# Impact of User Convenience on Appliance Scheduling of a Home Energy Management System

# Je-Seok Shin\*, In-Su Bae\*\* and Jin-O Kim<sup>†</sup>

**Abstract** – Regarding demand response (DR) by residential users (R-users), the users try to reduce electricity costs by adjusting their power consumption in response to the time-varying price. However, their power consumption may be affected not only by the price, but also by user convenience for using appliances. This paper proposes a methodology for appliance scheduling (AS) that considers the user convenience based on historical data. The usage pattern for appliances is first modeled applying the copula function or clustering method to evaluate user convenience. As the modeling results, the comfort distribution or representative scenarios are obtained, and then used to formulate a discomfort index (DI) to assess the degree of the user convenience. An AS optimization problem is formulated in terms of cost and DI. In the case study, various AS tasks are performed depending on the weights for cost and DI. The results show that user convenience has significant impacts on AS. The proposed methodology can contribute to induce more DR participation from R-users by reflecting properly user convenience to AS problem.

**Keywords**: Residential demand response, Home energy management system, User Convenience, Appliance usage pattern, Appliance scheduling, Discomfort index

#### 1. Introduction

In recent years, load management on the demand side has become more important. Load management initially focused on relatively large customers such as commercial and industrial users, because of the ease and high efficiency of their load management [1]. Smart grid technologies, which are based on the two-way exchange of electricity/ information, enable general end users to monitor and manage their power consumption. Various energy management systems (EMSs) have been developed for different load management subjects, such as factories, buildings, and homes. With the development of a variety of smart appliances and a communication and control infrastructure, residential users (R-users) are expected to significantly contribute to load management in the near future [2-4]. Thus, this study focuses on load management by residential users through home EMS (HEMS).

Various demand response (DR) programs have been developed for load management by R-users. DR programs commonly lead R-users to adjust their power consumption in response to external signals like the timevarying price, incentives, and emergency requests for load reduction [5]. Among the various DR programs, the price-based DR (P-DR) induces voluntary and non-

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compulsive DR participation through time-varying electricity prices [6-8]; schemes include the real-time price (RTP), critical peak price, inclining block rate, and time of use. Several studies have shown that RTP is more effective than other P-DR programs. However, it is difficult for R-users to monitor and control their power consumption in real time to RTP, and it can interfere with their DR participation [6, 9]. As one of the ways to resolve this problem, this paper considers the RTP which is announced before a day, named as day-ahead RTP (DARTP) [10-12]. Under DARTP, HEMS performs the appliance scheduling (AS) to establish a plan for using various appliances the next day. Then the HEMS notifies a result of the AS to the R-user through a communication interface. The AS result can be used as a guideline for using appliances or be reflected to the automatic control of appliances.

Several researchers have studied residential P-DR [13-17]; they mainly focused on minimizing the electricity costs by shifting the usage time or reducing the operation level of appliances within pre-specified ranges. However, the appliance usage by R-users may be influenced not only by the price, but also by other factors (i.e., the convenience for using appliances). For example, when shifting usage time of an appliance, some R-users may want to shift the usage time to more convenient times rather than times with low prices. Such R-users feel more convenience when using appliances at preferred times or operating level. Other several studies have dealt with residential P-DR considering user convenience [2,6,18-21]. However, they performed AS with certain operation ranges and preferred

<sup>†</sup> Corresponding Author: Dept. of Electrical Engineering, Hanyang University, Korea. (jokim@hanyang.ac.kr)

<sup>\*</sup> Dept. of Electrical Engineering, Hanyang University, Korea. (kjboy@hanyang.ac.kr)

<sup>\*\*</sup> Dept. of Electrical Engineering, Kangwon National University, Korea. (isbae@kangwon.ac.kr)

conditions pre-set by the user and user convenience was simply considered by the difference between the pre-set conditions and the scheduling result. Such the way may cause another inconvenience in P-DR participation through the AS because the user should sometimes adjust directly the conditions for using appliances. Furthermore, it may not be sufficient for reflecting user's preference for using appliances which can be influenced by the time-varying price or other factors.

In order to improve the above problems, this paper proposes a methodology to perform AS considering user convenience without the direct input of preferred conditions by the R-users. For this purpose, this paper first presents a methodology to model user's preferred conditions for the usage time or operating level, by applying a copula function or clustering method to the cumulative data. The comfort distribution or representative usage scenarios are obtained as the modeling results and used to formulate the degree of user convenience for major appliances as the discomfort index (DI). The AS problem is formulated in terms of cost and DI. In the case study, various AS tasks are performed to investigate the impacts of user convenience on the AS.

