New Coordination Approach to Minimize the Number of Re-adjusted Relays When Adding DGs in Interconnected Power Systems

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Abstract – The presence of DGs in power system networks tends to negatively affect the protective relays coordination. The proposed method introduces an approach to minimize the numbers of relays that acquire new settings on contrary to their original settings (case without DG), to achieve relays coordination in case of adding DG, since relays coordination with minimum number of relays of readjusted settings represents economical target, especially in networks containing mixture of electromechanical and adaptive digital relays. The scheme decides the possible minimum number of re-adjusted relays and their locations in an optimum manner to achieve proper relays coordination in case of adding DGs. The proposed approach is divided into two successive phases; the first phase is stopped when the first relays coordination solution is achieved. The second phase increases the possibility to keep higher number of relays at their original settings than that obtained in first phase through achieving multi solutions of relays coordination. The proposed approach is implemented and effectively tested on the well-known IEEE-39 bus test system.

Keywords: Distributed Generation (DG), Pickup Current Setting (IP), Relays Coordination, Time-Dial Setting (TDS).

1. Introduction

With the rapid increase in electrical energy demand, utilities are seeking for more power generation capacity. Newer technologies based on renewable energy sources are becoming more acceptable solutions as alternative energy generators. This renewable energy starts to spread electric power over distribution networks in the form of distributed generation (DG) [1]. Adding DG units in distribution networks will have major impacts on these networks' protection systems. These impacts include increasing short circuit levels, loss of protection coordination especially in case of directional overcurrent relays (DOCRs), bidirectionality of protection devices and protection blindness. Losing relays coordination results in unwanted false tripping for some healthy feeders. Furthermore, it may cause long time delay for tripping and isolating faulty feeders, resulting in significant fault currents overstresses on power system equipment and reducing their life time [2].

Various approaches have been proposed and reported in the literature to solve the coordination problem of directional overcurrent relays. These efforts may be categorized in two main categories. The first category is based on topological analysis, including graph theoretic and functional dependencies techniques [3-6]. The second category to solve the coordination problem of DOCRs is

For the sake of fixing relays settings for meshed distribution systems in both cases of with and without DG addition, it is proposed in [11] to ensure maximization of allowable DG penetration level at each bus based on measuring the rate of change of the maximum DG penetration level with respect to the rate of change of

based on using optimization techniques, by which the coordination problem could be formulated as a linear or nonlinear programming problem. In the linear model, the time dial settings are only optimized while the pickup current settings values are fixed [7]. Many efforts have been exerted to solve the relays coordination problem and get optimum solutions by applying different recent evolutionary algorithms (EAs) such as: Particle Swarm Optimization (PSO), Genetic Algorithm (GA), and Biogeography-Based Optimization (BBO) as introduced in [8-10]. In [8], a modified particle swarm optimization method is proposed to formulate DOCRs coordination problem as a mixed integer nonlinear problem to get optimal relays settings taking into consideration the discrete values for the pickup current settings. A method based on GA was developed to solve mis-coordination problem using continuous or discrete time setting multipliers [9]. Furthermore, some other hybrid techniques have been proposed to reach optimal solution of DOCRs coordination and overcome the drawback of low convergence speed of evolutionary algorithms; however, these algorithms such as hybrid BBO with linear programming (BBO-LP) are more complex for implementation [10].

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coordination time interval which can serve as an effective measure of DG impacts on relays coordination.

Authors believe that there is still much room for developing efficient schemes to solve relays coordination problem in interconnected power systems when adding DGs. Therefore, a coordination scheme is proposed in this paper to overcome the impact of installing DGs on the protection of interconnected power systems. Generally, the proposed method introduces an approach to minimize the numbers of relays that acquire new settings other than their original settings (case without DG), to achieve relays coordination in case of adding DG. The objective function in the proposed approach is the minimization of the total operating time of all primary relays for near end faults. The coordination problem is modeled as a linear programming (LP) problem. In such problems, a linear objective function is subject to linear equality and inequality constraints and can be solved using one of the linear programming techniques, namely: simplex, dual simplex, or two phase simplex technique [12]. To implement the proposed coordination scheme, the two phase simplex technique is applied using the MATLAB optimization function 'linprog', which is considered a simple and efficient tool.

The proposed scheme is tested on the meshed power distribution system of the IEEE 39-bus system equipped with synchronous based DGs, since synchronous based DGs generate higher fault current levels than inverter based DGs resulting in much more impact on the protection systems.

2. Conventional Coordination Problem

Achieving proper directional overcurrent relays coordination implies finding TDS and pickup current settings of all the DOCRs in the system so that the sum of operating times of the primary relays for near end faults is minimized while the coordination constraints are satisfied. Accordingly, the objective function is minimizing T as follows [11]:

$$Minimize T = \sum_{i=1}^{N} t_i \tag{1}$$

Where, T is the total time of N primary relays for near end faults and t_i is the operating time of the primary relay ith for its near end fault. Actually before adding the primary relay operating time to the summation of the objective function of Eq. (1), relay direction either in forward operation (to be added) or reverse operation (to be eliminated) is checked based on the angle between the relay fault current and its polarizing quantity that is not affected by the fault [13].

To ensure relays coordination, the operating time of the backup relay has to be greater than that of the primary relay for the same fault location by a coordination time interval including relay over travel time, breaker operating time, and safety margin for relay error as follows:

$$t_{j,i} - t_i \ge CTI_{j,i} \tag{2}$$

where $t_{j,i}$ is the operating time of the first back up *jth* relay for a near end fault at the *ith* relay, and $CTI_{i,i}$ is the coordination time interval for backup-primary relay pair (j,i). Based on the preceding conducted studies, coordination time interval can be taken between 0.2 s and 0.5 s.

