

Development of Models for Estimating Growth of Quinoa (*Chenopodium quinoa* Willd.) in a Closed-Type Plant Factory System

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Abstract. Crop growth models are useful tools for understanding and integrating knowledge about crop growth. Models for predicting plant height, net photosynthesis rate, and plant growth of quinoa (*Chenopodium quinoa* Willd.) as a leafy vegetable in a closed-type plant factory system were developed using empirical model equations such as linear, quadratic, non-rectangular hyperbola, and expolinear equations. Plant growth and yield were measured at 5-day intervals after transplanting. Photosynthesis and growth curve models were calculated. Linear and curve relationships were obtained between plant heights and days after transplanting (DAT), however, accuracy of the equation to estimate plant height was linear equation. A non-rectangular hyperbola model was chosen as the response function of net photosynthesis. The light compensation point, light saturation point, and respiration rate were 29, 813 and 3.4 $\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$, respectively. The shoot fresh weight showed a linear relationship with the shoot dry weight. The regression coefficient of the shoot dry weight was 0.75 ($R^2=0.921^{***}$). A non-linear regression was carried out to describe the increase in shoot dry weight of quinoa as a function of time using an expolinear equation. The crop growth rate and relative growth rate were 22.9 $\text{g}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ and 0.28 $\text{g}\cdot\text{g}^{-1}\cdot\text{d}^{-1}$, respectively. These models can accurately estimate plant height, net photosynthesis rate, shoot fresh weight, and shoot dry weight of quinoa.

Additional key words : crop growth rate, expolinear equation, photosynthesis rate, plant height

Introduction

A crop model is a simple representation of a crop, in general, it is used to study crop growth and calculate the growth of a specific species. There are many crop growth models that simulate physiological development, growth, and yield of crops on the basis of interactions between environmental variables and plant physiological processes (Miglietta and Bindi, 1993; Mo et al., 2005). Recently, crop growth models have been used to investigate the optimal control set points associated with plant factory operations (Ioslovich and Gutman, 2000), and these models have become an essential tool to support field research and to improve agricultural productivity. Also, crop growth models can be used in research, and applications such as yield predictions, agricultural planning, farm management, climatology and agrometeorology (Miglietta and Bindi, 1993).

A closed-type plant factory system is an automated facility for the production of plants; it provides the benefits of

consistent production of good quality vegetables, particularly through monitoring the growing conditions of the plants. Proper environmental control is essential for an increase in productivity and quality in plant factories (Morimoto et al., 1995).

Quinoa (*Chenopodium quinoa* Willd.) seed provides high nutritional values. The leaves and sprouts can also provide high nutritive values, as well as having high antioxidant and anticancer properties (Gawlik-Dzik et al., 2013; Paško et al., 2009; Schlick and Bubenheim, 1996); hence, there are a number of benefits to using these as vegetables. This experiment was carried out to collect basic data which could be used for the predicting potential effects on the growth rates of quinoa in a closed-type plant factory system.

Materials and Methods

1. Plant material

The experiment was conducted in a closed-type plant factory (700×500×300cm, L×W×H) at Jeju National University. The seeds were sown into 288 cells of a polyurethane sponge (2.5×2.5×2.5cm) in a plastic tray (30×23×6cm), and sub-irrigated once a day with tap water. Emerged seedlings

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with fully developed cotyledons were sub-irrigated once a day with a nutrient solution with electrical conductivity (EC) of $0.5\text{dS}\cdot\text{m}^{-1}$ and $1.0\text{dS}\cdot\text{m}^{-1}$ at intervals of one week before transplanting. At the fourth true leaf stage, plants were transplanted into plastic plugs in the holes of a trough. The plants were spaced 10cm apart within each trough and troughs were spaced 15cm apart ($67\text{plants}/\text{m}^2$). Plants were grown in the nutrient solution with an EC of $2.0\text{dS}\cdot\text{m}^{-1}$.