# 2. Methodology for Modeling Usage Pattern of **Appliance Usage**

In this paper, R-users are considered to be influenced by DARTP and other factors (e.g., outside temperature) when adjusting their appliance usage. The users would have their own usage patterns which involve their preference on the appliance usage. The closer a plan for the appliance usage is made to user's usage pattern, the more the user would feel the convenience. In this section, a methodology for modeling the usage pattern is proposed based on the copula function or clustering method. The usage pattern is modeled for appliances of the following categories [9, 16, 221:

Deferrable appliances (DAs): appliances of which usage time is determined depending on the electricity price, within available time ranges. Typical DAs include washing machines, dishwashers, and drying machines.

Curtailable appliances (CAs): appliances of which on/ off status and power consumption are controlled within available operational ranges. As typical CAs, there are a heating, ventilation and air conditioning (HVAC), electric water heater (EWH), and energy storage system (ESS).

### 2.1 Copula-based usage pattern modeling

The usage pattern of DAs can be expressed as a numerical correlation between the usage times (i.e., the start and end times) and the time-varying price. The usage pattern of HVAC can also be expressed by the inside temperature to be maintained over time, and the

outside temperature. Such numerical usage patterns can be modeled by applying a copula function [23-25].

The copula function is a way to identify the dependence between two or more random variables with individual distributions and represent it as a joint probability distribution. Among various copula functions, the Gaussian copula (GC) is used in this study:

$$GC(\phi_1(x_1),...,\phi_n(x_n)) = \phi(x_1,...,x_n)$$
 (1)

where x is a random variable that is the usage time for DAs or inside temperature for HVAC.  $\phi$  is a standard normal distribution function.

By applying  $\phi_n(x_n) = u_n$ , Eq. (1) can be rewritten as

$$GC(u_1,...,u_n;Rho) = \phi_n(\phi^{-1}(u_1),...,\phi^{-1}(u_n);Rho)$$
 (2)

where  $\mu$  is the variable normalized to the uniform distribution and  $\phi^{-1}$  is an inverse function of a standard normal distribution. Rho is the major parameter matrix for GC and can be obtained from a rank correlation coefficient such as Kendall's  $\tau$  or Spearman's  $\rho$ :

$$Rho = \sin\left(\frac{\tau\pi}{2}\right) = 2\sin\left(\frac{\rho\pi}{6}\right) \tag{3}$$

Fig. 1 shows the procedure of the GC-based modeling method, which is briefly explained by using HVAC. When modeling the usage pattern of HVAC, the inside temperature  $(Tp_{ln})$  is defined as the target variable, and the outside temperature ( $Tp_{Out}$ ) is defined as the reference variable. The usage pattern is modeled as the dependence between  $Tp_{In}$  and  $Tp_{Out}$ . By applying Eq. (3) to the cumulative data, the dependence between all the variables is estimated as the matrix Rho. If  $Tp_{ln}$  increases as  $Tp_{Out}$  decreases, then *Rho* consists of negative values. Conversely, Rho has positive values. As the absolute value of Rho comes closer to 1,  $Tp_{ln}$  can be regarded as influenced more significantly by  $Tp_{Out}$ .

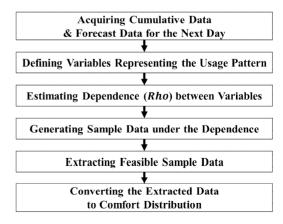


Fig. 1. Procedure of GC-based modeling

An appropriate number of sample data which have the dependence of the estimated Rho, can be generated by Eqs. (1) and (2). Fig. 2 shows the cumulative and sample data for  $Tp_{Out}(72)$  and  $Tp_{In}(76)$  among all variables (here, the time unit is 15 min.). Rho of them has been estimated as -0.9498.

Data corresponding to the reference variable,  $Tp_{Out}$ , among all sample data is compared with the forecasted one  $(Tp_{Out}^{FC})$  for the next day. By Eq. (4), only the sample data which contains the data of  $Tp_{Out}$  similar to  $Tp_{Out}^{FC}$ , is extracted. Fig. 2(b) shows the extracted sample data for  $Tp_{Out}^{FC}(72) = 3.2^{\circ} \text{C}$ .

$$ES = \left\{ SD_i \mid \sqrt{\sum_{\forall i} \left( Tp_{Out}^{SD_i} - Tp_{Out}^{FC} \right)^2 / T} \le \varepsilon_{ES} \right\}$$
 (4)

where ES is a set of the extracted sample data, SD is sample data containing data of all variables,  $Tp_{Out}^{SD}$  is data corresponding to reference variables, T is the length of the entire time period, and  $\varepsilon_{ES}$  is the permissible error.