The boundary conditions of relays settings can be formulated as linear inequality sets by:

$$TDS_{i,min} \le TDS_i \le TDS_{i,max}$$
 (3)

$$I_{P_{i,min}} \le I_{P_i} \le I_{P_{i,max}} \tag{4}$$

Where $TDS_{i,min}$, $TDS_{i,max}$ are the minimum and maximum TDS values of relay R_i respectively which are assumed to be 0.05 and 1.1 respectively. I_{P_i} is the pickup current setting of relay R_i , and its limits are chosen between 1.25 and 2 times the maximum load current seen by such relay. Relays characteristics are assumed identical and their functions are approximated by [8]:

$$t_{j,i} = \frac{0.14 \, TDS_j}{\left(\left(\frac{l_{f,j,i}}{l_{P_j}} \right)^{0.02} - 1 \right)} \tag{5}$$

Where $I_{f_{i,i}}$ is the short circuit current passing through the relay R_i for a fault at i.

For a fixed previously predefined value of I_{P_i} within its boundary limits, Eq. (5) can be expressed by TDS coefficient $(a_{i,i})$ for relay R_i as follows:

$$t_{j,i} = a_{j,i} \times TDS_j \tag{6}$$

where,

$$a_{j,i} = \frac{0.14}{\left(\left(\frac{l_{f,j,i}}{l_{P_j}}\right)^{0.02} - 1\right)}$$
 (7)

Based on predefined values of I_P for all relays, the objective function and the constraints given by Eq. (1), Eq. (2) and Eq. (3) can be expressed by Eq. (8), (9) and (10) respectively:

Minimize
$$T = \sum_{i=1}^{N} a_{i,i} \times TDS_i$$
 (8)

$$a_{i,i} \times TDS_i - a_{i,i} \times TDS_i \ge CTI_{i,i}$$
 (9)

$$0.05 \le TDS_i \le 1.1$$
 (10)

As discussed before, this coordination problem is solved in terms of TDS, given that I_P values of all the relays are predefined, based on the MATLAB optimization function 'linprog' that used with simplex two phase algorithm.

3. Proposed Approach Formulation for Readjusting Minimum Number of Relays

3.1 Methodology of the first phase of the proposed approach

The flowchart illustrated in Fig .1 shows detailed steps of the proposed approach. It starts with the solution of conventional coordination problem without DGs addition using previously predefined values of the pickup current for all relays within their limits. The problem of DOCRs coordination could be treated as a LP problem, and then the relays' TDS are calculated to get optimum solution. When a DG is added, the fault currents for all relays are recalculated using a developed MATLAB code and thus applying the original relays settings will result in some violated constraints.

The basic idea of the proposed approach is to restore overall relays coordination in case of adding DG while keeping most of relays at their original settings. To achieve such goal, the proposed approach is divided into two successive phases, where each phase includes number of trials to achieve relays coordination.

The first phase assumes a set $\{I\}$ that includes all violated constraints. It divides the relays into two groups. The first group includes the relays that we could have the ability to re-adjust their original settings, it includes backup-primary relay of each pair of violated constraints in set $\{I\}$. On the other hand, the second group includes the other remaining relays (not included in set $\{I\}$) which are kept fixed at their original settings during all trials of the scheme. Meanwhile, trials are carried out to keep most of relays in set $\{I\}$ at their original settings and reduce the number of relays that need to re-adjust their original settings with new settings as possible as we can. Nonetheless, changing settings for one of the relays in set {I} may remove an existing violated constraint, but may also generate another violated constraint associated with this relay, and not included in set $\{I\}$. Accordingly, a set $\{K\}$ is constructed, which is defined as the set that contains the violated constraints of set $\{I\}$ in addition to any other constraints associated with each relay in set $\{I\}$, and then tested based on linear programming.

In the first trial, linear programming is carried out on set $\{K\}$ at this step without any change of relays' I_P . If the relays coordination at this trial is not achieved, the relays' TDS are changed to their original TDS for NI randomly selected relays in set $\{I\}$ that satisfy Eq. (11) condition:

$$TDS_n^1 = TDS_n^0 \pm \varepsilon \tag{11}$$

Where, n is the relay address in set $\{I\}$ that satisfy Eq. (11), TDS_n^0 is the original TDS for relay n that calculated for relays coordination in case without DG, TDS_n^1 is the TDS of relay n that calculated after completion the first trial, and ε is the TDS tolerance coefficient which is

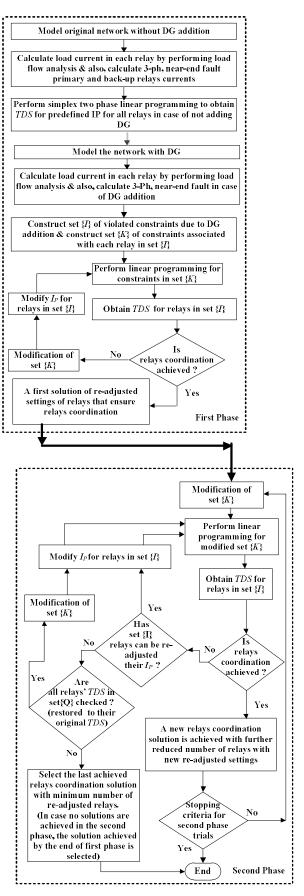


Fig. 1. Flowchart of the proposed approach

chosen so that $|\varepsilon| \le 0.01$ in the first phase.

Accordingly, N1 relays are restored their original settings at the starting of the second trial and the above step is repeated while relays I_P are changed for other relays other than N1 relays. Then, linear programming is performed on first modification of set $\{K\}$ (1st set $\{K\}$), and thus if relays coordination is not achieved in this second trial, the relays' TDS for N2 selected relays in set {I} that satisfy the condition of Eq. (12) will be changed to their original TDS.

$$TDS_n^2 = TDS_n^0 \pm \varepsilon \tag{12}$$

Where, TDS_n^2 is TDS for relay n in set $\{I\}$ that calculated at the completion of the second trial. Consequently, N2 relays are restored their original settings at the starting of the third trial and the above step is repeated while relays I_P are changed for the other relays other than N2 relays, then linear programming is carried out on this 2^{nd} set $\{K\}$.

