

Joint Blind Parameter Estimation of Non-cooperative High-Order Modulated PCMA Signals

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*Received February 27, 2018; revised April 25, 2018; accepted May 15, 2018;
published October 30, 2018*

Abstract

A joint blind parameter estimation algorithm based on minimum channel stability function aimed at the non-cooperative high-order modulated paired carrier multiple access (PCMA) signals is proposed. The method, which uses hierarchical search to estimate time delay, amplitude and frequency offset and the estimation of phase offset, including finite ambiguity, is presented simultaneously based on the derivation of the channel stability function. In this work, the structure of hierarchical iterative processing is used to enhance the performance of the algorithm, and the improved algorithm is used to reduce complexity. Compared with existing data-aided algorithms, this algorithm does not require a priori information. Therefore, it has significant advantage in solving the problem of blind parameter estimation of non-cooperative high-order modulated PCMA signals. Simulation results show the performance of the proposed algorithm is similar to the modified Cramer–Rao bound (MCRB) when the signal-to-noise ratio is larger than 16 dB. The simulation results also verify the practicality of the proposed algorithm.

Keywords: Co-frequency detection, PCMA, non-cooperative, parameters estimation, joint blind estimation

1. Introduction

Paired carrier multiple access (PCMA) is a technology used to improve the capacity of satellite communication, which has been widely used in recent years [1]. Communication signals sent by two ground stations are overlapped in time and frequency domains. In the system of cooperative PCMA communication, each ground station sends an uplink signal and receives a downlink mixed signal of the local signal and the signal of the other ground stations at the same time. In the system of non-cooperative PCMA communication, the third-party receiver cannot use the cooperative communication method directly to obtain the useful signal component without any a priori information of both parties. Therefore, the downlink mixed signal contains the fixed mixed mode of the two uplink signal components. The positive definite condition required by the normal signal blind separation cannot be constructed. Thus, obtaining similar effects with the traditional multi-channel reception is impossible despite the use of multiple receive terminals on the ground. Therefore, the interference suppression technology based on the multi-channel reception is no longer applicable [2], and only the single-channel reception blind demodulation method [3-4] can be used.

Before symbol sequence demodulation, the modulation parameters and channel response of each signal component should be estimated. The key issue is how to estimate the frequency offset, time delay, amplitude and phase offset.

Parameter estimation of non-cooperative PCMA signal can be divided into data-aided and non-data-aided algorithms. Data-aided algorithms rely on the signal frame format, which can estimate the parameters depending on the correlation of frame synchronisation header data [5-7]. However, these algorithms are not applicable in blind signal processing. In non-data-aided algorithms, the modulated-type PCMA signal is utilised in low-order modulated signal at first, which estimates the frequency offset by extracting discrete spectral lines of square spectrum and fourth-power spectrum [8-10]. However, numerous cross terms are found when the high-order spectrums and the statistics of the high-order modulated (such as 8PSK) signals are calculated. In estimation algorithms of time delay, the technique of interference blind separation based on particle filter can estimate delays of the two signal components simultaneously [11-12], but it has high complexity and is sensitive to frequency offset. A joint time-delay estimation method based on the maximum-likelihood algorithm is proposed [13]. This method is not sensitive to frequency offset and has lower complexity than the particle filtering method. However, a large number of approximations of the cross terms exist in the derivation process. Therefore, the method is not suitable for high-order modulated PCMA signal. Compared with the diversity of time delay estimation algorithms, amplitude estimation and phase offset estimation algorithms focus mainly on high-power methods [14], but the problem of having too many cross terms produced in high-order modulated PCMA signals still exists. Furthermore, a priori information on frequency offset must be known. In summary, in current situations in which high-order modulated PCMA signals usually appear [15], the blind parameter estimation is an urgent problem that needs to be solved.

This work is devoted to solving the problem of joint parameter estimation of high-order modulated PCMA signal in non-data-aided algorithms. With the aid of per-survivor processing (PSP) algorithm [16], channel stability function is defined. First, the method of joint hierarchically searching parameters is used. Then, channel parameters are estimated by searching the values of channel parameters that causes the channel stability function to reach

the minimum value. Blind estimation of all parameters is realised, and the cross terms are avoided at the same time.

2. English Abbreviations

Main notations used in this paper:

h_i, f_i, θ_i and $\tau_i (i=1,2)$ are the amplitudes, frequency offsets, initial phase offsets and time delays, respectively.

ζ_i : Phase value of i -th signal component.

\hat{X} : Estimation value of X .

$\mathbf{g}_i(\cdot)$: Pulse response of the channel filter.

\mathbf{s}_k : State grid at time k .

$\lambda(\mathbf{s}_{k-1} \rightarrow \mathbf{s}_k) = |e(\mathbf{s}_{k-1} \rightarrow \mathbf{s}_k)|^2$: Branch path metric at time k .

$\mathbf{s}_k^m (m=1,2,\dots,M^{4L_1})$: Possible state at time k .

$(\mathbf{s}_{k-1}^{\phi_{k+L_1}} | \mathbf{s}_k^m)$: All states at time $(k-1)$ that can reach state \mathbf{s}_k^m when the input symbol pair is

$\phi_{k+L_1} = (\hat{a}_{1,k+L_1}, \hat{a}_{2,k+L_1})$ at time k .

$\Gamma(\mathbf{s}_k^m)$: Accumulated path metric of \mathbf{s}_k^m .

$\hat{\mathbf{G}}_{i,k}^T(\mathbf{s}_k^m)$: Channel response estimation of the i -th signal component in time k at possible state \mathbf{s}_k^m .

$\eta_{i,k}(\mathbf{s}_k^m)$: Channel stability function corresponding to the surviving path of state \mathbf{s}_k^m at time k .

