Proposal for a Wavelength-Independent Optical Sensor Based on an Asymmetric Mach-Zehnder Interferometer

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A wavelength-independent optical sensor based on an asymmetric Mach-Zehnder interferometer (AMZI) is proposed. The optical sensor based on an AMZI is very sensitive to wavelength, and wavelength drift will lead to measurement error. The optical sensor is compensated to reduce its dependence on wavelength. The insensitivity of the optical sensor to wavelength mainly depends on the compensation structure, which is composed of an AMZI cascaded with another AMZI and can compensate the wavelength drift. The influence of wavelength drift on the optical sensor can be counteracted by carefully designing the size parameters of the compensation structure. When the wavelength changes from 1549.9 nm to 1550.1 nm, the error after compensation can be lower than 0.066%. Furthermore, the effect of fabrication tolerance on compensation results is analyzed. The proposed compensation method can also be used to compensate the drift of other parameters such as temperature, and can be applied to the compensation of other interference-based optical devices.

Keywords: Optical pressure sensor, Wavelength independent, Asymmetric Mach-Zehnder interferometer, Compensation structure

OCIS codes: (220.4610) Optical fabrication; (230.7380) Waveguides, channeled; (280.4788) Optical sensing and sensors

I. INTRODUCTION

A complex optical system requires many kinds of optical devices, such as a laser, optical fiber, optical switching device, optical delay device, nonlinear optical device, optical modulator, detector, optical attenuator, optical gyroscope, optical sensor. Moreover, many optical devices adopt the principle of interference, such as those based on the AMZI [1-3] or Fabry-Perot (FP) cavity [4, 5], which feature low insertion loss, simple structure, and ease of manufacture, and are widely used in the fields of optical-fiber communication and sensing. These include AMZI-based optical filters [6], optical amplifiers [7], optical switches, AMZI-coupled ring resonators [8], and optical sensors [9-13]; optical devices based on the FP cavity include lasers [14], erbium-doped fiber lasers, tunable filters [15], various optical sensors [16-19], and more. Most of the sensors based on the AMZI or FP cavity perceive the change in measurement parameters by detecting intensity, but nonmeasurement parameters can have an impact on the sensor’s measurement results. For an optical sensor based on an AMZI, changes in wavelength also affect the measurement results. The relationship between the nonmeasurement parameters and output light intensity of the sensor satisfies a sinusoidal curve. In addition, the relationship between wavelength and output light intensity of an interference optical device is also sinusoidal. Therefore, the influence of many non-measurement parameters on output light intensity of an interference optical device is similar to that of wavelength on the output light intensity of an AMZI.

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The wavelength drift of the light source is derived from the aging of the light source itself, and the change in the ambient temperature. In this study the influence of the light source’s wavelength drift on the system is analyzed. According to the actual application scenario, the wavelength range of the light source is set to determine the influence of wavelength change on the system. The transfer function of the output of the optical sensor with a change in wavelength is analyzed. Then, through the compensation structure we design, it is used to compensate the wavelength drift of the optical sensor based on an AMZI. Furthermore, better compensation can be obtained by optimizing the size of the structure. The proposed optical compensation structure is composed of an AMZI optical sensor cascaded with another AMZI. The error before and after compensation is analyzed. The results show that a well-designed compensation structure can reduce the influence of wavelength on the optical sensor. This compensation mechanism also can be used to compensate the drift of other nonmeasurement parameters, and can be applied to other interference-based optical devices.

II. BASIC THEORY

For an AMZI structure, the relationship between wavelength and output light intensity is sinusoidal, and many other optical devices have a similar transmission curve, such as the FP cavity and the directional coupler (DC).

For a DC with waveguide width of 0.5 µm, waveguide spacing of 0.1 µm, core and cladding refractive indices of 3.4 and 1.0 respectively, and couple length of 1 mm, the transmission curve is represented by red the dashed line in Fig. 1. The result for a FP cavity with cavity width of 48.4365 µm and refractive index of 1.46 is represented by the green dash-dotted line in Fig. 1. An AMZI with arm-length difference of 96.873 µm and waveguide effective refractive index of 1.46 is also indicated in Fig. 1, by the blue solid line.