If relays coordination is achieved in the third trial, and N3 relays in set $\{I\}$ are kept at their original settings by the completion of this trial, it will be verified that relays of original settings have been increased due to the N3 relays those gained in set $\{I\}$ through the three trials where $N1 \in N2 \in N3$. Finally, the first phase is stopped when the first solution for relays coordination is achieved.

3.2 Methodology of the second phase of the proposed approach

The second phase of the proposed scheme is an extension to the first phase except that TDS tolerance coefficient value will be greater than the zero value ($\epsilon \ge 0$). The objective of the second phase is achieving other solutions for relays coordination based on adding extra relays of original settings to those obtained based on first phase.

Suppose that, the trial step m+1 is the trial step at the end of first phase at which first solution of relays coordination occurs, and thus set $\{I\}$ at this step includes subset {Q} which have only relays of pickup currents identical to those of original settings. The second phase starts with trial step m+2 based on restoring TDS for chosen relays in subset {Q} to their corresponding original TDS, and then the set $\{K\}$ is modified. Consequently, and upon changing relays' IP, a new set of relays' TDS are obtained again by applying linear programming.

In case of achieving relays coordination at this trial, it is considered a second solution for relays coordination. Repeating the above steps, third, fourth and more solutions for achieving relays coordination could be obtained with further increased number of relays of original settings as the number of trials increases.

On the other hand, in case of not achieving relays coordination at the trial step m+2, the second phase could be restarted again but based on a lower number of selected relays in set {Q}. Finally, if there is no other solution for relays coordination, the trials are stopped and the relays have kept their original settings are those obtained by the end of the first phase.

Generally, the second phase trials will be stopped when no other solutions are found for relay coordination, or when more optimum solution for relays coordination is achieved with a total operating time of all primary relays for near end faults less than the other generated solutions and first phase solution.

4. Analysis and Results

The tested case study in this paper is the 39-bus IEEE system as shown in Fig. 2. It has 345, 230 and 22 kV buses, with 34 lines, 10 generators, 12 transformers and 84 directional overcurrent relays.

4.1 Optimal conventional relays coordination results for the system without DG

Continuous TDS & discrete I_P values are allowed in this study, a fixed I_P value corresponding to 1.25 times maximum load current is firstly chosen when, the actual load current in the forward direction of relay operation. Otherwise, I_P value of 150% (1.5 A) is assigned to relays when the actual load current in their reverse direction of operation as assumed in [14]. The values of Ips plug settings values as percentage of the secondary current tap for all relays are shown in Table 1. As clearly shown in the table, all the 84 relays have discrete values of Ips (50%, 75%, 100%, 125%, 150%, 175%, or 200%), except only one relay which is R3, it has Ip of 60%. The final achieved results upon adding DG, as will introduced later on, ensure that such relay should be an adaptive relay and have modified settings, so Ip of 60% is accepted in the case without adding DG for an adaptive one.

Consequently, by applying the steps illustrated in Section 2, relays TDS are generated to achieve optimal relays coordination. The results are given at CTI = 0.2 sec.

4.2 Examining proposed approach for the system with DG

Then the proposed approach is examined when a synchronous based DG is added at bus 28, the transient reactance and capacity of the DG are 0.2 pu and 10 MVA respectively. The DG is connected to the network through a transformer of 10 MVA capacity and 0.01 pu reactance. The system is modeled in MATLAB code with all of its detailed parameters. The near-end fault primary and backup relays currents are calculated in the presence of DG.

In fact, the proposed scheme can be applied for DG addition at any location; however, the DG has inserted at

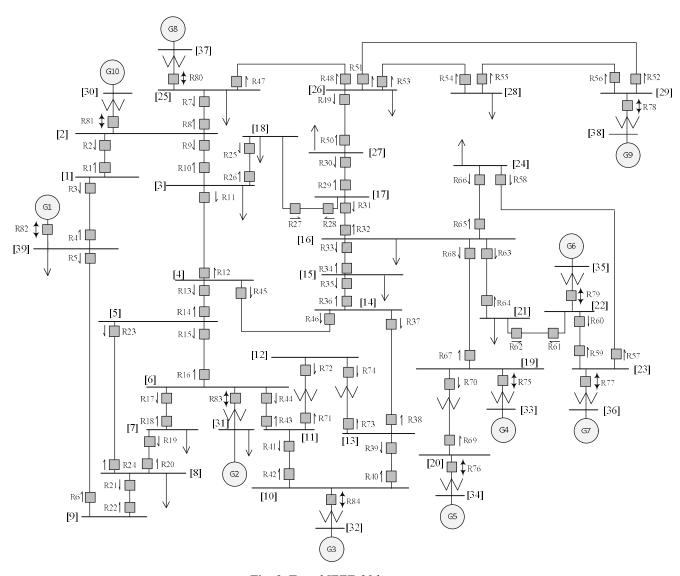


Fig. 2. Tested IEEE-39 bus system

bus 28 to get a complicated case of relays miscoordination. In such case, 47 violation constraints are found which nearly represent one third of the total constraints (140 constraints), also 61 relays out of total 84 relays have been affected by location of DG addition. According to the original calculated relays settings, Table 2 presents CTI of all backup-primary relay pairs in presence of DG. As shown, all 47 violated constraints are presented in shaded bold cells.

