# Drain-current Modeling of Sub-70-nm PMOSFETs Dependent on Hot-carrier Stress Bias Conditions

In Eui Lim, Heesauk Jhon, Gyuhan Yoon, and Woo Young Choi\*

Abstract—Stress drain bias dependent current model is proposed for sub-70-nm p-channel metal-oxide semiconductor field-effect transistors (pMOSFETs) under drain-avalanche-hot-carrier (DAHC-) mechanism. The proposed model describes the both on-current and off-current degradation by using two device parameters: channel length variation ( $\Delta L_{ch}$ ) and threshold voltage shift ( $\Delta V_{th}$ ). Also, it is a simple and effective model of predicting reliable circuit operation and standby power consumption.

*Index Terms*—PMOSFET, HEIP, off current, modeling, reliability

### **I. INTRODUCTION**

With Moore's law, metal-oxide-semiconductor fieldtransistors (MOSFETs) have experienced effect continuous downscaling which enable higher density and performance chips [1]. However, unbalanced downscaling of physical dimensions and operating voltage of MOSFETs has always accompanied some reliability issues such as the hot-carrier injection (HCI), bias-temperature instability (BTI), and time-dependent dielectric breakdown (TDDB) [2, 3]. These reliability issues generate defects which change the device electrical performance and decrease the life-time so that eventually deteriorate the product quality [4]. In addition, with the increase of demand for mobile device, offcurrent is also an important issue because it is directly



Fig. 1. Schematic of a pMOSFET under DAHC stress. Threshold voltage shift ( $\Delta V_{\text{th}}$ ) and channel length variation ( $\Delta L_{\text{ch}}$ ) are induced by oxide trapped electrons.

related to standby power consumption. Thus, the accurate degradation model describing both on-current and offcurrent is necessary to increase the product yield and quality and predict the power consumption in advance.

Among the reliability issues, drain-avalanche-hotcarrier-induced (DAHC-induced) device degradation is one of the most serious problems due to the abrupt increase of effective lateral electric field with downscaling [5]. In the case of pMOSFETs, DAHC stress generates gate-oxide trapped electrons through impact ionization. The trapped electrons attract holes around the channel-to-drain junction surface and finally invert part of n-type channel surface into p-type. It means that part of the channel is converted into the drain. Thus, effective channel length  $(L_{ch})$  and threshold voltage  $(V_{th})$ vary as shown in Fig. 1 [6]. It leads to the variation of on-current, off-current, circuit performance and power consuption [7, 8]. For those reasons, DAHC-induced current variation model of pMOSFETs is necessary. Some papers have already reported DAHC-induced pMOSFET current models. However, they cover either on-current or off-current based on analytical solutions which makes modeling more complex [9-12].

In this manuscript, DAHC-induced drain current

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variation model is proposed. Considering the physical meaning and exponential dependence of threshold voltage in subthreshold region including off-current,  $L_{ch}$  variation ( $\Delta L_{ch}$ ) and  $V_{th}$  shift ( $\Delta V_{th}$ ) are adopted as essential modeling parameters for accurate modeling. The proposed model is based on BSIM (Berkeley Short-channel IGFET Model) and applied to sub 70-nm pMOSFETs.

### **II. MEASUREMENT RESULTS**

For the confirmation of the proposed model, 70-nm pMOSFETs are measured at room temperature. DAHC stress is applied at critical gate bias conditions ( $V_{gs,c}$ ) which can obtain the maximum substrate current ( $I_{sub}$ ). During measurement,  $\Delta V_{th}$  and  $\Delta L_{ch}$  are extracted. In order to evaluate the accuracy of the proposed model, normalized on-current variation, normalized off-current variation and error rate are defined as follows:

$$\Delta I_{on} / I_{on} = \frac{(I_{on,stress} - I_{on,fresh})}{I_{on,fresh}} \times 100\%$$
(1)

$$\Delta I_{off} / I_{off} = \frac{(I_{off,stress} - I_{off,fresh})}{I_{off,fresh}} \times 100\%$$
(2)

$$Error-rate = \frac{(I_{\text{model}} - I_{\text{meas}})}{I_{\text{meas}}} \times 100\%$$
(3)

 $I_{\text{on,fresh}}$  and  $I_{\text{on,stress}}$  are  $I_{\text{ds}}$  at  $V_{\text{gs}}=V_{\text{ds}}=-1.2$  V before and after stress.  $I_{\text{off,fresh}}$  and  $I_{\text{off,stress}}$  are  $I_{\text{ds}}$  at  $V_{\text{gs}}=0$  V,  $V_{\text{ds}}=-1.2$  V before and after stress.  $I_{\text{meas}}$  and  $I_{\text{model}}$  mean measured and modeled drain current, respectively. Device parameters and stress conditions are summarized in Table 1.

