

# Optimal Voltage Vector Selection Method for Torque Ripple Reduction in the Direct Torque Control of Five-phase Induction Motors

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## Abstract

This paper presents an improved switching selection method for the direct torque control (DTC) of five-phase induction motors (IMs). The proposed method is conducted using optimal switching selection. A five-phase inverter has 32 voltage vectors which are divided into 30 nonzero voltage vectors and two zero voltage vectors. The magnitudes of the voltage vectors consist of large, medium, and small voltage vectors. In addition, these vectors are related to the torque response and torque ripple. When a large voltage vector is selected in a drive system, the torque response time decreases with an increased torque ripple. On the other hand, when a small voltage vector is selected, the torque response time and torque ripple increase. As a result, this paper proposes an optimal voltage vector selection method for improved DTC of a five-phase induction machine depending on the situation. Simulation and experimental results verify the effectiveness of the proposed control algorithm.

**Key words:** Five-phase inverter, Induction motor, Switching selection method, Voltage vector

## I. INTRODUCTION

A five-phase induction motor (IM) has many merits when compared with three-phase induction motors. First, a five-phase IM has concentrated windings instead of sinusoidal windings. It generates at least 10% more output torque when compared with a three-phase IM [1]-[3]. Second, a five-phase IM has more voltage vectors when compared with a three-phase IM. Consequently, a five-phase IM is good for direct torque control (DTC) because it is possible to choose an optimal voltage vector for DTC.

DTC has many advantages, such as a fast torque response, a simple control method without a coordinate transformation, robustness against motor parameter variations, and a high-power motor drive method [4]-[14]. Because DTC is used with a chosen voltage vector, many voltage vectors are able to

operate efficiently. Therefore, a five-phase IM is more efficient under DTC when compared with a three-phase IM [15]-[18].

However, DTC has drawbacks. A large torque ripple is generated in a low speed range because of the small back EMF of an induction machine. In addition, a short control period is required to achieve good performance, because DTC is performed by using a selected voltage vector during one control period. If the control period is long, torque ripple is produced by the applied effective voltage vector. Torque ripple reduction methods of DTC have been researched in [19]-[22]. Some of them have introduced a torque ripple reduction method for an interior permanent magnet synchronous motor (IPMSM). In addition, the other papers suggest methods to choose the optimal voltage vector selection method for the DTC of a five-phase IM [23], [24]. Depending on the magnitude of the voltage vector in a five-phase inverter, the torque and flux hysteresis bands using the DTC of five-levels are controlled by two different voltage vector magnitudes (large and medium voltage vectors) [23]. The hysteresis band in the case of seven levels is controlled by using all of the voltage vectors in a five-phase IM [24]. However, the look-up

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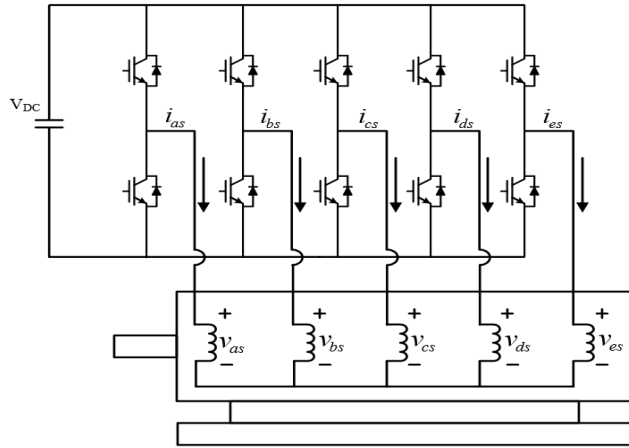


Fig. 1. Two-level inverter circuit for operating a five-phase IM.

$V_{L1}[11001], V_{L2}[11000]$	$V_{M1}[10000], V_{M2}[11101]$	$V_{S1}[01001], V_{S2}[11010]$
$V_{L3}[11100], V_{L4}[01100]$	$V_{M3}[01000], V_{M4}[11110]$	$V_{S3}[10100], V_{S4}[01101]$
$V_{L5}[01110], V_{L6}[00110]$	$V_{M5}[00100], V_{M6}[01111]$	$V_{S5}[01010], V_{S6}[10110]$
$V_{L7}[00111], V_{L8}[00011]$	$V_{M7}[00010], V_{M8}[10111]$	$V_{S7}[00101], V_{S8}[01011]$
$V_{L9}[10011], V_{L10}[10001]$	$V_{M9}[00001], V_{M10}[11011]$	$V_{S9}[10010], V_{S10}[10101]$
<Large Vector>	<Medium Vector>	<Small Vector>
< $V_s: 0.6472 V_{DC}$ >	< $V_s: 0.4 V_{DC}$ >	< $V_s: 0.2472 V_{DC}$ >

Fig. 2. Switching state in a five-phase inverter.

table for the voltage vector selection provided by [23], [24] has a large voltage vector magnitude in the steady state. As a result, the selection of a large voltage vector does not facilitate torque ripple reduction.