2. Closed-type plant factory system

Three-band radiation type fluorescent lamps (55W, Philips Co., Ltd., Amsterdam, the Netherlands) were used as the light source in the closed-type plant factory system. Light intensity (photosynthetic photon flux density, PPF) was measured with a quantum sensor (LI-190, Li-Cor Inc., Lincoln, NE, USA), and was maintained at $143\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$. The photoperiod was 16/8h (day/night). Temperature was maintained at $23\text{-}25^\circ\text{C}$, and relative humidity and CO_2 concentration were 50-70% and $400\text{-}600\mu\text{mol}\cdot\text{mol}^{-1}$, respectively. The nutrient film technique (NFT) system with three layers and four troughs per layer was used for the hydroponic system. Total volume of the nutrient solution in the tank was 90L and the nutrient solution was composed of 15 $\text{NO}_3\text{-N}$, 1 $\text{NH}_4\text{-N}$, 1 P, 7 K, 4 Ca, 2 Mg, 2 $\text{SO}_4\text{-S}$ $\text{mM}\cdot\text{L}^{-1}$. The EC of nutrient solutions was adjusted by mixing with tap water. The pH and EC of the nutrient solution in each treatment tank were measured daily, using a pH meter (HI 98106, Hanna Instruments Ltd., Leighton Buzzard, Bedfordshire, UK) and a portable conductivity meter (COM-100, HM Digital Inc., Culver City, CA, USA), respectively. The pH was adjusted to the range of 5.5-6.5 with potassium hydroxide (KOH) or phosphoric acid (H_3PO_4), and electrical conductivity was adjusted with concentrated nutrient solution or tap water as necessary. The nutrient solutions were supplied via semi-continuous nutrient cycling through the trough with the pump switching on or off every 10 minutes throughout the growing period. Nutrient solution was not renewed during the experimental period.

3. Measurements

Plant growth parameters including plant height, and fresh and dry weight of shoots were measured on 12 plants every 5 days after transplanting. Photosynthetic rate was measured 22 days after transplanting using a portable photosynthetic measurement system (Li-6400, Li-Cor Inc., Lincoln,

NE, USA). Plants were randomly selected with 10 replications, and measurements were made on fully expanded leaves.

4. Model construction and validation

Plant height was defined using the following linear and quadratic equations:

$$H = a\cdot\text{DAT} + b \text{ or } H = a + b\cdot\text{DAT} + c\cdot\text{DAT}^2 \quad (1)$$

where H is the plant height (cm), DAT is the number of days after transplanting (days), and a, b and c are constants.

Net photosynthetic rate (P_n) was defined with a non-rectangular hyperbola equation and was calculated according to Goudriaan and Van Laar (1994):

$$P_n = P_{\max} \cdot \{1 - \exp(-\alpha\text{PAR}/P_{\max})\} - R \quad (2)$$

where P_n is the net photosynthesis rate ($\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), P_{\max} is the potential photosynthesis rate ($\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), α is the initial gradient under low light conditions ($\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), PAR is the photosynthetic active radiation ($\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), and R is the photosynthesis rate ($\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$) at PAR 0.

The mathematical function used for expressing shoot dry weight by time is called an expolinear equation (Goudriaan and Monteith, 1990):

$$W_t = C_m/R_m \cdot \ln [1 + \exp\{R_m \cdot (t - t_b)\}] \quad (3)$$

where W_t is biomass (shoot dry weight, $\text{g}\cdot\text{m}^{-2}$) at t days from transplanting, C_m is the maximum crop growth rate ($\text{g}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$), R_m is the maximum relative growth rate ($\text{g}\cdot\text{g}^{-1}\cdot\text{d}^{-1}$) in the exponential growth phase, t is the time after transplanting (day), and t_b is the time at which the crop effectively reaches a linear phase of growth (lost time, d).

5. Statistical analysis

The experiment had a completely randomized design. Statistical analyses were carried out using the SAS system (Release 9.01, SAS institute Inc., Cary, NC, USA) and SigmaPlot (Version 9.01, Systat Software Inc. San Jose, CA, USA). The number of plants for making the plant height model was 16 plants, and the number of validated plants was 144 plants. Variables were estimated using the Gauss-Newton algorithm, a nonlinear least squares technique. The

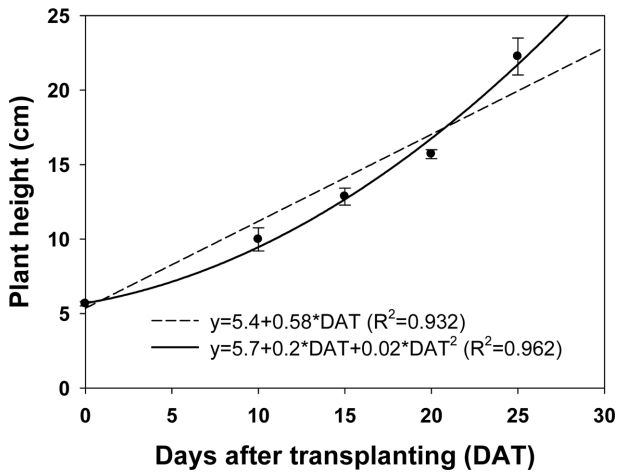


Fig. 1. Plant height changes of *Chenopodium quinoa* with days after transplanting (DAT). Linear and curve regression analyses were conducted for the modeling of plant height with DAT as a variable. Vertical bars indicated SE (n=4).

