

# A 3 kW Bidirectional DC-DC Converter for Electric Vehicles

Arsalan Ansari\*, Puyang Cheng\* and Hee-Jun Kim<sup>†</sup>

**Abstract** – A bidirectional DC-DC converter (BDC) is an indispensable electrical unit for the electric vehicles (EVs). High efficiency, high power density, isolation, light weight and reliability are all essential requirements for BDC. In this paper, a 3 kW BDC for the battery charger of EVs is proposed. The proposed converter consists of a half-bridge structure on the primary side and an isolation transformer and a synchronous rectifier structure on the secondary side. With this topology, minimum number of switching devices are required for bidirectional power flow between the two dc buses of EVs. The easy implementation of the synchronous rectification gives advantages in terms of efficiency, cost and flexibility. The proposed BDC achieves high efficiency when operating in both modes (step-up and step-down). A 3 kW prototype is implemented to verify theoretical analysis and the performance of the proposed converter.

**Keywords:** Bidirectional DC-DC converter, Battery charger, Electric vehicles, Efficiency

## 1. Introduction

With the global energy crisis the conventional vehicles (internal combustion engines) face the increasingly serious problems of energy. In contrast, the EVs especially battery electric vehicles (BEVs) depend on variety of options for its driving power. BEVs offer the advantages of safety, silent operation and no emissions when powered by renewable energy sources such as wind or solar which are virtually emission free [1]. These vehicles can also make efficient use of energy by storing energy recovered during braking or deceleration cycle in the batteries. The storage or charging process of the battery is achieved by a BDC, which is the key block in EV energy system to link high voltage (HV) dc bus and low voltage (LV) dc bus as shown in Fig. 1. This BDC should have high power density and high efficiency to meet the desired goals for EV's battery charger. When the EV is parked, the battery can be charged by the household utility outlet from the grid through the BDC. For the other case when the EV is in the driving state, the BDC provides the electrical power from LV battery to the motor through DC-AC inverter and also DC loads in the EV.

BDCs are broadly classified into isolated and non-isolated types. The conventional non-isolated buck/boost BDC cannot operate in the wide voltage conversion range [2]. The isolated BDC are preferred for EVs due to the advantages of high voltage conversion ratio and safety. Many different types of isolated BDCs [3-6] have been proposed due to these advantages, some full-bridge BDCs

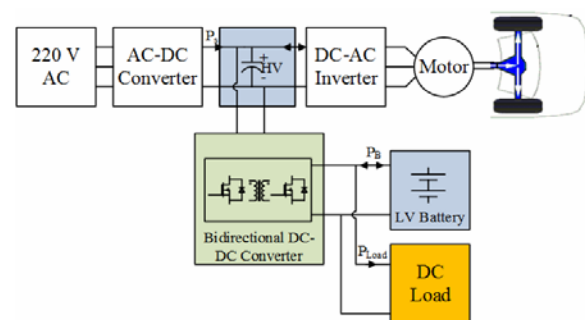


Fig. 1. The energy system of EV

[7-10] have also been proposed in recent years. However, full-bridge converters have the disadvantage of high voltage ripples if not employing an extra voltage clamping circuit [11]. By contrast, half-bridge converters [12-14] have a simple structure and a better anti-imbalance ability in the transformer. In some topologies of half-bridge converters, MOSFET body diodes are applied for synchronous rectification in both buck/boost modes [15], but high conduction losses result in low efficiency, thus limiting the use of these converters to only low power applications.

This paper describes the development of a 3 kW BDC for EVs. The converter consists of a half-bridge topology, an isolation transformer and a synchronous rectifier. The isolation transformer provides the advantages of wide conversion range and safety, and the easy implementation of synchronous rectification offers the benefits in terms of efficiency, cost and flexibility. However, this structure has been mostly proposed for less than 1.5 kW application [3, 11-13, 16-17], so the operation of more than 3 kW in both step-up and step-down modes has the practical significance for the EV battery charger products.

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## 2. Topology Configuration and Operational Principles

### 2.1 Topology configuration

Fig. 2 shows the circuit diagram of the proposed half-bridge BDC. The design uses a half-bridge connected with the DC power supply on the primary side and a center-tapped transformer and a synchronous rectification on the secondary side. The converter can operate in two modes, namely, step-down mode and step-up mode. All of the four switches  $Q_1$ – $Q_4$  are gated in both modes. Switch  $Q_1$  is complementary with switch  $Q_4$ , and switch  $Q_2$  is complementary with switch  $Q_3$ .