Figure 1 shows that the three curves basically coincide. Therefore, the transmission curves of many optical devices whose working principle is interference can be equivalent to that of an AMZI.

A general AMZI structure is shown in Fig. 2. It consists of two couplers and two interference arms of different lengths. After the light wave enters, it is divided along two paths by the 3-dB coupler. After passing through the two interference arms of lengths \( L_1 \) and \( L_2 \), and another 3-dB coupler, the light waves traveling along the two paths interfere and combine into a single output light wave. When sensing, under the influence of changes in the external environment the optical waveguide will expand or contract and the refractive index will change, which will cause the optical-path difference and phase between the two arms to change. The optical-path difference changes as

\[
\Delta L = L_1 - L_2. \tag{1}
\]

The phase difference between the two arms changes as

\[
\Delta \varphi = \frac{2 \pi}{\lambda} n_{\text{eff}} \Delta L. \tag{2}
\]

The ratio of output power to input power can be expressed as

\[
P_{\text{out}} / P_{\text{in}} = \frac{1}{2} (1 + \cos \Delta \varphi). \tag{3}
\]

In these expressions \( P_{\text{out}} \) is the output power, \( P_{\text{in}} \) is the input power, \( \Delta \varphi \) is the phase difference between the two interference arms of the AMZI, \( \lambda \) is the wavelength, \( n_{\text{eff}} \) is the effective refractive index of the waveguide, and \( \Delta L \) is the length difference between the two interference arms of the AMZI.

For a general AMZI structure, the power ratio between \( L_1 \) and \( L_2 \) is \( a (1-a) \). In waveguide optics this can be realized by a multimode interference structure [20]. The output light’s power can be expressed as

\[
P_{\text{out}} = \left[ aE_{\text{in}} e^{i\omega t} + (1-a)E_{\text{in}} \right] \left[ aE_{\text{in}} e^{i\omega t} + (1-a)E_{\text{in}} \right]^* \\
= [aE_{\text{in}} (\cos \Delta \varphi + i \sin \Delta \varphi) + (1-a)E_{\text{in}}] [aE_{\text{in}} (\cos \Delta \varphi + i \sin \Delta \varphi) + (1-a)E_{\text{in}}]^* \\
= [(a \cos \Delta \varphi + 1-a) + i a \sin \Delta \varphi] E_{\text{in}} [(a \cos \Delta \varphi + 1-a) - i a \sin \Delta \varphi] E_{\text{in}} \\
= P_{\text{in}} [(a \cos \Delta \varphi + 1-a)^2 - (i a \sin \Delta \varphi)^2] \\
= P_{\text{in}} [2a^2 - 2a + 1 + (2a - 2a^2) \cos \Delta \varphi], \tag{4}
\]
where $E_{in}$ is the electric field intensity of the input light, and $P_{in}$ and $P_{out}$ are the input and output optical power respectively. Letting $b = 2a^2 - 2a + 1$, we can obtain

$$P_{out} = b + (1 - b) \cos \Delta \phi .$$

We next define $P' = P_{out} / P_{in}$. The $(P')_{\text{min}} / (P')_{\text{max}}$ of the AMZI changes with $a$, as shown by the pink curve in Fig. 3. When $a$ changes from 0 to 0.5 and from 0.5 to 1, the corresponding $(P')_{\text{min}} / (P')_{\text{max}}$ curve is symmetric with respect to $a = 0.5$.

### III. COMPENSATION PRINCIPLE

The output of the optical sensor is very sensitive to the wavelength, and wavelength drift causes great sensing error. To make the optical sensor function normally in a working environment, it is necessary to eliminate the influence of other parameters. Using the inherent characteristic of the AMZI, that is, the output changes with wavelength, the error caused by wavelength drift can be compensated. It is found that adding an AMZI structure in front of or behind the original AMZI structure has an obvious effect on compensation for wavelength drift.

