


## ORIGINAL ARTICLE

# Compact tri-wideband bandpass filter with multiple transmission zeros

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This paper presents a tri-wideband bandpass filter (TWB-BPF) with compact size, high band-to-band isolation, and multiple transmission zeros (TZs). The proposed TWB-BPF is based on a multiple-mode resonator (MMR), which is interpreted by the method of the even- and odd-mode analysis technique. The MMR can excite 11 resonant modes, where the first two modes comprise the first passband, the next four modes form the second passband, and the last five modes are used to generate the third passband. In addition, 10 TZs are yielded to obtain high band-to-band isolation and wide stopband suppression characteristics up to  $14.95f_{c1}$  ( $f_{c1}$  is the center frequency of the first passband). To verify the proposed filter, a TWB-BPF with 3-dB fractional bandwidths (FBWs) of 37.4%, 43.5%, and 40.4% is designed, fabricated, and measured.

**KEYWORDS**

bandpass filter, multi-mode resonator, transmission zeros, tri-wideband, wide stopband

## 1 | INTRODUCTION

To meet the requirements of high data rate, high transmission capacity, and multiple services in modern communication systems, there have been accelerated developments to realize radio-frequency (RF) front-ends that are multi-band and broadband. In recent years, multi-band bandpass filters (BPFs) have attracted much interest. For example, various excellent works that focused mainly on multi-band and high selectivity have been reported [1–17]. In [1–5], step-impedance resonators are widely employed to design dual-band, tri-band, and quad-band BPFs. The method of combining several BPFs or resonators with common input/output ports is a straightforward and effective approach to design multi-band BPFs [6–9]. Using this approach, single-band, dual-band, tri-band, quad-band, and quint-band BPFs can be easily achieved [6]. In [10,11], the concept of signal multipath transmission is used to design high-performance tri-band BPFs. Owing to the merits of their simple structure

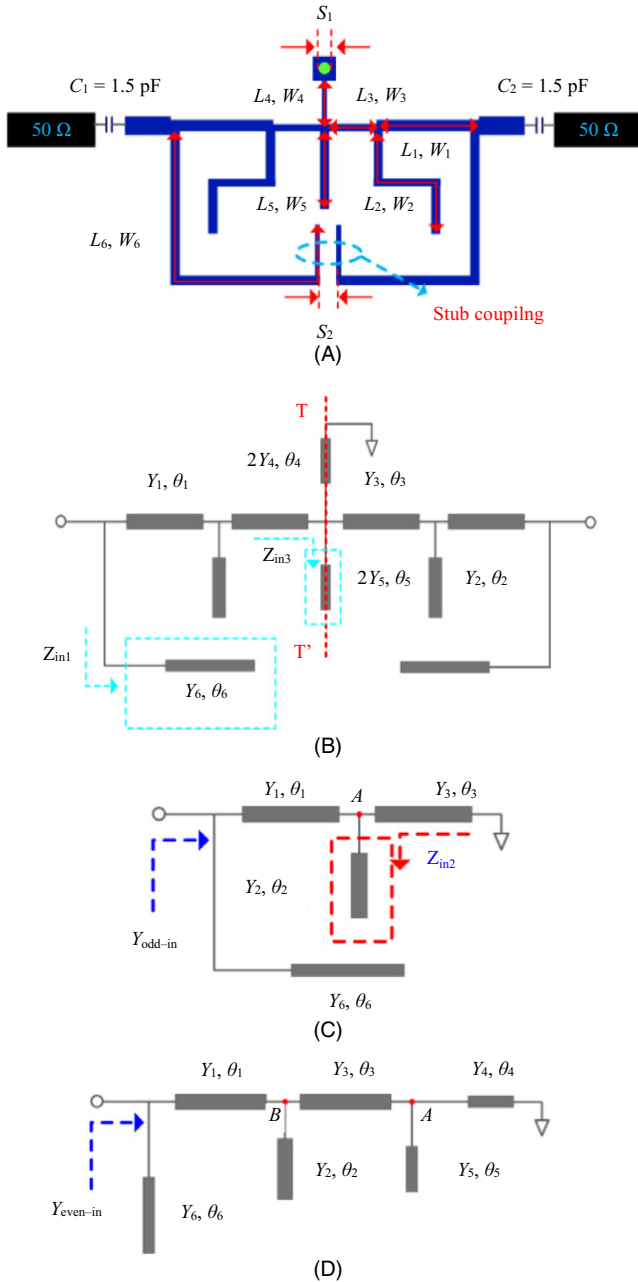
and controllable resonant frequencies, multiple-mode resonators (MMRs) are also widely used to design multi-band BPFs [12–18]. In [12], a very closely spaced passband and highly selective dual-band BPF are developed using MMR. Although the filters [1,3–6,8–14,18] have demonstrated their high performances, the narrow bandwidth is still insufficient to meet the requirements of broadband wireless communication systems. To solve this issue, several dual-/tri-wideband BPFs were developed to satisfy those requirements. The 3-dB fractional bandwidths (FBWs) of these reported multi-wideband BPFs are mainly about 10%–20%, while a TWB-BPF with 3-dB FBWs >40% is occasionally reported. Moreover, the notch-like stopband characteristics of these multi-wideband BPFs need to be further improved.

