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# A Hybrid DC/DC Converter for EV OBCs Using Full-bridge and Resonant Converters with a Single Transformer

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#### Abstract

This paper proposes a dc/dc converter for electric vehicle onboard chargers using a secondary resonant tank. To attain soft switching characteristics, such as zero voltage switching, magnetizing inductance has been used at the primary side of the transformer. The leakage inductance of the transformer is used as a resonant inductor on the secondary side to avoid the use of a separate inductor as resonance. The proposed converter is applicable for a wide load range. A 6.6KW prototype has been implemented for a wide range of load variations (250V, 330V, 360V, and 413V). A maximum efficiency of 97.4% is achieved at 413V.

Key words: Battery charger, DC/DC converter, Hybrid converter

### I. INTRODUCTION

Due to concerns over climate change and air polution in large urban cities, the demand for plug in hybrid electric vehicles (PHEVs) and electric vehicles (EVs) has been increasing over the years [1], [2]. High capacity battery packs have been extinsively used in PHEVs and EVs. These battery packs demand high efficiency, low cost and compact chargers. Among the existing solutions, the most common charger architecture consists of an AC/DC converter with power factor correction and an isolated DC/DC converter [3]-[5]. High efficiency is the main requirement for power converter topologies [6]. An onboard charger (OBC) is mounted on EVs and PHEVs to charge the batteries [7]. Until now, OBCs with a charging capacity of 3.3KW have been used in PHEV/EVs and they take approximately 8 hours to charge the batteries [8], [9]. A solution for minimizing the charging time by doubling the charging capacity of chargers is underway [10].

The DC/DC converter topologies use for OBCs should meet several requirements, such as, (a) wide output voltage control, (b) soft-switching in the primary switches under different

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Tel: +82-330-6357, Fax: +82-330-6977, Myongji University \*Department of Electrical Engineering, Myongji University, Korea load and battery voltages, (c) a low voltage rating in the secondary rectifiers, (d) the reduction of unnecessary loss by avoiding snubber circuits, (e) the switching frequency variation should be narrow to reduce the switching loss and to eliminate audible noise under wide load and battery voltages, and (f) the circulating current should be minimized [11].

In this paper, a hybrid PWM DC/DC converter comprised of a FB converter and a PWM resonant converter for EV OBCs is suggested. The proposed converter has operational characteristics that are a mixture of the resonant converter and the FB converter. Unlike previous hybrid converters, the resonant converter and FB converter use PWM operation so that the transformer structure can be simplified by coupling the two secondary sides. The proposed structure provides additional merits such as no dissipative snubber circuitry and no output filter. The ZV-ZCS operation of the bottom switches and the ZVS operation of the top switches can be accomplished by proper design of the resonant. Since the design of the proposed converter is related to various parameters such as the resonant tank, the transformer turns-ratio, the magnetizing inductance, and the duty-ratio, a design procedure is suggested. Based on this design procedure, the proposed converter is implemented and tested using a 6.6kW charger.

# II. PROPOSED CONVERTER

A. Description of the Proposed Converter

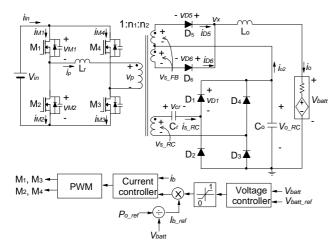


Fig. 1. Schematic diagram of the proposed converter.

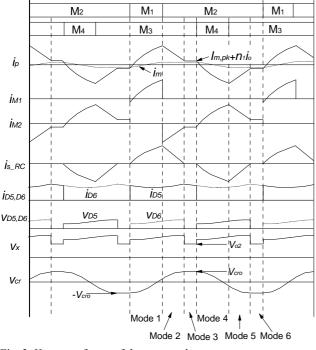


Fig. 2. Key waveforms of the proposed converter.

Fig. 1 shows a schematic diagram of the proposed charger. The rectifier of the proposed charger is comprised of 6 diodes. The diodes  $D_{I} \sim D_{4}$  are used for the resonant converter and  $D_{5} \sim D_{6}$  are used for the FB converter. The outputs of the rectifiers are connected in series. These two converters are coupled with a single transformer, and the switches  $M_{I} \sim M_{4}$  are commonly used for power control of the two converters.

#### B. Mode Analysis

Figs. 2 and 3 show key waveforms and operational mode diagrams of the proposed charger. The equivalent circuits of each mode are depicted in Fig. 4. Assuming that the magnetizing inductance of the transformer  $L_m$  is sufficiently large when compared with the resonant inductor  $L_r$ , the equivalent circuit can be redrawn as shown in Fig. 4(b) by

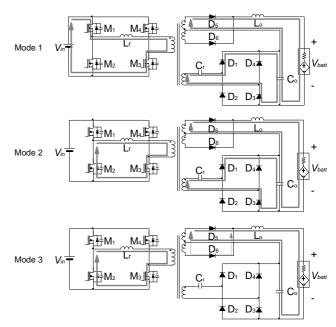


Fig. 3. Operational mode diagrams.