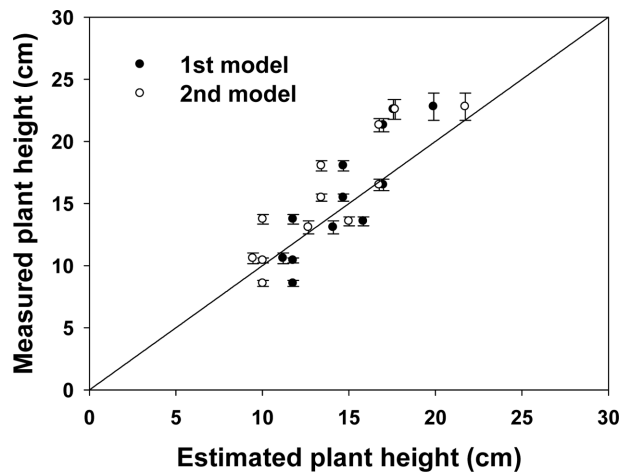


Fig. 2. Relationship between the estimated and measured plant height of *Chenopodium quinoa*. 1st model was $5.4+0.58 \cdot \text{DAT}$ and 2nd model was $5.7+0.2 \cdot \text{DAT}+0.02 \cdot \text{DAT}^2$. Vertical bars indicated SEs (n=12).

slopes, intercepts and regression coefficients of the models were compared using the SAS REG procedure. Correlation coefficients were calculated between the measured and estimated data.

Results and Discussion

Both linear and curve relationships were observed between the plant heights and days after transplantation (Fig. 1). The plant height model of quinoa was $5.4+0.58 \cdot \text{DAT}$ ($R^2=0.932$, $P<0.001$) or $5.7+0.2 \cdot \text{DAT}+0.02 \cdot \text{DAT}^2$ ($R^2=0.962$, $P<0.001$), producing a change in plant height of 0.58cm per day or 0.22cm per day. Measured and estimated plant heights were compared (Fig. 2). The linear or curve regression coefficients were 1.07 and 1.12, respectively. The measured and estimated plant heights were shown to be a reasonably good fit with two functions, however, a linear relationship was observed between plant height and days after transplantation. For example, when the distance between the light source and the plants is 30cm, they should be harvested in about 50 days after transplanting. Plant height is one of the most simple and important biomass yield components previous research has shown that increasing plant height is the most obvious and direct way to improve biomass yield for biofuel crops (Salas Fernandez et al., 2009). The potential growth, and hence the potential increase in total biomass, is adjusted daily according to the growth constraints. The adjusted daily total bio-

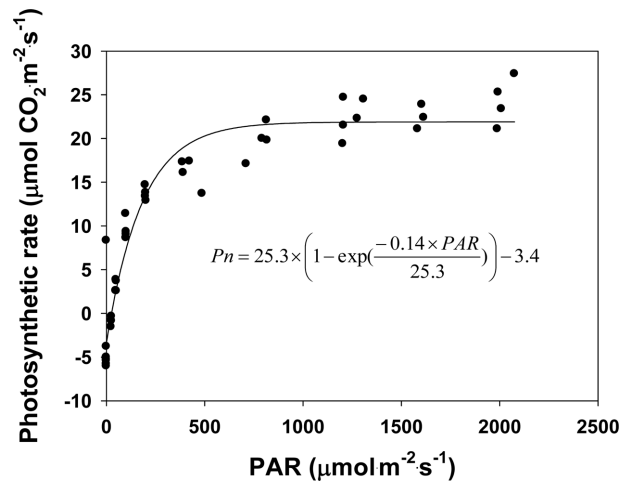


Fig. 3. Light response curves of *Chenopodium quinoa* leaves at $1,000 \mu\text{mol} \cdot \text{mol}^{-1}$ of CO_2 concentration, 50-60% of relative humidity, and 25.0°C of leaf temperature.

mass production accumulates through the growing season (Arnold et al., 1995). Therefore, total biomass in closed-type plant factory system could be estimated as plant height.