In this paper, a compact TWB-BPF based on a novel MMR, which is interpreted using the even- and odd-mode analysis method, is presented. The filter has a high band-to-band isolation and wide stopband suppression characteristics up to  $14.95f_{c1}$ . The center frequencies (CFs) of the TWB-

BPF are 1.07 GHz, 3.25 GHz, and 8.32 GHz with 3-dB FBWs of 37.4%, 43.5%, and 40.4%, respectively. To verify these results, a TWB-BPF with compact size, high band-to-band isolation, and wide upper stopband suppression was designed, fabricated, and measured. The measured and full-wave electromagnetic simulated results of the TWB-BPF agree well with each other.

## 2 | DESIGN OF TWB-BPF

Figure 1 shows the configuration of the proposed MMR, which consists of a cross-shaped resonator (denoted by  $(L_1, W_1)$ ,



**FIGURE 1** Proposed TWB-BPF (A) layout, (B) TLM, (C) odd-mode equivalent circuit, and (D) even-mode equivalent circuit

$(W_1)$ ,  $(L_3, W_3)$ ,  $(L_4, W_4)$ , and  $(L_5, W_5)$ ) with shorted circuit termination, and two sets of symmetrical stub-loaded resonators (denoted by  $(L_2, W_2)$ ,  $(L_6, W_6)$ , and  $(L_7, W_7)$ ). Figure 1A shows the layout of the proposed TWB-BPF. Figure 1B illustrates the transmission-line model (TLM) of the TWB-BPF. Considering that the structure is symmetrical with the T-T' plane, the even- and odd-mode analysis technique was employed to analyze this MMR. Figure 1C and D, respectively, show the odd-mode and even-mode equivalent circuits.

As illustrated in Figure 1C,  $Y_{odd-in}$  denotes the input admittance under odd-mode excitation. Likewise,  $Y_{even-in}$  represents the input admittance under even-mode excitation, as shown in Figure 1D. For simplicity, the parameter  $L_7$  is neglected. According to the transmission-line theory, we can derive the following results.

$$Y_{odd-in} = \frac{Y_1(Y_{inA} + jY_1 \tan \theta_1)}{Y_1 + jY_{inA} \tan \theta_1} + jY_6 \tan \theta_6, \quad (1)$$

$$Y_{inA} = j(Y_2 \tan \theta_2 - Y_3 \cot \theta_3), \quad (2)$$

$$Y_{even-in} = \frac{Y_1(Y_{inB} + jY_1 \tan \theta_1)}{Y_1 + jY_{inB} \tan \theta_1} + jY_2 \tan \theta_2, \quad (3)$$

$$Y_{inB} = \frac{Y_3(Y_{inA} + jY_3 \tan \theta_3)}{Y_3 + jY_{inA} \tan \theta_3} + jY_2 \tan \theta_2, \quad (4)$$