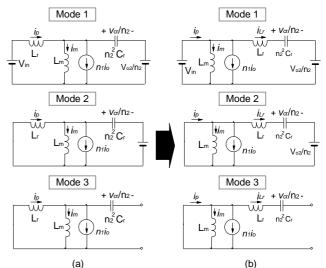


Fig. 4. (a) Equivalent circuits of each modes. (b) Modifications of equivalent circuits.

exchanging the locations of  $L_r$ , the parallel network of  $L_m$  and  $n_l i_o$ . Where,  $n_l$  is transformer turns-ratio of the FB converter and  $i_o$  is the output current. By modifying the equivalent circuits, the transformer primary current  $i_p$  can be divided into the three independent components of the magnetizing current  $i_m$ , the output current referred to the primary side  $n_l i_o$ , and the resonant current  $i_{Lr}$ . As a result, the two converter operations can be analyzed independently. Before analysis, it is assumed that the transformer has no leakage inductance and that all of the switching devices are ideal. In addition, the output voltage of the resonant converter  $v_{o_RC}$  has a constant value that is lower than the battery voltage  $V_{batt}$ , and the resonant capacitor voltage  $v_{cr}$  does not exceed  $V_{batt}$ . The detailed operational modes are explained as follows:

1) Mode 1 ( $t_0 \le t < t_1$ ): When  $M_1$  is turned on at  $t_0$ , the

primary current  $i_p$  flows through  $M_1$ ,  $M_3$ ,  $L_r$ , and the transformer primary; and the secondary current of the resonant converter  $i_{s\_RC}$  is increased from zero in a resonant manner through  $C_r$ ,  $D_1$ ,  $D_3$ ,  $C_{o2}$ , and the transformer secondary. Since  $i_{Lr}$  means the primary side current of the resonant converter, the relationship between  $i_{Lr}$  and  $i_{s\_RC}$  is equal to  $i_{Lr}=n_2i_{s\_RC}$ . From the equivalent circuit of mode 1,  $v_{cr}/n_2$  and  $i_{Lr}$  can be expressed as follows:

$$\frac{v_{cr}(t)}{n_2} = \left(V_{in} - \frac{V_{o\_RC}}{n_2}\right) - \left(V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o\_RC}}{n_2}\right) \cos \omega_r t \quad (1)$$

$$i_{Lr}(t) = \frac{1}{Z_r} \left( V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o\_RC}}{n_2} \right) \sin \omega_r t$$
(2)

where,  $\omega_r = 1/[n_2 (L_r C_r)^{0.5}]$  and  $Z_r = (1/n_2) (L_r/C_r)^{0.5}$ . In equations (1) and (2),  $n_2$  is the transformer turns-ratio of the resonant converter, and  $v_{cr}$  is the resonant capacitor voltage. In addition,  $V_{cro}$  is the peak voltage of  $v_{cr}$ . Since the primary current  $i_p$  is the sum of  $i_m$ ,  $n_1 i_o$ , and  $i_{Lr}$ , it is written as:

$$i_{p}(t) = i_{m}(t) + n_{l}i_{o}(t) + i_{Lr}(t) = \frac{V_{in}}{L_{m}}(t) - \frac{V_{in}}{2L_{m}}DT_{s} + n_{l}i_{o}(t) + i_{Lr}(t)$$
(3)

where,  $L_m$ ,  $T_s$ , and D refer to the magnetizing inductance, switching period, and duty-ratios of  $M_1$  and  $M_4$ , respectively. During this mode, the transformer secondary voltage of the resonant converter  $v_{s\_RC}$  is  $V_{o\_RC}+v_{cr}$  and it appears at the transformer secondary voltage of the FB converter  $v_{s\_FB}$  as  $(n_1/n_2)$  ( $V_{o\_RC}+v_{cr}$ ). Thus, the output voltage of the FB rectifier  $v_x$  becomes  $V_{o\_RC}+(V_{o\_RC}+v_{cr})(n_1/n_2)$  so that the voltage applied across the output inductor  $L_o$  can be written as follows:

$$v_{L} = V_{o_{-RC}} + \frac{n_{1}}{n_{2}} (v_{cr} + V_{o_{-RC}}) - V_{batt}$$
(4)