3. Signal Model

In the system of non-cooperative PCMA communication, the ground station receives the mixed signal of two MPSK- or QAM-modulated signal components. The received signal is sampled at symbol period T_s , and its discrete-time form can be written as

$$y_k = h_1 e^{j(2\pi f_1 k T_s + \theta_1)} x_{1,k} + h_2 e^{j(2\pi f_2 k T_s + \theta_2)} x_{2,k} + v_k, \quad (1)$$

where $v_k (k=1,2,\dots)$ is the complex additive white Gaussian noise sampled sequences with zero mean and variance σ^2 . $x_{1,k}$ and $x_{2,k}$ are the mixed signal components. The modulated mode of the two components is assumed to be the same and independent of each other. Then, $x_{i,k}$ can be expressed as

$$x_{i,k} = \sum_{m=-L_1}^{L_1} a_{i,m} g_i(kT_s - mT_s + \tau_i), \quad (2)$$

where h_i, f_i, θ_i and $\tau_i (i=1,2)$ are the amplitudes, frequency offsets, initial phase offsets and time delays, respectively. The phase value $\zeta_i = 2\pi f_i k T_s + \theta_i$ is defined. $a_{1,k}$ and $a_{2,k}$ are the two transmission signal component sequences, whose values depend on the modulated mode. $\mathbf{g}_i(\cdot)$ is the pulse response of the channel filter (consisting of shaped and matched filters). Its effective range is $[-L_1 T_s, L_1 T_s]$, L_1 is the number of filter trailing symbols. $\mathbf{G}_{i,k} = \{h_i e^{j(2\pi f_i k T_s + \theta_i)} g_i(kT_s + L_1 T_s + \tau_i : kT_s - L_1 T_s + \tau_i)\}$, $\mathbf{a}_{i,k} = \{a_{i,k-L_1:k+L_1}\}$. The received signal can be written as

$$y_k = \mathbf{G}_{1,k}^T \mathbf{a}_{1,k} + \mathbf{G}_{2,k}^T \mathbf{a}_{2,k} + v_k. \quad (3)$$

The purpose of demodulation in signal receiver is to estimate the sequence of two symbol sequences $\{a_{1,k}, a_{2,k}, k = 0, 1, \dots\}$ according to the received sequences $\{y_k, k = 0, 1, \dots\}$, where the reconstructed channel $\mathbf{G}_{i,k}$ plays an important role. In this work, amplitude h_i , time delay τ_i , phase value ζ_i (with ambiguity) and frequency offsets f_i of the two signal components are estimated accurately to prepare for the reconstruction of the channel and separation process in back-end separation algorithm.

4. Blind parameter estimation algorithm based on channel stability function

Parameter estimation of the PCMA signal can be combined with the blind separation process of mixed signals. First, a large number of channel responses can be reconstructed through hierarchical traversing parameters (time delays, phase values and amplitudes of the two mixed signal components) in a definite range. Subsequently, a small amount of mixed signal data ($K < 50$) can be separated blindly with each reconstructed channel response. Second, the channel response is updated, and the channel stability function is calculated, as shown in (11). The more accurate the initial parameter value is set, the smaller the channel response update changes in the separation process and the smaller the corresponding channel stability function. Therefore, PCMA signal parameter estimation can be realised by searching the minimum channel stability function. The frequency offset of the baseband received signal is about $10^{-2}f_d$ order of magnitude, where f_d is the symbol rate. So the phase value could be considered constantly because of the limited length of the mixed signal when estimating the time delay τ_i , amplitude h_i and phase value ζ_i . Therefore, the algorithm is not affected by the frequency offset when estimating the parameters of time delay, amplitude and phase value. The frequency offsets of the two mixed signal components are estimated through the same method based on the estimation of time delays, amplitudes and phase values, except that a larger amount of mixed signal data ($K > 50$) would be utilised in a blindly separated process.

The rest of this section is organised as follows. Section 4.1 describes the basic PCMA signal blind separation method. Section 4.2 derives the channel stability function based on the iterative PSP algorithm and describes the parameter estimation algorithm based on channel stability function. Section 4.3 focuses on the algorithm improvement. Section 4.4 discusses the complexity of this method. The algorithm flow chart is shown in Fig. 1.

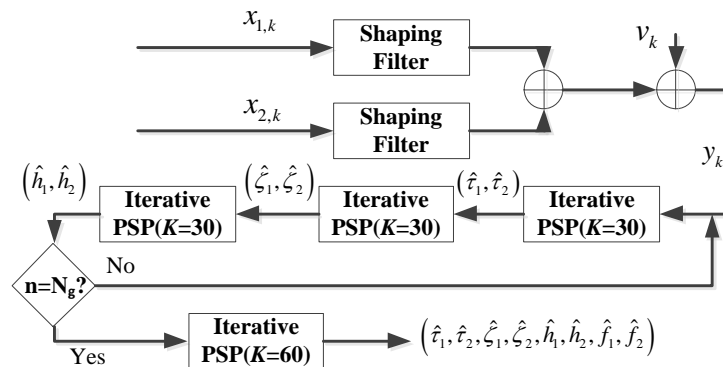


Fig. 1. Algorithm flow chart in this work

4.1 Blind separation of PCMA signal

The maximum likelihood estimation of the transmitted symbol sequence is realised by searching the transmitted sequence Φ that maximises the probability of receiving sequence Y in the joint space composed of Φ and channel response G :

$$\Phi = \arg \max p(Y | \Phi, G). \quad (4)$$

First, the state transition grid is constructed by taking the PSP algorithm as an example. The state grid at time $k-1$ is defined as $s_{k-1} = [\hat{a}_{1,k-L_1:k+L_1-1}, \hat{a}_{2,k-L_1:k+L_1-1}]$. The input symbol pair of the two signal components and output symbol at time k are defined as $(\hat{a}_{1,k+L_1}, \hat{a}_{2,k+L_1})$ and y_k , respectively. $\hat{a}_{i,k}$ represents the estimation of $a_{i,k}$. If the state grid moves from s_{k-1} to s_k , where $s_k = [\hat{a}_{1,k-L_1+1:k+L_1}, \hat{a}_{2,k-L_1+1:k+L_1}]$, then the state transition process is as shown below:

