

## Research Paper

# Electronic Structure of Ce-doped ZrO<sub>2</sub> Film: Study of DFT Calculation and Photoelectron Spectroscopy

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**Abstract** In this study, we evaluated the change of electronic structure during redox process in cerium-doped ZrO<sub>2</sub> grown by sol gel method. By sol-gel method, we could obtain cerium-doped ZrO<sub>2</sub> in high oxygen partial pressure and low temperature. After post annealing process in nitrogen ambient, the film is deoxidized. We used spectroscopic and theoretical methods to analysis change of electronic structure. X-ray absorption spectroscopy (XAS) for O K1-edge and Density Functional Theory (DFT) calculation using VASP code were performed to verify the electronic structure of the film. Also, high resolution x-ray photoelectron spectroscopy (HRXPS) for Ce 3d was carried out to confirm chemical bond of cerium doped ZrO<sub>2</sub>. Through the investigation of the electronic structure, we verified as followings. (1) During reduction process, binding energy of oxygen is increase. Simultaneously, oxidation state of cerium was change to 4+ to 3+. (2) Cerium 4+ and cerium 3+ states were generated at different energy level. (3) Absorption states in O K edge were mainly originated by Ce 4+ f<sub>0</sub> and Ce 3+, while occupied states in valance band were mainly originated from Ce 4+ f<sub>2</sub>.

**Keywords:** Electronic structure, Ce-doped ZrO<sub>2</sub>, DFT Calculation, XPS, XAS

## I. Introduction

Cerium doped ZrO<sub>2</sub> that generally called CSZ (cerium stabilized zirconium oxide), is used for several purposes related reduction process, such as oxygen reservoir and ionic conductor [1,2]. The chemical properties of cerium which has two oxidation states 3+ and 4+, makes it possible that large amount of reduction process [3]. When oxygen partial pressure is high, cerium are fully oxidized and become 4+ states. On the other hands, when oxygen partial pressure is low, cerium is deoxidized and become 3+ states. Therefore, cerium-doped ZrO<sub>2</sub> can store oxygen by change of partial pressure of oxygen or conduction of oxygen ion. Since application area of cerium-doped ZrO<sub>2</sub> is closely related with its chemical state, chemical property of cerium-doped ZrO<sub>2</sub> is intensively researched in many paper [4-6]. These researches are focus on chemical states of cerium with oxygen composition change or oxygen stores capacity. On the other hands, researches of electronic structure of cerium-doped ZrO<sub>2</sub> are relatively deficient, in spite of its interesting properties such as cerium f-orbital and various oxidation states. Therefore, in this study, we evaluated the electronic structure of cerium-doped ZrO<sub>2</sub> by combined spectroscopic and theoretical methods. Also,

high resolution x-ray photoelectron spectroscopy (HRXPS) was carried out to confirm chemical bond of cerium-doped ZrO<sub>2</sub>. Highly oxidized sample was prepared by sol-gel method in low temperature (300°C) and atmosphere pressure. Then post annealing at 700°C in nitrogen ambient was performed to deoxidize sample. We choose doping level of cerium 10% because significant change in crystal structure of ZrO<sub>2</sub> is not introduced. Therefore, effect of cerium reduction can be separated from the change in crystal structure. At the same time, 10% of cerium is enough portions to observe the modulation in electronic structure without structural change using spectroscopy method.

We observed two gap states at below conduction band edge in XAS spectrum. These intensities are modulated with change in oxidant state of cerium. Calculated electronic structure by DFT is support the experimental result which shows change in electronic structure during reduction process.

## II. Experiment

We deposited 5-nm-thick ZrO<sub>2</sub> and cerium-doped ZrO<sub>2</sub> films using sol-gel synthesis [7]. Zirconium-n-butoxide was used as a base solution for ZrO<sub>2</sub> and cerium-doped ZrO<sub>2</sub>. To incorporate cerium into the ZrO<sub>2</sub> film, approximately 10 mol % cerium nitrate hexahydrate was added to the base solution. Acetic acid and nitric acid were

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used as the chelating agent and catalyst, respectively. Cerium nitrate hexahydrate was added to zirconium-n-butoxide, and the mixture was stirred for 3 hours to obtain a completely mixed solution. The sol was placed on the silicon substrate using a spin coater, and subsequently heated to 100°C. Finally, the sample was heated to 300°C in air to finalize the film synthesis. To modulate oxidation states of samples by redox, both films were annealed at 700°C under ambient nitrogen for 2 minutes.