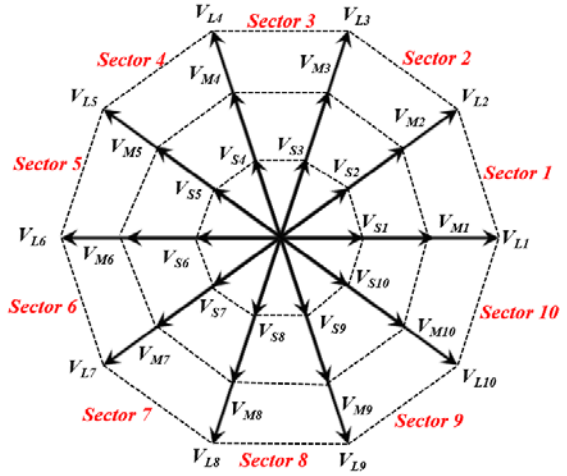
This paper proposes an improved method for the voltage vector selection in a five-phase IM for DTC. The voltage vectors of a five-phase IM are composed of nonzero voltage vectors, which consist of a large voltage vector, a medium voltage vector, and a small voltage vector. The large voltage vector has a fast torque response in the transient state. However, if the large voltage vector is selected, the steady-state torque ripple increases in the low-speed area. As a result, in order to reduce the torque ripple, medium and small voltage vectors are used in the steady state. In addition, a large voltage vector is only used in the transient state. The proposed control strategy is verified by simulation and experiment results.

## II. IMPROVED SWITCHING SELECTION METHOD

### A. Voltage Vectors of a Five-Phase Inverter

A schematic of a five-phase IM drive is shown in Fig. 1. This paper uses a two-level inverter to operate a five-phase IM. The five-phase inverter is composed of two switches in each leg, which are operated complementarily. The voltage vectors of the five-phase inverter are composed of 32 voltage vectors. The switching states consist of two-zero voltage vectors and 30 nonzero voltage vectors.

Formulas for the phase and magnitude values of the voltage



L: Large, M: Medium, S: Small

Fig. 3. Space vector plane in a five-phase VSI.

TABLE I  
PROPOSED LOOKUP TABLE FOR VOLTAGE VECTOR SELECTION

$C_F$	$C_T$	Sector Number									
		1	2	3	4	5	6	7	8	9	10
+	+3	$V_{L3}$	$V_{L4}$	$V_{L5}$	$V_{L6}$	$V_{L7}$	$V_{L8}$	$V_{L9}$	$V_{L10}$	$V_{L1}$	$V_{L2}$
	+2	$V_{M3}$	$V_{M4}$	$V_{M5}$	$V_{M6}$	$V_{M7}$	$V_{M8}$	$V_{M9}$	$V_{M10}$	$V_{M1}$	$V_{M2}$
	+1	$V_{S3}$	$V_{S4}$	$V_{S5}$	$V_{S6}$	$V_{S7}$	$V_{S8}$	$V_{S9}$	$V_{S10}$	$V_{S1}$	$V_{S2}$
	-1	$V_{S9}$	$V_{S10}$	$V_{S1}$	$V_{S2}$	$V_{S3}$	$V_{S4}$	$V_{S5}$	$V_{S6}$	$V_{S7}$	$V_{S8}$
	-2	$V_{M9}$	$V_{M10}$	$V_{M1}$	$V_{M2}$	$V_{M3}$	$V_{M4}$	$V_{M5}$	$V_{M6}$	$V_{M7}$	$V_{M8}$
	-3	$V_{L9}$	$V_{L10}$	$V_{L1}$	$V_{L2}$	$V_{L3}$	$V_{L4}$	$V_{L5}$	$V_{L6}$	$V_{L7}$	$V_{L8}$
-	+3	$V_{L4}$	$V_{L5}$	$V_{L6}$	$V_{L7}$	$V_{L8}$	$V_{L9}$	$V_{L10}$	$V_{L1}$	$V_{L2}$	$V_{L3}$
	+2	$V_{M4}$	$V_{M5}$	$V_{M6}$	$V_{M7}$	$V_{M8}$	$V_{M9}$	$V_{M10}$	$V_{M1}$	$V_{M2}$	$V_{M3}$
	+1	$V_{S4}$	$V_{S5}$	$V_{S6}$	$V_{S7}$	$V_{S8}$	$V_{S9}$	$V_{S10}$	$V_{S1}$	$V_{S2}$	$V_{S3}$
	-1	$V_{S8}$	$V_{S9}$	$V_{S10}$	$V_{S1}$	$V_{S2}$	$V_{S3}$	$V_{S4}$	$V_{S5}$	$V_{S6}$	$V_{S7}$
	-2	$V_{M8}$	$V_{M9}$	$V_{M10}$	$V_{M1}$	$V_{M2}$	$V_{M3}$	$V_{M4}$	$V_{M5}$	$V_{M6}$	$V_{M7}$
	-3	$V_{L8}$	$V_{L9}$	$V_{L10}$	$V_{L1}$	$V_{L2}$	$V_{L3}$	$V_{L4}$	$V_{L5}$	$V_{L6}$	$V_{L7}$

