

# Secure Mobile Agents in eCommerce with Forward-Secure Undetachable Digital Signatures

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Yang Shi, Qinpei Zhao, and Qin Liu

**We introduce the idea of a forward-secure undetachable digital signature (FS-UDS) in this paper, which enables mobile agents to generate undetachable digital signatures with forward security of the original signer's signing key. The definition and security notion of an FS-UDS scheme are given. Then, the construction of a concrete FS-UDS scheme is proposed; and the proof of security for the proposed scheme is also provided. In the proposed scheme, mobile agents need not carry the signing key when they generate digital signatures on behalf of the original signer, so the signing key will not be compromised. At the same time, the encrypted function is combined with the original signer's requirement; therefore, misuse of the signing algorithm can be prevented. Furthermore, in the case where a hacker has accessed the signing key of the original signer, he/she is not able to forge a signature for any time period prior to when the key was obtained.**

**Keywords:** Mobile agents, forward-secure, undetachable digital signatures.

## I. Introduction

With the fast development of distributed computing technologies, mobile agent systems and related technologies have attracted great interest. A mobile agent system consists primarily of *mobile agents* and *platforms*. An *agent* is a type of computer software that acts autonomously on behalf of a person or an organization [1].

Platforms that can create, execute, interpret, transfer, and terminate agents are *agent systems*. Mobile agents have a high mobility to transport themselves from one platform in a network to another and can automatically suspend execution on one platform and migrate to another to resume their computations. The ability to travel enables a mobile agent to move to a destination agent system that contains an entity in which the agent wants to interact.

The advent of electronic commerce practices has increased the demand for interoperable applications that allow for the flexible exchange of data across enterprise borders, different IT-platforms, and different information systems. For example, an intelligent trade agent (ITA) that roams a network [2] buying and selling goods through three different merchant's hosts within a network is shown in Fig. 1. Moreover, many mobile agent-based technologies have been developed and put into practice, such as those in [3]–[8].

The aforementioned applications cannot be realized securely without suitable security technologies. However, the fact is that mobile agents are exposed to serious security threats; for example, malicious hosts might endanger passing mobile agents. As security threats have become a bottleneck in the development and maintenance of mobile agent-based applications [9], there has become an urgent calling for efficient and practical security solutions that can achieve a good

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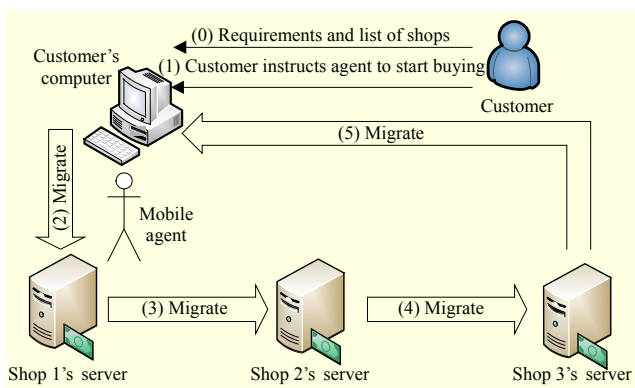


Fig. 1. ITA roams network buying and selling goods.

balance between security and mobility in mobile agent-related studies.

Security problems of mobile agent systems stemming from the mobility of mobile agents can be categorized into the following two subjects [10]: agent-side security and platform-side security. This study focuses on agent-side security and aims to provide a practical security solution under mobility. Furthermore, the study addresses the worst situation of agent-side threats when the agents run in an untrusting environment or, more specifically, the agents are subject to attacks from malicious platforms. Because mobile agents frequently migrate among various hosts (platforms<sup>1)</sup>) due to their mobility, they run the risk of exposing themselves to untrusting environments more often than static agents. In such environments, the proposed forward-secure undetachable digital signature technique can provide the integrity and validity of business contracts, as well as safeguarding the confidentiality of the user's private signing key.

## II. Mobile Agent Security and Undetachable Digital Signatures

The protection of a mobile agent from possible attacks by malicious hosts is referred to as the problem of malicious hosts. Hohl [11] identified a considerable number of such attacks including spying out code, data, and control flow; manipulation of code, data, and control flow and so on. Thus, threats from potentially malicious hosts have become a great obstacle to the widespread deployment of mobile agent technology-based applications in electronic commerce.

In traditional digital signature schemes, mobile agents need to carry the implementation of the signing algorithm with the private key to generate signatures on behalf of the original user,

<sup>1)</sup> In the study, host and platform are used interchangeably to refer a place where mobile agents operate.