XAS was performed to confirm the electronic structures of the ZrO<sub>2</sub> and cerium-doped ZrO<sub>2</sub> films using the synchrotron 8A1 beam line in Korea. The absorption spectra of O K<sub>1</sub>-edge at photon energies ranging from 520 to 560 eV was measured using the total electron yield mode in the normal direction. Since metal oxides hybridize with oxygen 2*p* and 2*s*-orbitals, the O K<sub>1</sub>-edge spectrum represents the electronic structure of the hybridized orbital. [8]. XAS spectrums are deconvoluted by Gaussian peaks. The number of peaks was determined via crystal field theory.

HRXPS was performed using a monochromatic Al K $\alpha$  X-ray source (1486.6 eV) to verify the chemical bonding of cerium-doped ZrO<sub>2</sub>. Spectra were obtained for the chemical bonding states, including oxygen 1*s*, zirconium 3*d* and cerium 3*d*. All spectra were corrected to eliminate the charging effect using the carbon 1*s* peak at 285.0 eV. The background was removed using a Shirley-type subtraction, and the full-width at half maximum (FWHM) values of the constituent peaks were kept constant. Fitting curves were determined using Gaussian and Lorentzian distributions, in which the Gaussian distribution ratio was higher than 80%.

To verify origin of gap states that generated by Ce doping in ZrO<sub>2</sub>, we performed DFT calculation. In our calculation, we used VASP code [9] with GGA PBESol [10] functional. We geometry optimized the monoclinic and tetragonal ZrO<sub>2</sub> structure with under 0.25/Å k-spacing. Although the crystal structure of the as-grown films is amorphous, the atomic structure of the as-grown films was considered to be monoclinic. Considering that the amorphous structure in the DFT calculation requires a large unit cell that consumes computational time, the monoclinic and tetragonal ZrO<sub>2</sub> unit cell structure was geometrically optimized for both lattice parameter and atomic position, with a 6×6×6 k-point set and a 500-eV cut-off energy. For both unit cells, the initial structure followed those observed in the experimental results. Structure is relaxed until 0.02 eV/Å condition is satisfied. After geometry optimize, we build 2×2×2 supercell for monoclinic structure and 3×3×2 supercell for tetragonal to prevent mirror charge effect. Then we change one Zirconium to Cerium. Monoclinic structure system contains 31 Zirconium 1 Cerium and 64 oxygen. Tetragonal structure system contains 35 Zirconium 1 Cerium and 72 oxygen. For supercell calculation we choose 3×3×3 k-points. From XPS results, we made Ce 3+ by eliminate