In the step-down mode, the primary side DC power supply  $V_H$  (210–380 V) charges the secondary side battery  $V_L$  (21–29 V), and  $Q_3$  and  $Q_4$  provide rectification. In contrast,  $Q_1$  and  $Q_2$  operate as rectifiers in the step-up

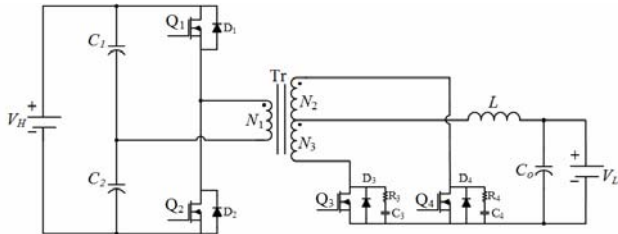


Fig. 2. Circuit diagram of the proposed converter

mode when  $V_L$  supplies the high side battery  $V_H$ . For mathematical insight into the proposed converter, some assumptions are made as: (i) the ON-state resistance  $R_{DS(ON)}$  of all switches is ignored; (ii) the capacitors  $C_1$ ,  $C_2$  and  $C_0$  are large enough, and the voltage across the capacitors can be taken as constant; and (iii) the capacitance of the capacitors  $C_1$  and  $C_2$  is equal i.e.  $C_1=C_2=C$ . Thus,  $V_{C1}=V_{C2}=V_H/2$ ; and (iv)  $D_1$ – $D_4$  are the body diodes of  $Q_1$ – $Q_4$ , and the diode forward resistance is zero.

### 2.2 Operational principles of the proposed BDC

#### 2.2.1 Step-down mode

This is similar to a buck converter operational mode in which  $V_H$  supplies  $V_L$  with the charging current,  $i_L$ . The equivalent circuits are shown in Fig. 3. The pulse-width modulation (PWM) technique is used to control the switches  $Q_1$ – $Q_4$ . In both modes  $Q_1$  and  $Q_2$  are gated, with the duty cycle less than 0.5, while the duty cycle of  $Q_3$  and  $Q_4$  is more than 0.5. Fig. 4 shows some typical waveforms for the step-down mode. The operating principles during one switching period are described as follows:

**Stage 1 [ $t_0$ – $t_1$ ]:** Switch  $Q_1$  turns on and switch  $Q_4$  turns off at  $t_0$ , while switch  $Q_3$  remains on. The current flow path for this stage is shown in Fig. 3(a). In this stage  $v_{AB}=V_H/2$ , the current  $i_1$  flows through  $Q_1$  as  $i_p$ , which is reflected from inductor current  $i_L$ . The current  $i_L$  increases linearly and flows totally through switch  $Q_3$  to charge the battery