The optical sensor based on an AMZI is compensated, and the schematic diagram of a self-compensating optical sensor is shown in Fig. 4. It consists of two AMZIs in series: one is the sensing AMZI, and the other is the compensating AMZI. The refractive index of the compensation area does not change with the external environment, while the refractive index of the sensing area does. The AMZI’s power splitter and coupler are in asymmetric multimode interference, which can realize any proportion of power distribution [20]. Through a compensating structure, the influence of wavelength drift on the sensor can be curtailed, and the stability and accuracy of the sensor can be improved.

According to Eq. (5), the transmission function of the sensing AMZI can be expressed as

$$\frac{P_{\text{out}}}{P_{\text{in}}} = b + (1 - b) \cos \Delta \phi_1,$$

where $\Delta \phi_1 = \frac{2\pi}{\lambda} n_{\text{eff}} \cdot \Delta L_1 / \lambda$ is the phase difference between the two arms of the sensing AMZI, and $n_{\text{eff}}$ and $\Delta L_1$ are the effective refractive index and arm-length difference of the sensing AMZI respectively.

The compensating AMZI’s transmission function can be expressed as

$$\frac{P_{\text{out}}}{P_{\text{in}}} = b + (1 - b) \cos \Delta \phi_2,$$

where $\Delta \phi_2 = \frac{2\pi}{\lambda} n_{\text{eff}} \cdot \Delta L_2 / \lambda$ is the phase difference between the two arms of the compensating AMZI, and $n_{\text{eff}}$ and $\Delta L_2$ are the effective refractive index and arm-length difference of the compensating AMZI respectively.

Adjusting the arm-length difference can change the phase difference between the two AMZIs. The phases of the AMZIs are

$$\Delta \phi_1 = \frac{2\pi}{\lambda_0} n_s(x) \cdot \Delta L_1, \quad \Delta \phi_2 = \frac{2\pi}{\lambda_0} n_1 \cdot \Delta L_2,$$

where $n_s(x)$ is the refractive index that changes with the sensing environment, and $x$ is the sensing parameter (temperature, pressure, etc.). In the initial state $x_0$, we have $n_s(x_0) = n_1$. By this point, thus

$$\Delta \phi_1 = \Delta \phi_1 + \Phi,$$

$$\Phi = \frac{2\pi}{\lambda_0} n_1 \cdot \Delta L_2 - \frac{2\pi}{\lambda_0} n_s(x) \cdot \Delta L_1 - \frac{2\pi}{\lambda_0} n_1 \cdot dL,$$

where $\Phi$ (value $0-2\pi$) is the difference in phase differences between the two AMZIs, and $dL$ is the difference in arm-length differences between the AMZIs.
The final sensing curve can be expressed as

\[
\left( \frac{P_{\text{out}}}{P_{\text{in}}^{\text{final}}} \right) = \left( \frac{P_{\text{out}}}{P_{\text{in}}^1} \right) \times \left( \frac{P_{\text{out}}}{P_{\text{in}}^2} \right)
\]

\[
= [h_1 + (1-h_1)\cos \Delta \phi_1] [h_2 + (1-h_2)\cos \Delta \phi_2].
\]  

When \( x = x_0 \), the final sensing curve can be expressed as

\[
\left( \frac{P_{\text{out}}}{P_{\text{in}}^{\text{final}}} \right) = \left( \frac{P_{\text{out}}}{P_{\text{in}}^1} \right) \times \left( \frac{P_{\text{out}}}{P_{\text{in}}^2} \right)
\]

\[
= [h_1 + (1-h_1)\cos \frac{2\pi}{\lambda_0} \cdot n_1 \cdot \Delta L_1]
\]

\[
\cdot [h_2 + (1-h_2)\cos \frac{2\pi}{\lambda_0} \cdot n_2 \cdot \Delta L_2 + \Phi].
\]  

When the wavelength does not drift, the final sensing curve can be written as

\[
\left( \frac{P_{\text{out}}}{P_{\text{in}}^{\text{final}}} \right) = \left( \frac{P_{\text{out}}}{P_{\text{in}}^1} \right) \times \left( \frac{P_{\text{out}}}{P_{\text{in}}^2} \right)
\]

\[
= [h_1 + (1-h_1)\cos \frac{2\pi}{\lambda_1} \cdot n_1 \cdot \Delta L_1]
\]

\[
\cdot [h_2 + (1-h_2)\cos \frac{2\pi}{\lambda_0} \cdot n_2 \cdot \Delta L_2 + \Phi].
\]  