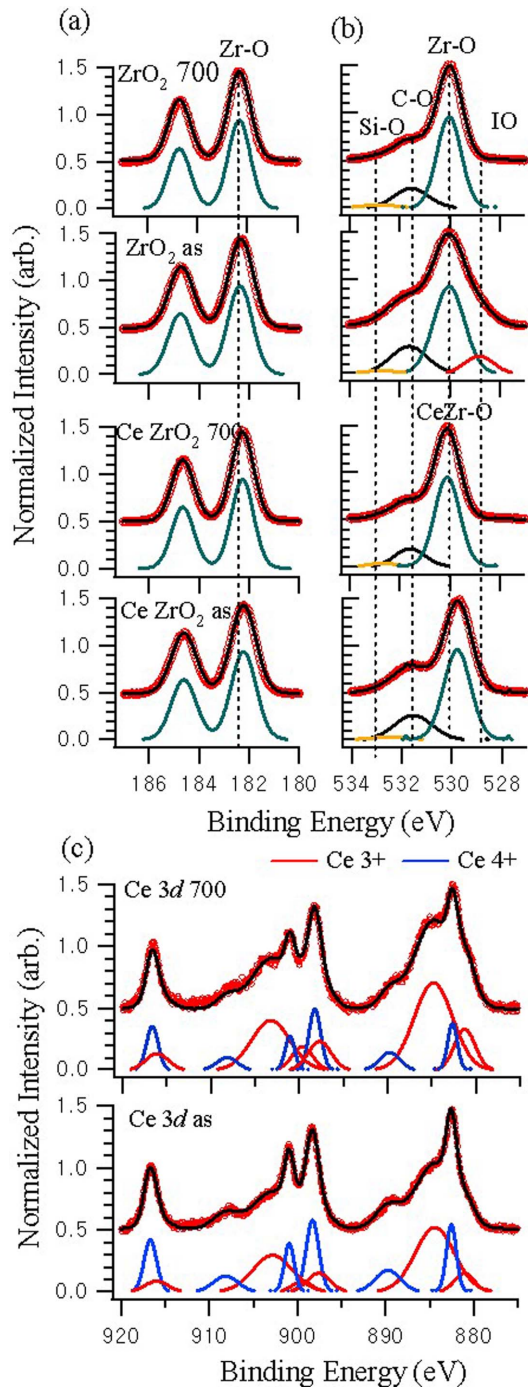
oxygen near doped Ce. Also, to simulate *f*<sub>0</sub>, *f*<sub>1</sub> and *f*<sub>2</sub> states of Ce, we introduced 0, 1, 2 electrons in systems. Therefore, we present density of states for Ce 4+ *f*<sub>0</sub>, *f*<sub>1</sub> and *f*<sub>2</sub> in monoclinic and tetragonal structure. In addition, density of states by Ce 3+ with 3-fold oxygen vacancy and 4-fold oxygen for monoclinic structure and Ce 3+ with oxygen vacancy for tetragonal structure are presented.

### III. Result and Discussion

#### 1. High resolution x-ray photoelectron spectroscopy (HRXPS)

Figure 1 represents zirconium 3*d* at a) and oxygen 1*s* at b) spectrum of XPS. In both as grown and annealed ZrO<sub>2</sub>, a very clear and sharp zirconium 3*d* spectrum without any shoulder and broadness is obtained. The binding energy of peak is 182.3 eV, which is well consistent with reported values for zirconium oxide [11]. The spectrum can be deconvoluted by only one sub-peak that spin orbit splitting is 2.4 eV. The bonding characteristic of cerium doped ZrO<sub>2</sub> is nearly same with the pure ZrO<sub>2</sub>, as shown in the zirconium 3*d* spectrum. On the other hands, binding properties of oxygen in pure ZrO<sub>2</sub> are significantly different from that of the cerium doped ZrO<sub>2</sub>, as shown at oxygen 1*s* spectra. The oxygen 1*s* spectrum for as-grown ZrO<sub>2</sub> can be deconvoluted with four sub-peaks, which are associated with oxygen interstitial (528.8 eV) ZrO<sub>2</sub> (530 eV), carbon oxide (531.6 eV) and silicon oxide (532.4 eV). In sol-gel method, ZrO<sub>2</sub> is synthesized in air under the high oxygen partial pressure. Accordingly, the ZrO<sub>2</sub> grown by sol-gel method can contain much interstitial oxygen [12]. In the as grown ZrO<sub>2</sub>, the excess oxygen is contributed to the weak bonding. Therefore, it can be interpreted that highly oxidized film is successfully achieved by sol-gel method. After post-annealing process at nitrogen ambient, the excess oxygen in ZrO<sub>2</sub> diffused out as O<sub>2</sub> gas or reacted with silicon substrate. The removal of excess oxygen can be confirmed by decrease of low binding energy peak of oxygen 1*s* spectrum. Reaction with silicon substrate can be also verified by increase of silicon oxide peak in oxygen 1*s* spectra, comparing the as-grown ZrO<sub>2</sub> and annealed ZrO<sub>2</sub>. Another important characteristic of ZrO<sub>2</sub> film grown by sol-gel method is that the peak with very high intensity caused by carbon oxide located at 531.6 eV is observed in both ZrO<sub>2</sub> and cerium-doped ZrO<sub>2</sub>. Although the peak located at 531.6 eV, shown at oxygen 1*s* spectra, can be caused by ZrO<sub>2-x</sub> or carbon oxide, it is more reasonable that the peak is resulted from the formation of carbon oxide because any ZrO<sub>2-x</sub> peaks are not observed in zirconium 3*d* spectrum. Large amount of carbon oxide is reasonable because the samples are synthesized using carbon based solution process by sol-gel method.