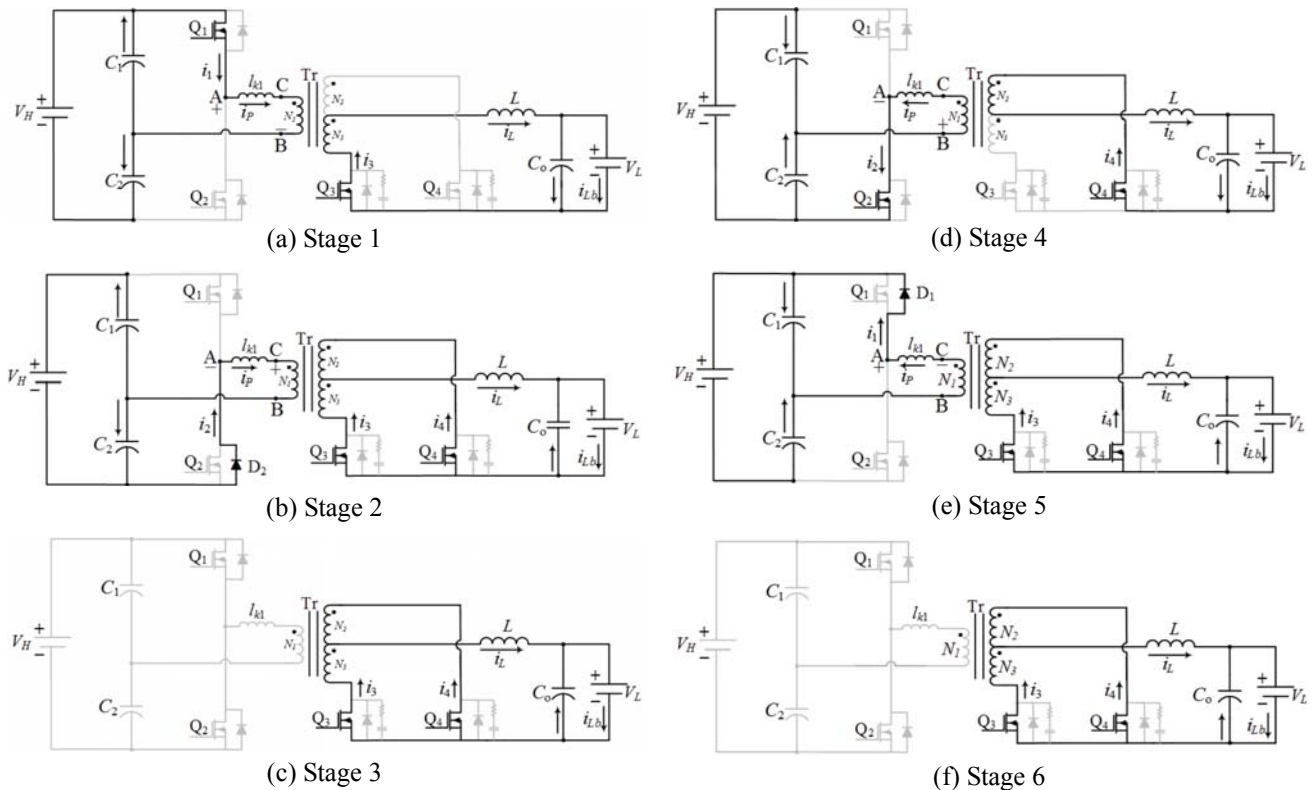


Fig. 3. Equivalent circuits for the step-down mode

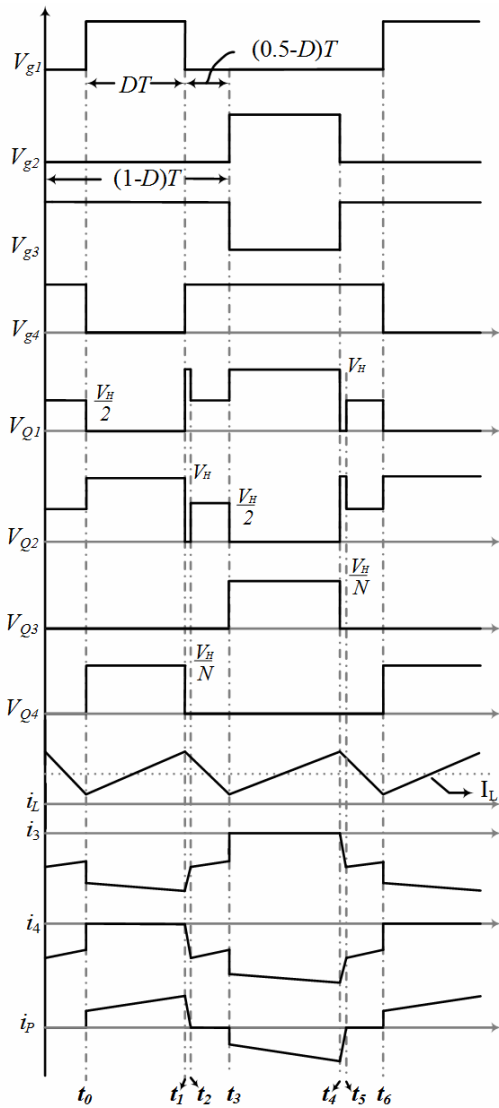


Fig. 4. Theoretical waveforms for the step-down mode

$V_L$ .

**Stage 2 [ $t_1-t_2$ ]:** Switch  $Q_1$  turns off and switch  $Q_4$  turns on at  $t_1$ , while switch  $Q_3$  still remains on. Because of the transformer leakage inductance  $l_{k1}$ , there is freewheeling current through  $D_2$  [Fig. 3(b)],  $v_{CA}=V_H/2$  and  $i_p$  decreases linearly to zero. In this stage  $v_A$  is clamped to ground so  $v_{Q2}=0$  and  $v_{Q1}=V_H$ . Meanwhile  $i_4$  increases and  $i_3$  decreases linearly and at  $t_2$ ,  $i_3=i_4=i_L/2$ .

**Stage 3 [ $t_2-t_3$ ]:** Switch  $Q_1$  and  $Q_2$  are in off state and  $v_{Q1}=v_{Q2}=V_H/2$ . In this stage,  $v_{AB}=0$ , no power is transferred to secondary side and the energy stored in the inductor  $L$  charges the low side battery  $V_L$  [Fig. 3(c)]. The current  $i_L$  is shared equally by switches  $Q_3$  and  $Q_4$ .

**Stage 4 [ $t_3-t_4$ ]:** Switch  $Q_2$  turns on and switch  $Q_3$  turns off at  $t_3$ , while switch  $Q_4$  remains on. The current flow path is shown in Fig. 3(d). This is a similar operation to stage 1 [ $t_0-t_1$ ], but the voltage  $v_{AB}=-V_H/2$ . The current  $i_2$  is built as  $-i_p$ . In this stage,  $Q_4$  is conducting and  $i_4$  increases linearly as  $i_L$ .

**Stage 5 [ $t_4-t_5$ ]:** Switch  $Q_2$  turns off and switch  $Q_3$  turns on at  $t_4$ . Switch  $Q_4$  still remains on. Because of  $l_{k1}$ ,  $D_1$  conducts and  $v_A$  is clamped as  $V_H$ , therefore  $v_{Q2}=V_H$  and  $v_{Q1}=0$  [Fig. 3(e)]. Meanwhile  $i_3$  increases and  $i_4$  decreases linearly and at  $t_5$ ,  $i_3=i_4=i_L/2$ .

**Stage 6 [ $t_5-t_6$ ]:** The operation of this stage is the same as stage 3. The current path for this stage is shown in Fig. 3(f).