vectors are:

$$\frac{2}{5}(S_a + aS_b + a^2S_c + a^3S_d + a^4S_e) = f_{ds1}^s + jf_{qs1}^s, \quad (1)$$

$$(a = e^{j2\pi/5})$$

$$\theta_{ph} = \tan^{-1}\left(\frac{f_{qs1}^s}{f_{ds1}^s}\right), \quad (2)$$

where,  $f_{ds1}^s$  and  $f_{qs1}^s$  are the dq-axis stationary reference frame voltage vectors by the switching state, and  $\theta_{ph}$  is the phase angle. The magnitude of the voltage vectors is presented using (1) in Fig. 2.  $V_{xy}[S_a S_b S_c S_d S_e]$  represents the switching state of the five-phase inverter in Fig. 2. Where,  $x$  is the large, medium, and small magnitude.  $y$  is the number of sector intervals according to the phase angle.  $S_a$  presents the switching state of the upper switch of phase A. For example, if the upper switch

of phase A is turned on,  $S_a$  becomes 1. The voltage vector magnitudes are divided into three categories:  $0.6472 V_{DC}$  (the value of the large voltage vector),  $0.4 V_{DC}$  (the value of the medium voltage vector), and  $0.2472 V_{DC}$  (the value of the small voltage vector) [25]. The voltage vector plane of the five-phase IM is shown in Fig. 3. The voltage vector plane is represented using the voltage vector phase and magnitude. The large, medium, and small voltage vectors are placed at the same phase region. The phase angle of  $V_{Ll}$ ,  $V_{Ml}$ , and  $V_{Sl}$  is  $0^\circ$  by using (2). In addition, each voltage vector is divided by intervals of  $36^\circ$  according to the sector. It should be noted that the torque ripple and torque response speed can change in accordance with three voltage vectors of different magnitudes. Therefore, these vectors can be used to reduce the torque ripple for a five-phase IM.

### B. Proposed Switching Selection Method

An optimal switching selection method is introduced by using the voltage vectors of a five-phase inverter. In order to control the flux and torque, the voltage vectors are selected from the hysteresis comparator output of the torque and flux [26].

The rotor flux formula is:

$$v_{dqs}^s = R_s i_{dqs}^s + \frac{d\lambda_{dqs}^s}{dt}, \lambda_{dqs}^s = \int (v_{dqs}^s - R_s i_{dqs}^s) dt, \quad (3)$$

$$\lambda_{dqr}^s = \frac{L_r}{L_m} (\lambda_{dqs}^s - \sigma L_s i_{dqs}^s), \theta_e = \tan^{-1} \left( \frac{\lambda_{dqr}^s}{\lambda_{dr}^s} \right), \quad (4)$$

where,  $v_{dqs}^s$ ,  $R_s$ ,  $i_{dqs}^s$ ,  $\lambda_{dqs}^s$ ,  $\lambda_{dqr}^s$ ,  $\sigma$ ,  $L_s$ ,  $L_r$ ,  $L_m$ , and  $\theta_e$  indicate the dq-axis voltage of the synchronous reference frame, stator resistance, stator dq-axis current, stator synchronous reference frame flux, rotor synchronous reference frame flux, leakage flux, stator inductance, rotor inductance, mutual inductance, and flux angle, respectively. The voltage model is used for calculating the flux angle and rotor flux, since it is a convenient flux estimator for IM control. Some motor parameters are needed to use the voltage model. Using (3) and (4), the estimated flux angle can be divided into 10 sectors of  $36^\circ$  each. After that, the voltage vector is selected by considering the output of the comparator and the estimated flux angle.

The proposed voltage vector selection for DTC is summarized as shown in Table I. In addition, the medium and small voltage vectors used in the steady state are indicated in the table. The large voltage vector is used in the transient state according to the proposed algorithm.  $C_T$  and  $C_F$  present the output values of the torque and flux comparator [27]. If  $C_T$  is +2 and -2, the medium voltage vector is selected. If  $C_T$  is +1 and -1, the small voltage vector is selected.