Ce doped ZrO<sub>2</sub> shows different behavior: i.e., there is no oxygen interstitial peak in both as-grown and annealed Ce doped ZrO<sub>2</sub>. Doping of lanthanides to ZrO<sub>2</sub> stabilize



**Figure 1.** XPS spectra for (a) Zr 3d spectra for annealed undoped ZrO<sub>2</sub>, as-grown un-doped ZrO<sub>2</sub>, annealed Ce-doped ZrO<sub>2</sub> and as-grown Ce-doped ZrO<sub>2</sub> (b) O 1s spectra for annealed un-doped ZrO<sub>2</sub>, as-grown un-doped ZrO<sub>2</sub>, annealed Ce-doped ZrO<sub>2</sub> and as-grown Ce-doped ZrO<sub>2</sub> (c) Ce 3d spectra for Ce-doped ZrO<sub>2</sub> for annealed Ce-doped ZrO<sub>2</sub> and as-grown Ce-doped ZrO<sub>2</sub>.

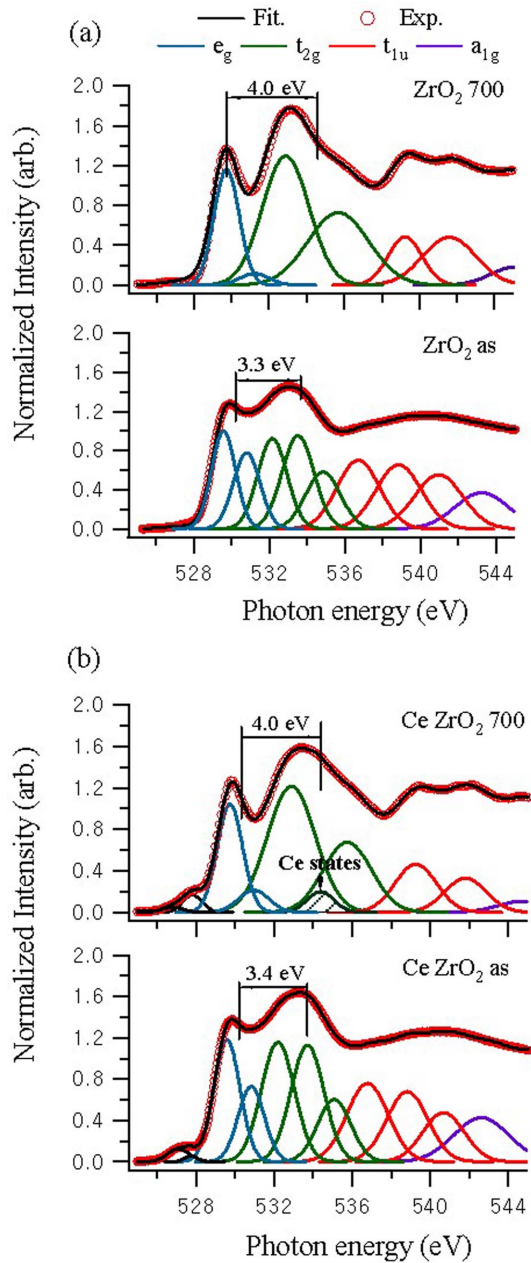
oxygen deficiency [13]. Therefore, doping of Ce increase formation energy for oxygen interstitial, which well explains the change in chemical state. After annealing process, binding energy of CeZr-O is shift to lower energy. This shift is larger than that of ZrO<sub>2</sub>. By Ce doping, change amount oxygen proportion become larger. This is possible due to transition of Ce oxidation states which is shown in

Fig 1(c) Ce 3d spectra.