The response of the net photosynthesis rate (P_n) of quinoa to various light levels was measured and modeled (Fig. 3). The non-rectangular hyperbola model (Goudriaan and Van Laar, 1994) was chosen as the response function of net photosynthesis. From our results, the light compensation point was $29 \mu\text{mol} \cdot \text{m}^{-2} \cdot \text{s}^{-1}$ and the light saturation point was

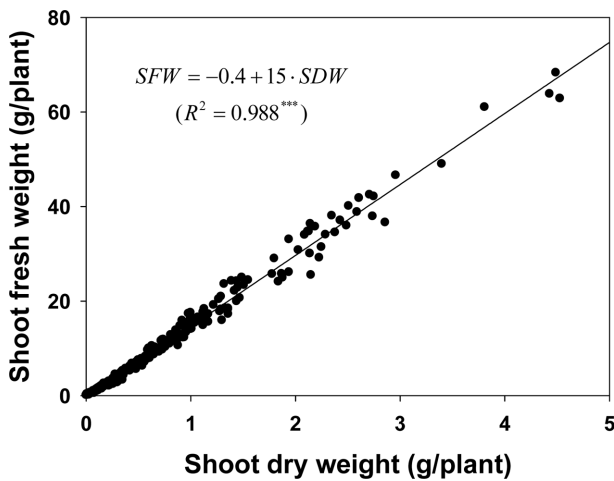


Fig. 4. Relationship between shoot dry weight and shoot fresh weight of *Chenopodium quinoa* (n=333).

$813\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$ for the quinoa grown for 22 days under a closed-type plant factory system with fluorescent lamps ($143\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), and the respiration rate was $3.4\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$. The potential photosynthesis rate (P_{max}) was $25.3\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$, and the initial gradient under low light conditions (α) was $0.14\mu\text{mol}\cdot\text{CO}_2\cdot\text{m}^{-2}\cdot\text{s}^{-1}$. The equation of the non-rectangular hyperbola has frequently been used to describe observed leaf photosynthetic responses to environmental variables (Calama et al., 2013; Cannell and Thornley, 1998; Kim et al., 2004; Lieth and Pasian, 1990; Thornley, 2002).

Shoot fresh weight (SFW, g/plant) was shown to be closely related to shoot dry weight (SDW, g/plant), the SFW had a linear relationship with the SDW (Fig. 4). From the model, the SFW was calculated as 15 times the SDW. The measured and estimated SFWs were shown to have a reasonably good fit with this function. Most research on crop productivity has usually concentrated on dry matter, however, fresh weight is of economic interest in the commercial vegetable production sector (Cho and Son, 2009).

A non-linear regression was carried out to describe the increase in shoot dry weight of quinoa as a function of time using an expolinear equation. The maximum crop growth rate was $22.9\text{g}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$, the maximum relative growth rate was $0.28\text{g}\cdot\text{g}^{-1}\cdot\text{d}^{-1}$ in the exponential growth phase, and the time at which the crop effectively reached a linear phase of growth was 13 days (Fig. 5). The curve of the function indicated a pattern of expolinear growth as suggested by Goudriaan and Monteith (1990). Basically, the growth of

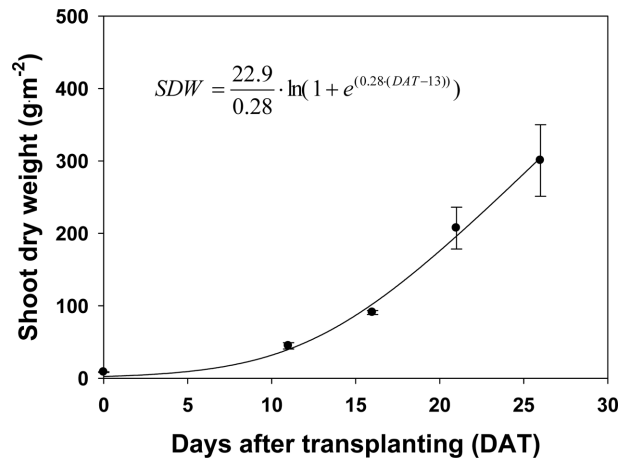


Fig. 5. Shoot dry weights ($\text{g}\cdot\text{m}^{-2}$) of quinoa with days after transplanting. Vertical bars indicated SEs of the means of 4 replications.