$$s_{k-1} \xrightarrow[\hat{a}_{1,k+L_1}, \hat{a}_{2,k+L_1}]{y_k} s_k.$$

With the influence of Gaussian white noise, likelihood function (4) at time K could be written as

$$\begin{aligned} p(Y | \Phi, G) &= p(y_{0:K} | \hat{a}_{1,0:K+L_1}, \hat{a}_{2,0:K+L_1}, \hat{G}_{1,0:K}, \hat{G}_{2,0:K}) \\ &= \prod_{k=0}^K p(y_k | \hat{a}_{1,k}, \hat{a}_{2,k}, \hat{G}_{1,k}, \hat{G}_{2,k}) \\ &= F \cdot \exp\left(-\frac{1}{2\sigma^2} \sum_{k=0}^K |y_k - \hat{G}_{1,k}^T \hat{a}_{1,k} - \hat{G}_{2,k}^T \hat{a}_{2,k}|^2\right) \end{aligned} \quad (5)$$

where $F = \left(\frac{1}{\sqrt{2\pi}\sigma}\right)$ and \hat{G} is the estimation of the real channel G . According to (5), the branch path metric at time k could be defined as

$$\lambda(s_{k-1} \rightarrow s_k) = |e(s_{k-1} \rightarrow s_k)|^2, \quad (6)$$

$$e(s_{k-1} \rightarrow s_k) = y_k - \hat{G}_{1,k}^T \hat{a}_{1,k}(s_{k-1} \rightarrow s_k) - \hat{G}_{2,k}^T \hat{a}_{2,k}(s_{k-1} \rightarrow s_k), \quad (7)$$

where $\hat{a}_{i,k}(s_{k-1} \rightarrow s_k)$ is the symbol vector of the i th channel signal corresponding to the grid state transition $(s_{k-1} \rightarrow s_k)$. $s_k^m (m=1, 2, \dots, M^{4L_1})$ represents the possible state at time k , where M is the modulation order. For each state s_k^m , (8) is performed to obtain the accumulated path metric:

$$\Gamma(s_k^m) = \min_{\left(s_{k-1}^{\phi_{k+L_1}} | s_k^m\right)} \left(\Gamma(s_{k-1}^{\phi_{k+L_1}} | s_k^m) + \lambda\left(\left(s_{k-1}^{\phi_{k+L_1}} | s_k^m\right) \rightarrow s_k^m\right) \right), \quad (8)$$

where $\left(s_{k-1}^{\phi_{k+L_1}} | s_k^m\right)$ represents all states at time $(k-1)$ that can reach state s_k^m if the input symbol pair is $\phi_{k+L_1} = (\hat{a}_{1,k+L_1}, \hat{a}_{2,k+L_1})$ at time k , $\Gamma(s)$ represents the path metric of state s and $\left(s_{k-1}^{\phi'} | s_k^m\right)$ represents the state at time $(k-1)$ that reaches the minimum value of (8). The channel response is estimated based on the corresponding symbol sequences of each surviving path.

$$\hat{G}_{i,k}^T(s_k^m) = \hat{G}_{i,k-1}^T(s_{k-1}^{\phi'} | s_k^m) + \mu e\left(\left(s_{k-1}^{\phi'} | s_k^m\right) \rightarrow s_k^m\right) \hat{a}_{i,k}\left(\left(s_{k-1}^{\phi'} | s_k^m\right) \rightarrow s_k^m\right), \quad (9)$$

where μ is the step factor, whose convergence condition is $0 < \mu < \frac{2}{\lambda_{\max}}$ [17]. λ_{\max} is the maximum eigenvalue of the received signal autocorrelation matrix. Channel is initialised to $\hat{\mathbf{G}}_{i,0}^T$, which is determined by the initial time delay, phase value and amplitude value. Channel reconstruction $\hat{\mathbf{G}}_{i,k}^T$ is used to calculate the branch path metric at time $k+1$.

4.2 Parameter estimation algorithm based on channel stability function

According to (9), we define the channel stability function corresponding to the surviving path of state s_k^m at time k as

$$\eta_{i,k}(s_k^m) = \left\| \hat{\mathbf{G}}_{i,k}^T(s_k^m) - \hat{\mathbf{G}}_{i,k-1}^T(s_{k-1}^{\phi_{\min}} | s_k^m) \right\|_2. \quad (10)$$

The minimum cumulative metric state is defined as $s_K = \min_m \Gamma(s_K^m)$ at time K . Thus, the state reserved s_k ($k = K-1, K-2, \dots, 1$) at each time can be derived. In this case, the corresponding channel stability function of K symbol pairs is defined as

$$\eta_K = \sum_{i=1}^2 \eta_{i,K} = \sum_{i=1}^2 \sum_{k=1}^K \left\| \hat{\mathbf{G}}_{i,k}^T(s_k) - \hat{\mathbf{G}}_{i,k-1}^T(s_{k-1} | s_k) \right\|_2. \quad (11)$$

where $\|\mathbf{V}\|_2$ represents the 2-norm of vector \mathbf{V} . The channel response can be reconstructed for each set of initial time delay, amplitude and phase value parameters. The channel stability function η_K at time K can be obtained correspondingly. The parameters that minimise the channel stability function are selected as the final parameter estimation.