Red colored peaks in Fig 1(c) are correlated to the chemical bonding states of cerium 3+. Blue colored peaks are associated with cerium 4+. Each bonding is deconvoluted with three peaks, which are originated from many body charge transfer effects of f-orbitals of cerium. Since f-orbital of cerium has two empty states at lower energy than its Fermi level, when core hole generated, electron is transferred to empty states and lower Fermi level in order to screen effect of core hole. Therefore cerium has three states in f-orbital as shown in XPS spectra which are non( $f_0$ ), one( $f_1$ ) and two( $f_2$ ) electron-occupied states. The shape of blue colored peaks in the XPS spectra is consistent to previously reported bond of cerium 4+: i.e.,  $f_0$ ,  $f_1$  and  $f_2$  peaks arise at 883.8 eV, 890.8 eV and 899.7 eV. The peak differences in  $\Delta f_0-f_1$  and  $\Delta f_1-f_2$  are 7.0 eV and 8.9 eV, respectively. The value of the spin-orbit splitting and its relative intensity is 18.4 eV and 0.73. In addition, red colored peaks are in accord with reported cerium spectra of cerium 3+: i.e.,  $f_0$ ,  $f_1$  and  $f_2$  peaks are observed at 882.2 eV, 886.1 eV and 898.6 eV, where  $\Delta f_0-f_1$  is 3.9 eV and  $\Delta f_1-f_2$  is 12.5 eV. The value of the spin-orbit splitting and relative intensity is 18.4 eV and 0.57. The relative intensity and the energy separation of the peaks are in good agreement with the reported result [14,15]. As shown in Fig 1(c), composition of Ce3+ and Ce4+ is dramatically changed after annealing process. When Ce doped ZrO<sub>2</sub> is highly oxidized, composition of Ce4+ is similar to composition of Ce3+. When film is deoxidized by annealing process, intensity of Ce4+ peaks is decreased while intensity of peaks is increased.

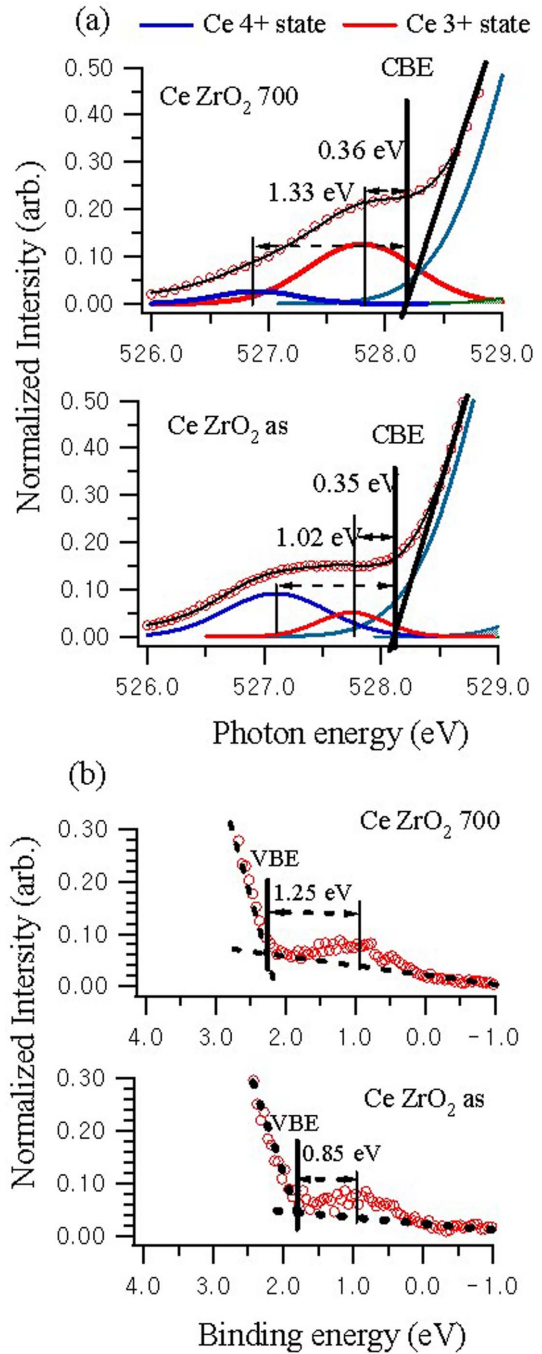
## 2. X-ray absorption spectroscopy (XAS)