$$Y_{inA} = j(Y_5 \tan \theta_5 - Y_4 \cot \theta_4), \quad (5)$$

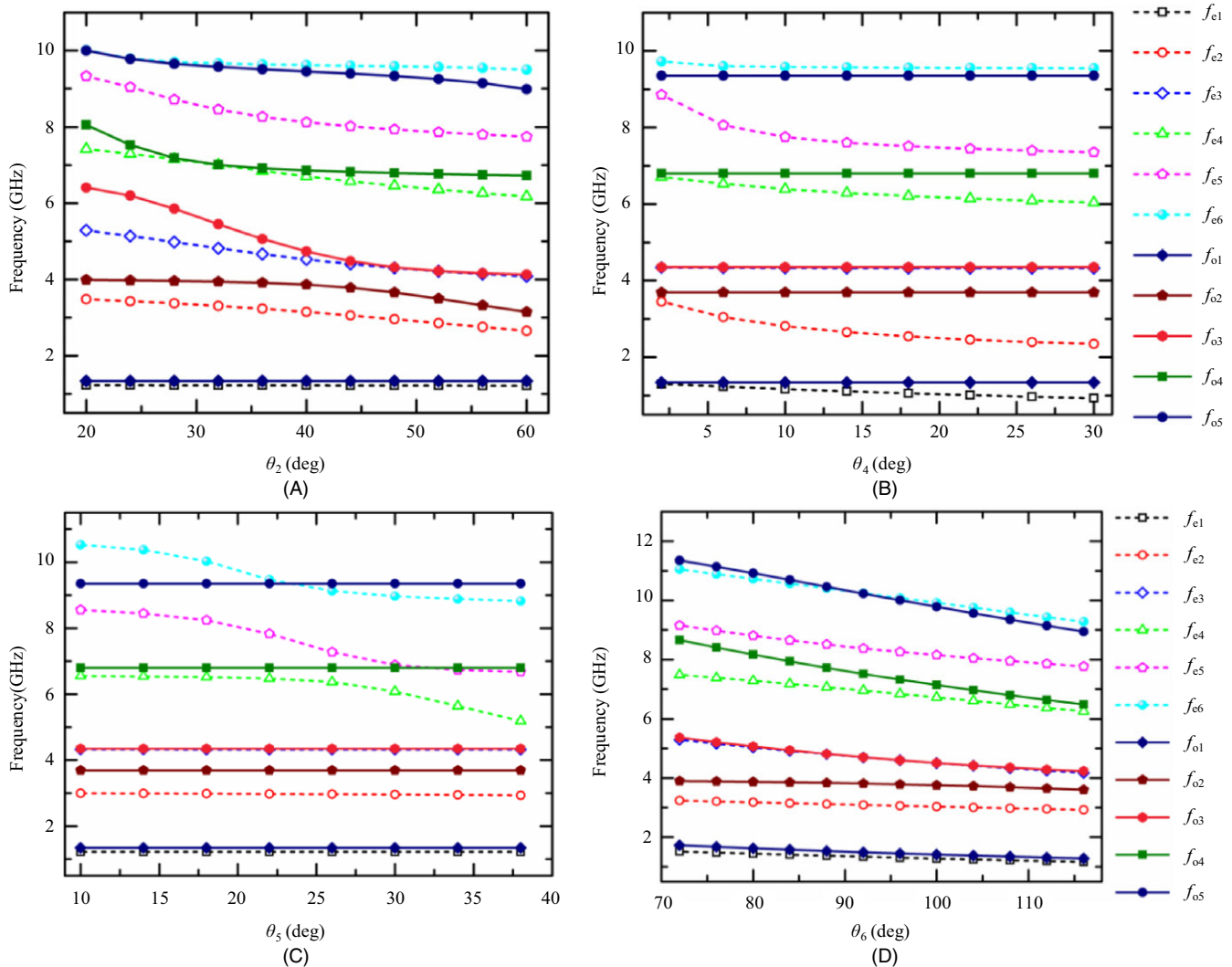
where  $Y_n$  ( $n = 1, 2, 3, 4, 5$ , and  $6$ ) and  $\theta_n$  ( $n = 1, 2, 3, 4, 5$ , and  $6$ ) represent the characteristic admittance and electrical length, respectively. For simplicity, we let the center frequency  $f_0 = 2.4$  GHz (reference frequency for electrical length calculation),  $Y_3 = 1/160$  S,  $Y_1 = Y_2 = Y_4 = Y_5 = Y_6 = 0.01$  S. According to the resonant condition, we have:

$$\text{Im}(Y_{odd-in}) = 0, \quad (6)$$

$$\text{Im}(Y_{even-in}) = 0. \quad (7)$$

As an example, the circuit parameters are set as  $\theta_1 = 45^\circ$ ,  $\theta_2 = 47^\circ$ ,  $\theta_3 = 10^\circ$ ,  $\theta_4 = 7^\circ$ ,  $\theta_5 = 21^\circ$ ,  $\theta_6 = 106^\circ$ ,  $Z_1 = Z_2 = Z_4 = Z_5 = Z_6 = 100 \Omega$ ,  $Z_3 = 80 \Omega$ , and  $Z_n$  ( $n = 1, 2, 3, 4, 5$ , and  $6$ ) denote the characteristic impedance. Therefore, the resonant frequencies can be solved numerically based on (6) and (7).

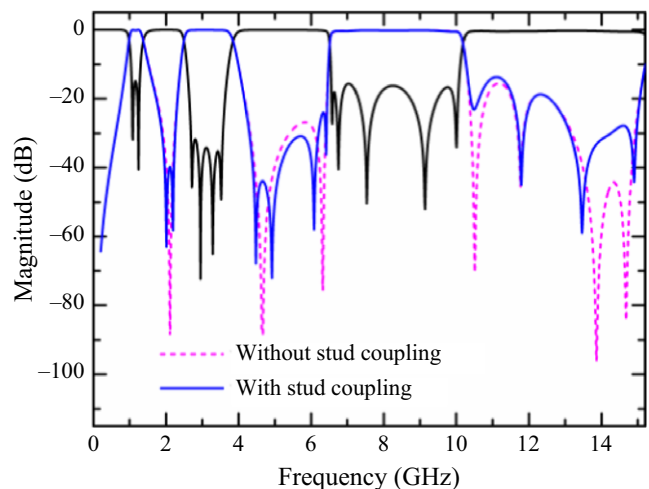
In detail, the initial circuit parameter values of the electrical lengths are calculated at  $f_0$ . When a certain frequency  $f_i$  is considered, the values of the electrical lengths can be redefined as  $\theta_n^* = \theta_n f_i / f_0$  ( $n = 1, 2, 3, 4, 5$ , and  $6$ ). Then, we substitute the updated values of the electrical lengths into (1–7). For example, if (6) is satisfied, it means that  $f_i$  is an odd-mode resonant frequency for which we are searching.



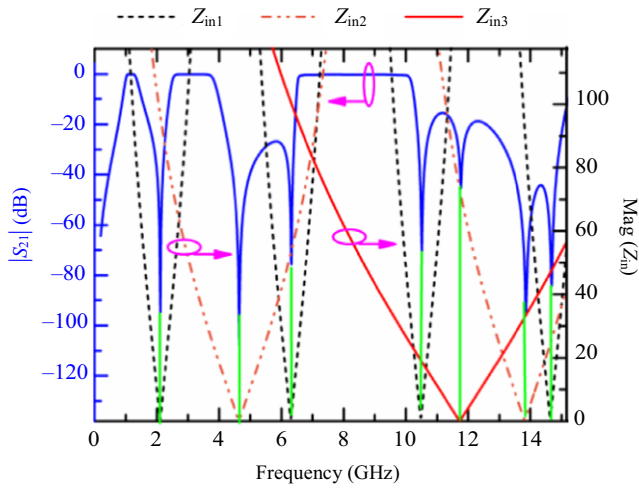
**FIGURE 2** Properties of resonance frequencies vs (A)  $\theta_2$ , (B)  $\theta_4$ , (C)  $\theta_5$ , and (D)  $\theta_6$