Based on the aforementioned stages of the proposed approach, set $\{I\}$ of all violated constraints is constructed (47 constraints of 61 relays), and therefore other relays not included in set $\{I\}$ are kept fixed at their original settings (23 relays). As discussed before, all relays in set $\{I\}$ are of variable settings, and thus set $\{K\}$ of all constraints associated to each relay in set $\{I\}$ is constructed. The constraints before starting trials of the proposed scheme were 140 with no change of I_P . Table 3 shows the results of

re-adjusting minimum number of relays settings in case of adding DG, where:

- Symbol '*' indicates relays' I_P of same original setting values as calculated in Table 1,
- Cells have bold values, either shaded or not, indicate relays' TDS obtained at the completion of each trial step (1st, 2nd, 3rd, ...) which are identical to the original TDS,
- Cells have shaded values indicate modified values of relays' *TDS* at the starting of each trial step to be identical to the original *TDS* (*N1*, *N2*, *N3*....),
- Cells have normal values (not bold or not shaded) refer to relays' re-adjusted settings that obtained at the completion of each trial step.
- Settings of 23 relays: R1, R21, R22, R38, R53, R63, R67, R68, R69, R70, R71, R73, R74, R75, R76, R77, R78, R79, R80, R81, R82, R83 and R84 are kept fixed at original settings during all trials, and thus they are not shown in the table.

Table 1. Ips Plug Settings Values as Percentage of the Secondary Current Tap for Relays in Power System without DG

Ip	Value	Iр	Value	Iр	Value	Ip	Value	Ip	Value	Ip	Value
Ip1	150	Ip15	150	Ip29	150	Ip43	175	Ip57	175	<i>Ip71</i>	125
Ip2	75	Ip16	125	<i>Ip30</i>	50	Ip44	150	Ip58	150	Ip72	150
Ip3	60	Ip17	100	Ip31	150	Ip45	150	Ip59	150	<i>Ip73</i>	125
Ip4	150	Ip18	150	Ip32	100	Ip46	150	Ip60	175	<i>Ip74</i>	150
Ip5	150	Ip19	100	Ip33	175	Ip47	50	Ip61	125	<i>Ip75</i>	125
Ip6	150	Ip20	150	Ip34	150	Ip48	150	Ip62	150	Ip76	175
Ip7	125	Ip21	150	Ip35	150	Ip49	150	Ip63	150	Ip77	125
Ip8	150	Ip22	50	Ip36	150	Ip50	150	Ip64	175	<i>Ip78</i>	175
Ip9	200	<i>Ip23</i>	175	<i>Ip37</i>	150	Ip51	150	Ip65	150	<i>Ip79</i>	150
Ip10	150	Ip24	150	Ip38	175	Ip52	100	Ip66	50	Ip80	125
<i>Ip11</i>	75	Ip25	100	<i>Ip39</i>	150	Ip53	150	Ip67	100	Ip81	150
Ip12	150	IP26	150	Ip40	175	Ip54	100	Ip68	150	Ip82	200
Ip13	150	IP27	150	Ip41	150	Ip55	150	Ip69	150	Ip83	125
<i>Ip14</i>	100	Ip28	100	Ip42	200	Ip56	175	<i>Ip70</i>	100	Ip84	150

^{*} Shaded cells mean actual current is in reverse direction of relay operation.

Table 2. CTI of All Backup-Primary Relay Pairs in Presence of DG at bus 28

CTI	Value (in sec)	CTI	Value (in sec)	CTI	Value (in sec)	СТІ	Value (in sec)	СТІ	Value (in sec)
CTI 4,1	0.2	CTI 54,49	-0.0177	CTI 78,56	0.3295	CTI 12,26	0.2008	CTI 40,73	28.1141
CTI 7,2	0.6361	CTI 52,49	0.0876	CTI 54,51	0.6899	CTI 82,4	0.2000	CTI 76,69	0.5676
CTI 10,2	0.6482	CTI 47,49	0.2336	CTI 47,51	0.8972	CTI 6,4	0.1997	CTI 75,70	2.2586
CTI 81,2	0.6565	CTI 7,9	0.1912	CTI 50,51	0.7187	CTI 82,5	0.2718	CTI 75,67	0.2000
CTI 1,8	0.2005	CTI 1,9	0.2095	CTI 55,52	0.1573	CTI 3,5	0.1991	CTI 69,67	0.2000
CTI 10,8	0.1983	CTI 12,10	0.3610	CTI 78,52	0.5018	CTI 25,11	0.2788	CTI 38,46	0.4091
CTI 81,8	0.2005	CTI 25,10	0.1985	CTI 49,30	0.1769	CTI 9,11	0.4385	CTI 35,46	0.4020
CTI 48,7	0.1915	CTI 29,50	0.1999	CTI 32,29	0.2970	CTI 14,12	0.2001	CTI 14,45	0.2391
CTI 80,7	0.2101	CTI 52,53	0.7327	CTI 27,29	0.3087	CTI 46,12	0.1990	CTI 11,45	0.1983
CTI 8,47	0.1997	CTI 47,53	0.8367	CTI 26,27	0.1998	CTI 41,40	0.1998	CTI 2,3	0.1997
CTI 80,47	0.3153	CTI 50,53	0.6589	CTI 30,28	0.2047	CTI 84,40	0.2005	CTI 42,43	0.1998
CTI 54,48	0.1457	CTI 56,54	0.2517	CTI 32,28	0.2039	CTI 74,39	0.2000	CTI 83,43	1.2895
CTI 52,48	0.2521	CTI 53,55	0.2521	CTI 28,25	0.1981	CTI 37,39	0.1998	CTI 72,43	0.4075
CTI 50,48	0.2174	CTI 51,56	0.1958	CTI 9,26	0.1964	CTI 84,39	0.4840	CTI 44,41	0.1999
CTI 72,41	0.1987	CTI 83,16	0.4133	CTI 11,13	0.4629	CTI 23,21	0.3319	CTI 60,57	0.2000
CTI 39,42	0.1998	CTI 35,37	0.1996	CTI 16,14	0.1999	CTI 19,24	0.1997	CTI 77,57	0.2530
CTI 84,42	0.2677	CTI 45,37	0.2053	CTI 24,14	0.2000	CTI 22,24	0.2833	CTI 65,58	0.1998
CTI 18,44	0.1997	CTI 74,38	0.2855	CTI 5,22	0.2000	CTI 21,6	0.2000	CTI 77,59	0.2000
CTI 83,44	0.2071	CTI 40,38	0.2000	CTI 13,23	0.2969	CTI 66,63	0.5385	CTI 58,59	0.1993
CTI 43,17	0.5030	CTI 33,35	0.1990	CTI 16,23	0.5114	CTI 67,63	0.5342	CTI 64,65	0.2010
CTI 15,17	0.1996	CTI 38,36	0.2001	CTI 31,33	0.1962	CTI 31,63	0.4370	CTI 67,65	0.6035
CTI 83,17	0.7235	CTI 45,36	0.1994	CTI 66,33	0.2903	CTI 34,63	0.5299	CTI 31,65	0.5099
CTI 20,18	0.2000	CTI 30,31	0.1928	CTI 67,33	0.2909	CTI 61,64	0.1998	CTI 34,65	0.6021
CTI 83,18	1.6627	CTI 27,31	0.2039	CTI 36,34	0.1999	CTI 62,60	0.1990	CTI 57,66	0.1995
CTI 24,15	0.4112	CTI 34,32	0.1991	CTI 17,19	0.1997	CTI 79,60	0.2003	CTI 66,68	1.2629
CTI 13,15	0.1997	CTI 66,32	0.2002	CTI 22,20	0.2001	CTI 59,61	0.1999	CTI 64,68	0.8590
CTI 18,16	0.4136	CTI 67,32	0.2002	CTI 23,20	0.1994	CTI 79,61	0.3970	CTI 34,68	1.2603
CTI 43,16	0.1993	CTI 46,13	0.5022	CTI 19,21	1.6215	CTI 63,62	0.2000	CTI 31,68	1.1670