Fig. 4 shows the output torque using each of the voltage vectors in the five-phase inverter system. Fig. 4(a) presents the output torque in a short control period. The torque is controlled in the hysteresis band. On the other hand, Fig. 4(b) has a long control period. When a large voltage vector is selected during a

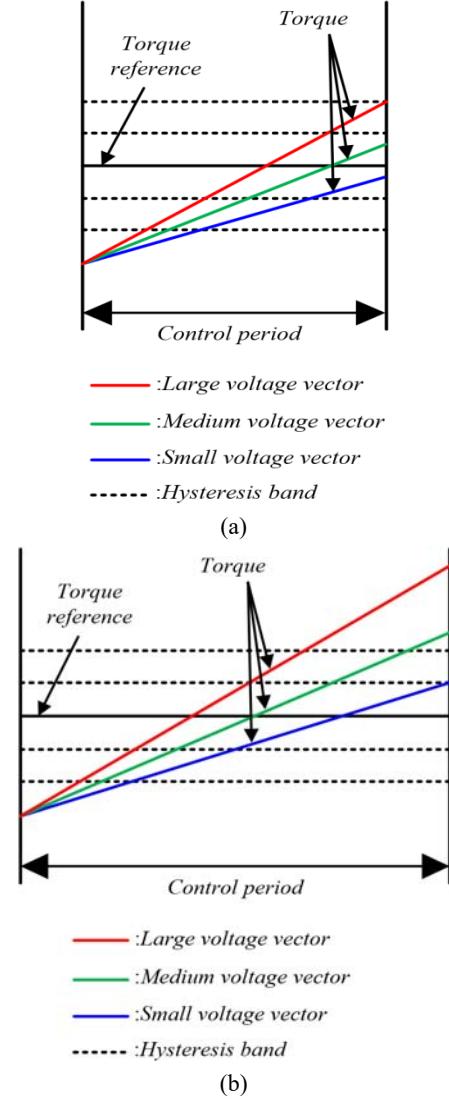


Fig. 4. Output torque using each of the voltage vectors in a five-phase inverter system. (a) Short control period. (b) Long control period.

long control period, the torque is controlled over the hysteresis band in each control time. As a result, a large torque band is produced in each control time. As a result, a large torque is produced by the large voltage vector. When a small voltage vector is selected at the same time, a small torque is produced by the small voltage vector. If the look-up table has a large voltage vector for the DTC, the torque ripple increases in a long control period and steady state. The large voltage vector is not used in the look-up table of the proposed method. Therefore, the torque ripple is reduced when compared to the conventional method. In addition, the proposed method has good performance in the low speed area where a large voltage vector is not required.

In order to reduce the torque ripple in the transient state, Fig. 5 shows the proposed selection method of a large voltage in the transient state. At first, this method can be verified using the difference of  $T_{ref}(k-1)$  and  $T_{ref}(k)$ . Second, if the difference

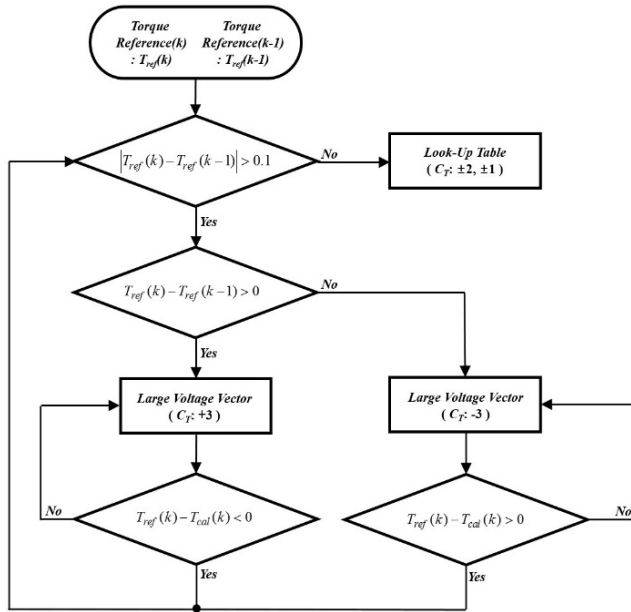


Fig. 5. Proposed large voltage vector selection method for a transient state.

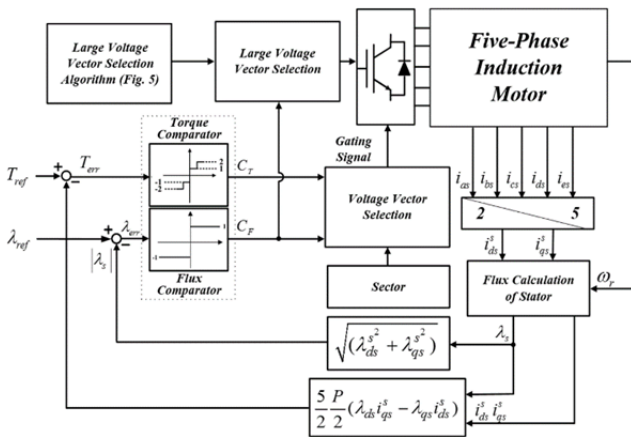
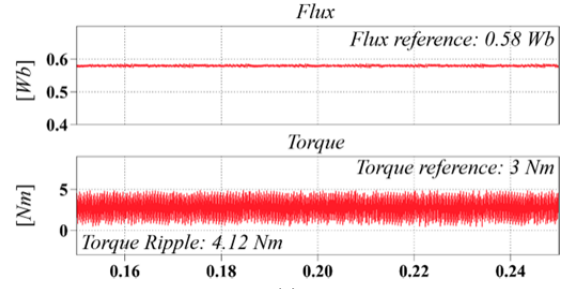