$$\{\hat{\tau}_i, \hat{h}_i, \hat{\zeta}_i\} = \arg \min_{\tau_i, h_i, \zeta_i} \left\{ \eta_K | \tau_i, h_i, \zeta_i \right\}, \quad (12)$$

where $\hat{\tau}_i$ and \hat{h}_i are the estimation of the PCMA signal time delays and amplitudes, respectively, and $\hat{\zeta}_i$ is the estimation of the phase value. If frequency offsets f_i are known, then $\hat{\theta}_i = \hat{\zeta}_i - 2\pi f_i k T_s$ represents the phase offset estimation. In MPSK-modulated situation, ambiguity on possessing integer multiple of $\frac{2\pi}{M}$ in $\hat{\theta}_i$ relative to the true phase offset value will arise because of the symmetry of modulated phase, which requires the removal of other means (such as differential coding and synchronous code). The channel response is reconstructed for each set of initial frequency offset f_i' through the same method, and the corresponding channel stability function η_K is obtained at time K . Parameter f_i' that minimises the channel stability function is selected as the final frequency offset estimation:

$$\left\{ \hat{f}_i' \right\} = \arg \min_{f_i'} \left\{ \eta_K | f_i', \hat{\tau}_i, \hat{h}_i, \hat{\zeta}_i \right\}. \quad (13)$$

In summary, joint estimation algorithm steps based on channel stability function are as follows.

Initialisation: Normalise the energy of received sequence. The channel amplitude ratio is initialised to 1:1 and phase values are initialised to zero. The complexity and performance of the algorithm are considered comprehensively to set the value of separation symbol length K and algorithm iteration number N_g .

For the n th iteration:

Step 1: The time delays (τ_1', τ_2') are traversed hierarchically in a definite range. The channel response $\hat{\mathbf{G}}_{i,0}^T(\tau_1', \tau_2')$ is then reconstructed. The estimation of time delay $(\hat{\tau}_1, \hat{\tau}_2)$ is determined when the channel stability function $\{\eta_K | \tau_1', \tau_2'\}$ according to (11) reaches the minimum value. The estimation result of time delays $(\hat{\tau}_1, \hat{\tau}_2)$ is carried to Step 2.

Step 2: The phase values (ζ_1', ζ_2') are traversed hierarchically in a definite range. The channel response $\hat{\mathbf{G}}_{i,0}^T(\hat{\tau}_1, \hat{\tau}_2, \zeta_1', \zeta_2')$ is reconstructed. The estimation of phase value $(\hat{\zeta}_1, \hat{\zeta}_2)$ is determined when the channel stability function $\{\eta_K | \hat{\tau}_1, \hat{\tau}_2, \zeta_1', \zeta_2'\}$ according to (11) reaches the minimum. The estimation result of phase values $(\hat{\zeta}_1, \hat{\zeta}_2)$ is carried to Step 3.

Step 3: The amplitudes (h_1', h_2') are traversed hierarchically in a definite range. The channel response $\hat{\mathbf{G}}_{i,0}^T(\hat{\tau}_1, \hat{\tau}_2, \hat{\zeta}_1, \hat{\zeta}_2, h_1', h_2')$ is also reconstructed. The estimation of amplitude (\hat{h}_1, \hat{h}_2) is determined when the channel stability function $\{\eta_K | \hat{\tau}_1, \hat{\tau}_2, \hat{\zeta}_1, \hat{\zeta}_2, h_1', h_2'\}$ according to (11) reaches the minimum.

Step 4: $n=N_g$, $\{\hat{\tau}_1, \hat{\tau}_2, \hat{\zeta}_1, \hat{\zeta}_2, \hat{h}_1, \hat{h}_2\}$ is the final result of the estimation of time delay, phase value and amplitude. The result is carried to Step 5. Otherwise, by setting $n = n + 1$, the parameter value is initialised to $\{\hat{\tau}_1, \hat{\tau}_2, \hat{\zeta}_1, \hat{\zeta}_2, \hat{h}_1, \hat{h}_2\}$ and return to step 1.

Step 5: The frequency offsets (f_1', f_2') are traversed hierarchically in a definite range. Then, the channel response $\hat{\mathbf{G}}_{i,0}^T(f_1', f_2')$ is reconstructed. The estimation of frequency offsets (\hat{f}_1, \hat{f}_2) is determined when the channel stability function $\{\eta_K | f_1', f_2', \hat{\tau}_1, \hat{\tau}_2, \hat{\zeta}_1, \hat{\zeta}_2, \hat{h}_1, \hat{h}_2\}$ according to (11) reaches the minimum value.

We take Step 1 as an example to describe the hierarchical traversing process. For the initialization of $m = 1$ st staging process, the traversal spaces of τ_1' and τ_2' are $[-T_s/2, T_s/2]$. μ_τ^1 is the initial step size. N_e is the number of hierarchical iterations. During the m -th staging process, $\frac{T_s}{\rho^{m-1} \mu_\tau^m} \cdot \frac{T_s}{\rho^{m-1} \mu_\tau^m}$ groups of delay parameters are traversed to search time delay estimation $(\hat{\tau}_1', \hat{\tau}_2')$ that enables channel stability function $\{\eta_K | \tau_1', \tau_2'\}$ to reach the minimum value, where ρ ($\rho > 1$) is the shrinkage ratio. If $m = N_e$, $(\hat{\tau}_1, \hat{\tau}_2)$ is determined as the result of time delay estimation. Otherwise $m = m+1$. The traversal spaces are set to $\left\{ \left(\hat{\tau}_1' - \frac{T_s}{2\rho^{m-1}} \sim \hat{\tau}_1' + \frac{T_s}{2\rho^{m-1}} \right), \left(\hat{\tau}_2' - \frac{T_s}{2\rho^{m-1}} \sim \hat{\tau}_2' + \frac{T_s}{2\rho^{m-1}} \right) \right\}$. Step size is set to $\mu_\tau^{m+1} = \frac{\mu_\tau^m}{\rho}$, and the $m+1$ -th hierarchical process is performed. The difference between Step 5 and the previous

steps (Step 1, Step 2 and Step 3) is the selection of traversal step. The initialization of frequency offsets should be more accurate, that is, the value of μ_f^1 in Step 5 should be smaller than μ_r^1 in Step 1. Otherwise, the difference between the estimated phase and real phase values exhibits a periodic variation with the symbol separation process. Therefore, the frequency offsets are separately estimated in this study.