2) Mode 2 ( $t_1 \le t < t_2$ ): When  $M_1$  is turned off and  $M_2$  is turned on, the primary current  $i_p$  flows through  $M_3$ , the body diode of  $M_2$ , and the transformer primary; and the secondary current  $i_{s_{RC}}$  has same current path as that of mode 1 until  $i_{s_{-RC}}$  is decreased to zero. From the equivalent circuit of mode 2,  $v_{cr}/n_2$  and  $i_{Lr}$  can be expressed as follows:

$$\frac{v_{cr}(t)}{n_2} = -\frac{V_{o\_RC}}{n_2} - \left(-\frac{V_{cr}(t_1)}{n_2} - \frac{V_{o\_RC}}{n_2}\right) \cos\omega_r t + Z_r i_{Lr}(t_1) \sin\omega_r t \quad (5)$$

$$i_{Lr}(t) = \frac{1}{Z_r} \left( -\frac{V_{cr}(t_1)}{n_2} - \frac{V_{o_-RC}}{n_2} \right) \sin \omega_r t + i_{Lr}(t_1) \cos \omega_r t \quad (6)$$

 $i_{Lr}(t_1)$  and  $v_{cr}(t_1)/n_1$  in equations (5) and (6) are the initial conditions of mode 2 and they can be found from equations (1) and (2) as follows:

$$\frac{v_{cr}(t_1)}{n_2} = \frac{v_{cr}(DT_s)}{n_2} = \left(V_{in} - \frac{V_{o\_RC}}{n_2}\right) - \left(V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o\_RC}}{n_2}\right) \cos\omega_r DT_s \quad (7)$$

$$i_{Lr}(t_1) = i_{Lr}(DT_s) = \frac{1}{Z_r} \left( V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o_-RC}}{n_2} \right) \sin \omega_r DT_s$$
(8)

In addition, since the transformer primary is shorted by the  $M_2$  and  $M_3$  switches, the magnetizing current  $i_m$  is kept constant.

Therefore,  $i_p$  becomes:

$$i_{p}(t-t_{1}) = \frac{V_{in}}{2L_{m}}DT_{s} + n_{1}i_{o}(t) + i_{Lr}(t-t_{1})$$
<sup>(9)</sup>

This mode continues until  $i_{Lr}$  is decreased to zero and its duration can be derived as the following equation with equations (6)-(8).

$$T_{M2} = \frac{1}{\omega_r} \tan^{-1} \left( -\frac{b}{a} \right) \tag{10}$$

Where:

$$a \equiv -V_{in} + \left(V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o_{-RC}}}{n_2}\right) \cos \omega_r DT_s$$
$$b \equiv \left(V_{in} + \frac{V_{cro}}{n_2} - \frac{V_{o_{-RC}}}{n_2}\right) \sin \omega_r DT_s$$

Referring to the key waveforms and operational mode diagram of mode 2, the conduction path of the rectifiers in the resonant converter is kept the same as that of mode 1. Thus,  $v_x$  is maintained as  $V_{o_RC}+(V_{o_RC}+v_{cr})(n_1/n_2)$  and the operation of the FB converter is the same as that of mode 1.

3) Mode 3 ( $t_2 \le t < t_3$ ): After  $i_{s_{RC}}$  is decreased to zero, the diodes  $D_1$  and  $D_3$  are turned off and only the magnetizing current  $i_m$  and output current referred to the primary side  $n_1 i_o$  circulate together through  $M_3$  and the body diode of  $M_2$ . In addition, the resonant capacitor voltage  $v_{cr}$  is maintained as  $v_{cr}(t_2)$ . Since  $v_{cr}(t_2)$  is equal to  $V_{cro}$ , it can be derived as the following equation with equations (5) and (10).

$$v_{cr}(t_2) = V_{cro} = \frac{n_2 V_{in} (n_2 V_{in} - V_{o\_RC}) (1 - \cos \omega_r DT_s)}{2 V_{o\_RC} - n_2 V_{in} (1 - \cos \omega_r DT_s)}$$
(11)

To prevent abnormal turn-on of the rectifying diodes of the resonant converter during mode 3, the maximum value of  $V_{cro}$  should not exceed  $V_{o_{RC}}$  of the proposed converter. Thus, the resonant parameters should be designed to meet this condition and this is imposed as one of the design guidelines. When  $M_3$  is turned off and  $M_4$  is turned on, the next half cycle begins and its operation is similar to the previous half cycle.