### 2.2.2 Step-up mode

For the step-up mode, the equivalent circuits considering the leakage inductance of the proposed converter are shown in Fig. 5. In this operational mode,  $V_L$  discharges to supply the primary side output voltage of  $V_H$  with current  $i_1$  or  $i_2$ . Because of the existence of the transformer secondary side leakage inductance  $l_{k2}$  and  $l_{k3}$ , there will be current stress on  $Q_3$  and  $Q_4$ . For protection of  $Q_3$  and  $Q_4$ , the RC snubber circuit is necessary in parallel connection with  $Q_3$  and  $Q_4$ . The theoretical waveforms are shown in Fig. 6, and modes of operation in one period ( $t_0-t_6$ ) are described as follows:

**Stage 1 [ $t_0-t_1$ ]:** Switch  $Q_3$  is turned on at  $t_0$ , with switch  $Q_4$  remaining on while  $Q_1$  and  $Q_2$  are in the off state. The current flow path for this stage is shown in Fig. 5(a). The secondary side of the transformer is effectively shorted, and  $v_{AB}=0$ . Meanwhile, the energy is stored in the inductor  $L$ , while no energy is transferred to the primary side. In this stage,  $i_L$  increases linearly and is divided equally between  $Q_3$  and  $Q_4$ . The primary side battery  $V_H$  is charged by the capacitors  $C_1$  and  $C_2$ .

**Stage 2 [ $t_1-t_2$ ]:** Switch  $Q_4$  is turned off while switch  $Q_1$  is turned on at  $t_1$ , with switch  $Q_3$  remaining on. Because of the leakage inductance  $l_{k2}$ , there is stress on  $Q_4$  and the RC snubber is charged by  $i_4$  [Fig. 5(b)]. The current  $i_4$  decreases linearly to zero and  $i_3$  increases linearly to  $i_L$ , building  $i_1$  as  $i_p$  which increases linearly.

**Stage 3 [ $t_2-t_3$ ]:** In this stage  $v_{AB}=0$  [Fig. 5(c)], the energy stored in  $L$  is transferred to the primary side,  $i_L$  and decrease in linearity. The capacitor  $C_2$  is discharged and capacitor  $C_1$  is charged.

**Stage 4 [ $t_3-t_4$ ]:** Switch  $Q_4$  is turned on, with switch  $Q_3$  remaining on while switch  $Q_1$  is turned off at  $t_3$ . This stage is similar to stage 1 in which the inductor  $L$  stores energy again, and the inductor current  $i_L$  is equally shared by switches  $Q_3$  and  $Q_4$  [Fig. 5(d)]. Capacitor  $C_1$  and  $C_2$  discharge to supply the primary side DC source  $V_H$ .

**Stage 5 [ $t_4-t_5$ ]:** At  $t_4$  Switch  $Q_3$  is turned off, with switch  $Q_2$  turned on and switch  $Q_4$  remaining on. Because of the leakage inductance  $l_{k3}$  [Fig. 5(e)], there is stress on  $Q_3$  and the RC snubber is charged by  $i_3$ . The current  $i_3$  decreases linearly to zero with  $i_4$  increasing linearly to  $i_L$ , building  $i_1$  as  $-i_p$ .

**Stage 6 [ $t_5-t_6$ ]:** In this stage [Fig. 5(f)],  $i_4$  is built as  $i_L$  which decreases in linearity and energy is transferred to primary side. The capacitor  $C_2$  is charged by  $i_2$  conducted by  $Q_2$ , which decreases linearly.