4.3 Algorithm improvement

The number of states that should be calculated for each symbol demodulation is complex for high-order modulated mixed signals. The number of reserved states at time k is M^{4L_1} , as described in Section 4.1. In this study, the N_{\max} -PSP algorithm is used to reduce the number of surviving paths [14]. The impossible path will be discarded to reduce the computation, and the maximum number of paths N_{\max} will be retained based on a certain metric principle. If the number of surviving paths at state s_k is L_n , the number of extensive branch paths is M^{2L_n} when the state changes from s_k to s_{k+1} . If $M^{2L_n} \leq N_{\max}$, then $L_{n+1} = M^{2L_n}$. Otherwise, all paths are sorted based on the path metric, and the best N_{\max} paths are kept, which update $L_{n+1} = N_{\max}$.

4.4 Complexity analysis

In this study, the parameter estimation algorithm is based on blind separation. The number of real multiplication and real addition is used as the complexity evaluation criteria. The computational complexity of the algorithm is derived mainly from the calculation of path metric in the separation algorithm and the tracking of channel response. In calculating the branch metric, complexity is concentrated mainly on the calculation of (8). $KM^{2(2L_1+1)}(16L_1+9)$ times of real addition and $KM^{2(2L_1+1)}(16L_1+10)$ times of real multiplication are required. In tracking the channel response, complexity is concentrated in (9) and (10). $2KM^{2(2L_1+1)}(24L_1+11)$ times of real addition and $16KM^{2(2L_1+1)}(2L_1+1)$ times of real multiplication are required. Thus, considering algorithm iteration number N_g and hierarchical iteration N_e , the total times of real addition and multiplication are about $4N_g N_e KM^{2(2L_1+1)}(64L_1+31)$ and $8N_g N_e KM^{2(2L_1+1)}(24L_1+13)$, respectively. The total times of real addition and multiplication are reduced to about $4N_g N_e KM^2(64L_1+31)N_{\max}$ and $8N_g N_e KM^2(24L_1+13)N_{\max}$, respectively if we adopt the improved N_{\max} -PSP algorithm. The complexity of N_{\max} -PSP algorithm is much lower than the unimproved algorithm. **Table 1** shows the complexity of the algorithm.

Table 1. Complexity of the Proposed Algorithm

| Algorithm | Real additions | Real multiplications |
|---------------------------|-------------------------------------|-------------------------------------|
| PSP algorithm | $4N_g N_e KM^{2(2L_1+1)}(64L_1+31)$ | $8N_g N_e KM^{2(2L_1+1)}(24L_1+13)$ |
| N_{\max} -PSP algorithm | $4N_g N_e KM^2(64L_1+31)N_{\max}$ | $8N_g N_e KM^2(24L_1+13)N_{\max}$ |

The performance of the algorithm reaches the stability function by using a small number of separation symbols (generally $K < 60$). Under this condition, the complexity of the algorithm is maintained at a low level. Thus, this algorithm could be used in practical signal processing.

5.Simulation

In this study, we use 8PSK modulated PCMA signals as an example to study the performance of the proposed algorithm. When $K = 30$, the square root raised cosine FIR with a roll-off factor of 0.35 is employed in the shaping and matched filters of the two signals. The effective interval of ISI is $[-3T_s, 3T_s]$. Time delays τ_1 and τ_2 , phase values θ_1 and θ_2 , amplitudes h_1 and h_2 , and frequency offsets f_1 and f_2 are selected randomly in space $[-T_s/2, T_s/2]$, $[-\pi, \pi]$, $[0.5, 1.5]$ (the amplitude ratio of the energy-normalized mixed signal) and $[-10^{-2}, 10^{-2}]$ (relative to the symbol rate), respectively. The two-way signal delays, amplitudes and phase values are generated randomly. The values of the remaining simulation parameters are presented in **Table 2**.

Table 2. Simulation Parameters

| | |
|---|---|
| Initial step size | $\mu_\tau^1 = 0.1T_s, \mu_\theta^1 = 0.2\pi, \mu_h^1 = 0.1$ and $\mu_f^1 = 10^{-4}$ (relative to symbol rate) |
| Shrinkage ratio in $\{\tau, \theta, h\}$ estimation | $\rho_\tau = \rho_\theta = \rho_h = 10$ |
| Shrinkage ratio in f estimation | $\rho_f = 100$ |
| N_{\max} | 64 |
| Hierarchical iteration number | $N_e = 2$ |
| Algorithm iteration number | $N_g = 3$ |
| Step size | $\mu = 0.01$ |

The mean (normalized) estimated variance σ_e^2 is used to measure the parameter estimation performance, which is defined as the mean estimation variance of two signal components (normalized), that is, $\sigma_e^2 = (\sigma_{\varphi_1}^2 + \sigma_{\varphi_2}^2)/2$ ($\varphi \in \{\tau, h, f\}$) and $\sigma_{\varphi_i}^2 = (\varphi_i - \hat{\varphi}_i)^2$.