^{*} Shaded bold cells show the mis-coordinated backup-primary relay pairs in presence of DG.

As the objective of the proposed approach is to keep most of relays at their original settings and fulfill relays coordination in case of adding DG, detailed results for gradually reducing the number of relays that need readjusting their original settings to achieve relays coordination are shown below:

 During the first trial to obtain relays coordination, a set $\{K\}$ of 134 constraints associated with 61 relays in set $\{I\}$ is developed, then linear programming is performed on set $\{K\}$ with no change of I_P for all relays, and thus [TDS]¹ is obtained at the end of first trial, where [TDS]¹

- is the TDS for all relays in set $\{I\}$ that calculated at the completion of the first trial. By the end of this trial, it is found that relays coordination is not achieved.
- Consequently, the second trial is initiated by comparing the obtained $[TDS]^1$ for 61 relays in set $\{I\}$ and their corresponding original values in [TDS]⁰. Therefore only 11 relays are selected to change their TDS into their corresponding original values (N1 relays). Cells have shaded values in 'Second Trial column' refer to these relays (e.g. TDS of R19 is changed from 0.3046 to 0.3052 at the start of the second trial). 1^{st} modified set $\{K\}$

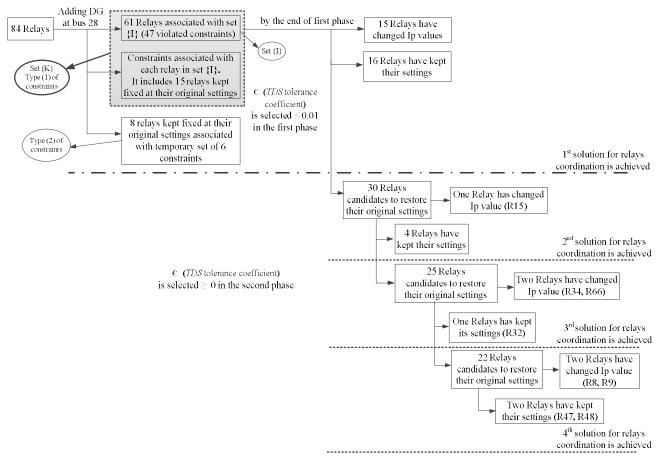


Fig. 3. Summary for the proposed approach results in case of adding DG at bus 28 during the first and second stages

is constructed to have 124 constraints taking into consideration the original settings for both 11 relays in set $\{I\}$ and the 23 relays not included in set $\{I\}$. I_P for other relays other than the 11 relays in set $\{I\}$ are changed and then linear programming steps are applied on the new 1st set $\{K\}$.

The third trial is started to achieve relays coordination when comparing the obtained $[TDS]^2$ for relays in set $\{I\}$ and their corresponding original values in [TDS]⁰, and consequently only 5 relays satisfying the condition of Eq. (12) are selected in addition to 11 relays (those obtained in second trial) to restore their TDS at their corresponding original values in this trial, cells have shaded values in 'Third Trial column' refer to these relays (N2 relays). 2^{nd} set $\{K\}$ is constructed to have 118 constraints taking into consideration the original settings for both 16 relays in $set\{I\}$ and the 23 relays not included in set $\{I\}$. I_P for other relays other than the 16 relays in set $\{I\}$ are changed and then linear programming steps are applied. Based on the achieved results, it is found that relays coordination is achieved for the first time at this third trial keeping 16 of 61 relays in set $\{I\}$ at their original settings. Hence, 39 relays are kept at their original settings as shown in 16 cells that have bold values in 'Third Trial column', in addition to 23 relays not included in set $\{I\}$.

However there is still a possibility to further increase this number of relays with original settings and achieve relays coordination based on the second phase as follows:

- The fourth trial is initiated to achieve a second solution of relays coordination; the above steps are repeated with ε ≥ 0. The set {Q}, which includes relays that can change their *TDS* to their corresponding original values, is {R7, R8, R9, R10, R12, R13, R15, R23, R26, R27, R29, R32, R34, R36, R37, R39, R45, R46, R47, R48, R50, R51, R54, R55, R57, R60, R62, R64, R65, and R66}. Four relays in set {Q} are selected and tested in addition to 39 relays. *I_P* is changed for relays to be as listed in 'Fourth Trial column' in Table 3, and then linear programming is performed on 3rd set {*K*} ensured that a second solution of relay coordination is achieved in the fourth trial while keeping 43 relays at their original settings.
- R32 is added in the fifth trial, thus achieving third solution of relays coordination, while addition of R47 and R48 in the sixth trial ensured fourth solution of relays coordination when 46 relays are kept at their original settings (cells have bold values in 'Sixth Trial column').