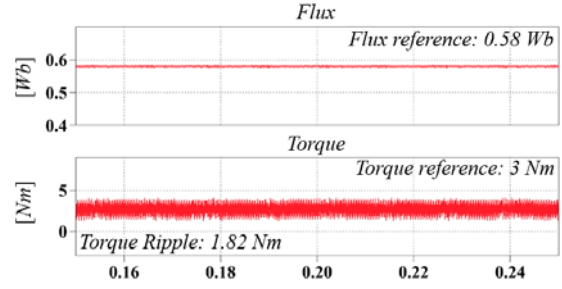
Fig. 6. Control block diagram of the proposed voltage vector selection method.

between  $T_{ref}(k-1)$  and  $T_{ref}(k)$  is bigger than 0.1 for the threshold, this situation becomes a transient state. Then a large voltage vector ( $C_T: +3$  or  $-3$ ) is selected in accordance with the difference between the torque references. After that, the next voltage vector is selected in accordance with the difference between  $T_{ref}(k)$  and  $T_{cal}(k)$ . On the other hand, when it is less than 0.1, this situation becomes a steady state. After that, small and medium voltage vector ( $C_T: \pm 1, \pm 2$ ) are selected using the magnitude of  $T_{ref}$  which can be divided into hysteresis bands. For example, when the torque reference is changed from 3 Nm to 5 Nm,  $T_{ref}(k-1)$  and  $T_{ref}(k)$  are 3 Nm and 5 Nm in the proposed method. Moreover, when  $T_{ref}(k-1)$  and  $T_{ref}(k)$  are not equal, a large voltage vector is selected.

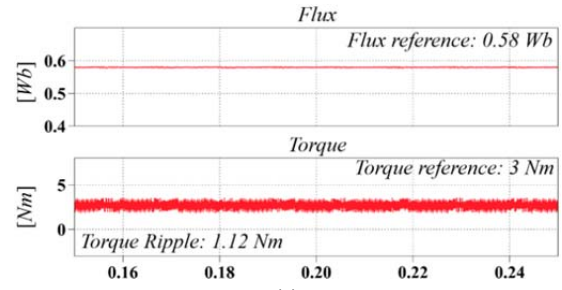
Fig. 6 shows a control block diagram of the proposed voltage vector selection method. A transient state is used for the large voltage vector as shown in Fig. 5. In addition, small and medium voltage vectors are used for the steady state.



(a)



(b)



(c)

Fig. 7. Torque and flux control using different voltage vector magnitudes. (a) Large voltage vector. (b) Medium voltage vector. (c) Small voltage vector.

Therefore, when Fig. 6 is used in the five-phase inverter, the torque ripple can be reduced when compared with the conventional method.

### III. SIMULATION RESULTS

Simulation results are used to verify the optimal voltage vector selection method. The control time of the proposed method for the simulation is set to 100  $\mu$ s. Furthermore, the speed is set to 300 rpm, the torque reference is set to 5 Nm, and the reference of the rated flux is 0.4 Wb in the PLECS tool.

Simulation results of the torque and flux control using different voltage vectors are shown Fig. 7. First, Fig. 7(a) shows the torque ripple when the DTC uses a large voltage vector. It has a torque ripple value of 3.07 Nm. The simulation result in the case of a small voltage vector is represented in Fig. 7(c).

As a result, when a small voltage vector is used for DTC, the torque ripple is 1.16 Nm, which is a reduction of approximately 1.19 Nm when compared with the case of a large voltage vector. In the steady state, the torque ripple has a minimum value when using a small voltage vector.

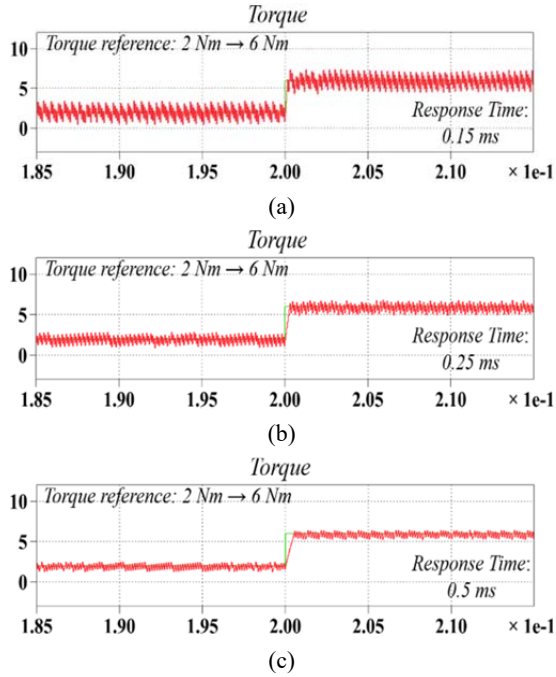


Fig. 8. Change in the torque reference (2 Nm  $\rightarrow$  6 Nm). (a) Large voltage vector. (b) Medium voltage vector. (c) Small voltage vector.