Fig. 3 shows the extracted sample data for  $Tp_{ln}$  and

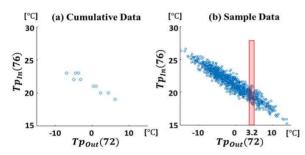


Fig. 2. Cumulative and sampling data generated by GC

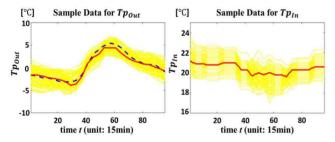
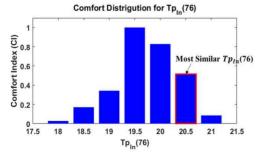


Fig. 3. Extracted sample data for



**Fig. 4.** Comfort distribution for  $T_{n}$  (76)

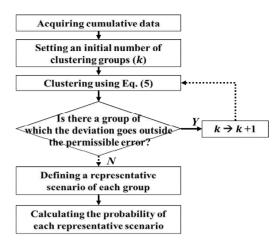


Fig. 5. Procedure for clustering-based modeling

 $Tp_{Out}$  during the entire time period, where lines represent the extracted sample data. The thick and dotted line is  $\mathit{Tp}_{\mathit{Out}}^{\mathit{FC}}$  , while the thicker lines represent  $\mathit{Tp}_{\mathit{Out}}$  and  $\mathit{Tp}_{\mathit{In}}$  of the most similar sample data to  $Tp_{Out}^{FC}$ .

By counting the number of data of the extracted  $Tp_{ln}$ for each time, the frequency distribution for each time is obtained. This is then converted to the comfort distribution through the normalization process. Fig. 4 shows the comfort distribution for  $Tp_{In}(76)$ , which indicates that the R-user has different preferences depending on  $Tp_{In}$ .

### 2.2 Clustering-based usage pattern modeling

The usage pattern of EWH is related to the hot water usage. Expressing when and how much hot water is used through any comfort distribution is difficult. Appliances, such as EWH can be modeled by a scenario-based approach applying a clustering method. Fig. 5 shows the procedure of K-clustering-based method for modeling the usage pattern.

Among the cumulative data for the hot water usage, the similar data is grouped together by using Eq. (5) [26].

$$\underset{k,S}{\operatorname{arg\,min}} \left\{ \sum_{i=1}^{k} \sum_{j \in S_{i}} \sum_{\forall t} \sqrt{\left| \theta_{j}(t) - \overline{\theta_{i}(t)} \right|^{2}} \leq \varepsilon_{KC} \right\}$$
 (5)

where S is the set of representative scenarios, k is the number of groups,  $\theta_i(t)$  is the data at time t (for an EWH, this is the quantity of heat for the used hot water),  $\theta_i(t)$  is data corresponding to the centroid of the i-th group, and  $\mathcal{E}_{KC}$  is the permissible error. The centroid of each group is defined as the representative scenario, and its probability is calculated as the ratio of the number of data in the group to the total cumulative data.

# 3. Appliance Scheduling Formulation

The AS problem can be expressed by an objective

function which is formulated with two terms: the electricity cost, EC and discomfort index, DI.

$$\min F = \omega_{EC} \times \frac{EC - EC^{Min}}{EC^{Max} - EC^{Min}} + \omega_{DI} \times \frac{DI - DI^{Min}}{DI^{Max} - DI^{Min}}$$
 (6)

where  $\omega_{EC}$  and  $\omega_{DI}$  are weighting factors. Depending on the weighting factors, diverse plans for using appliances can be established. EC and DI are normalized by their min/maximum values, respectively. Under conditions of  $\omega_{EC} = 1$  and  $\omega_{DI} = 0$ ,  $EC^{\min}$  and  $DI^{\max}$  can be calculated, and  $EC^{\text{max}}$  and  $DI^{\text{min}}$  can be obtained under conditions of  $\omega_{EC} = 0$  and  $\omega_{DI} = 1$ .

#### 3.1 AS Problem for DAs

The electricity cost of DA,  $EC_{DA}$  is expressed by

$$EC_{DA} = \sum_{\forall t} \pi(t) \cdot P_{DA}^{R} \cdot \mu_{DA}(t)$$
 (7)

where  $\pi$  is DARTP,  $P_{DA}^{R}$  is the rated power of DA, and  $\mu_{\rm DA}$  is a status variable and is 0 or 1 depending on whether the DA is stopped or operating, respectively.

By the copula-based method, the comfort distribution for DAs is obtained as in Fig. 6, where CI is the comfort index normalized to have 1 as a maximum value. DI is calculated by 1-CI.  $t_{DA}^{\alpha}$  and  $t_{DA}^{\beta}$  indicate the available time range for using DA beyond the threshold.  $t_{DA}^{\alpha,BF}$  and  $t_{DA}^{\beta,BF}$  represent the best fitted start and end times.