Table 3. Proposed Approach Results of Re-adjusting Minimum Number of Relays Settings in Case of Adding DG

Relay		nal Settings thout DG	First Trial		Second Trial		Third	l Trial	For	Fourth Trial		Fifth Trial		Sixth Trial	
no.	Iр	TDS	Iр	TDS	Ip	TDS	Iр	TDS	Ip	TDS	Iр	TDS	Ip	TDS	
R2	*	0.3182	*	0.3186	*	0.3182	*	0.3182	*	0.3182	*	0.3182	*	0.3182	
R3	*	0.2783	*	0.2786	*	0.2782	75	0.2481	75	0.2481	75	0.2481	75	0.2481	
R4	*	0.6574	*	0.6571	*	0.6574	*	0.6574	*	0.6574	*	0.6574	*	0.6574	
R5 R6	*	0.5986 0.3838	*	0.5986 0.3838	*	0.5986 0.3838	300	0.5986 0.2811	300	0.5986 0.2811	300	0.5986 0.2811	300	0.5986 0.2811	
R7	*	0.3371	*	0.3403	*	0.3318	*	0.2811	*	0.3402	*	0.3402	*	0.2811	
R8	*	0.6888	*	0.6864	*	0.6459	*	0.6205	*	0.6205	*	0.6205	4800	0.0748	
R9	*	0.3704	*	0.3714	*	0.3603	*	0.3401	*	0.3713	*	0.3713	300	0.286	
R10	*	0.6329	*	0.6318	*	0.6005	*	0.5809	*	0.5809	*	0.5809	*	0.4072	
R11	*	0.4815	*	0.4819	*	0.4804	*	0.4815	*	0.4815	*	0.4815	*	0.4815	
R12	*	0.6858	*	0.6834	*	0.6652	*	0.6278	*	0.6858	*	0.6858	*	0.6858	
R13 R14	*	0.5096 0.4235	*	0.6142 0.4222	*	0.6153 0.4231	*	0.4757 0.4235	*	0.5096 0.4235	*	0.5096 0.4235	*	0.5096 0.4235	
R14	*	0.4233	*	0.4222	*	0.4231	*	0.4235	200	0.4233	200	0.4233	200	0.4233	
R16	*	0.2445	*	0.4321	*	0.4331	200	0.3137	200	0.1602	200	0.1602	200	0.1602	
R17	*	0.2303	*	0.23	*	0.2303	150	0.1669	150	0.1669	150	0.1669	150	0.1669	
R18	*	0.319	*	0.319	*	0.319	200	0.2585	200	0.2585	200	0.2585	200	0.2585	
R19	*	0.3052	*	0.3046	*	0.3052	*	0.3052	*	0.3052	*	0.3052	*	0.3052	
R20	*	0.539	*	0.5391	*	0.539	*	0.539	*	0.539	*	0.539	*	0.539	
R23	*	0.2627	*	0.2629	*	0.2628	*	0.2628	*	0.2628	*	0.2628	*	0.2628	
R24 R25	*	0.479 0.702	*	0.4778 0.7018	*	0.4786 0.6725	200	0.426	200	0.426 0.5324	200	0.426 0.5324	200	0.426 0.5324	
R26	*	0.766	*	0.7662	*	0.6723	*	0.5324	*	0.3324	*	0.3324	× ×	0.3324	
R27	*	0.6594	*	0.6595	*	0.6329	*	0.5843	*	0.6065	*	0.6065	*	0.6065	
R28	*	0.5052	*	0.5058	*	0.488	140	0.4074	140	0.4074	140	0.4074	140	0.4074	
R29	*	0.6757	*	0.6744	*	0.7107	*	0.6462	*	0.6757	*	0.6757	*	0.6757	
R30	*	0.8057	*	0.8125	*	0.7338	100	0.6101	100	0.6101	100	0.6101	100	0.6101	
R31	*	0.6529	*	0.6553	*	0.5808	2400 *	0.1307	2400	0.1307	2400	0.1307	2400	0.1307	
R32 R33	*	0.5297 0.4242	*	0.5283 0.4245	200	0.5128 0.3987	200	0.488	200	0.4915 0.3987	200	0.5297 0.3987	200	0.5297 0.3987	
R34	*	0.5943	*	0.5933	*	0.5785	*	0.5548	*	0.5581	200	0.5357	200	0.5357	
R35	*	0.6547	*	0.6547	*	0.6547	*	0.6547	*	0.6547	*	0.6547	*	0.6547	
R36	*	0.6906	*	0.6897	*	0.675	*	0.6513	*	0.6545	*	0.6851	*	0.6851	
R37	*	0.6883	*	0.6879	*	0.688	*	0.6811	*	0.6811	*	0.6811	*	0.6811	
R39	*	0.5983	*	0.5979	*	0.5983	*	0.5909	*	0.5909	*	0.5909	*	0.5909	
R40 R41	*	0.3427 0.6532	*	0.3426 0.6532	*	0.3427 0.6532	200	0.3427 0.5971	200	0.3427 0.5971	200	0.3427 0.5971	200	0.3427 0.5971	
R41	*	0.0332	*	0.0532	*	0.0332	240	0.3971	240	0.3971	240	0.3971	240	0.3971	
R43	*	0.2706	*	0.2702	*	0.2706	*	0.2706	*	0.2706	*	0.2706	*	0.2706	
R44	*	0.7491	*	0.7491	*	0.7491	*	0.7491	*	0.7491	*	0.7491	*	0.7491	
R45	*	0.6752	*	0.6747	*	0.6723	*	0.6665	*	0.6665	*	0.6708	*	0.6708	
R46	*	0.3281	*	0.3273	*	0.3199	*	0.3046	*	0.3283	*	0.3283	*	0.3283	
R47	*	0.5419	*	0.5394	*	0.5011	*	0.4771	*	0.4771	*	0.4771	*	0.5419	
R48 R49	*	0.5392 0.3516	*	0.5472 0.3601	*	0.5894 0.3301	250	0.5145	* 250	0.5471 0.2305	250	0.5471 0.2305	* 250	0.5392 0.2305	
R50	*	0.5685	*	0.5671	*	0.6035	*	0.2303	*	0.2303	*	0.2303	× ×	0.2303	
R51	*	0.2888	*	0.3077	*	0.2951	*	0.2904	*	0.2904	*	0.2904	*	0.3002	
R52	*	0.1544	*	0.1721	*	0.1599	*	0.1544	*	0.1544	*	0.1544	*	0.1544	
R54	*	0.1564	*	0.1908	*	0.1772	*	0.1688	*	0.1688	*	0.1688	*	0.1688	
R55	*	0.243	*	0.2664	*	0.2664	*	0.26	*	0.26"	*	0.26	*	0.26	
R56	*	0.1488	*	0.1606	*	0.152	*	0.1488	*	0.1488	*	0.1488	*	0.1488	
R57 R58	*	0.2151 0.3874	*	0.2147 0.3877	*	0.2101 0.387 4	*	0.2028	*	0.2038	*	0.2032	*	0.2032	
R58 R59	*	0.3874	*	0.38//	*	0.3874	200	0.3874 0.3449	200	0.3874 0.3449	200	0.3874 0.3449	200	0.3874 0.3449	
R60	*	0.4289	*	0.4283	*	0.4213	*	0.4101	*	0.4117	*	0.4108	*	0.4108	
R61	*	0.1346	*	0.1346	*	0.1346	*	0.1346	*	0.1346	*	0.1346	*	0.1346	
R62	*	0.3315	*	0.3315	*	0.3272	*	0.3204	*	0.3213	*	0.3207	*	0.3207	
R64	*	0.1573	*	0.1572	*	0.1571	*	0.1571	*	0.1571	*	0.1571	*	0.1571	
R65	*	0.5114	*	0.5118	*	0.5115	*	0.5115	*	0.5115	*	0.5115	*	0.5115	
R66 R72	*	0.4016 0.2796	*	0.4006 0.2798	*	0.3907 0.2798	*	0.3746 0.2796	*	0.3768 0.2796	100	0.2628 0.2796	100	0.2628 0.2796	
K/2			•					relays		nd solution		solution		th solution	
		Relays ination is not	Relays ot coordination is		Relays coordination is not		coordination		for relays		for relays		for relays		
		nieved yet		achieved yet		nieved yet		n(End of		dination is		ination is		dination is	
				-	J		First Phase)		achieved		achieved		achieved		