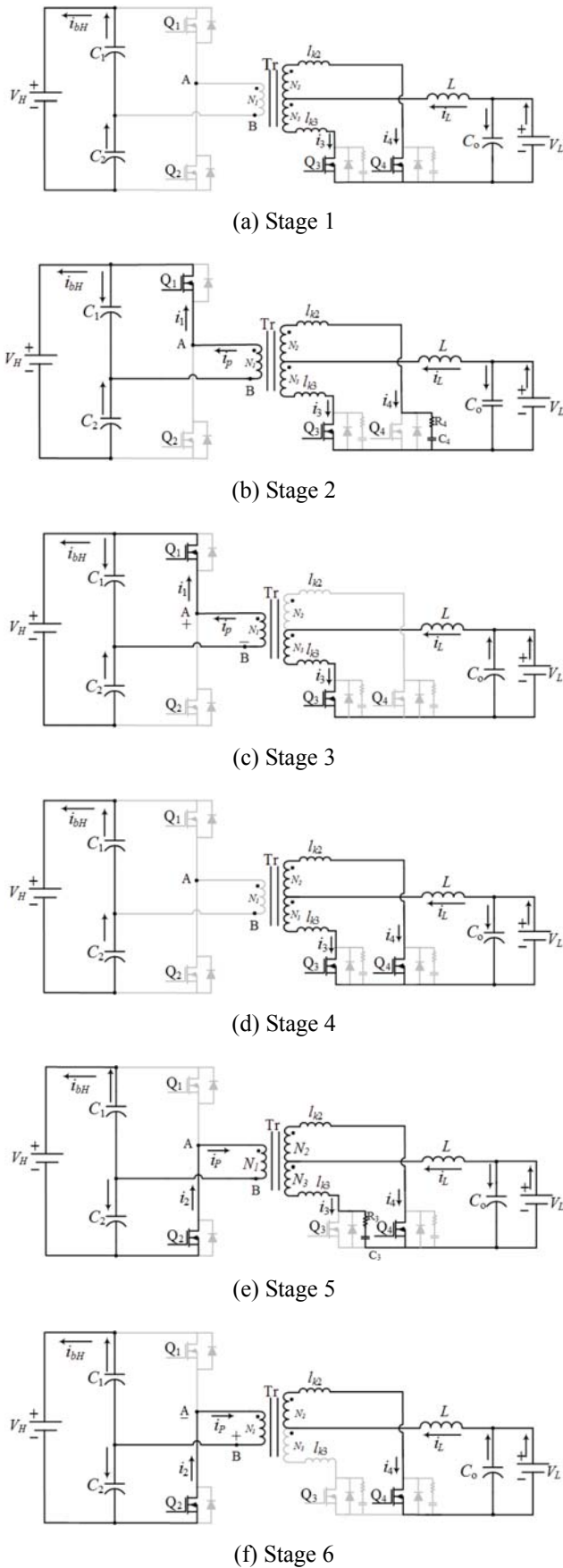


Fig. 5. Equivalent circuits for the step-up mode

### 3. Circuit Design Analysis

The BDC operates in step-down and step-up modes. Design parameters for the step-down mode will be discussed in detail. The parameters obtained can be used for step-up mode as well. The theoretical analysis and design guidelines will be discussed in this section.

#### 3.1 Step-down mode

When the number of turns on the secondary windings are equal, that is,  $N_2=N_3$ , then  $N$  can be defined as the transformer turns ratio, as  $N_1/N_2$  or  $N_1/N_3$ . The relationship between  $V_H$  and  $V_L$  is expressed as:

$$V_L = \frac{D \cdot V_H}{N} \quad (1)$$

where  $D$  is the duty ratio of  $Q_1$  and  $Q_2$ .

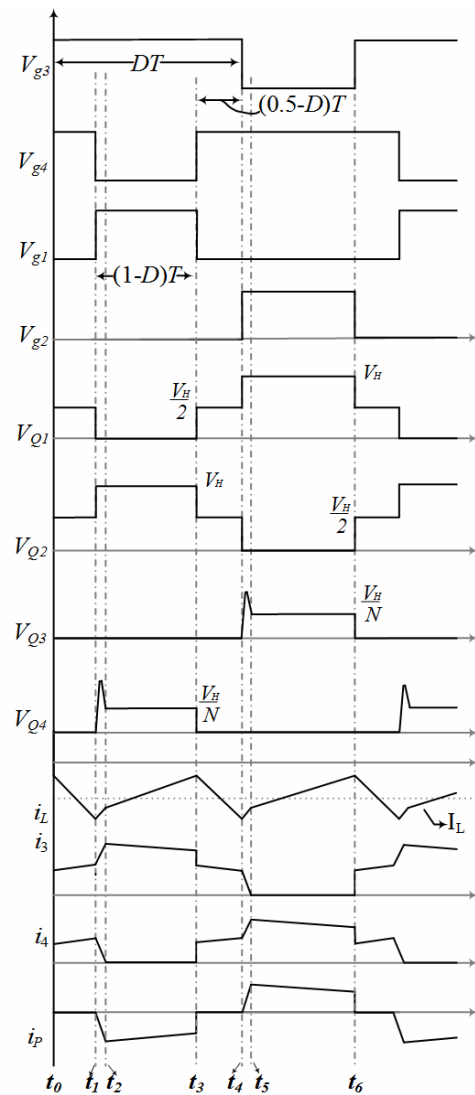


Fig. 6. Theoretical waveforms of the step-up mode



To design the inductor  $L$ , the inductor current ripple  $\Delta i_L$  and the minimum duty ratio  $D_{min}$  should be considered. The inductance  $L$  can be calculated as:

$$L \geq \frac{(0.5 - D_{min}) \cdot V_L}{\Delta i_L f_s} \quad (2)$$

When designing output capacitor  $C_o$ , the transient overshoot should be taken into account. Because of the inductor  $L$ , the energy stored in  $L$  will be transferred to  $C_o$  if there is a sudden change of load, causing a sudden change of  $V_{C_o}$ . According to the design specification, the overshoot voltage should be less than 3% of  $V_L$ , so that for a 50% to full load situation,  $C_o$  can be calculated as:

$$C_o \geq \frac{V_L (0.5 - D_{min}) T_S^2}{8L \Delta v_{c_o}} \quad (3)$$

and for the equivalent series resistance (ESR) of  $C_o$ , the value of ESR should be limited by the following equation:

$$R_{ESR} \leq \frac{\Delta v_{c_o}}{\Delta i_{c_o}} \quad (4)$$

So several capacitors may be connected in parallel, if necessary, to meet the requirements of ESR.

The two capacitors  $C_1$  and  $C_2$  should be large enough to constrain the input current ripple and equally share  $V_H$  for  $Q_1$  and  $Q_2$ .