As shown in Figure 2, we investigate the resonant frequencies of the MMR vs various values of  $\theta_2$ ,  $\theta_4$ ,  $\theta_5$ , and  $\theta_6$ . As can be seen, 11 resonant modes have been excited, where  $f_{o1}$ ,  $f_{o2}$ ,  $f_{o3}$ ,  $f_{o4}$ , and  $f_{o5}$  denote the odd-mode resonant frequencies determined by (6), whereas  $f_{e1}$ ,  $f_{e2}$ ,  $f_{e3}$ ,  $f_{e4}$ ,  $f_{e5}$ , and  $f_{e6}$  represent the even-mode resonant frequencies determined by (7). It can be observed from Figure 2A that  $f_{ei}$  ( $i = 2, 3, 4, 5, 6$ ) and  $f_{oi}$  ( $i = 2, 3, 4, 5$ ) decrease with the increase in  $\theta_2$ , whereas  $f_{o1}$  and  $f_{e1}$  change slightly. As shown in Figure 2B,  $\theta_4$  mainly affects the resonant frequencies of  $f_{ei}$  ( $i = 1, 2, 4, 5, 6$ ) with  $f_{oi}$  ( $i = 1, 2, 3, 4, 5$ ) unchanged. As illustrated in Figure 2C,  $f_{e4}$ ,  $f_{e5}$ , and  $f_{e6}$  decrease dramatically, whereas the others resonant frequencies remain unchanged with the increase in  $\theta_5$ . As shown in Figure 2D, the 11 resonant frequencies decrease with the increase in  $\theta_6$ .

As illustrated in Figure 3, the frequency responses of the TWB-BPF are simulated using TLM. It can be



**FIGURE 3** Simulated results of frequency responses with and without stub coupling



**FIGURE 4** Frequency responses of  $|S_{21}|$  and  $Z_{in}$

observed that the filter has 11 transmission poles (TPs), where the first two poles compose the first passband, the next four poles form the second passband, and the last five

poles are used to construct the third one. It can be observed that three additional TZs are generated by introducing stub coupling. In order to determine how the TZs are generated, the relationship between TZ and  $Z_{in}$  is investigated, as shown in Figure 4. It can be found that a TZ will be generated at a certain frequency, where  $Z_{in} = 0$  is satisfied. This is attributed to the introduction of virtual ground to short out the transmission signals. Finally, the condition for the generation of TZs can be expressed as:

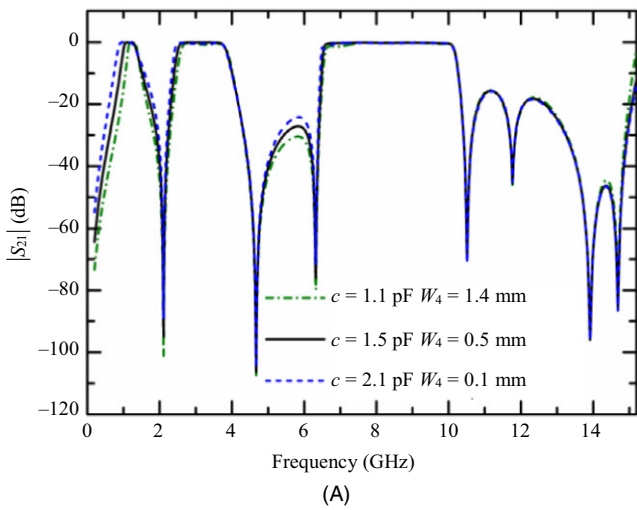
$$Z_{in1} = -jZ_6 \cot \theta_6 = 0, \quad (8)$$

$$Z_{in2} = -jZ_2 \cot \theta_2 = 0, \quad (9)$$

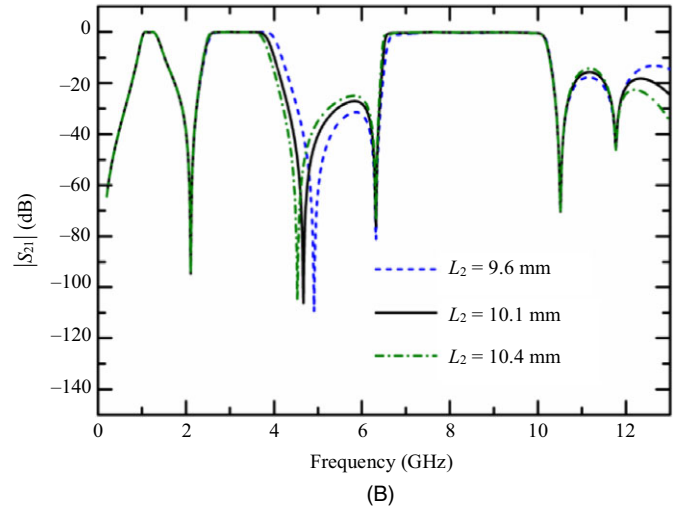
$$Z_{in3} = -jZ_5 \cot \theta_5 = 0. \quad (10)$$