Table 4. Results of Applying Proposed Scheme Based on Assumed value of ε as in Technique [15] for Re-adjusting Relays Settings in case of adding DG

Relay no.	Original Set	tings without DG	Firs	t Trial	Sec	ond Trial	Third Trial		
	Iр	TDS	Iр	TDS	Iр	TDS	Ip	TDS	
R2	*	0.3182	*	0.3186	*	0.3186	*	0.3133	
R3	*	0.2783	*	0.2786	*	0.2786	75	0.2481	
R4	*	0.6574	*	0.6571	*	0.6571	*	0.6574	
R5	*	0.5986	*	0.5986	*	0.5986	*	0.5986	
R6	*	0.3838	*	0.3838	*	0.3838	300	0.2811	
R7	*	0.3371	*	0.3403	*	0.3198	*	0.3162	
R8	*	0.6888	*	0.6864	*	0.5692	*	0.6185	
R9	*	0.3704	*	0.3714	*	0.3448	*	0.3401	
R10	*	0.6329	*	0.6318	*	0.5412	*	0.5793	
R11	*	0.4815	*	0.4819	*	0.4453	*	0.4611	
R12	*	0.6858	*	0.6834	*	0.6365	*	0.6278	
R13	*	0.5096	*	0.6142	*	0.4993	*	0.4583	
R14	*	0.4235	*	0.4222	*	0.3975	*	0.3933	
R15	*	0.3443	*	0.4321	*	0.3355	*	0.301	
R16	*	0.2445	*	0.2439	*	0.2319	200	0.1506	
R17	*	0.2303	*	0.23	*	0.2226	150	0.1568	
R18	*	0.319	*	0.319	*	0.319	200	0.2585	
R19	*	0.3052	*	0.3046	*	0.2926	*	0.2823	
R20	*	0.539	*	0.5391	*	0.5391	*	0.5009	
R23	*	0.2627	*	0.2629	*	0.2629	*	0.2476	
R24	*	0.479	*	0.4778	*	0.4544	200	0.4005	
R25	*	0.702	*	0.7018	*	0.6171	200	0.5281	
R26	*	0.766	*	0.7662	*	0.7023	*	0.691	
R27	*	0.6594	*	0.6595	*	0.5956	*	0.5843	
R28	*	0.5052	*	0.5058	*	0.4541	140	0.4046	
R29	*	0.6757	*	0.6744	*	0.6119	*	0.6462	
R30	*	0.8057	*	0.8125	*	0.7338	100	0.6066	
R31	*	0.6529	*	0.6553	*	0.5808	2400	0.1307	
R32	*	0.5297	*	0.5283	*	0.4525	*	0.4853	
R33	*	0.4242	*	0.4245	200	0.3487	200	0.3987	
R34	*	0.5943	*	0.5933	*	0.5208	*	0.5521	
R35	*	0.6547	*	0.6547	*	0.6547	*	0.6547	
R36	*	0.6906	*	0.6897	*	0.6173	*	0.6486	
R37	*	0.6883	*	0.6879	*	0.6183	*	0.6367	
R39	*	0.5983	*	0.5979	*	0.5265	*	0.5454	
R40	*	0.3427	*	0.3426	*	0.3426	*	0.3427	
R41	*	0.6532	*	0.6532	*	0.6532	200	0.5971	
R42	*	0.2911	*	0.2908	*	0.2492	240	0.2357	
R43	*	0.2706	*	0.2702	*	0.2235	*	0.2404	
R44	*	0.7491	*	0.7491	*	0.7491	*	0.7491	
R45	*	0.6752	*	0.6747	*	0.6143	*	0.6404	
R46	*	0.3281	*	0.3273	*	0.3082	*	0.3046	
R47	*	0.5419	*	0.5394	*	0.5011	*	0.4752	
R48	*	0.5392	*	0.5472	*	0.5195	*	0.5145	
R49	*	0.3516	*	0.3601	*	0.3301	250	0.2276	
R50	*	0.5685	*	0.5671	*	0.5432	*	0.539	
R51	*	0.2888	*	0.3077	*	0.2951	*	0.2866	
R52	*	0.1544	*	0.1721	*	0.1599	*	0.1516	
R54	*	0.1564	*	0.1908	*	0.1772	*	0.1681	
R55	*	0.243	*	0.2664	*	0.2664	*	0.2568	
R56	*	0.1488	*	0.1606	*	0.152	*	0.1461	
R57	*	0.2151	*	0.2147	*	0.1923	*	0.202	
R58	*	0.3874	*	0.3877	*	0.3877	*	0.385	
R59	*	0.3787	*	0.3787	*	0.3787	200	0.3449	
R60	*	0.4289	*	0.4283	*	0.394	*	0.4089	
R61	*	0.1346	*	0.1346	*	0.1346	*	0.1346	
R62	*	0.3315	*	0.3315	*	0.3105	*	0.3196	
R64	*	0.1573	*	0.1572	*	0.1572	*	0.1566	
R65	*	0.5114	*	0.5118	*	0.5118	*	0.5091	
R66	*	0.4016	*	0.4006	*	0.3516	*	0.3728	
R72	*	0.2796	*	0.2798	*	0.2798	*	0.2783	
2012	Relays coordinate	ation is not achieved yet		dination is not ieved yet		ordination is not chieved yet	Solution for relays coordination is achieved		

