). T_{max} was minimised at $\mu N/p_s \approx 5 \times 10^{-8}$, corresponding to VG 68. Further, in Fig. 10, all L_Q/L values are located on one curve against $\mu N/p_s$ under these numerical conditions. $\mu N/p_s \approx (4\text{--}7) \times 10^{-8}$ coincided with $L_Q/L \approx 0.4\text{--}0.3$. These results indicate that an optimum hydraulic oil with a specific VG can be selected for given operating conditions of p_s and N . Otherwise, a preferable operating condition is established to determine a specific VG oil.

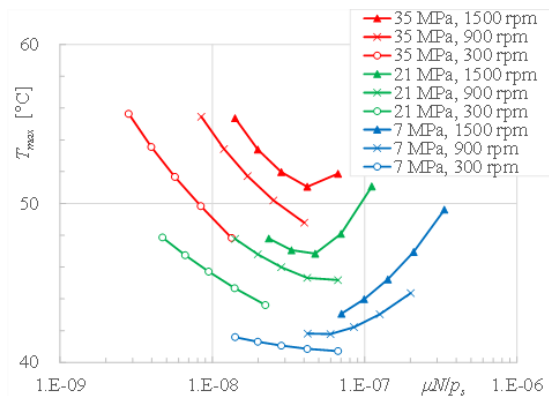


Fig. 9 Relationship between maximum temperature (T_{max}) and operating parameter ($\mu N/p_s$)

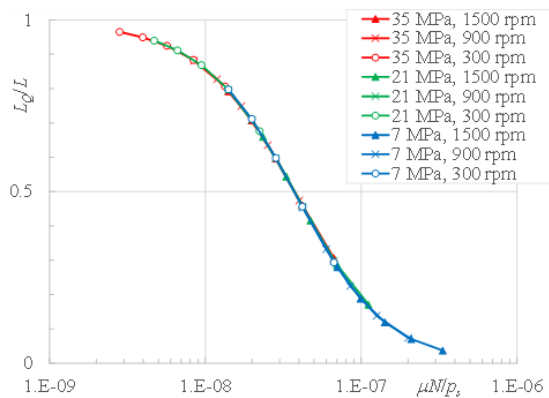


Fig. 10 Relationship between power loss ratio (L_Q/L) and operating parameter ($\mu N/p_s$)

4. Conclusion

Using a THL theory-based slipper model and considering the oil viscosity changes against the temperature distribution in the film, an optimum viscosity of five hydraulic oils with ISO VG 22–100 was explored. Under the operating conditions of a supply pressure of 7–35 MPa and rotational speed of 300–1500 rpm (5–25 rps), an optimum kinematic viscosity was numerically determined in terms of minimised power losses and temperature increment.

Conflicts of Interest

The author declares that there is no conflict of interest.

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