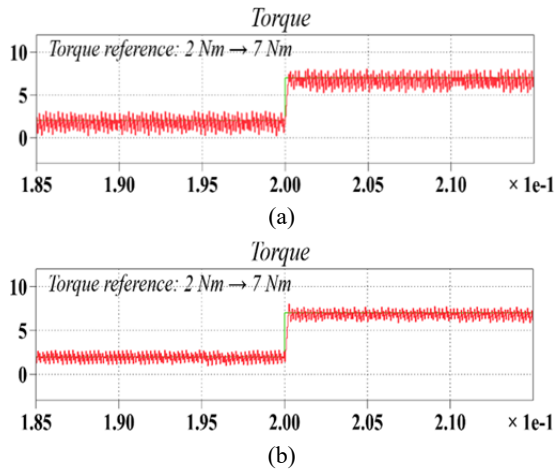


Fig. 9. Change in the torque reference (2 Nm  $\rightarrow$  7 Nm): (a) seven-level hysteresis band; (b) proposed method.

Fig. 8 shows simulation results of the DTC method for each of the voltage vectors in a transient state. At 0.2 s, the torque reference is changed from 2 Nm to 6 Nm. When a large voltage vector is selected for the DTC in a five-phase inverter, the time of the torque response is 0.15 ms in the transient state. On the other hand, when a small voltage vector is selected, the torque response time is 0.5 ms in the transient state. This means that the large voltage vector has the best performance considering the torque response time in a transient state owing to a maximum voltage input.

Comparison results of the seven-level comparator method and the proposed method are shown in Fig. 9. The torque response time of Fig. 9(a) is equal to that of Fig. 9(b) in the

TABLE II  
COMPARISON RESULTS OF THE VOLTAGE VECTORS

Comparison results Voltage vector	Torque ripple	Response time
Large voltage vector	4.12 Nm	0.15 ms
Medium voltage vector	1.82 Nm	0.25 ms
Small voltage vector	1.12 Nm	0.5 ms

TABLE III  
SPECIFICATIONS OF A FIVE-PHASE IM

Parameter	Value
Capacity	1.5 kW
Rated voltage	220 V
Rated frequency	60 Hz
Rated current	4.9 A
Rated speed	1684 rpm

transient state because both methods use large voltage vectors. However, the torque ripple of Fig. 9(a) is larger than that of Fig. 9(b) because a large voltage vector is being used in both the transient state and the steady state in Fig. 9(a). The proposed method is controlled by a medium voltage vector and a small voltage vector ( $C_r$ : +2, +1, -1, -2) in the steady state. Therefore, the torque ripple of Fig. 9(b) is reduced in the steady state using the proposed method.

Table II shows the torque ripple and torque response time using each of the voltage vectors. It is noted that a large voltage vector produces a large torque ripple. However, the torque response time is fast. In addition, a small voltage vector produces a small torque ripple. However, the torque response time is slow. Therefore, if a large vector is used only in the transient state, the torque ripple is reduced and the torque response is fast.

#### IV. EXPERIMENT RESULTS

The motor specifications are listed in Table III. The experimental setup consists of a load motor, a five-phase IM, a control board, and a power board, as shown in Fig. 10. A DSP controller, TMS320F 28335 from Texas Instruments, is used for the digital implementation of the proposed technique. The sampling time of the digital controller in the experimental setup is set to 100  $\mu$ s.

Fig. 11 illustrates experimental results for different voltage vectors. The parameters are as follows: 3 Nm torque, 0.58 Wb flux, and 300 rpm speed. The case of a large voltage vector is shown in Fig. 11(a). It is clear that the torque ripple value is approximately 2.58 Nm. For a small voltage vector, the torque ripple is much smaller, with a value of 1.28 Nm. Therefore, the torque ripple decreases when using a small voltage vector.