 $DI_{DA}$  is evaluated considering both the comfort distribution and best fitted operating times. In Eq. (8), the first term means the average of inconvenience level during using DA and second term means the ratio of a difference between the scheduled and best fitted times for start and end times, to each possible time range, respectively [6]:

$$DI_{DA} = \gamma_{DA} \times \left(1 - \frac{1}{Task_{DA}} \times \sum_{t=t_{DA}^{\alpha}}^{t_{DA}^{\beta}} CI_{DA}(t) \cdot \mu_{DA}(t)\right) + (1 - \gamma_{DA})$$

$$\times \frac{1}{2} \left(\frac{\sqrt{(ST_{DA} - t_{DA}^{\alpha,BF})^{2}}}{(t_{DA}^{\beta} - Task_{DA}) - t_{DA}^{\alpha,BF}} + \frac{\sqrt{(ET_{DA} - t_{DA}^{\beta,BF})^{2}}}{t_{DA}^{\beta,BF} - (t_{DA}^{\alpha} + Task_{DA})}\right)$$
(8)

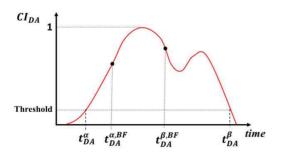


Fig. 6. Comfort distribution of DA

where  $\gamma_{DA}$  is a weights between the two terms.  $Task_{DA}$ is the required operating time of DA and represented by Eq. (9).  $ST_{DA}$  and  $ET_{DA}$  are the scheduled start and end times and expressed by Eq. (10).

$$\sum_{\forall t} \mu_{DA}(t) = Task_{DA}, \qquad t_{DA}^{\alpha} \le t \le t_{DA}^{\beta}$$
 (9)

$$ST_{DA} = \min_{t} \left\{ t \mid \mu_{DA}(t) = 1, \quad t_{DA}^{\alpha} \le t \le t_{DA}^{\beta} \right\}$$

$$ET_{DA} = \max_{t} \left\{ t \mid \mu_{DA}(t) = 1, \quad t_{DA}^{\alpha} \le t \le t_{DA}^{\beta} \right\}$$
(10)

DAs are divided into types depending on the continuity of operation: non-interruptible (NDA) and interruptible (IDA). Once NDS start, they operate continuously until  $Task_{DA}$  is satisfied. IDAs can be stopped and restarted sometimes until  $Task_{DA}$  is satisfied. These constraints are represented by

$$\sum_{t=t_{DA}^{\alpha}}^{t_{DA}^{\beta}} \left( \mu_{DA}(t-1) - \mu_{DA}(t) \right)^{2} = 2$$
 if) DA is NDA 
$$\sum_{t=t_{DA}^{\beta}}^{t_{DA}^{\beta}} \left( \mu_{DA}(t-1) - \mu_{DA}(t) \right)^{2} = 2 \times NI_{DA}$$
 if) DA is IDA

where  $\mu_{DA}(t_{DA}^{\alpha}-1)=0$ ,  $NI_{DA}$  and  $dlt_{DA}$  are the number of times and the delay duration an IDA can be stopped during operation, respectively, and  $ET_{DA} - ST_{DA} + 1 \le dlt_{DA}$ .

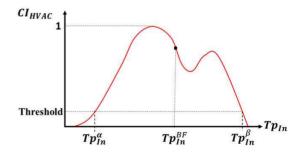
#### 3.2 AS Problem for HVAC

The electricity cost of HVAC,  $EC_{HVAC}$  is

$$EC_{HVAC} = \sum_{\forall t} \pi(t) \cdot P_{HVAC}^{R} \cdot \mu_{HVAC}(t)$$
 (12)

where  $P_{HVAC}^{R}$  is the rated power of HVAC and  $\mu_{HVAC}$  is a status variable and can have one of discrete values equally split within 0 and 1 to consider diverse operational states rather than a simple on/off operation.

Fig. 7 shows the comfort distribution for  $Tp_{In}$  at a certain time, where  $Tp_{ln}^a$  and  $Tp_{ln}^\beta$  indicate the allowable range of  $Tp_{ln}$  at that time, and  $Tp_{ln}^{BF}$  is the best fitted one.