#### C. Voltage Gain of the Proposed Converter

Referring to Fig. 2, the voltage waveform applied across the output inductor can be depicted as Fig. 6. In order for the inductor current to stay in the stead-state, the following condition should be satisfied.

$$\frac{2}{T_s} \left[ \int_{0}^{DT_s + T_{h_2}} V_{o_2} + \frac{n_1}{n_2} (v_{cr} + V_{o_RC}) - V_{batt} dt + (V_{o_RC} - V_{batt}) (T_s - DT_s - t_x) \right] = 0 \quad (12)$$

Since the average value of  $v_{cr}$  during  $DT_s+T_{M2}$  is equals to zero in the steady-state, the relationship between  $V_{batt}$  and  $V_{o RC}$  can be derived from equation (12) as follows:

$$V_{batt} = \frac{n_1}{n_2} V_{o_{-RC}} \left( D + \frac{T_{M2}}{T_s} \right) + V_{o_{-RC}}$$
(13)

To derive the relationship between  $V_{co2}$  and  $I_o$ , information on

the input power that the resonant converter is responsible for is required. The input current  $i_{in}$  is the sum of  $i_{MI}$  and  $i_{M4}$ , and  $i_{M4}$  has the same waveform as  $i_{MI}$  except for a phase delay of 180°. Thus, it is sufficient to consider the input current during half a cycle. Referring to Fig. 2,  $i_{MI}$  is equal to ip during mode 1, and  $i_p$  is expressed as equation (3). Accordingly, it can be seen that the average input power of the resonant converter  $P_{in,R}$  can be calculated by averaging the product of  $v_{in}$  and  $i_{Lr}$ over half of the switching cycle. From equations (2) and (11), it can be derived that:

$$P_{in.R} = \frac{2}{T_s} \int_{0}^{T_s/2} v_{in}(t) i_{Lr}(t) dt = \frac{2V_{in} n_2^2 C_r}{T_s} \frac{2 \frac{V_{o\_RC}}{n_2} \left( V_{in} - \frac{V_{o\_RC}}{n_2} \right) \times Q}{2 \frac{V_{o\_RC}}{n_2} - V_{in} Q}$$
(14)

where,  $Q=1-\cos\omega_r DT_s$ . The output power of the resonant converter  $P_{o,R}$  can be expressed as:

$$P_{o2} = V_{o\_RC} I_o \tag{15}$$

By equating equation (14) with equation (15),  $V_{o_{RC}}$  can be derived as:

$$\frac{V_{o_{-RC}}}{n_2} = \frac{4V_{in}^2 n_2^2 C_r Q + V_{in} I_o T_s Q}{2I_o T_s + 4V_{in} n_2^2 C_r Q}$$
(16)

Therefore, the battery voltage can be written as follows:

$$V_{batt} = \left[ n_1 \left( D + \frac{t_x}{T_s} \right) + n_2 \right] \left( \frac{4V_{in}^2 n_2^2 C_r Q + V_{in} I_o T_s Q}{2I_o T_s + 4V_{in} n_2^2 C_r Q} \right)$$
(17)

#### D. ZVS Switching Condition

Fig. 5 shows the expanded switching waveforms to illustrate the ZVS operation and equivalent circuits during  $T_{dead}$  of the dead-time between the gate signals of top and bottom switches. Where,  $C_{ds}$  is the drain-source capacitance of the primary switches. Referring to these figures, the ZVS conditions of  $M_2$  and  $M_3$  are easily satisfied because the peak current of  $i_p$  is used for ZVS. However, the ZVS of  $M_1$  and  $M_4$  is only aided by the magnetizing current and output current referred to the primary side [11]. Assuming that the dead-time is short enough for the magnetizing current during dead-time to be constant and that the output current ripple is negligibly small, the magnitude of  $i_p$  during the dead-time between  $M_1$  and  $M_4$  can be found as follows:

$$i_p = I_{m,pk} + n_1 i_o \approx \frac{V_{in}}{2L_m} DT_s + n_1 I_o$$
 (18)

This current changes the potentials of the output capacitances of the top and bottom switches from zero to the input voltage. Referring to the equivalent circuit in Fig. 5, the potential changing time  $\Delta T$  can be derived as follows:

$$\Delta T = \frac{2C_{ds}V_{in}}{\frac{V_{in}}{2L_m}DT_s + n_1I_o}$$
(19)

To achieve the ZVS of  $M_1$  and  $M_4$ ,  $\Delta T$  should be shorter than  $T_{dead}$ . From this condition, for  $L_m$  to meet ZVS can be found as follows:

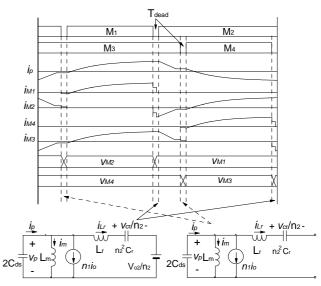


Fig. 5. Expanded switching waveforms and equivalent circuits during dead-times.