In practical applications, there are many reasons causing the voltage imbalance. A few of those are: 1) the conduction periods of the two high side switches  $Q_1$  and  $Q_2$  are not strictly equal, 2)  $C_1$  and  $C_2$  are charged and discharged in turns, and if the capacitance value is not big enough, there will be big voltage ripple which may cause voltage imbalance.

To avoid the voltage imbalance, it is necessary to keep the equal conduction periods for  $Q_1$  and  $Q_2$  to the maximum possibility, and it should be noted that the switch  $Q_4$  is complementary with  $Q_1$  and it is the same situation for  $Q_2$  and  $Q_3$ . For  $C_1$  and  $C_2$ , there is

$$dv = i_p \frac{dt}{C} \quad (5)$$

where  $i_p$  is the transformer primary side current.

It can be seen that if  $C$  is big enough, the ripple will be small and it will not affect the circuit operations.

The maximum voltage stress and RMS/max current ratings should be considered when selecting the switches of both sides.  $Q_1$  and  $Q_2$  have the ratings of:

$$V_{DS(peak)} = V_H \quad (6)$$

$$I_{RMS} = \frac{I_L \cdot \sqrt{2D}}{N} \quad (7)$$

$$I_{max} = \frac{I_{L(max)}}{N} \quad (8)$$

$Q_3$  and  $Q_4$  have the ratings of:

$$V_{DSpeak} = \frac{V_H}{N} \quad (9)$$

$$I_{RMS} = [I_b^2 \cdot D + \left(\frac{I_b^2}{2}\right)^2 \cdot (1-2D)]^{1/2} \quad (10)$$

$$I_{max} = I_{L(max)} \quad (11)$$

### 3.2 Step-up mode

For this mode,  $V_L$  is the input voltage, and  $V_H$  is output voltage. Therefore:

$$V_H = \frac{N \cdot V_L}{1 - D'} \quad (12)$$

where  $D'$  is the duty ratio of  $Q_3$  and  $Q_4$ .

Because the BDC operates just as the current flows inversely, but the voltage polarity remains unchanged, so the design parameters of all components of step-down mode can be employed in the step-up mode.

## 4. Experimental Results

A 3 kW prototype, as shown in Fig. 7, was built and tested to evaluate the performance of the proposed BDC. The experimental parameters and circuit components are given in Table 1. The experimental waveforms of step-down and step-up modes are shown in Fig. 8 to Fig. 13.

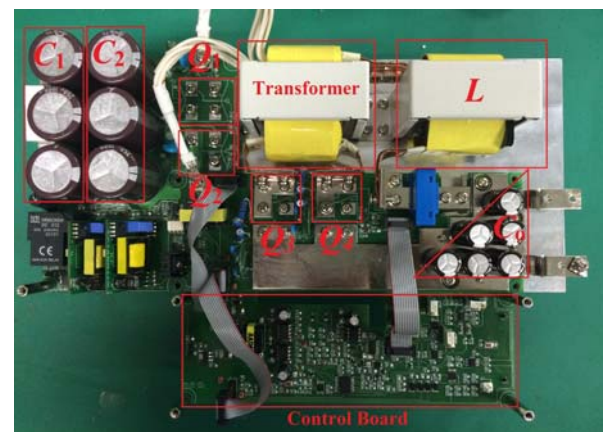


Fig. 7. Detailed photograph of the 3 kW proposed BDC

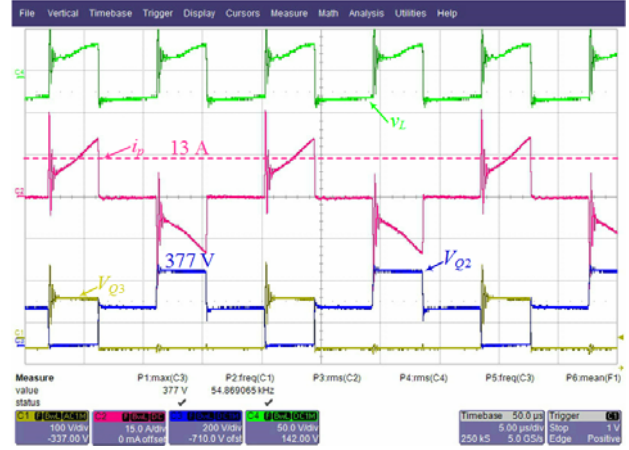
Fig. 8 shows the voltage across two switches  $Q_1$  and  $Q_4$ , which is  $V_{Q1}$  and  $V_{Q4}$ , respectively, and the input and the output voltage  $V_H$  of 380 V and  $V_L$  of 29.6 V at light load. One can see that the voltage stress on switch  $Q_1$  is equal to  $V_H$ , and that on switch  $Q_4$  is equal to  $V_H/N$ . The output

voltage  $V_L$  is well regulated at 29 V. In this situation, the duty ratio of switches  $Q_1$  and  $Q_2$  is 23.4%.