**Fig. 7.** Comfort distribution for  $Tp_{In}$  at a certain time t

 $DI_{HVAC}$  of HVAC can be calculated by Eq. (13), where the first term means total inconvenience level during using HVAC. The second term means the ratio of the difference between the scheduled and best fitted  $Tp_{ln}$  to its possible

$$DI_{HVAC} = \frac{1}{T} \sum_{\forall t} \left\{ \begin{cases} \gamma_{HVAC} \times (1 - CI_{HVAC}(Tp_{ln}(t))) + (1 - \gamma_{HVAC}) \times \\ \sqrt{(Tp_{ln}(t) - Tp_{ln}^{BF}(t))^{2}} \\ \max \{Tp_{ln}^{BF}(t) - Tp_{ln}^{\alpha}(t), Tp_{ln}^{\beta}(t) - Tp_{ln}^{BF}(t)\} \end{cases} \right\}$$
(13)

The dynamic equation for  $Tp_{ln}$  according to HVAC operation over time can be represented by [16, 27]

$$Tp_{In}(t+1) = \varepsilon_{HVAC} \cdot Tp_{In}(t) + (1 - \varepsilon_{HVAC}) \left\{ Tp_{Out}(t) \pm \frac{CoP_{HVAC} \cdot P_{HVAC}^R \cdot \mu_{HVAC}(t)}{A_{In}} \right\}$$

$$(14)$$

where  $Tp_{ln}^{\alpha}(t) \le Tp_{ln}(t) \le Tp_{ln}^{\beta}(t)$ ,  $\varepsilon_{HVAC}$  is a heat emission constant,  $CoP_{HVAC}$  is the coefficient of HVAC performance, and  $A_{ln}$  is the thermal mass inside the room.

#### 3.3 AS Problem for EWH

In the case of EWH, the hot water usage pattern is modeled as several representative scenarios. Therefore, the electricity cost of EWH,  $EC_{EWH}$  can be expressed as the expected cost for all scenarios:

$$EC_{EWH} = \sum_{\forall S} \left\{ \sum_{\forall t} \pi(t) \cdot P_{EWH}^{S} \cdot \mu_{EWH}^{S}(t) \right\} \cdot Pb^{S}$$
 (15)

where  $P_{EWH}^R$  is the rated power of an EWH,  $\mu_{EWH}^S$  is a status variable under a scenario S and can have one of several discrete values between 0 and 1.  $Ph^{S}$  is the probability of the scenario S.

Fig. 8 depicts the representative scenarios for the hot water usage expressed in terms of the quantity of heat.

At first, AS for EWH is performed considering a scenario S. Then, the scheduling result is checked as

 $Q_{hw}(t)$  Representative Scenarios of HW usage

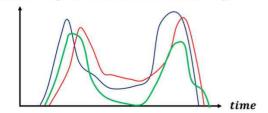


Fig. 8. Representative scenarios for hot water usage

regards whether the hot water demand of other scenarios  $(\hat{S})$  is met or not. If the hot water demand is not met, Ruser would feel inconvenience depending on the unmet demand. Under scenario S, the expected amount of the hot water demand unmet for other scenarios,  $DI_{FWH}^{S}$  can be expressed by (16) and (17):

$$DI_{EWH}^{S} = \sum_{\forall \hat{s}} \sum_{\forall t} nd^{\hat{s},S}(t) \cdot Pb^{\hat{s}}$$
(16)

$$nd^{\hat{S},S}(t) = \begin{cases} 0 & \text{if } ) \ Q_{Tk}^{\hat{S},S}(t) \ge Q_{HW}^{\hat{S}}(t) \\ Q_{HW}^{\hat{S}}(t) - Q_{Tk}^{\hat{S},S}(t) & \text{otherwise} \end{cases}$$
(17)

where  $Q_{HW}^{\hat{S}}$  is the heat quantity of hot water used according to scenario  $\hat{S}$ , and  $Q_{Tk}^{\hat{S},S}$  is the heat quantity of water within a water tank, under the situation that R-user uses hot water in accordance with  $\hat{S}$  but EWH operates according to S.  $nd^{\hat{S},S}$  is the heat quantity of a shortfall in hot water within the tank under such the situation.

The expected  $DI_{EWH}$  for all of the scenarios is

$$DI_{EWH} = \sum_{\forall S} DI_{EWH}^{S} \cdot Pb^{S} \tag{18}$$

The dynamic equation and constraint for  $Q_{Tk}^{\hat{S},S}$  can be expressed by [27]

$$Q_{Tk}^{\hat{S},S}(t+1) = Q_{Tk}^{\hat{S},S}(t) - Q_{HW}^{\hat{S}}(t) + CoP_{EWH} \cdot P_{EWH}^{R} \cdot \mu_{EWH}^{S}(t) - \frac{A_{Tk} \cdot (Q_{Tk}^{\hat{S},S}(t) - Q_{Out})}{V_{Tk} \cdot R_{Tk}}$$
(19)

where  $Q_{Tk}^{Min} \leq Q_{Tk}^{\hat{S},S}(t) \leq Q_{Tk}^{Max}$ ,  $CoP_{EWH}$  is the coefficient of the EWH performance and  $A_{Tk}$ ,  $V_{Tk}$ , and  $R_{Tk}$  are the cross-section area, volume, and thermal coefficient of resistivity, respectively, of the water tank.  $Q_{Tk}^{Min}$  and  $Q_{Tk}^{Max}$ are the min/maximum limits for the heat quantity of hot water in the tank, respectively.