When the wavelength drifts negatively to \( \lambda_1 - \Delta \lambda \), the final sensing curve can be written as

\[
\left( \frac{P_{\text{out}}}{P_{\text{in}}^{\text{final}}} \right) = \left( \frac{P_{\text{out}}}{P_{\text{in}}^1} \right) \times \left( \frac{P_{\text{out}}}{P_{\text{in}}^2} \right)
\]

\[
= [h_1 + (1-h_1)\cos \frac{2\pi}{\lambda_1} \cdot n_1 \cdot \Delta L_1]
\]

\[
\cdot [h_2 + (1-h_2)\cos \frac{2\pi}{\lambda_0} \cdot n_2 \cdot \Delta L_2 + \frac{\Delta \lambda}{\lambda_0} \cdot \Phi].
\]  

When the wavelength drifts positively to \( \lambda_2 + \Delta \lambda \), the final sensing curve can be written as

\[
\left( \frac{P_{\text{out}}}{P_{\text{in}}^{\text{final}}} \right) = \left( \frac{P_{\text{out}}}{P_{\text{in}}^1} \right) \times \left( \frac{P_{\text{out}}}{P_{\text{in}}^2} \right)
\]

\[
= [h_1 + (1-h_1)\cos \frac{2\pi}{\lambda_2} \cdot n_1 \cdot \Delta L_1]
\]

\[
\cdot [h_2 + (1-h_2)\cos \frac{2\pi}{\lambda_0} \cdot n_2 \cdot \Delta L_2 + \frac{\Delta \lambda}{\lambda_0} \cdot \Phi].
\]  

If \( t_1 \) represents the transmission curve of the central wavelength \( \lambda_0 \), \( t_2 \) represents the transmission curve of the central wavelength negatively drifted to \( \lambda_1 \), and \( t_3 \) represents the transmission curve of the central wavelength positively drifted to \( \lambda_2 \). The maximum sensing error \( E_{\text{max}} \) after wavelength drift is expressed as

\[
E_{\text{max}} = \max \left[ \min \left( t_1(\lambda), t_2(\lambda), t_3(\lambda) \right) \right], \lambda \in [\lambda_1, \lambda_2].
\]  

\[
[\lambda_1, \lambda_2] \text{ is the range of wavelength drift, and } E_{\text{max}} \text{ is the maximum sensing error within the sensing range of refractive-index change, } [n_1, n_2].
\]  

IV. DESIGN OPTIMIZATION AND PERFORMANCE ANALYSIS OF COMPENSATION STRUCTURE

\( E_{\text{max}} \) can be reduced by adjusting \( b_1 \), \( b_2 \), \( AL_{1_1} \), and \( AL_{2_2} \). In the following analysis the wavelength-drift range is 1549.9-1550.1 nm. We take a SiO₂ sensor as the first example for compensation.

First, the influence of \( \Phi \) on sensing is analyzed as follows: Set the effective refractive-index range of the sensor to [1.46,1.4601]. Therefore the effective refractive index of the compensating AMZI is 1.46. The values of \( b_1 \) and \( b_2 \) are both 0.8, and \( AL_{1_1} = 425.386116915 \) μm. \( \Phi \) changes with \( AL_{2_2} \). Figure 5 shows the trend of \( E_{\text{max}} \) with \( \Phi \); it can be seen that the sensing error is smaller when \( \Phi = 1.2\pi \).

Next, the influence of \( b_1 \) and \( b_2 \) on the sensor is analyzed.

According to the results of Fig. 5, let \( \Phi = 1.2\pi \) and \( AL_{1_1} = 425.386116915 \) μm. Figure 6 shows the trend of \( E_{\text{max}} \) changing with \( b_1 \) and \( b_2 \), and it can be seen that a smaller \( E_{\text{max}} \) can be realized when \( b_1 = b_2 \). Figure 7 shows the value of \( E_{\text{max}} \) when \( b_1 = b_2 = 0.8 \); it can be seen that when \( b_1 = b_2 = 0.8 \), \( E_{\text{max}} \) is about 0.1034, reaching the minimum.