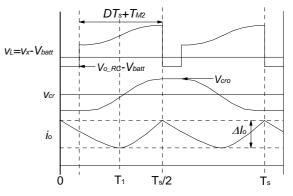


Fig. 6. Waveforms of the voltage applied across output inductor  $v_{L_2}$  resonant capacitor voltage  $v_{cr_2}$  and inductor current ripple  $\Delta i_{a_1}$ .

$$L_m \le \frac{V_{in} DT_s}{2\left(\frac{2C_{ds}V_{in}}{T_{dead}} - n_1 I_o\right)}$$
(20)

The worst case for selecting  $L_m$  happens at  $D_{min}$  and  $I_{o,min}$ , that is, the minimum battery voltage and the minimum charging current. Since values of  $D_{min}$  and  $I_{o,min}$  that are too small increase the circulating current and the turn-off switching loss of the upper switches. Proper values of  $D_{min}$  and  $I_{o,min}$  should be selected considering the operational characteristics of the charger.

#### E. Voltage Stresses of the FB Output Diodes

During the powering durations from mode 1 to mode 2, the transformer secondary voltage of the resonant converter stage  $v_{s\_RC}$  is  $v_{cr}+V_{o\_RC}$ . As a result, the transformer secondary voltage of the FB stage  $v_{s\_FB}$  becomes  $(n_l/n_2)(v_{cr}+V_{o\_RC})$ . The anode-to-cathode voltage of the diode in the FB stage is twice  $v_{s\_FB}$ . Because mode 3 is the freewheeling duration, the maximum voltage stress occurs at the end of mode 2, and it can be written as follows:

$$V_{D5,6_{max}} = 2\frac{n_1}{n_2}(v_{cr}(t_2) + V_{o_{RC}}) = 2\frac{n_1}{n_2}(V_{cro} + V_{o_{RC}}) \quad (21)$$

From equation (21), it can be known that if  $n_1$  is a lot smaller than  $n_2$ , the voltage stress of  $D_5$  and  $D_6$  can be reduced to the level where Schottky diodes with a low on-drop voltage are available. In addition, the leakage inductance is used for the resonant parameter so that the voltage spikes caused by the diode junction capacitance and leakage inductance do not exist.

#### F. Output Inductor Ripple

Fig. 6 shows waveforms of the voltage applied across the output inductor  $v_L$ , the resonant capacitor voltage  $v_{cr}$ , and the inductor current ripple  $\Delta i_o$ . With equation (4),  $\Delta i_o$  can be written as:

$$\Delta i_o = \int_{T_1}^{T_s/2} \frac{v_L}{L_o} dt = \frac{1}{L_o} \int_{T_1}^{T_s/2} \left( V_{o_RC} + \frac{n_1}{n_2} (v_{cr} + V_{o_RC}) - V_{batt} \right) dt \quad (22)$$

To derive the design equation of the output inductor, the following assumptions are made:

- The duration of mode 3 is small enough to be zero at the maximum battery voltage and maximum load.
- 2) The waveforms of  $v_{cr}$  during mode 1 and mode 2 are near to a sinusoidal waveform.

From these two assumptions,  $DT_s+T_{M2}$ ,  $T_l$ , and  $v_{cr}$  can be approximated as  $T_s/2$ ,  $T_s/4$ , and  $-V_{cro}\cos(2\pi t/T_s)$ , respectively. Therefore, equation (23) can be rewritten as:

$$\Delta i_{o} \approx \frac{1}{L_{o}} \left[ \frac{T_{s}}{4} \left( V_{o2} + \frac{n_{1}}{n_{2}} V_{o_{-}RC} - V_{batt} \right) - \frac{n_{1}}{n_{2}} \int_{T_{s/4}}^{T_{s}/2} \cos(2\pi t/T_{s}) dt \right]$$
(23)

In addition, the inductor current ripple  $\Delta i_o$  at the maximum load condition can be derived as follows:

$$\Delta i_{o} = \frac{1}{L_{o}} \left[ \frac{T_{s}}{4} \left( V_{o_{-RC}} + \frac{n_{1}}{n_{2}} V_{o_{-RC}} - V_{batt} \right) + \frac{n_{1}}{n_{2}} \frac{T_{s}}{2\pi} V_{cro} \right]$$
(24)

#### III. DESIGN PROCEDURE

As mentioned in the mode analysis in Section II, the resonant parameters should be designed to meet the condition that  $V_{cro}$  does not exceed  $V_{batt}$ . In addition, the duration from mode 1 to mode 2,  $DT_s+T_{M2}$  should be shorter than  $T_s/2$  to minimize the turn-off switching losses of the bottom switches and the output diodes. Therefore, some design procedures to meet the design conditions are given below.