5.1 Modified Cramer–Rao Bound (MCRB) of parameter estimation

We define parameter set $w = (\tau, h, f)^T = (w_1, w_2, \dots, w_6)^T$, where $\boldsymbol{\tau} = (\tau_1, \tau_2)^T$, $\mathbf{h} = (h_1, h_2)^T$ and $\mathbf{f} = (f_1, f_2)^T$. The received signal vector is denoted by \mathbf{y} . When estimating the parameters w jointly, CRB for the estimation of parameter w_m ($m = 1, 2, \dots, 6$) is a lower bound on the variance of any unbiased estimate, as shown in (14) and (15).

$$E_y \left[(\hat{w}_m - w_m)^2 \right] \geq \text{CRB}_w(w_m) = [\mathbf{I}^{-1}(\mathbf{w})]_{m,m}, \quad (14)$$

$$[\mathbf{I}(\mathbf{w})]_{m,n} = E_y \left[-\frac{\partial^2 \ln p(\mathbf{y}|\mathbf{w})}{\partial w_m \partial w_n} \right], \quad (15)$$

where CRB_w indicates CRB of the joint estimation of \mathbf{w} , $\mathbf{I}(\cdot)$ is the Fisher information matrix, $[\cdot]_{m,n}$ denotes the matrix factor with row m and column n ($n = 1, \dots, 6$), $E_y[\cdot]$ denotes the statistical expectation of \mathbf{y} and $p(\mathbf{y}|\mathbf{w})$ is the probability density function of \mathbf{y} for a given \mathbf{w} . Accordingly, log likelihood function $\ln p(\mathbf{y}|\mathbf{w})$ with an unknown s can be expressed as follows:

$$\ln p(\mathbf{y}|\mathbf{w}) = \ln E_s \left[p(\mathbf{y}|\mathbf{w}, \mathbf{A}) \right] = \ln \left(\sum_{j=0}^{M^{2L}-1} \Pr[\mathbf{A} = \mathbf{c}_j] p(\mathbf{y}|\mathbf{w}, \mathbf{c}_j) \right), \quad (16)$$

where $L = 2L_1 + 1$, $\mathbf{A} = \{\mathbf{a}_1, \mathbf{a}_2\}$, $p(\mathbf{y}|\mathbf{w}, \mathbf{A})$ is the probability density function of \mathbf{y} for the given \mathbf{w} and \mathbf{A} and $E_s[\cdot]$ denotes the statistical expectation over \mathbf{A} . We assume that the data symbols are independent of one another regardless of whether they originate from the same or different sources. Hence, we obtain $\Pr[\mathbf{A} = \mathbf{c}_j] = M^{-2L}$. High complexity is required to solve $\ln p(\mathbf{y}|\mathbf{w})$ for

a large L . Therefore, MCRB is adopted to assess performance bound, which is slightly looser than the true CRB, that is,

$$\text{CRB}_{\mathbf{w}}(w_m) \geq [\mathbf{I}^{-1}(\mathbf{w}, \mathbf{A})]_{m,m} = \text{MCRB}_{\mathbf{w}}(w_m), \quad (17)$$

$$[\mathbf{I}(\mathbf{w}, \mathbf{A})]_{m,n} = E_{\mathbf{A}} \left\{ E_{\mathbf{y}|\mathbf{A}} \left[-\frac{\partial^2 \ln p(\mathbf{y}|\mathbf{w}, \mathbf{A})}{\partial w_m \partial w_n} \right] \right\}. \quad (18)$$

For a given \mathbf{w} and \mathbf{A} and corresponding receiving $\hat{\mathbf{y}}$, the ML function $p(\mathbf{y}|\mathbf{w}, \mathbf{A})$ attains a complex Gaussian distribution, as shown in the following expression:

$$p(\mathbf{y}|\mathbf{w}, \mathbf{A}) = (\pi N_0)^{-1/2} \exp\left(-\frac{1}{N_0} \int |y - \hat{y}|^2 dt\right). \quad (19)$$

The following formula can be derived as follows [18]

$$\text{MCRB}_{\mathbf{w}}(\tau_i) = \frac{(1 + \eta_i)}{2L \dot{F}_2(0)/F_2(0) E_s/N_0}, \quad (20)$$

$$\text{MCRB}_h(h_i) = \frac{N_0}{2CLF_2(0)}, \quad (21)$$

$$\text{MCRB}_{\mathbf{w}}(f_i) = \frac{3(1 + \eta_i)}{2\pi^2(L^2 - 1)LT^2 E_s/N_0}, \quad (22)$$

where $\eta_i = \begin{cases} \lambda^2, & i=1 \\ 1/\lambda^2, & i=2 \end{cases}$, $\lambda = h_2/h_1$ and $F(\omega)$ is the Fourier transform of $G_i(t)$.

$F_2(\omega) = F(\omega) \otimes F(\omega) / 2\pi$, where \otimes is the convolution operation, $\dot{F}_2(\omega) = dF_2(\omega)/d\omega$ and

$$E[a_m^{i_1} (a_n^{i_2})^*] = \begin{cases} C & \text{for } m=n \text{ and } i_1 = i_2 \\ 0 & \text{otherwise} \end{cases}.$$

5.2 Simulation performance of the algorithm

The received signal is oversampled by 4. The simulation results are compared with MCRB [18-20], with $N_g = 3$ and $K = 30$.