Oxygen K-edge XAS spectra of as-grown and annealed ZrO<sub>2</sub> are shown in lower side of Fig. 2. XAS spectra represent the energy state in conduction band caused by the arrangement of oxygen around transition metal of metal oxide film. The first states denoted by  $e_g$  are lowest energy state in the conduction band owing to two-fold degeneration, which is associated with  $d_{x^2-y^2}$  and  $d_{z^2}$  component of oxygen position. The next states of  $t_{2g}$  are resulted from tri fold degeneration, which is related with  $d_{xy}$ ,  $d_{yz}$  and  $d_{zx}$ . The trifold degeneration also generates the third states of  $t_{1g}$  state, which is constituted by three degenerated states of  $p_x$ ,  $p_y$ , and  $p_z$ . The last states of  $a_{1g}$  are caused by s-orbital of transition metal, not degenerated states. In as-grown ZrO<sub>2</sub> spectrum in Fig. 2, the energy difference between two peaks of  $t_{2g}$  and  $e_g$ , about 3.2 eV, is caused by Crystal field splitting. The first peak of  $e_g$  can be deconvoluted into two peaks with the energy difference of 1.20 eV. The second peak of  $t_g$  can be also deconvoluted into three peaks which are separated by 1.3 eV and 1.4 eV. The increase in the energy difference between  $t_{2g}$  and  $e_g$  after the annealing treatment at 700°C can be closely related to Crystal field effect: i.e., the increase in the energy



**Figure 2.** XAS spectra for (a) annealed un-doped ZrO<sub>2</sub> and as-grown un-doped ZrO<sub>2</sub> (b) annealed Ce-doped ZrO<sub>2</sub> and annealed Ce-doped ZrO<sub>2</sub>.

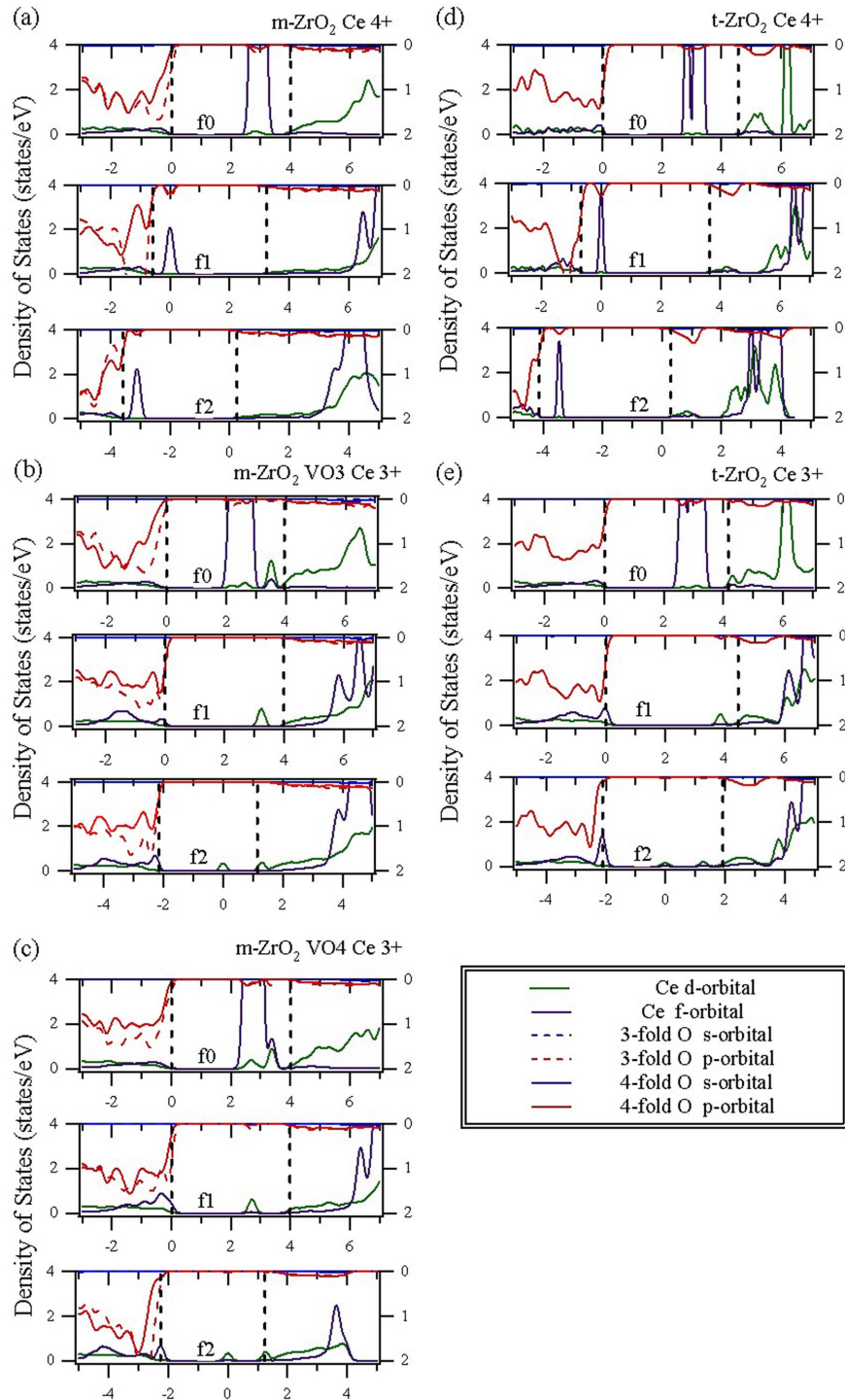
difference is enhanced as the crystal structure is changed to cubic-like structure. The peak splitting in  $t_{2g}$  and  $t_{1g}$  is caused by Jahn-Teller effect: i.e., since the degenerated states are changed from monoclinic to tetragonal structure, the 3 peak splitting in  $t_{2g}$  and  $t_{1g}$  is changed to 2 peak splitting. Thus degeneration of  $d_{zx}$  and  $d_{yz}$  is still remaining in tetragonal structure, resulting in deconvoluted two energy states with the energy difference of 2.9 eV. Similarly,  $t_{1u}$  state that consists with  $p_x$ ,  $p_y$  and  $p_z$ , can be deconvoluted into two peaks in tetragonal structure. Therefore, broken degenerations induce the change in the energy states: i.e., the 3 degenerated states are changed to 2 states, separated by  $d_{x^2-y^2}$  and  $d_{z^2}$  for  $e_{1g}$ ,  $d_{xy}$ ,  $d_{yz}$ , and  $d_{zx}$