**Step 1:** Select  $D_{max}$ ,  $n_2$ , and  $V_{o\_RC}$ .

Referring to equation (11),  $V_{cro}$  should not have a negative value so that  $n_2V_{in}$  should be larger than the maximum  $V_{o\_RC}$ . Based on this condition, the range of  $n_2$  that guarantees normal operation can be written as:

$$n_2 \ge \frac{V_{o\_RC,\max}}{V_{in}} \tag{25}$$

From equation (16), it can be known that the minimum  $n_2$  happens when the duty-ratio D is equal to 0.5 and the switching frequency  $f_s$  is equal to the resonant frequency  $f_r$ . These conditions mean that the converter has complete resonant operation. However, the operational duty-ratio is used below 0.5 to guarantee the duration of mode 1, and  $f_s$  is always higher than  $f_r$  for the PWM control. Therefore,  $n_2$  should be selected with a value that is sufficiently larger than the minimum value resulting from equation (25). Finally, the maximum operational duty-ratio  $D_{max}$  is chosen considering the duration of mode 2.

**Step 2:** Find the resonant frequency  $\omega_r$ .

Using equations (10) and (11) and the selected values in step 1,  $V_{cro}$  and  $T_{M2}$  can be plotted according to the resonant frequency  $\omega_r$  at  $V_{batt,max}$  and  $V_{in}$ . From this plot, an appropriate resonant frequency can be chosen to meet the conditions of  $V_{cro} < V_{batt,max}$  and  $DT_s + T_{M2} < T_s/2$ .

Step 3: Find the resonant tank parameters.

From the results of step 2 and equation (16), a resonant capacitor  $C_r$  can be selected to meet the condition that the value of  $V_{o\_RC}$  calculated at  $D_{max}$  is equal to or slightly larger than the selected  $V_{o\_RC,max}$ . After that, the resonant inductor  $L_r$  is calculated with the selected  $C_r$  and  $n_2$ .

**Step 4:** Find *n*<sub>1</sub>.

With  $T_{M2}$  found in step 2, and  $V_{o\_RC,max}$  recalculated in step 3, the minimum  $n_1$  can be obtained using equation (13).

Step 5: Check whether the design meets the conditions of  $V_{cro} < V_{batt}$  and  $DT_s + T_{M2} < T_s/2$  under all of the battery voltage ranges.

It is sufficient that this step be performed at the maximum charging powers according to the battery voltages because  $V_{cro}$  and  $DT_s+T_{M2}$  are increased as the load becomes heavy.

#### IV. DESIGN AND EXPERIMENTAL RESULTS

A 6.6kW prototype charger has been designed ( $V_{in}$ =400V,  $V_{batt}$ =250V~420V/ $I_{o,max}$ =20A) and its switching frequency is 50kHz.

**Step 2:** Fig. 7 shows the plots of  $DT_s+T_{M2}$  and  $V_{cro}$  according to resonant frequency variations with the selected values of step 1 and equations (10) and (11) at  $V_{in}$ =400V and  $V_{o_RC,max}$ =394V. From this figure,  $DT_s+T_{M2}$  and  $V_{cro}$  has been selected as 8.97µs and 163V at  $\omega_r$ =235krad/sec in this design. **Step 3:** From the results of step 2 and equation (16), the voltage gain of the resonant converter can be plotted as shown in Fig. 8 according to variations of  $C_r$ . In order for the

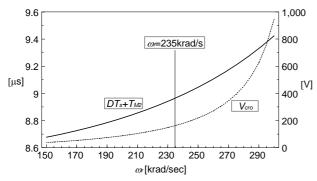


Fig. 7. Plot of  $DT_s+T_{M2}$  and  $V_{cro}$  according to resonant frequency variations with the selected values of step 1 at  $V_{in}$ =400V and  $V_{o RC,max}$ =394V.

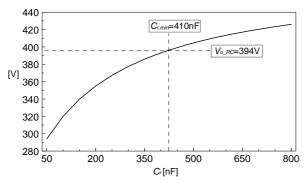


Fig. 8. Output voltage of resonant converter stage according to  $C_r$  variations at maximum load conditions.

prototype converter to meet the selected value of  $V_{o_RC,max}$ , the minimum voltage gain of the converter must be 0.985. The minimum value of  $C_r$  to meet this gain is 410nF. However, too large a  $C_r$  increases the switch current stresses as shown in equation (2). Thus,  $C_r$ =500nF has been selected, and 25.1µH of  $L_r$  was calculated as a result.