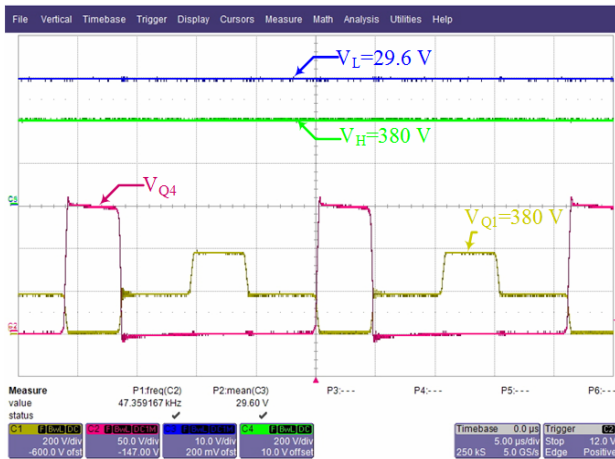
Fig. 9 shows the inductor current  $i_L$  and the switch

**Table 1.** Experimental parameters

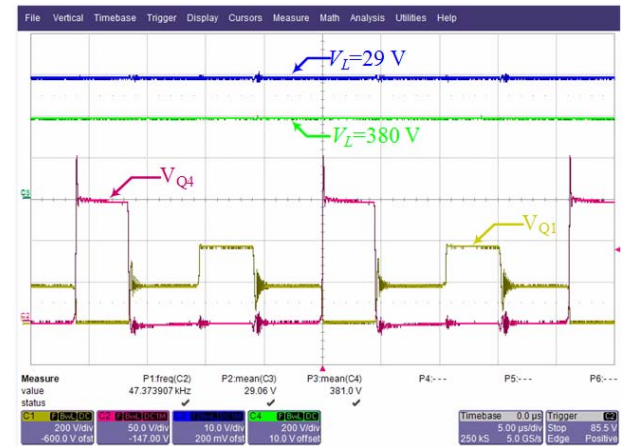
Parameters	Value
$C_1$ & $C_2$	1000 $\mu$ F/250 V $\times$ 3 in parallel
$C_o$	1000 $\mu$ F/50 V $\times$ 6 in parallel
$Q_1$ & $Q_2$	IXFN60N80P
$Q_3$ & $Q_4$	IXFN210N30P3
$L$	10 $\mu$ H
Switching Frequency	50 kHz
Max: Output Power	3 kW
$R_3, R_4$	8 $\Omega$
$C_3, C_4$	103 k/1 kV
Transformer para:	
$N_1$	7.5
$N_2$ & $N_3$	2.5
$l_{k1}/l_{m1}$	28 $\mu$ H/0.5 mH= 0.56%
$l_{k2}$ or $l_{k3}/l_{m2}$ or $l_{m3}$	1.2 $\mu$ H/55 $\mu$ H= 2.1%



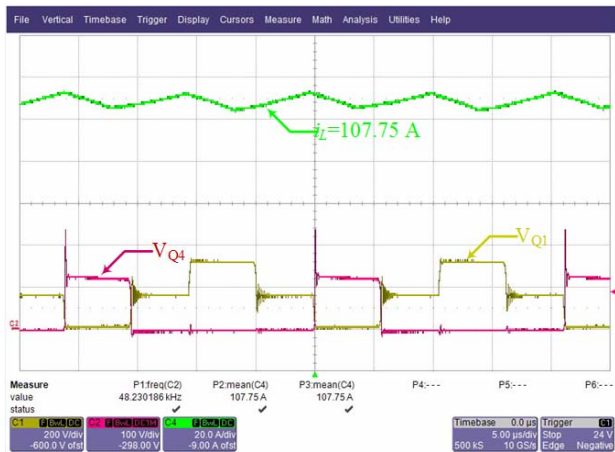
**Fig. 10.** Step-down mode experimental waveforms at 1 kW



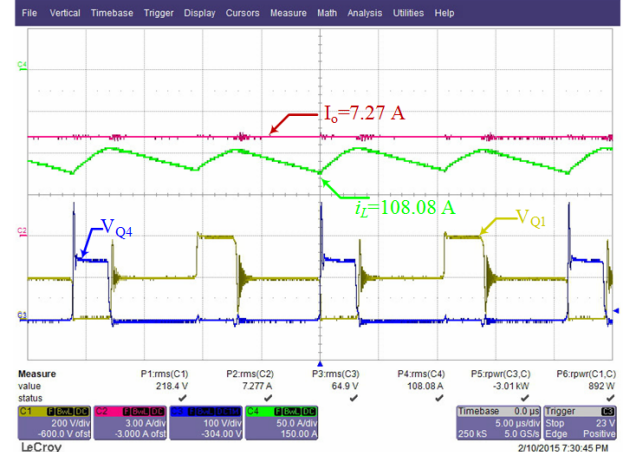
**Fig. 8.** Step-down mode experimental waveforms at light load



**Fig. 11.** Step-up mode experimental waveforms at light load



**Fig. 9.** Step-down mode experimental waveforms at full load



**Fig. 12.** Step-up mode experimental waveforms at full load

voltages  $V_{Q1}$  and  $V_{Q4}$  at full load. It can be seen that the average output current  $i_{L,Av}$  is 107.75 A, achieving 3.1 kW output power.