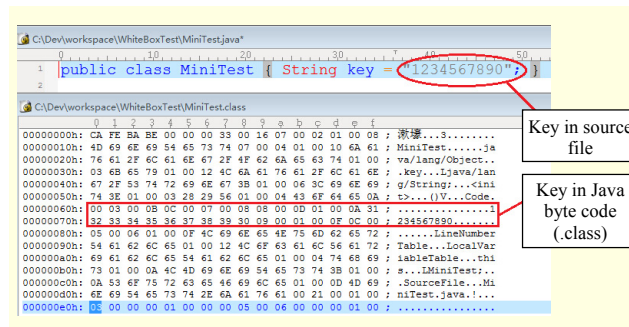


Fig. 2. Segment of Java byte code of agent.

so an adversary can misuse the signing algorithm or even extract the private signing key from the agent. For example, an attacker who has control of a malicious host can find the signing key from Java byte code, as illustrated in Fig. 2 (that is, a screen snapshot of a Hex file editor).

Hence, Sander and Tschudin proposed the idea of undetachable digital signatures [12], which allows a mobile agent to effectively produce a digital signature inside a remote and possibly malicious host without the host being able to deduce the agent's secret (for example, the signing key) or reuse the implementation of the signing algorithm for arbitrary documents.

The general mathematical description of an undetachable signature function is as follows. Suppose that  $Sig$  is the signing algorithm used by  $C$  (a customer) to produce the digital signature  $z = Sig(m)$  for an arbitrary message  $m$ . The undetachable signing algorithm  $f_{Signed}$  should subject to (1), where  $f$  is an auxiliary binding function.

$$f_{Signed} = Sig \circ f. \quad (1)$$

To create an undetachable signature on a shop's server, (2) is computed by calling  $f_{Signed}$  from the customer's mobile agent.

$$z = f_{Signed}(m). \quad (2)$$

Although the signature function  $Sig$  is not known by others, everyone can verify the validity of message  $m$  by using a specialized verification algorithm.

Since the first concrete construction of an undetachable digital signature based on RSA [13] was published in 2001, a variety of undetachable signature schemes have been proposed [13]–[17]. The latest one to date, [18], is a threshold version using conic curves, which was proposed in 2013.

At the same time, digital signature schemes also face a significant key leakage problem on the original signer's local host, while undetachable signatures only protect the signing key from leakage on potentially malicious remote hosts. In the event that the customer's host is infiltrated by an attacker, there would be a serious security problem because the original

private signing key would be compromised.

The possibility of the occurrence of this security problem increases with the fast development of advanced persistent threats (APTs), such as “Operation Aurora” and “Stuxnet Worm.”

Intuitively, a forward-secure signature technique could be used to control this risk. The principles behind forward-secure signature schemes are discussed briefly in [19]–[21]. In these schemes, the whole lifetime of a cryptosystem is divided into a number of time periods. At the end of each time period, the user computes a new signing key for the next time period using a one-way function and the old key is then erased. In this way, the user’s signing key changes for different time periods, but the public key (verification key) is fixed during the whole lifetime. Each signature is associated with one time period, and the validity of a time period needs to be verified during signature verification. As a result, an adversary cannot forge any signature of any time period prior to the time when they obtained the signing key (for example, via cracking the host of the signer).

Traditional undetachable signature techniques (for example, [13]–[18]) mainly focus on protecting the signing key from being compromised, as well as preventing the misuse of the signature function/algorithm on malicious shop servers. On the other hand, normal forward-secure signature schemes do not fulfill the undetachable property, which is required to sign a contract securely by using a mobile agent on remote and potentially malicious hosts.

To fix this gap, we introduce the idea of a forward-secure undetachable digital signature (FS-UDS). The definition and security notion of an FS-UDS are given. Then, the construction of a concrete FS-UDS is proposed. The proposed FS-UDS enables mobile agents to generate undetachable digital signatures with forward security of the original signer’s signing key. The main novelties of the scheme are as follows:

- It takes into account both the security of the customer’s host and the security of shop servers.
- It is the first undetachable digital signature scheme that supports forward-secure key evolution. Although there are many published forward-secure signature schemes, it is not a trivial work to design a scheme that fulfills the undetachable property given by equation (1).
- It is carefully designed such that the security of the scheme can be reduced to that of solving a hard mathematical problem (that is, the computational co-Diffie–Hellman problem on a co-GDH group pair).

To introduce the concrete scheme, we first give the formal definition and security notions of undetachable signature schemes in the next section. These are also contributions to theoretical aspects of mobile agent security.

### III. Definition and Security Notions

#### 1. Definition

In this section, the definition of an FS-UDS is proposed. Furthermore, the security notions of FS-UDS are given. Before the definition, we first list frequently used symbols in Table 1.