**Step 4:** Since  $C_r$  is selected so that the gain of the resonant converter is larger than 0.985,  $V_{o_RC,max}$  is recalculated and it is 405V. Using this recalculated  $V_{o_RC,max}$ , the minimum value of  $n_1$  can be found using equation (13). The calculated value is 0.0991 and 0.1 has been used in this design.

**Step 5:** Fig. 9 shows the plot of  $V_{cro}$ ,  $V_{batt}$ ,  $V_{o_RC}$ , and  $DT_s+T_{M2}$  according to the duty-ratio and charge current variations using equations (10), (11), (16), and (17). This figure shows that the maximum chargeable voltage at  $I_{batt,max}$ =20A is 407.7V under the duty-ratio limitation and that it is 458V under the operational condition limitation. In addition, the maximum chargeable voltage at  $I_{batt,max}$ =15.7A is 420V under the duty-ratio limitation and it is 468V under the operational conditions of  $V_{cro} < V_{o_RC}$  and  $DT_s+T_{M2} < T_s/2$  under all of the battery voltage ranges. From Fig. 9, it can be known that the difference between  $V_{o_RC}$  and  $V_{cro}$  becomes larger as  $V_{batt}$  increases, while  $V_{cro}$  is kept nearly constant. Thus, these converter characteristics and equation (24) show that the maximum current ripple happens at the

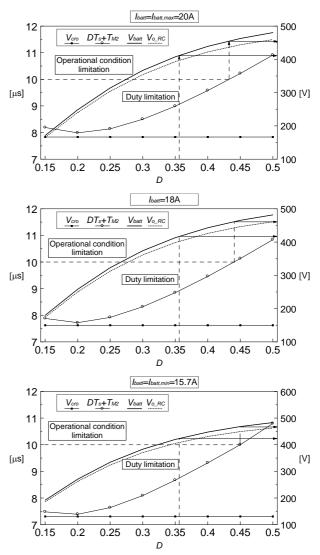


Fig. 9. Plots of  $V_{cro}$ ,  $V_{batt}$ , and  $DT_s + T_{M2}$  according to duty-ratio variations and charging profile

maximum battery voltage. Referring to Fig. 9,  $V_{o RC}$  and  $V_{cro}$ at V<sub>batt</sub>=420V are 405.4V and 130.8V, respectively. Therefore,  $L_o$  can be calculated as 65µH when the output current ripple is selected as 10% of a maximum current of 20A. This is a very low inductor value compared with conventional FB chargers because a FB charger having the same specifications as the proposed charger requires an output inductor that is around 2mH. In addition, the low current ripple of the proposed charger provides another merit since a bulky current filter is not required. As mentioned in section III, the worst case for selecting  $L_m$  happens at  $D_{min}$  and  $I_{o,min}$  and they are 0.2 and 20A from Fig. 9. Using this information and the selected devices,  $L_m$  can be calculated as about 286µH at  $T_{dead}$ =300ns. In this design, 256µH has been used. Fig. 10 shows the implemented prototype, and Table I presents a key components list of the prototype charger. It shows that  $A_p$  of the transformer in the proposed charger is 61.5cm<sup>4</sup> at a 6.6kW output, while those in references [12] and [13] are

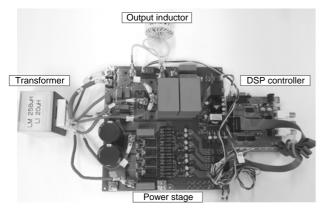


Fig. 10. Implemented prototype.

	TABLE I
	KEY COMPONENT LIST
Component	Implementation
$M_1 \sim M_4$	IPW65R041CFD×2
$D_1 \sim D_2$	DSSK 60-02A
$D_4 \sim D_6$	FFH50US60S
Transformer	1: $n_1$ : $n_2$ =1:0.1:1.2 (EE6565 × 2 stack) $L_{lkg}$ =25 $\mu$ H, $L_m$ =256 $\mu$ H, $A_p$ =61.5cm <sup>4</sup>
$L_o$	65µH(CH467060 High flux core)
$C_r$	500nF (Film capacitor)
$C_o$	200µF
500 400 200 100 2 4	0.5 0.4 0.3 0.2 0.1 0.2 0.1 0.1 0.2 0.1 0.2 0.1 0.1 0.2 0.1 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.1 0.2 0.2 0.1 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2
6000 5000 [W] 4000 3000	

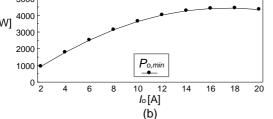


Fig. 11. Battery voltages calculated at (a) minimum duty-ratios to meet ZVS of  $M_1$  (or  $M_4$ ) and (b) minimum load conditions for ZVS of  $M_1$  (or  $M_4$ ).