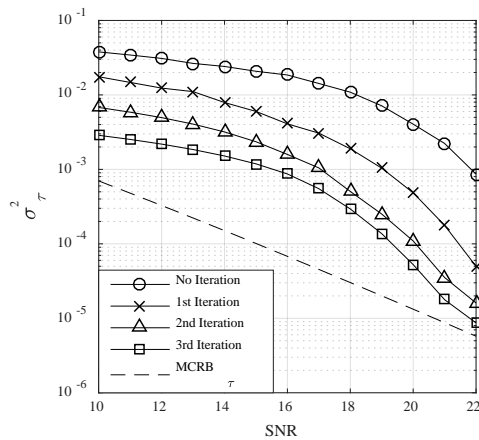


Fig. 2. Performance of time delay estimation

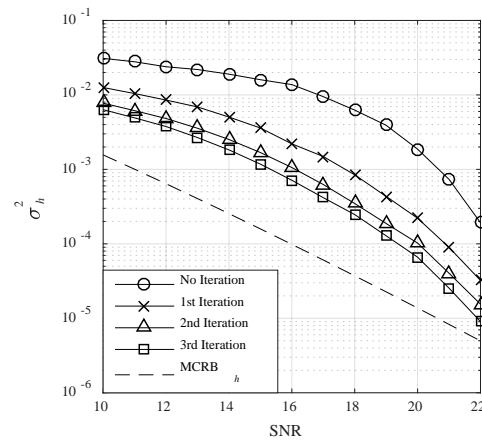


Fig. 3. Performance of amplitude estimation

The curves of σ_r^2 and σ_h^2 versus the signal-to-noise ratio (SNR) in different iterations are shown in Figs. 2 and 3, respectively. The time delay estimation variance rapidly approaches the bound above 18 dB. Compared with no iteration in the 10^{-3} order of magnitude of σ_r^2 , the algorithm obtains nearly 2 dB and nearly 3 dB SNR gain after the first and second iterations, respectively. At the same time, compared with no iteration in the 10^{-3} order of magnitude of σ_h^2 , the algorithm obtains nearly 1.5 dB and nearly 2.5 dB SNR gain after the first and second iterations, respectively. These results can be explained as follows. The parameter values are initialized accurately with the increase in the number of iterations, and they provide considerable reliable prior information for the back-end separation algorithm. The channel stability function under the condition of correct parameters is highlighted, and the performance of the algorithm is improved. When the number of iterations is more than 2, the accuracy of priori information is saturated to enhance the performance of the back-end separation algorithm. Thus, the improved space of performance is small. The selected number of iterations is twice considering the complexity of each iterative operation. The upper limit of iteration number N_g in subsequent simulation is also set to 2. The performance of frequency offset estimation is shown in Fig. 4, where $K = 60$.

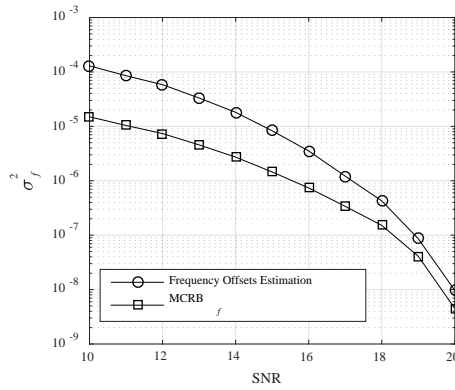


Fig. 4. Performance of frequency offset estimation

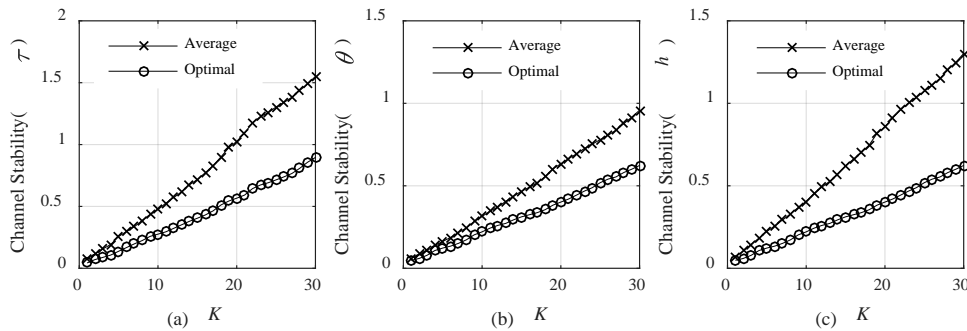


Fig. 5. Channel stability ($N_g=0$)

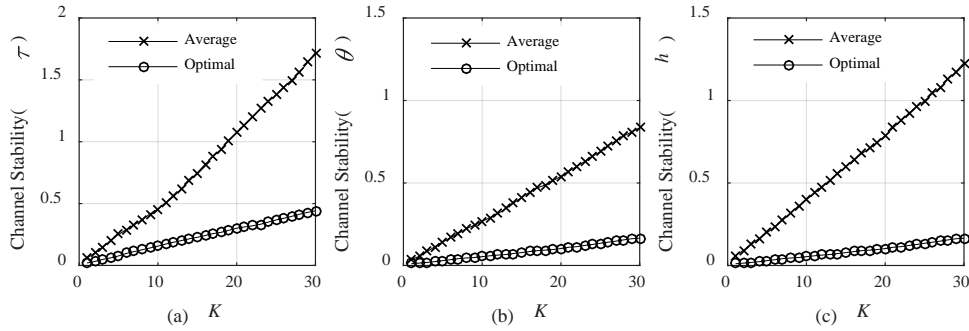


Fig. 6. Channel stability ($N_g=2$)

The channel stability function curves versus the number of separated symbols are presented in **Figs. 5** and **6**, which represent no iteration and second iteration, respectively. The estimated target parameters in **Figs. 5(a)**, **5(b)** and **5(c)** are time delays, phase offsets and amplitudes, respectively. On the basis of parameter setting, the number of tracking curves is 100 in each figure. “Average” represents the channel stability average curve for 100 experimental parameters, whereas “Optimal” represents the channel stability curve under optimal parameter condition. With an increase in the number of iterations, the gap between the “Optimal” curve and the “Average” widens, and a wide gap leads to a reliable result.

5.3. Estimation performance of phase offset

This method obtains the phase offsets with certain ambiguity. The initial phase values $\theta_i (i=1,2)$ of two signal components are generated randomly. Monte Carlo experiments are performed 30 times to estimate the mixed-signal phase offset. SNR = 14 dB, $N_g = 2$ and the remaining parameters are the same as those in Section 5.1.

The estimation results on the phase offsets of two-way signal components are shown in **Figs. 7(a)** and **7(b)**. $\theta_i (i=1,2)$ and $\hat{\theta}_i$ denote the true and estimated values, respectively. As shown in **Fig. 7**, the phase-offset estimation is obtained with the integer ambiguity of $\pi/4$ for 8PSK modulation PCMA signals. This estimation is obtained from the symmetry of MPSK modulated signals, and should be removed by other means (such as differential coding and synchronization code). Therefore, the traversal space of phase is reduced to $\pi/4$ in the algorithm to reduce complexity. If ambiguity is removed, the phase estimation performance of this algorithm is shown in **Fig. 8**. If signal frequency offset f_i is not equal to zero, the phase value range of symbol sequence used in this method is Kf_i , where $f_i < 0.01$ (relative to symbol rate) in general. Thus, the phase values of K -symbols are constant. This condition is also the reason for the estimations on time delays and amplitudes not being affected by the error of frequency offsets.