As the total operating time of all primary relays for near end faults $(\sum_{i=1}^{84} a_{i,i} \times TDS_i)$ equals 74.803 sec, 75.532 sec, 75.728 sec, and 74.372 sec by the end of first phase (end of 3rd trial), end of 4th trial, end of 5th trial, and end of 6th trial respectively, the second phase will be stopped at the 6th trial at which relays coordination is achieved with a total operating time of all primary relays for near end faults less than the corresponding values of other trials.

Up to the authors' knowledge, very few published research works have investigated the idea of achieving minimum number of relays that acquire new relays settings in case of adding DG. Reference [15] represents one of such studies where nonlinear / linear optimization models are applied using GAMS. It is worth mentioning that the proposed approach is compared with the published method in [15]. So that, the proposed scheme is applied on IEEE-39 bus system but based on $\varepsilon = 0$ as in technique [15], for re-adjusting relays settings in case of adding DG. The obtained results are shown in Table 4. It is clear that the first trial is the same as achieved by the proposed scheme when relays are initially assumed to be kept at their original settings. At the starting of the second trial, only four relays R5, R35, R44 and R61 are selected to be added to those keeping their original settings where $\varepsilon = 0$. During the second trial, I_P is only changed for R33 to be as in our study however relays coordination is not achieved. By the third trial completion, the relays coordination is achieved by changing relays' I_P as shown in Table. 4, and keeping the two relays R4, R40 at their original settings, in addition to R5, R35, R44, R61 and the initially 23 relays.

According to the aforementioned results, those are summarized in Fig. 3; the proposed approach has succeeded in achieving its first solution for relays coordination when keeping 39 relays at their original settings, while in the fourth solution 46 relays are obtained for a more optimum relays coordination solution. On the other hand, when applying the proposed approach but based on $\varepsilon = 0$ for re-adjusting relays settings in case of adding DG as in technique [15], it has only kept 29 relays at their original settings to achieve a unique solution for relays coordination.

We can summarize that the proposed method has two merits. The first merit is achieving relays coordination and finding out lower number of relays of new settings compared to the other obtained based on using the proposed method but implemented on $\varepsilon = 0$ as in previous techniques, this can be achieved in first phase. The second merit is obtaining further reduced number of relays of new settings, through generating many other solutions of relays coordination

5. Conclusion

Relays coordination with minimum number of relays of re-adjusted settings represents economical target, especially

in networks containing mixture of electromechanical and adaptive digital relays. The paper introduces a new approach to achieve relays coordination in interconnected power systems utilizing DGs with minimum number of relays of re-adjusted settings. An integrated model, using linear programming based on MATLAB optimization toolbox is introduced to verify the effectiveness of the proposed scheme on IEEE-39 bus test system. The proposed approach calculates re-adjusted settings for minimum number of relays and defines their locations to achieve relays coordination in case of adding DG. Initially, first phase is carried out to decrease the number of relays of readjusted settings and obtaining first relays coordination solution, then the second phase is carried out to gradually decrease this number at sequential stages for obtaining different relays coordination solutions.

When comparing the performance of the proposed approach with other published techniques, the achieved results ensured the effectiveness of the proposed approach. In its first phase and by the completion of 3 trials, relays coordination solution is achieved by keeping 39 relays at their original settings, while implementing our approach but, based on assumptions of other published technique, have only succeeded in keeping 29 relays at their original settings. Besides, the number of relays that kept their original settings is increased to be 46 relays in the second phase through more than one solution for relays coordination.

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