**Figure 3.** (a) Pre-edge magnification of XAS spectra for annealed Ce-doped ZrO<sub>2</sub> and as-grown Ce-doped ZrO<sub>2</sub> (b) XPS Valence band spectra for Ce-doped ZrO<sub>2</sub> and as-grown Ce-doped ZrO<sub>2</sub>

for  $t_{2g}$ ,  $p_x$ ,  $p_y$ ,  $p_z$  for  $t_{1g}$  in tetragonal structure. Moreover, the increase in the energy difference between  $e_g$  and  $t_{2g}$  caused by Crystal field splitting can be clearly illustrated because the tetragonal structure is more cubical structure than monoclinic structure [16].

XAS spectra in 528 eV to 544 eV range for Ce doped ZrO<sub>2</sub> is similar to spectra of ZrO<sub>2</sub>. Peak position of each states almost same within 0.1 eV. This means similarity in crystal structure of ZrO<sub>2</sub> and Ce doped ZrO<sub>2</sub>. Considering that As-grown Ce doped ZrO<sub>2</sub> is monoclinic and annealed



**Figure 4.** Density of states for Ce and bonded oxygen (a) Ce 4+ of monoclinic Ce-ZrO<sub>2</sub> (b) Ce 3+ with 3-fold oxygen vacancy of monoclinic Ce-ZrO<sub>2</sub> (c) Ce 3+ with 4-fold oxygen vacancy of monoclinic Ce-ZrO<sub>2</sub> (d) Ce 4+ of tetragonal Ce-ZrO<sub>2</sub> (e) Ce 3+ with oxygen vacancy of tetragonal Ce-ZrO<sub>2</sub>.