That is,

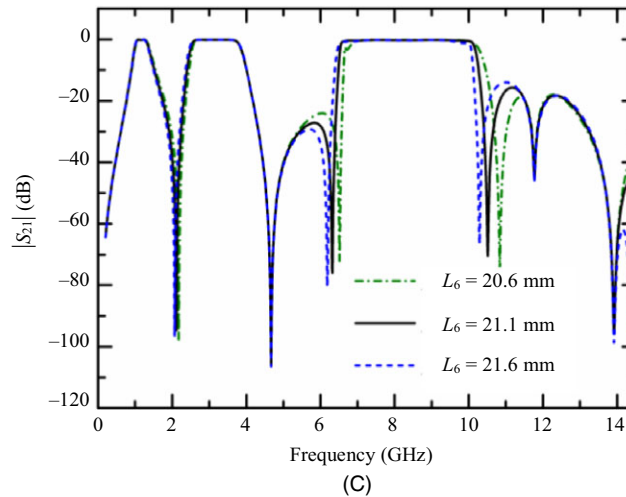
$$f_{TZ} = \frac{(2n+1)c}{4L_6\sqrt{\epsilon_{re}}} \quad (n = 0, 1, 2, \dots), \quad (11)$$



(A)

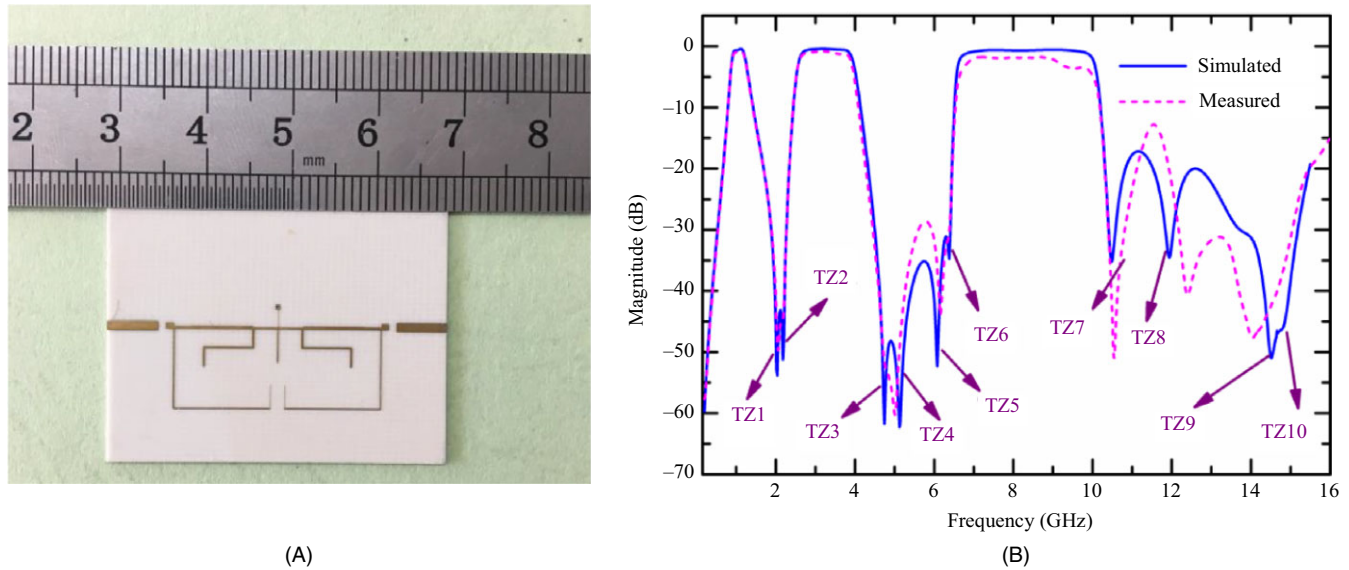


(B)



(C)