Fig. 2 shows that  $\Delta I_{on}/I_{on}$  show two distinct degradation mechanisms depending on DAHC stress time. At short stress time,  $\Delta I_{on}/I_{on}$  increases as stress time increases. It is originated from hot-electron-inducedpunchthrough (HEIP) which makes  $L_{ch}$  smaller and oxide-trapped electrons more. On the other hand, at long stress time,  $\Delta I_{on}/I_{on}$  decreases as stress time increases. It is explained by donor-like interface-state-generation (ISG) which introduces positive oxide charge effects [13]. The reason for the degradation mechanism change is that increased lateral electric field induced by HEIP makes channel holes more energetic [14]. Thus, more donor states are generated and positive oxide charge effects

Table 1. Device parameters and stress conditions

Device type	pMOSFET		
Channel width [µm]	10		
Channel length [nm]	~ 70		
Stress V <sub>ds</sub> [V]	-2.4, -2.6, -2.8		
Stress $V_{gs}$ [V]	V <sub>gsc</sub>		



**Fig. 2.** Stress time dependent on-current variation of 70-nm pMOSFETs under DAHC stress. HEIP and ISG are dominant under short-term and long-term stress, respectively.



Fig. 3. Stress time dependent off-current variation of 70-nm pMOSFETs under DAHC stress. Unlike on-current cases, off-current increases continuously.

overwrite negative oxide charge effects as stress time increases. The transition region between the two degradation mechanisms will be called a turn-around point.

Fig. 3 shows the influence of DAHC stress time on  $\Delta I_{\text{off}}$  / $I_{\text{off}}$  of pMOSFETs. Unlike  $\Delta I_{\text{on}}/I_{\text{on}}$ ,  $\Delta I_{\text{off}}$  / $I_{\text{off}}$  increases as stress time increases. The reason for this offcurrent behavior is that positive oxide charge effects at low gate bias are so weak that negative oxide charge effects are still dominant [15]. In addition, Fig. 2 and 3 show the drain bias dependency on  $\Delta I_{\text{on}}/I_{\text{on}}$  and  $\Delta I_{\text{off}}/I_{\text{off}}$ . As stress drain bias increases, the initial values of  $\Delta I_{\text{on}}/I_{\text{on}}$ also increase and turn around points appear at shorter



**Fig. 4.** Modeling process of drain-current increase modeling under DAHC stress by using BSIM4.

stress time. It is because higher drain bias induces more electron trapping in the gate oxide. Also,  $\Delta I_{off} / I_{off}$  increases as drain bias increases in the same manner. It should be noted that our proposed model is valid up to the turn-around point where  $\Delta I_{on}/I_{on}$  increases as stress time increases. The turn-around points are 57 s at  $V_{ds}$ = -2.4 V, 18 s at  $V_{ds}$ = -2.6 V and 2 sat  $V_{ds}$ = -2.8 V, respectively.

# III. MODELING PROCESS AND ITS VERIFICATION

The proposed model is fed into commercial BSIM. Its modeling process is shown in Fig. 4. First, the BSIM describing the drain current of fresh pMOSFETs is prepared. The error between the fresh BSIM and measurement data is < 1 %. Second, the model parameters ( $\Delta V_{\text{th}}$ ,  $\Delta L_{\text{ch}}$ ) are extracted from the measured data. Third, these DAHC- induced degraded parameters (K) are expressed as semi-empirical equation with from of (K=A+B·ln(t+C)) [12]. The proposed model equation follows logarithmic time dependence because oxide trapped electron behavior obeys logarithmic time dependence [16]. In addition, empirical stress drain bias term is added to express drain bias dependency with more accurate modeling results. Finally, the degradation model is fed into the fresh BSIM for comparison.

Before building the drain-bias-dependent model, the stress-bias-dependent model is developed. Fig. 5 compares the measured and modeling results at  $V_{\rm ds}$ =-2.4 V. As stress drain bias increases, both  $\Delta V_{\rm th}$  and  $\Delta L_{\rm ch}$ 



Fig. 5. Model and measurement data of stress time dependent  $\Delta V_{\rm th}$  and  $\Delta L_{\rm ch}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\rm ds}$ = - 2.4 V at  $V_{\rm gs}$ = $V_{\rm gs,c}$ .