Fig. 10 shows the step-down 1 kW experimental waveforms. Channel 1 and channel 3 show the drain-to-source voltage  $V_{Q3}$  and  $V_{Q2}$ . The input voltage can be seen from the maximum value of  $V_{Q2(max)}$  as 377 V and the output voltage is 29 V. In this situation the duty ratio of  $Q_1$  and  $Q_2$  is about 23.1%. Channel 2 shows transformer primary side current which changes the direction accordingly when  $Q_1$  or  $Q_2$  are turned on. The average value of every conduction period is

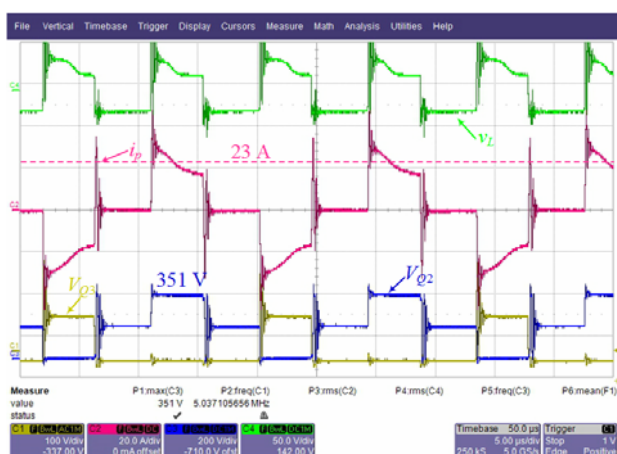


Fig. 13. Step-up mode experimental waveforms at 2 kW

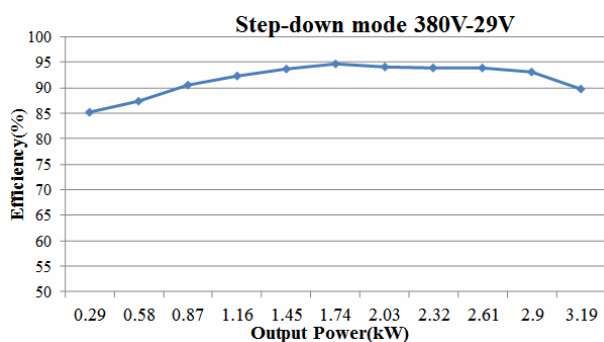


Fig. 14. System efficiency in step-down mode

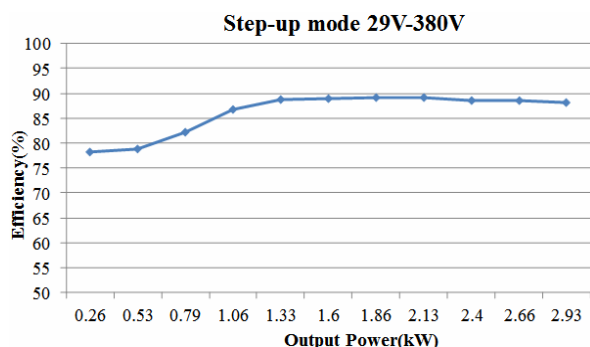


Fig. 15. System efficiency in step-up mode

about 13 A. Channel 4 shows the voltage across  $L$ .

Fig. 11 shows  $V_{Q1}$ ,  $V_{Q4}$ ,  $V_L$  and  $V_H$  for the step-up mode at light loads. It should be noted that the output voltage is well regulated at 380 V, and the maximum voltage on switch  $Q_1$  is equal to  $V_H$  and that on switch  $Q_4$  is  $V_H/N$ . In this situation, the duty ratio of  $Q_3$  and  $Q_4$  is 77.2%.

Fig. 12 shows the average input current of -108.08 A, output current of 7.26 A, and the voltage across switches  $Q_1$  and  $Q_4$  at full load conditions. The input and output power obtained are 3.13 kW and 2.76 kW, respectively.

Fig. 13 shows the step up mode 2 kW experimental waveforms. The input voltage is 29 V and the output voltage can be seen from  $V_{Q2(max)}$  as 351 V. In this situation the duty ratio of  $Q_3$  and  $Q_4$  is about 75.2%. Channel 2 shows transformer primary side current  $i_p$  with the average value of every conduction period about 23 A. Channel 4 shows the voltage across the inductor  $L$ .

Fig. 14 shows the measured efficiencies of the proposed BDC when it operates in step-down mode. The converter achieves efficiency of higher than 90% from 30% to full load.

Fig. 15 shows the measured efficiencies of the proposed converter when it operates in step-up mode. It can be seen that more than 88% of the efficiency is achieved from 30% to full load.

## 5. Conclusion

A 3 kW BDC for EVs is proposed in this paper. With a simple topology structure, the converter consists of a half-bridge on the primary side and a synchronous rectifier on the secondary side. Four switches are employed in both the step-down mode and step-up mode. The theoretical analyses have been proved by the experimental results of the 3 kW prototype circuit. When operating in step-down mode, an efficiency was achieved of more than 90% from 30% to the full load, while an efficiency of 88.2% is achieved at full load for the step-up mode.

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