**FIGURE 5** Resonance properties vs (A) capacitance and  $W_4$ , (B)  $L_2$ , (c)  $L_6$



**FIGURE 6** (A) Photograph of the fabricated TWB-BPF, (B) simulated and measured results of the TWB-BPF

$$f_{TZ} = \frac{(2n+1)c}{4L_2\sqrt{\epsilon_{re}}} \quad (n = 0, 1, 2, \dots), \quad (12)$$

$$f_{TZ} = \frac{(2n+1)c}{4L_5\sqrt{\epsilon_{re}}} \quad (n = 0, 1, 2, \dots). \quad (13)$$

As shown in Figure 5A, the first passband can be adjusted by tuning the capacitance and  $W_4$ , while the second and third passbands remain almost unchanged. Figure 5B shows that the second passband can be shifted by changing  $L_2$ . Furthermore, the variation in  $L_2$  does not affect the other passbands. Figure 5C shows that  $L_6$  only affects the third passband.

### 3 | EXPERIMENTAL VERIFICATION

For validation, a TWB-BPF was fabricated on a substrate of Rogers 4003 with parameters:  $\epsilon_r = 3.38$ ,  $h = 0.508$  mm, and  $\tan \delta = 0.0027$ . The physical dimensions of this BPF were optimized by Sonnet 15.52, and the parameters are given as  $L_1 = 9.3$ ,  $W_1 = 0.45$ ,  $L_2 = 10.3$ ,  $W_2 = 0.3$ ,

$L_3 = 2.9$ ,  $W_3 = 0.3$ ,  $L_4 = 2.1$ ,  $W_4 = 0.1$ ,  $L_5 = 4$ ,  $W_5 = 0.2$ ,  $L_6 = 20.6$ ,  $W_6 = 0.2$ ,  $L_7 = 2.85$ ,  $W_7 = 0.1$ ,  $S_1 = 0.3$ , and  $S_2 = 1.6$  (unit: mm). The frequency responses of the simulated and measured results are shown in Figure 6. It can be observed that the measured CFs are centered at 1.07 GHz, 3.25 GHz, and 8.32 GHz with 3-dB FBWs of 37.4%, 43.5%, and 40.4%, respectively. The minimum insertion losses (ILs) of the three passbands are 0.75 dB, 0.83 dB, and 1.78 dB, respectively. It can be seen that the maximum band-to-band isolations are about 50 dB and 60.3 dB, respectively. A wide stopband suppression up to  $14.95f_{c1}$  with a rejection level of 13 dB was achieved. A comparison between this work and some reported tri-band BPFs is summarized in Table 1, and shows that the TWB-BPF has a low IL, compact size, and broad bandwidth.

### 4 | CONCLUSION

In this paper, we presented a compact TWB-BPF based on a novel MMR, and its resonant behavior was analyzed.

**TABLE 1** Comparison with some reported tri-band BPFs

Filter	CFs (GHz)	3-dB FBWs (%)	ILs (dB)	TPs/TZs	Size ( $\lambda_g \times \lambda_g$ )
[2]	1.9/5.65/9.2	53/17.7/10.87	3.65/3.65/3.65	6/2	$0.694 \times 0.076$
[3]	1.57/3.9/7	4.1/2/3	2.0/2.1/1.8	6/6	$0.145 \times 0.113$
[7]	2/3.6/5.5	18.5/10.1/13.2	3.0/3.0/3.0	6/6	$0.303 \times 0.156$
[11]	1.575/1.8/2.4	6.1/3.5/3.1	0.7/0.9/0.9	6/6	$0.21 \times 0.12$
[17]	1.25/3.5/6.82	24.4/18.3/13.8	0.45/0.42/1.26	6/7	$0.156 \times 0.149$
This work	1.07/3.25/8.32	37.4/43.5/40.4	0.75/0.83/1.78	11/10	$0.166 \times 0.073$

The proposed TWB-BPF has a wide bandwidth in each passband, a high band-to-band isolation, low IL, and wide stopband suppression, which makes the filter attractive for multiple services and broadband wireless communication systems.

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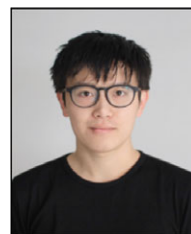
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