ZrO<sub>2</sub> is tetragonal, small difference in spectra for this range is originated from Ce-O hybridized state. Since amount of this states is  $\sim 1/10$ , comparing with Zr-O hybridization states, it is hard to deconvolute the peak in as-grown film. When film is annealed only, one Ce states is deconvoluted in  $t_{2g}$  states. On the other hands, pre-edge absorption of Ce doped ZrO<sub>2</sub> is totally different from pre-edge absorption of ZrO<sub>2</sub>. Although there is no observable pre-edge absorption both as-grown and annealed ZrO<sub>2</sub>, large pre-edge

absorption for Ce doped ZrO<sub>2</sub> is observed. In Fig 3(a), XAS pre-edge absorption states for Ce-doped ZrO<sub>2</sub> are presented. By Ce doping, two states is generated at 0.35 eV and 1.02 eV from conduction band edge (CBE). Absorption intensity of states which is located at 1.02 eV from CBE is larger than that of states located at 0.36 eV from CBE. When film is annealed, position and relative intensity of absorption is changed: i.e., peak positions of the two states are shifted to 1.33 eV and 0.36 eV from

CBE. Relative absorption intensity of closer from CBE become larger. XPS Ce 3d spectra result which shows change in oxidation states Ce 4+ to Ce 3+ imply that two pre-edge states is originated from different oxidized Ce. For annealed tetragonal structure, Ce 3+ is generated closer from CBE state and Ce 4+ is generated far from CBE state. For monoclinic structure, by DFT calculation result, we conclude that absorption peak located at 1.03 eV from CBE is caused by Ce 3+ with four-fold oxygen vacancy and Ce 4+. While absorption peak at 0.35 eV from CBE is originated from Ce 3+ with three-fold oxygen vacancy. In order to measure the occupied chemical state of the ZrO<sub>2</sub> film, XPS valance band spectra was obtained, as shown in Fig 3(b). In as-grown Ce-doped ZrO<sub>2</sub> film, there is one peak exist at 0.85 eV from valance band edge (VBE). When sample is annealed, this peak shift to 1.25 eV from VBE. Not like unoccupied states in XAS spectra, gap state cannot be deconvoluted to two peaks. With DFT calculation, we verified that occupied state contains only Ce 4+ originated state.

### 3. DFT Calculation

In monoclinic structure, Ce 4+ generates unoccupied states at 1.0 eV from CBE when Ce 4+ is  $f_0$  state. Ce 4+ also generate occupied state at 0.3 eV from VBE when Ce 4+ is  $f_2$  state. These states shift by crystal structure change to tetragonal. Unoccupied Ce 4+  $f_0$  state is located at 1.2 eV from CBE. Occupied Ce 4+  $f_2$  state is located at 0.3 eV from 0.5 eV. In monoclinic structure, two kind oxygen exist; ie 3-fold oxygen and 4-fold oxygen. Absence of 3-fold or 4-fold oxygen generate different gap-state. Ce 3+  $f_1$  with 3-fold oxygen vacancy generates some states at 0.5 eV from CBE. Ce 3+  $f_1$  with 4-fold oxygen vacancy generate a state at 1eV from CBE which is overwrapped with Ce 4+  $f_0$  state. Therefore, Ce 3+ state with 4-fold oxygen vacancy can't be deconvoluted from Ce 4+  $f_0$  state in experiment. In tetragonal structure there is only one kind oxygen state: i.e., Ce 3+  $f_1$  with oxygen vacancy generates a state at 0.5 eV from CBE.

This result is consistent with the observed XAS and XPS result. By annealing process, crystal structure is changed from monoclinic to tetragonal. At the same time, state located at far from CBE is shifted 1.02 eV to 1.33 eV. State which is located at 0.35 eV from CBE is not shift. Gap state in XPS valance band spectrum is also shift from 0.85 eV to 1.25 eV with the transformation of crystal structure. Although, exact states position are different by DFT error for transition metal, the peak change in experimental data ca be well described by calculation result.

## IV. Conclusions

In this study, we observed the change in electronic structure

of Ce doped ZrO<sub>2</sub> with oxygen content change by annealing in nitrogen ambient. As-grown Ce doped ZrO<sub>2</sub> which is synthesized by sol-gel method in 300°C air, is monoclinic structure. After annealing process crystal structure changed to tetragonal. In XPS spectra, chemical shift of oxygen 1s ZrCe-O bond is occurred by deoxidation after the annealing process. At the same time, in Ce 3d spectra, transformation of Ce 4+ to Ce 3+ by deoxidation is observed. By Ce doping, gap states are generated, which is confirmed by XAS pre-edge absorption and XPS valance band spectra. Performing DFT calculation, we concluded that these states are originated from Ce 4+  $f_0$ ,  $f_2$  and Ce 3+  $f_1$ . Ce  $f_2$  generates occupied states, which is consistent with XPS valance spectra.

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