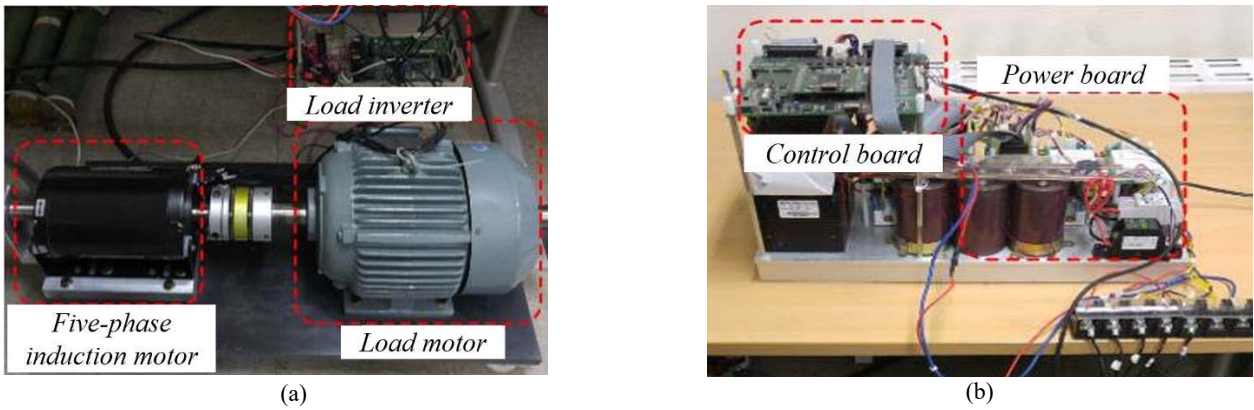


Fig. 10. Experimental setup. (a) Five-phase IM and load motor. (b) Control board and power board.

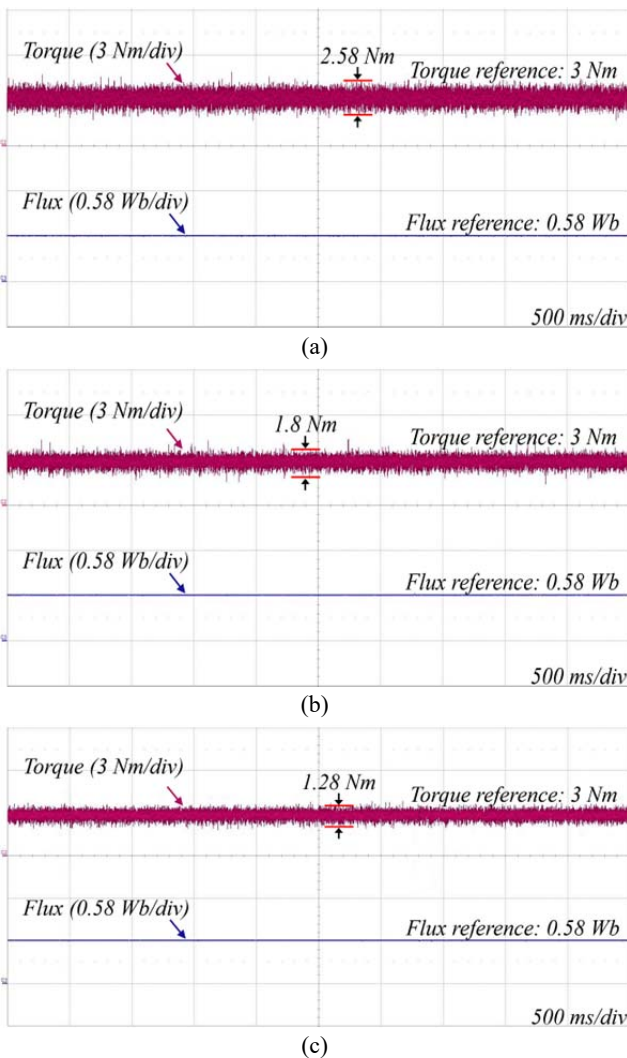


Fig. 11. Experiment results of the torque and flux control using the different voltage vector magnitudes. (a) A large voltage vector. (b) A medium voltage vector. (c) A small voltage vector.