Finally, when \( \Phi = 1.2\pi \) and \( b_1 = b_2 = 0.8 \), there are multiple options for \( AL_{1_1} \) and \( AL_{2_2} \). The value of AMZI arm-length difference \( AL_{1_1} \) is analyzed, and the results are shown
in Table 1. This table shows that $E_{\text{max}}$ increases with increasing of $\Delta L_1$. In other words, for a specified value of $E_{\text{max}}$, the smaller the arm length difference, the larger the effective-index dynamic range of the sensor. The maximum sensing error and the dynamic range of effective-index change can be measured according to the demands of the specific application.

After another round of optimization, when $b_1 = b_2 = 0.8$, $\Delta L_1 = 425.386116915\,\mu m$, and $\Delta L_2 = 426.0083\,\mu m$ ($\Phi = 1.175\pi$), $E_{\text{max}}$ is reduced to 0.06606%.

The compensation of optical sensors based on lithium niobate and silicon is also analyzed in the same way. The refractive index of lithium niobate is about 2.2, and that of silicon is about 3.4. The sensing area of the lithium niobate sensor is set to be $[2.2,2.2001]$, and that of the silicon sensor is set as $[3.4,3.4001]$. The $b$ value of the AMZI is 0.8. The parameter design and results before and after compensation of the optical sensors are shown in Table 2. It can be seen that for the three materials, the sensing error...
is reduced from 8.9% to below 0.066% in some cases.

The sensing curves before and after compensation in Table 2 are shown in Figs. 8, 9, and 10 respectively. It can be seen that the compensated results are satisfying, and the sensing curves almost coincide.

V. FABRICATION TOLERANCE ANALYSIS

In this section, the influence of the error in the sensor-fabrication process is analyzed using a two-dimensional calculation.

The influence of waveguide width on the measurement results is analyzed. The width of the waveguide layer is 4 µm, the refractive index of the core layer is 1.464821, and that of the cladding layer is 1.45. When the width of the waveguide increases or decreases by 0.1 µm, the Transverse Electric (TE) effective index of the waveguide changes to 1.4601374 and 1.459857, respectively. For this situation, the sensing curve after compensation is shown in Fig. 11. The maximum error in Fig. 11(a) is 0.2406%, and that in Fig. 11(b) is 0.7284%.

Generally, the influence of the fabrication process on the length of the two interference arms of the AMZI is the same, so ΔL is almost constant. In spite of this, the change in sensing curve when ΔL has errors due to other special reasons is analyzed. Figure 12 shows the sensing curve when the arm-length difference of the two AMZIs increases or decreases by 0.1µm at the same time. The maximum error in Fig. 12(a) is 0.3713%, and that in Fig. 12(b) is 1.007%.

From Figs. 11 and 12, the error caused by the manufacturing process is not conducive to sensing. A change in waveguide width will change the effective-index range and increase the sensing error, and error in arm-length difference will also increase sensing error. Nonetheless, for a manufacturing error of ±0.1 µm, the measurement error can still be held below 1%.

FIG. 9. For the optical sensor made of lithium niobate, the comparison of the sensing curves between (a) uncompensated and (b) compensated systems.

FIG. 10. Based on the silicon optical sensor, the comparison of the sensing curves between (a) uncompensated and (b) compensated systems.
VI. CONCLUSION

A wavelength-independent optical sensor based on the AMZI is introduced. The compensation structure consists of two AMZIs in series, one as a sensor and the other as a compensator. For optical sensors based on silicon dioxide, lithium niobate, and silicon, the transmission curves with and without a compensation structure are analyzed. The error when using a compensation structure is less than 0.066%, which is only 0.8% of without compensation. At the same time, the variation range of output light intensity after compensation is reduced to about 78% of that without compensation. Finally, the fabrication tolerance is analyzed, and the sensing error can be less than 1% for a fabrication tolerance of ±0.1 µm. This compensation structure could also be used to compensate for the drift of other nonmeasurement parameters, such as temperature, and could be applied to other interference-based optical devices.

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