#### 3.4 AS Problem for ESS

ESS is considered as an option to further reduce the electricity cost. The objective function for the ESS can be expressed by

$$\min F_{ESS} = \sum_{\forall t} \pi(t) \times \left( P_{Other}(t) + P_{ESS}^{R} \cdot \mu_{ESS}(t) \right)$$

$$P_{Other}(t) = P_{BA}(t) + \sum_{\forall DA} P_{DA}(t) + P_{HVAC}(t) + P_{EWH}(t)$$
(20)

Where  $P_{BA}$  is a total power consumption of basic appliances which are not the subject of AS,  $P_{ESS}^{R}$  is the rated power of ESS when charging or discharging power.  $\mu_{\rm ESS}$  is a status variable with a discrete value between -1 and 1; the positive values indicate a charging operation, whereas the negative values represent discharging.

The ESS operation is limited by the allowable range of the state of charge (SOC). This can be represented by

$$SOC_{ESS}(t) = SOC_{ESS}(t-1) + \frac{P_{ESS}^{R} \cdot \mu_{ESS}(t)}{E_{ESS}^{R} \cdot \eta_{ESS}(t)}$$
where  $SOC_{ESS}^{Min} \leq SOC_{ESS}(t) \leq SOC_{ESS}^{Max}$  (21)

where  $E_{\rm ESS}^{\rm R}$  is the rated energy capacity of the ESS,  $\eta_{\rm ESS}$  is the charging/discharging efficiency, and  $SOC_{\rm ESS}^{\rm Min}$  and  $SOC_{ESS}^{Max}$  are the min/maximum limits, respectively.

# 4. Numerical Case Study

Various AS tasks are performed according to  $\omega_{EC}$  and  $\omega_{DI}$  to investigate the impacts of user convenience on AS.

Table 1. Detailed Information on Appliances

Appliances		$P_{DA}^{R}$ [kw]	$Task_{DA}$	$dlt_{DA}$	$NI_{DA}$		
rr ·		DA C 3	(the time unit: 15		min.)		
$DA_1$	IDA	[0.55, 0.55, 0.75, 0.75]	4	4	2		
$DA_2$	IDA	[0.55, 0.55, 0.75, 0.75]	4	4	2		
$DA_3$	IDA	[0.75, 0.75]	2	6	2		
$DA_4$	NDA	[1.2, 1.2]	2	0	1		
$DA_5$	NDA	[0.6, 0.6, 0.6, 0.75, 0.75]	5	0	1		
$DA_6$	IDA	[1.0, 1.0, 0.75, 0.75]	4	2	2		
HVAC	$P_{HVAC}^{R} = 3.0 \text{kW}, \ \varepsilon_{HVAC} = 0.95, \ CoP_{HVAC} = 25, \ A_{In} = 1.2$						
EWH	$P_{EWH}^{R} = 2.0 \text{kW}, CoP_{EWH} = 300, A_{Tk} = 8, V_{Tk} = 125,$						
	$R_{Tk} = 12, \ Q_{out} = 300, \ Q_{Tk}^{Min} = 2,500, \ Q_{Tk}^{Max} = 10,000$						
Egg	$P_{ESS}^{R} = 1.2 \text{kW}, \ E_{ESS}^{R} = 3.6 \text{kWh}, \ \eta_{ESS} = 1.0,$						
ESS		$E_{ESS}^{Init} = 1.8$ kWh, $SOC_{ESS}^{Max} =$	=1.0, <i>SOC</i>				

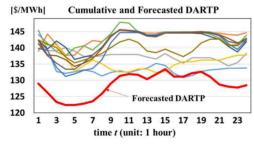
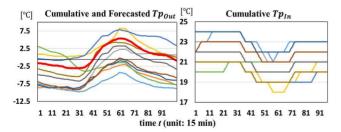


Fig. 9. Cumulative and forecasted DARTP



**Fig. 10.** Cumulative data of  $Tp_{\uparrow}$ 

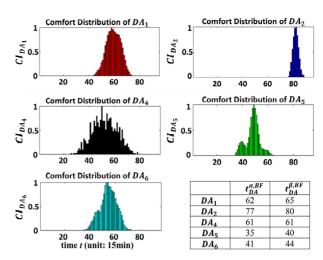
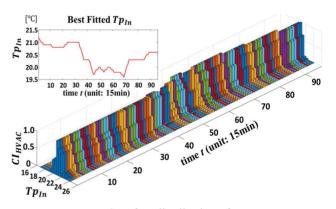


Fig. 11. Comfort distributions of DAs



**Fig. 12.** Comfort distributions for

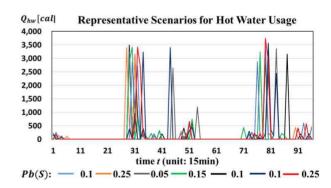


Fig. 13. Representative scenarios for hot water usage

The subject of AS consists of six DAs and HVAC, EWH, and ESS. Table 1 presents detailed information for the appliances, where  $DA_1$ ,  $DA_2$  and  $DA_3$  mean the 1<sup>st</sup>, 2<sup>nd</sup>, and 3<sup>rd</sup> usage of a dishwasher during the day, respectively.  $DA_4$ ,  $DA_5$ , and  $DA_6$  are a vacuum cleaner, a washing machine, and an electric laundry dryer.