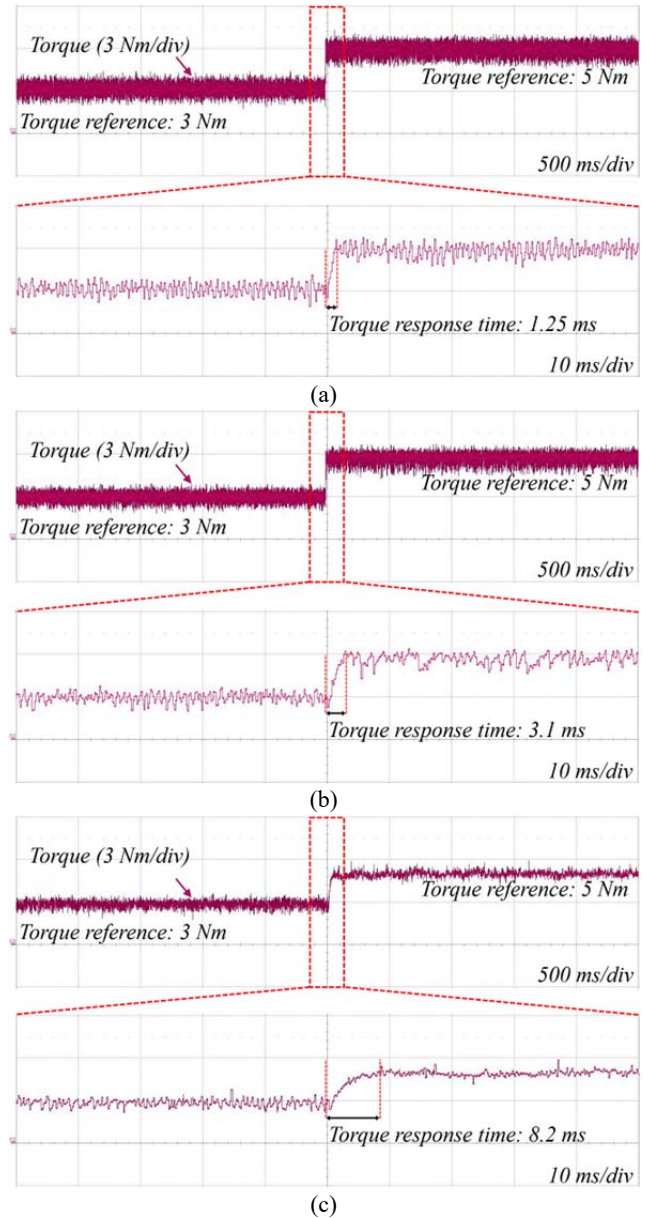


Fig. 12. Experimental results for a change in the torque reference (3 Nm → 5 Nm). (a) A large voltage vector. (b) A medium voltage vector. (c) A small voltage vector.

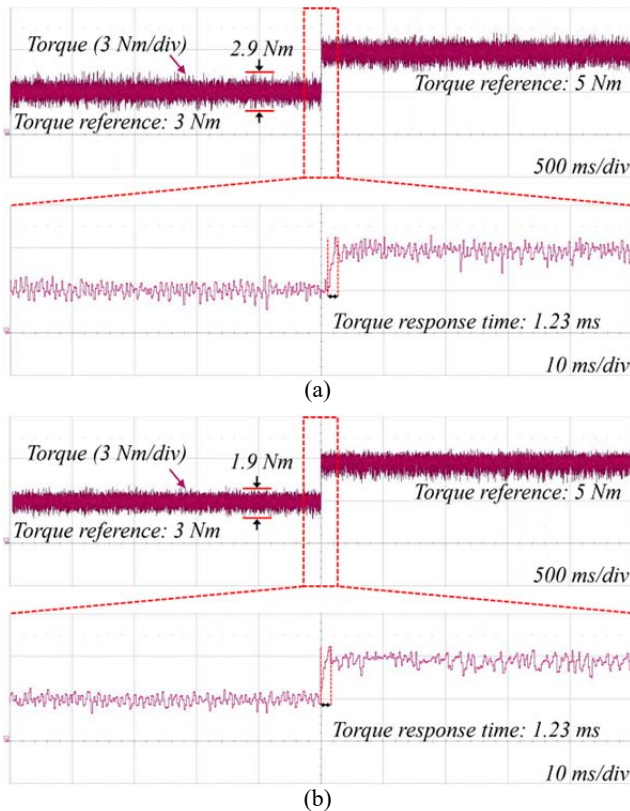


Fig. 13. Experimental results for a change in the torque reference (3 Nm  $\rightarrow$  5 Nm). (a) Seven-level hysteresis band. (b) Proposed method.

Experimental results for the transient state when the load is changed from 3 Nm to 5 Nm are shown in Fig. 12. The best results in terms of the torque response time are shown in Fig. 12(a), with a response time of 1.25 ms. On the contrary, in Fig. 12(c), the response time is slow with a value of 8.2 ms.

Fig. 13 shows experimental results for both the conventional and proposed methods. Because large voltage vectors are used for both methods, the torque response times are identical. However, the torque ripple is increased with the conventional method because a large voltage vector should be selected in a system with a long control period. With the proposed method, the torque ripple value is much smaller when compared with that of the conventional method. The effectiveness of the proposed method is confirmed by Fig. 13.

## V. CONCLUSION

An improved voltage vector selection algorithm for the DTC of five-phase induction machines is proposed in this paper. The voltage vector of a five-phase inverter has different magnitudes; a large voltage vector has  $0.6472 V_{DC}$ , a medium voltage vector has  $0.4 V_{DC}$ , and a small voltage vector has  $0.2472 V_{DC}$ . The magnitude of the voltage vector is related to the torque ripple and the torque response time. A large voltage vector has the best torque response speed. However, medium and small voltage vectors have less torque ripple. In this paper,

a large voltage vector is only selected in the transient state. Meanwhile, medium and small voltage vectors are selected in the steady state. As a result, the torque ripple is reduced in the steady state, and the performance of the torque response speed is improved. The validity of the proposed method is demonstrated through simulation and experimental results.

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