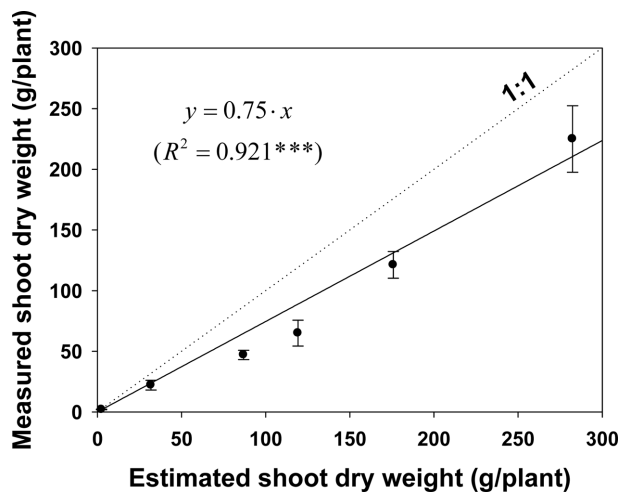


Fig. 6. Relationship between the estimated and measured shoot dry weights of *Chenopodium quinoa*. Vertical bars indicated SEs (n=4).

crop was exponential with a maximum relative growth rate, and later becomes linear with a maximum crop growth rate. The expolinear growth model as a type of crop growth model has been applied to many crops and has the potential to predict crop growth and yield.

The measured and estimated shoot dry weights were compared (Fig. 6). The regression coefficient was 0.75 ($R^2=0.921$, $P<0.001$), indicating estimated shoot dry weights were 25% less than the measured values. The measured and estimated shoot dry weights were shown to be a reasonably good fit with this function. The crop yield was

calculated as the total dry matter multiplied by the harvest index (Mo, et al., 2005). For instance, with fresh weight per plant at harvest (30g), we can estimate plant height (about 10cm), harvest time (about 18 days), and fresh weight per area (about 2kg·m⁻²).

It is concluded from this modeling study that growth and yield of quinoa in a closed-type plant factory system respond to photosynthetic active radiation. The non-rectangular hyperbola model was chosen as the response function for net photosynthesis. The modeling growth and yield responses to environmental variables are very useful for the prediction of attainable quinoa yield and to identify the constraints on crop production and management strategies. The results of the present study evidence the importance of continuous research on the economic feasibility for producing quinoa as a leafy vegetable grown in a closed-type plant factory system.

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완전제어형 식물공장에서 퀴노아 (*Chenopodium quinoa* Willd.)의 생장을 예측하기 위한 모델 개발

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적 요. 작물 생육 모델은 작물의 생육을 이해하고 통합하기 위해 유용한 도구이다. 완전제어형 식물공장에서 엽채류로 활용하기 위한 퀴노아(*Chenopodium quinoa* Willd.)의 초장, 광합성률, 성장 모델을 예측하기 위한 모델을 1차식, 2차식 및 비선형 및 선형지수 등식을 사용하여 개발하였다. 식물 생육과 수량은 정식 후 5일간격으로 측정하였다. 광합성과 성장 곡선 모델을 계산하였다. 초장과 정식 후 일수(DAT)간의 선형 및 곡선 관계를 얻었으나, 초장을 정확하게 예측하기 위한 모델은 선형 등식이었다. 광합성률 모델을 비선형 등식을 선택하였다. 광보상점, 광포화점, 및 호흡률은 각각 29, 813 and $3.4 \mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$ 였다. 지상부 생체중과 건물중은 선형 관계를 보였다. 지상부 건물중의 회귀계수는 0.75 ($R^2=0.921^{***}$)였다. 선형지수 수식을 사용하여 시간 함수에 따른 퀴노아의 지상부 건물중 증가를 비선형 회귀식으로 수행하였다. 작물생장률과 상대생장률은 각각 $22.9 \text{ g}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ and $0.28 \text{ g}\cdot\text{g}^{-1}\cdot\text{d}^{-1}$ 였다. 이러한 모델들은 정확하게 퀴노아의 초장, 광합성률, 지상부 생체중과 건물중을 예측할 수 있다.

추가주제어 : 작물생장률, 선형지수 등식, 광합성률, 초장