Fig. 9 shows the cumulative and forecasted DARTP with the unit of 1hour. Fig. 10 represents the cumulative and forecasted  $Tp_{Out}$  and  $Tp_{In}$  with the unit of 15 min.

Because  $DA_3$  is mainly used at late night, it is assumed to react only to DARTP. Therefore, its usage pattern is not modeled. Fig. 11 shows the modeling results for other five DAs together with their best fitted times.

Fig. 12 shows the comfort distribution for  $Tp_{ln}$  over time together with the best fitted  $Tp_{ln}$ .

Fig. 13 shows the representative scenarios for the hot water usage obtained by the clustering-based method.

In order to compare diverse results of AS depending on the weighting factors  $\omega_{EC}$  and  $\omega_{DI}$ , several cases are defined:

- Base Case: Focusing fully on economic efficiency (i.e.,  $\omega_{EC} = 1.0$ ,  $\omega_{DI} = 0$ ).
- Case I: Focusing fully on user convenience (i.e.,  $\omega_{EC} = 0$ ,  $\omega_{DI} = 1.0$ ).
- Case II: AS under condition of  $\omega_{EC} = 0.75$ ,  $\omega_{DI} = 0.25$ .
- Case III: AS under condition of  $\omega_{EC} = 0.5$ ,  $\omega_{DI} = 0.5$ .
- Case IV: AS under condition of  $\omega_{EC} = 0.25, \omega_{DI} = 0.75$ .

Each appliance may operate with more states than the two states (i.e., 'on and off'). The AS problem is to determine the status variables,  $\mu$  of each appliance over the entire time period and is solved based on the branch and bound method (B&B) [28], in this paper.

Table 2 presents the AS results for all DAs. In Base Case, individual DAs operate during times with low electricity prices within the respective allowable time ranges. As increases, the operating time moves to more convenient times (i.e., times closer to the modeled usage pattern).

Figs. 14 and 15 show the AS results for HVAC in the Base Case and Case I. In the Base Case, HVAC operates less frequently but with a higher power when operating to satisfy  $Tp_{In}$  of the minimum level and to minimize the cost. Thus,  $EC_{HVAC}$  is \$2.525, while  $DI_{HVAC}$  is 0.9461. Meanwhile, in Case I, the HVAC operates more frequently with a lower power to maximize the level of convenience of the R-user. As a result,  $EC_{HVAC}$  increases to \$2.945,

**Table 2.** AS Results for DAs

No. Case	No. DA	$\mu_{DA}(t) = 1$	EC <sub>DA</sub>	$DI_{DA}$	No. DA	$\mu_{DA}(t) = 1$	$EC_{DA}$	DIDA
Base	1	49-52	84.7	0.684	2	86-89	83.2	0.941
I		61-64	85.2	0.126		81,82 85,86	83.4	0.397
II		61-64	85.2	0.126		81-83, 85	83.5	0.238
III		61-64	85.2	0.126		81-84	83.6	0.183
IV		57-60	86.7	0.064		80-83	84	0.122
Base		17, 20	45.9	(=)	4	26, 27	74.1	0.988
I		17,20	45.9	-		27, 28	74.1	0.986
II	3	17, 20	45.9	7 <b>=</b> 5		27, 28	74.1	0.986
III		17, 20	45.9	-		49, 50	78.2	0.16
IV		17, 20	45.9	427		49, 50	78.2	0.16
Base	5	33-37	106.9	0.839	6	35, 36, 39, 40	113.8	0.866
I		33-37	106.9	0.839		49-52	114.1	0.278
II		48-52	107.8	0.178		49-52	114.1	0.278
III		48-52	107.8	0.178		50-53	114.4	0.177
IV		47-51	108	0.15		52-55	115	0.066

while  $DI_{HVAC}$  decreases to 0.0979.

Table 3 presents the numerical AS results of HVAC for all cases, where  $EC_{HVAC}$  increases as the user convenience for HVAC is more weighted.

Fig. 16 shows the AS results for the EWH in the Base Case and Case I, where thick lines represent the power consumption of EWH over time and the dotted lines denote the quantities of heat for hot water in the tank.