**Definition 1.** An FS-UDS  $FSUSig = (KGen, KUpd, Sign, Vrfy, UndSigFunGen, UndSig, UndVrfy)$  consists of the following seven algorithms:

- The key generation algorithm,  $KGen$ , takes as input a security parameter,  $1^k$ , where  $k \in \mathbb{N}$ ; the total number of periods  $T$  over which the scheme will operate; and possibly other parameters to return a base public key,  $U_0$ , and corresponding base secret key (signing key),  $s_0$ . The algorithm is probabilistic.
- The secret key update algorithm,  $KUpd$ , takes as input the secret signing key of the previous period,  $s_{j-1}$ , to return the secret signing key of the current period,  $s_j$ . The algorithm is usually deterministic.
- The undetachable signing function generation algorithm,  $UndSigFunGen$ , is a probabilistic polynomial-time algorithm, which takes the requirement of a customer,  $REQ_C$ ; the customer’s identity,  $ID_C$ ; and the customer’s public key and private key of the current period as inputs. The algorithm outputs a pair of functions,  $f(\cdot)$  and  $f_{Signed_j}(\cdot)$ .
- The undetachable signing algorithm,  $FSUndSig$ , is a polynomial-time algorithm, which takes the contract (or a relative hash value) as input. The algorithm outputs an undetachable digital signature  $z = \zeta_j = \langle \zeta, j \rangle$ .
- The undetachable signature verification algorithm,  $UndVrfy$ , is a polynomial-time algorithm, which takes the contract and an undetachable signature  $z$  as input. The algorithm outputs either “Accept” or “Reject,” simply “1” or “0.”
- The signing algorithm,  $Sign$ , takes the secret signing key of the current period,  $s_j$ , and a message,  $M$ , to return a signature of  $M$  for period  $j$ . We write this as  $\sigma_j \leftarrow Sign_{s_j}(M)$ . The algorithm might be probabilistic. The signature is always a pair consisting of the value  $j$  of the current period and a tag  $\sigma$ .
- The verification algorithm,  $Vrfy$ , takes the public key ( $PK$ ), message ( $M$ ), and candidate signature  $(\langle j, \sigma \rangle)$  to return a bit, with “1” meaning accept and “0” meaning reject. We write this as  $b \leftarrow Vrfy_{U_0}(M, \langle j, \sigma \rangle)$ .

#### 2. Security Notions

For the formalization of the security definition, we set up

Table 1. Frequently used symbols.

Symbol	Description
$1^k$	Security parameter, $k \in \mathbb{N}$
$U_0$	Base public key
$s_0$	Base secret key (signing key)
$j$	Index of the time period
$s_j/s_{j-1}$	Secret signing key of the time period $j/j-1$
$CERT_j$	Certification (of underlying public key) of the period $j$
$REQ\_C  ID_C$	Customer $C$ 's requirement and identity
$f_{Signed_j}$	Implementation of undetachable signing function of time period $j$
$f$	Auxiliary function of $f_{Signed_j}$
$Msg$	Message (usually a contract)
$Z$	Undetachable signature
$\sigma, \sigma_j$	Normal signatures

a fixed key-evolving undetachable signature scheme  $FSUSig = (KGen, KUpd, Sign, Vrfy, UndSigFunGen, UndSig, UndVrfy)$ . An adversary,  $F$ , is viewed as functioning in three stages — the chosen message attack and chosen restriction attack phase; the break-in phase (breakin); and the forgery phase (forge). Its success probability in breaking the forward-security of the undetachable signature scheme is evaluated by the following two experiments. Note that we write  $1^k, \dots, T$  as the arguments to the key generation algorithm to indicate the possible presence of extra arguments.

Experiment FU-ForgeSig( $FSUndSig, F, 1^k, \dots, T$ )

$(U_0, s_0) \xleftarrow{\$} KGen(1^k, \dots, T); j \leftarrow 0$

Repeat

$j \leftarrow j+1; s_j \leftarrow KUpd(s_{j-1})$

$d \leftarrow F^{Sign_{s_j}(\cdot), UndSigFunGen_{s_j}(\cdot)}(CMA - CRA, U_0)$

Until  $((d = breakin) \vee (j = T))$

If  $((d \neq breakin) \wedge (j = T)) \quad j \leftarrow T+1$

$(\langle \sigma, b \rangle, M) \leftarrow F(\text{forge}, s_j)$

If  $\left( \left( Vrfy_{U_0}(\langle \sigma, b \rangle, M) = 1 \right) \wedge (1 \leq b < j) \right) \wedge (M \notin L_b^{Sign}) \wedge (M \notin L_b^{UndSigFunGen})$  return 1

Else return 0

In the experiment FU-ForgeSig,  $L_b^{Sign}$  and  $L_b^{UndSigFunGen}$  are the query lists coming from the signing query  $Sign_{s_b}(\bullet)$  of period  $b$  and the undetachable signature function generation query  $UndSigFunGen_{s_b}(\bullet)$  of period  $b$ , respectively.