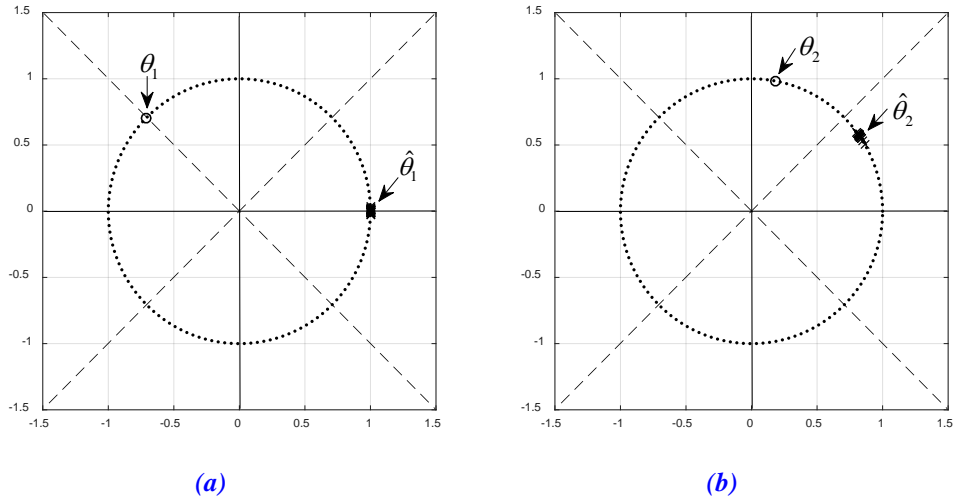


Fig. 7. Performance of phase offset estimation
 (a) First-way signal component, (b) Second-way signal component

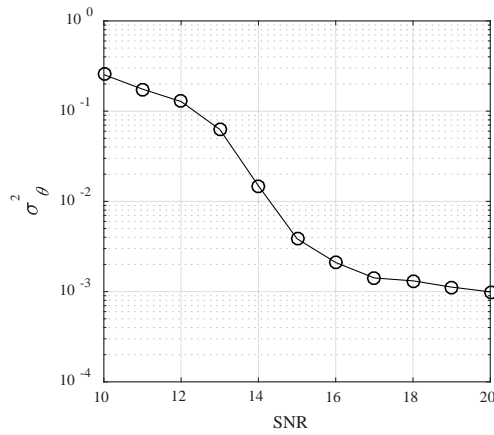


Fig. 8. Performance of phase offset estimation

5.4. Effect of parameter settings on algorithm performance

In this section, the time delay is used as the target parameter. **Figs. 9** and **10**. show the effect of oversampling factor N and separated symbol length K on algorithm performance. The remaining parameters are the same as those in Section 5.1. As shown in **Fig. 9**, an obvious improvement in the performance of the algorithm is observed when the oversampling factor increases from $N = 1$ to $N = 2$ (the estimation variance is reduced about one-order of magnitude less than 16 dB), and increases steadily when $N > 2$. **Fig. 10** shows that the performance of the algorithm is improved with the increase on the number of separated symbols K .

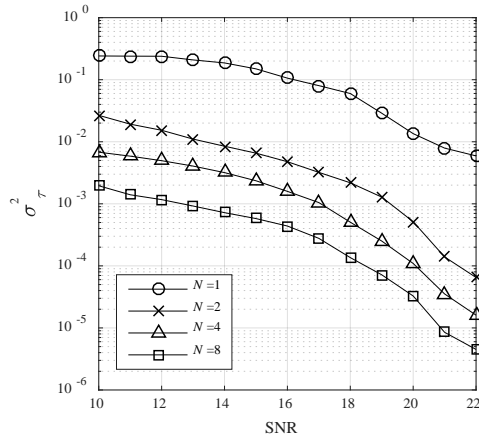


Fig. 9. Effect of N on estimation performance

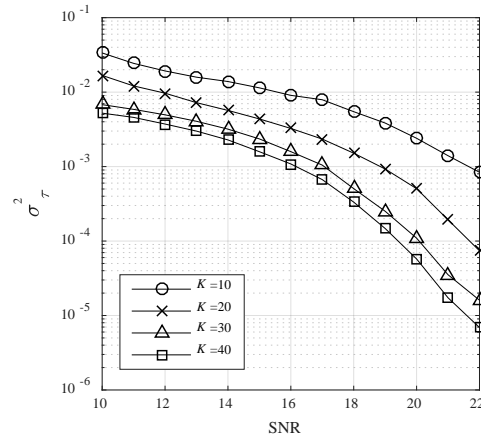


Fig. 10. Effect of K on estimation performance

6. Conclusion

In this study, the blind estimation on high-order modulated PCMA signal parameters is realized through the hierarchical searching method based on the derivation of channel stability function. Currently, traditional algorithms have not been able to solve effectively the blind estimation problem of 8PSK modulated PCMA signal parameters without priori information. Compared with the traditional data-aided algorithms, the significant advantage of the proposed method is that no cross-term approximation is performed, leading to a more stable performance. This method does not require any prior information, which meets the requirements of blind processing. In this study, 8PSK modulated PCMA signals are used as an example to examine the algorithm performance, and it can also be extended to other high-order MPSK and QAM modulated PCMA signals.

7. Acknowledgments

This work was supported by the National Natural Science Foundation of China (No. 61401511) and the National Natural Science Foundation of China (No. U1736107).

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