**Fig. 6.** Model and measurement data of stress time dependent  $\Delta I_{\rm on} / I_{\rm on}$  and  $\Delta I_{\rm off} / I_{\rm off}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\rm ds}$ = - 2.4 V at  $V_{\rm gs}$ = $V_{\rm gs,c}$ .

increase, which is described by Eqs. (4, 5). Fig. 6 shows modeling results of  $\Delta I_{\rm on}/I_{\rm on}$  and  $\Delta I_{\rm off}/I_{\rm off}$ .

$$\Delta V_{th}(t_{str}) = 1.129 + 0.394 \times \ln(t_{str} + 0.5) \,[\text{mV}] \qquad (4)$$

$$\Delta L_{ch}(t_{str}) = 0.746 + 0.173 \times \ln(t_{str} + 0.5) \text{ [nm]}$$
 (5)

Fig. 7 compares the measured and modeling results at  $V_{\rm ds}$ =-2.6 V. As stress drain bias increases, both  $\Delta V_{\rm th}$  and  $\Delta L_{\rm ch}$  increase, which is described by Eqs. (6, 7). Fig. 8 shows modeling results of  $\Delta I_{\rm on}/I_{\rm on}$  and  $\Delta I_{\rm off}/I_{\rm off}$ .

$$\Delta V_{th}(t_{str}) = 2.700 + 0.543 \times \ln(t_{str} + 0.5) \,[\text{mV}]$$
 (6)

$$\Delta L_{ch}(t_{str}) = 1.229 + 0.133 \times \ln(t_{str} + 0.5) \text{ [nm]}$$
(7)

Fig. 9 compares the measured and modeling results at  $V_{\rm ds}$ =-2.8 V. As stress drain bias increases, both  $\Delta V_{\rm th}$  and  $\Delta L_{\rm ch}$  increase, which is described by Eqs. (8, 9). Fig. 10 shows modeling results of  $\Delta I_{\rm on}/I_{\rm on}$  and  $\Delta I_{\rm off}/I_{\rm off}$ .



**Fig. 7.** Model and measurement data of stress time dependent  $\Delta V_{\text{th}}$  and  $\Delta L_{\text{ch}}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\text{ds}}$ = - 2.6 V at  $V_{\text{gs}}$ = $V_{\text{gs,c}}$ .



**Fig. 8.** Model and measurement data of stress time dependent  $\Delta I_{\rm on} / I_{\rm on}$  and  $\Delta I_{\rm off} / I_{\rm off}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\rm ds}$ = - 2.6 V at  $V_{\rm gs}$ = $V_{\rm gs,c}$ .



**Fig. 9.** Model and measurement data of stress time dependent  $\Delta V_{\text{th}}$  and  $\Delta L_{\text{ch}}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\text{ds}}$ = - 2.8 V at  $V_{\text{gs}}$ = $V_{\text{gs,c}}$ .

$$\Delta V_{th}(t_{str}) = 5.385 + 1.101 \times \ln(t_{str} + 0.5) \text{ [mV]}$$
(8)

$$\Delta L_{ch}(t_{str}) = 1.627 + 0.063 \times \ln(t_{str} + 0.5) \text{ [nm]}$$
(9)

Fig. 11 and 12 show the drain-bias-dependent  $\Delta V_{\text{th}}$  and  $\Delta L_{\text{ch}}$  model results, respectively. Thus,  $\Delta V_{\text{th}}$  and  $\Delta L_{\text{ch}}$  are expressed as functions of stress drain bias and time as



**Fig. 10.** Model and measurement data of stress time dependent  $\Delta I_{\rm on}/I_{\rm on}$  and  $\Delta I_{\rm off}/I_{\rm off}$  of a 70-nm PMOSFET. DAHC stress conditions are  $V_{\rm ds}$ = - 2.8 V at  $V_{\rm gs}$ = $V_{\rm gs,c}$ .



**Fig. 11.** Stress drain bias dependent  $\Delta V_{\text{th}}$  model results of a 70nm PMOSFET with measurement data. DAHC stress conditions are  $V_{\text{ds}}$ = - 2.4 V, -2.6 V, and -2.8 V at  $V_{\text{gs}}$ = $V_{\text{gs,c}}$ .