89.32cm<sup>4</sup> at a 3.5kW output, where  $A_p$  means the product of the window area and the cross-sectional area of the transformer core. Fig. 11(a) shows the battery voltages at the minimum duty-ratios to meet the ZVS calculated with equations (17) and (20). From this figure, it can be seen that the minimum load conditions for the ZVS of  $M_1$  (or  $M_4$ ) can

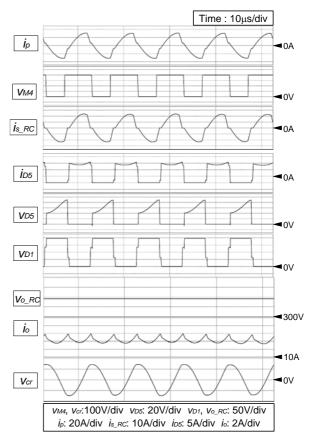


Fig. 12. Simulated switching waveforms measured at  $V_{batt}$ =420V  $/P_o$ =6.6kW.

be depicted according to battery current, as shown in Fig. 11(b). The ZV-ZCS of  $M_2$  (or  $M_3$ ) is met under the overall load range due to its switching characteristics as explained in the mode analysis. Figs. 12 and 13 show switching waveforms simulated and measured at  $V_{hatt}=420\text{V}/P_{o}=6.6\text{kW}$ . The switching waveforms show good agreement with the theoretical analysis. In addition, the output current ripples are below 2A under the entire battery voltage range with a small output inductor. The ringing voltage of  $V_{DI}$  is caused by resonance between the diode junction capacitance and the resonant inductor reflected to the secondary side. In addition, the parasitic inductance of the interconnection causes the very high frequency voltage spike of  $V_{D5}$  with the diode junction capacitance. Fig. 14 shows the measured current and voltage waveforms of  $M_1$  and  $M_2$ . Form this figure, the ZVS of the upper switch and the ZV-ZCS of the lower switch are well accomplished. Fig. 15 shows the measured efficiency according to the battery voltages. The efficiency has been measured with a YOKOGAWA WT500 power analyzer. It shows that a 97.2% efficiency has been recorded at 360V/6.6kW and that a maximum efficiency of 97.4% has been measured at 413V/6.6kW. Although the rectifier is comprised of 6 diodes and all of the diodes are used for carrying battery charging current, serious efficiency degradation does not occur because the maximum increase of

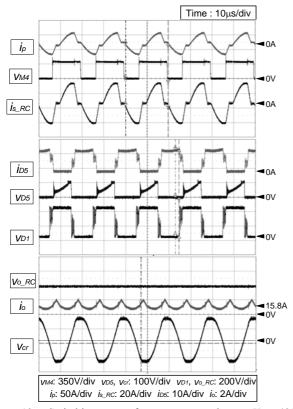


Fig. 13. Switching waveforms measured at  $V_{batt}$ =420V / $P_o$ =6.6kW.

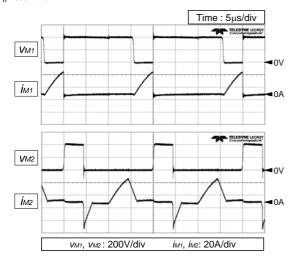


Fig. 14. Measured current and voltage waveforms of  $M_1$  and  $M_2$ .

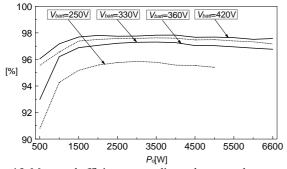


Fig. 15. Measured efficiency according to battery voltages.

the rectifier conduction loss contributed by the Schottky diodes of the FB stage is approximately 14W when the battery charging current is at its maximum.

# V. CONCLUSIONS

A hybrid PWM DC/DC converter comprised of a FB converter and a resonant converter has been proposed for OBCs. The proposed converter has the mixed operational characteristics of the two converters and all of them use PWM, which simplifies the transformer structure by coupling the two secondary sides. The switching characteristics are similar to those of a PWM resonant converter so that the ZV-ZCS operation of at the bottom switches and the ZVS operation of the top switches can be accomplished by proper design of the resonance. In addition, the proposed structure provides merits such as no dissipative snubber circuitry and no output filter. Some analyses to explain the operation of the charger and select its design parameters has been performed. Based on these analyses, design equations have been derived. To verify the performance, a 6.6KW prototype charger has been implemented with the design guidelines. Experimental results show that a maximum efficiency of 97.4% has been obtained at 413V/6.6kW. Therefore, it may be suitable for the DC/DC stage in single-phase PHEV/EV chargers requiring high efficiency.

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