Compared with the Base Case, EWH operates more frequently in Case I to keep water in the tank at a higher  $Q_{Tk}$  for preparing for various scenarios of the hot water

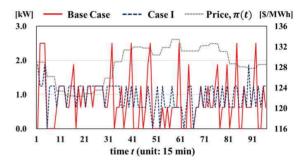
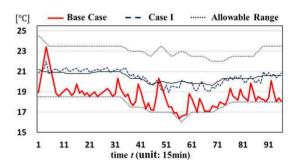
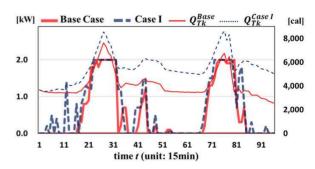


Fig. 14. Results of AS for HVAC in Base Case and Case I



**Fig. 15.** Results of  $Tp_{In}$  in Base Case and Case I



**Fig. 16.** Results of AS for EWH

Table 3. Numerical Results for HVAC and EWH

Cases	$\omega_{\scriptscriptstyle EC}$	$EC_{HVAC}$	$DI_{HVAC}$	$EC_{EWH}$	$DI_{\it EWH}$
Base	1	2.525	0.946	1.674	3284.896
I	0.75	2.762	0.146	1.778	1051.624
II	0.5	2.863	0.109	1.843	730.122
III	0.25	2.924	0.099	1.980	201.201
IV	0	2.944	0.098	2.090	45.105

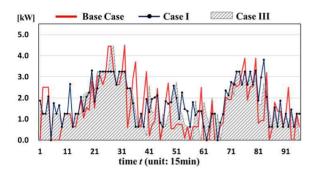


Fig. 17. AS results for all appliances

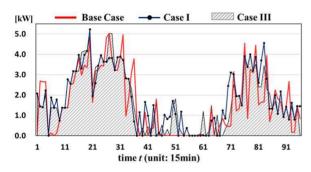


Fig. 18. AS results for all appliances with ESS

usage. Table 3 also presents the numerical results of EWH in detail, where the tradeoff between  $EC_{EWH}$  and  $DI_{EWH}$ can be observed.

Fig. 17 shows the final results of AS for DAs, HVAC, and EWH. In the Base Case, the appliances intermittently operate, but generally consume more power when the electricity price is low. Consequently, the total electricity cost is \$4.707. However, the results of Cases I and II show that power consumption is slightly less but more frequent to improve the convenience. As a result, the total power consumption is increased. Moreover, the total costs increase to \$5.217 and \$5.552, respectively.

The electricity cost for the three cases when considering ESS are reduced to \$4.676, \$5.186, and \$5.520, respectively. However, the peak load for all the cases increase because the ESS is mainly charged at times with low prices. From Fig. 18, it can be seen that the impacts of user convenience on AS is similar to the previous results shown in Fig. 17 because the ESS is only used for the cost reduction. Therefore, even when considering ESS, it can be again confirmed that the user convenience should be considered in performing AS for P-DR.

## 5. Conclusion

This paper proposes a methodology for AS that reflects user convenience based on the usage pattern. Two methods are introduced to model the usage patterns: a copula-based method for DAs and HVAC, and a clustering-based method for EWH. Based on the results of the usage pattern modeling, the discomfort index, DI is formulated to evaluate the degree of user convenience for using appliances. The AS problem are expressed by two terms of cost and DI. In the case study, various AS tasks are performed according to two weighting factors for cost and DI. The results show that the user convenience significantly affects AS, and R-user can make a variety of plans for using appliances the next day depending on the relative importance of user convenience to cost. However, a major issue remains, which is the decision-making problem to select the most preferred one among the diverse schedules. A follow-up study for the decision-making problem are conducting and the proposed methodology would contribute to induce more usefully P-DR participation from R-users.

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Je-Seok Shin He received the B.S. degrees in 2010, and is currently a Ph.D. candidate in department of Electrical Engineering, Hanyang University, Seoul, Korea. His research interests are demand response, smart energy management system, small and large scale system optimization.



In-Su Bae He received B.S., M.S., and Ph.D. degrees in electrical engineering from Hanyang University, Seoul, Korea, in 1998, 2003, and 2007, respectively. Since 2008, he has been with the department of electrical engineering, Kangwon National University, Samcheok, Korea. His main research

interests include power system reliability, planning, and optimization.



Jin-O Kim He received the B.S. and M.S. degrees in electrical engineering from Seoul National University, Seoul, Korea, respectively, and the Ph.D. degree from Texas A&M University, College Station, TX, USA. Currently, he is a Professor with the Department of Electrical Engineering, Hanyang

University, Korea. His research interests are power system reliability and economics, smart grid, micro-grid with renewable energy sources.