**Fig. 12.** Stress drain bias dependent  $\Delta L_{ch}$  model results of a 70nm PMOSFET with measurement data. DAHC stress conditions are  $V_{ds}$ = - 2.4 V, -2.6 V, and -2.8 V at  $V_{gs}$ = $V_{gs,c}$ .

shown in Eqs. (10, 11).

Fig. 13 and 14 show  $\Delta I_{\rm on}/I_{\rm on}$  and  $\Delta I_{\rm off}/I_{\rm off}$  modeling results using the proposed drain-bias-dependent model. Fig. 15 shows the measurement and BSIM *I-V* curves at  $V_{\rm ds}$ =-2.6 V using the proposed drain-bias-dependent model. The errors between the model and measurement



Fig. 13. On-current degradation modeling results by using stress drain bias dependent model. Maximum difference of  $\Delta I_{on}/I_{on}$  is 0.37 % at  $V_{ds}$ =-2.4 V.



**Fig. 14.** Off-current degradation modeling results by using stress drain bias dependent model. Maximum difference of  $\Delta I_{\text{off}}/I_{\text{off}}$  is 4.27 % at  $V_{\text{ds}}$ =-2.8 V.

data are 0.37% for  $\Delta I_{\rm on}/I_{\rm on}$  and 4.27% for  $\Delta I_{\rm off}/I_{\rm off}$ .

$$\Delta V_{th}(t_{str}, V_{ds}) = \{-1.0816 + 0.00353 \cdot \exp(2.6830 \cdot |V_{ds}|)\} + \{0.3397 + 7.1330 \cdot 10^{-9} \cdot \exp(6.6021 \cdot |V_{ds}|)\} \cdot \ln(t_{str} + 0.5) \text{ [mV]}$$
(10)

$$\Delta L_{ch}(t_{str}, V_{ds}) = \{3.4906 - 28.0050 \cdot \exp(-0.9678 \cdot |V_{ds}|)\} + \{0.2285 - 7.5313 \cdot 10^{-5} \cdot \exp(2.7483 \cdot |V_{ds}|)\} \cdot \ln(t_{str} + 0.5) \text{ [nm]}$$
(11)

Table 2 summarizes the modeling results. It turns out that the proposed model well describes the *I-V* characteristics before and after DAHC stress.

### **IV. CONCLUSIONS**

The Model describing both on-current and off-current degradation of sub-70-nm pMOSFETs has been proposed and discussed. In order to reflect the DAHC-



**Fig. 15.** Measurement and modeling  $I_{ds}-V_{gs}$  results at  $V_{ds}$ =-2.6 V condition (a) linear-scale  $I_{ds}-V_{gs}$  at stress time equal to 10 s, (b) log-scale  $I_{ds}-V_{gs}$  at stress time equal to 10 s.

Table 2. Drain bias dependent modeling results

Stress V <sub>ds</sub>	Stress time	$(\Delta I_{\rm on}/I_{\rm on})$	$(\Delta I_{\rm on}/I_{\rm on})$	$(\Delta I_{\rm off}/I_{\rm off})$	$(\Delta I_{\rm off}/I_{\rm off})$
[V]	[s]	meas.	BSIM	meas.	BSIM
- 2.4 V	1	2.06	1.897	5.991	5.654
	2	2.447	2.123	6.52	6.472
	4	2.746	2.385	6.625	7.426
	6	2.882	2.549	7.656	8.031
	10	3.131	2.765	8.000	8.827
	18	3.341	3.02	9.381	9.781
	32	3.525	3.276	10.377	10.743
	57	3.694	3.481	11.257	11.098
-2.6 V	1	3.211	3.096	15.481	16.169
	2	3.360	3.296	16.426	17.504
	4	3.769	3.528	16.964	19.064
	6	3.732	3.673	16.169	20.053
	10	3.918	3.863	20.182	21.358
	18	4.119	4.012	22.320	21.934
-2.8 V	1	4.331	4.214	30.631	34.902
	2	4.596	4.404	36.778	37.546

induced stress effects, two device parameters ( $\Delta V_{\text{th}}, \Delta L_{\text{ch}}$ ) are used by using BSIM. Our empirical model describes the measured  $\Delta I_{\text{on}}/I_{\text{on}}$  and  $\Delta I_{\text{off}}/I_{\text{off}}$  with difference up to 0.37% and 4.27% respectively. It will be useful to predict circuit aging and power consumption.

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