Experiment FU-ForgeUndSig( $FSUndSig, F, 1^k, \dots, T$ )

$(U_0, s_0) \xleftarrow{\$} KGen(1^k, \dots, T); j \leftarrow 0$

Repeat

$j \leftarrow j+1; s_j \leftarrow KUpd(s_{j-1})$

$d \leftarrow F^{Sign_{s_j}(\cdot), UndSigFunGen_{s_j}(\cdot)}(CMA - CRA, U_0)$

Until  $((d = breakin) \vee (j = T))$

If  $((d \neq breakin) \wedge (j = T)) \quad j \leftarrow T+1$

$(\langle \zeta, b \rangle, RES, M) \leftarrow F(\text{forge}, s_j)$

If  $\left( \left( UndVrfy_{U_0}(\langle \zeta, b \rangle, RES, M) = 1 \right) \wedge (1 \leq b < j) \right) \wedge (RES \notin T_b^{Sign}) \wedge (RES \notin T_b^{UndSigFunGen})$  return 1

Else return 0

In the experiment FU-ForgeUndSig,  $T_b^{Sign}$  and  $T_b^{UndSigFunGen}$  are the query lists coming from the signing query  $Sign_{s_b}(\bullet)$  of period  $b$  and the undetachable signature function generation query  $UndSigFunGen_{s_b}(\bullet)$  of period  $b$ , respectively.

**Remark 1.**  $RES$  is a restriction. It is usually in the form of  $REQ||ID_C$ , where  $REQ$  is the requirement of a customer ( $C$ ) and  $ID_C$  is the customer's identity.

**Definition 2.** The insecurity function of  $FSUndSig$  is defined as

$InSec(FSUndSig, 1^k, \dots, T; \tau, q_s, q_u) = \text{Max}_{F=\langle F_1, F_2 \rangle}$

$$\left\{ \Pr \left[ \left( 1 = \text{FU-ForgeSig}(FSUndSig, F_1, 1^k, \dots, T) \right) \vee \left( 1 = \text{FU-ForgeUndSig}(FSUndSig, F_2, 1^k, \dots, T) \right) \right] \right\} \quad (3)$$

The maximum here is over all  $F = \langle F_1, F_2 \rangle$  for which the following are true: the execution time of the above two experiments, plus the size of the code of  $F$ , is at most  $t$ ;  $F$  makes a total of at most  $q_s$  queries to the signing oracles and at most  $q_u$  queries to the undetachable signature function generation oracles across all the stages in all experiments.

**Remark 2.** The execution time is that of the entire experiment, not just that of  $F$ . So, it includes, in particular, the time to compute answers to oracle queries.

## IV. Concrete Construction

### 1. Public Setting

The public setting  $\Omega = (\mathbb{G}_1, \mathbb{G}_2, \hat{e}(\cdot, \cdot), q, P, H_1(\cdot), H_2(\cdot))$  consists of the following components and algorithms:

- $\mathbb{G}_1$  is a multiplicative cyclic group of prime order  $q$ ,  $\mathbb{G}_2$  is also a multiplicative cyclic group of the same order.
- $G$  and  $P$  are fixed generators of  $\mathbb{G}_1$  and  $\mathbb{G}_2$ , respectively.

- $\hat{e}: \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_T$  is a bilinear map.
- $H_1: \{0,1\}^* \rightarrow Z_q^*$  and  $H_2: \{0,1\}^* \rightarrow \mathbb{G}_1$  are two specialized hash maps.

**Remark 3.** We suppose that there exists an isomorphism  $\psi: \mathbb{G}_2 \rightarrow \mathbb{G}_1$  with  $\psi(P) = G$ .

## 2. Mathematical Problems and Computational Assumptions

**Definition 3.** Decision co-Diffie–Hellman (co-DDH) problem on  $(\mathbb{G}_1, \mathbb{G}_2)$ : Given  $P, P^a \in \mathbb{G}_2$  and  $Y, Y^b \in \mathbb{G}_1$  as input, the solution of the problem is “yes” if  $a = b$ , otherwise it is “no.” Note that when the solution is “yes,” we say that  $(P, P^a, Y, Y^b)$  is a co-Diffie–Hellman tuple (co-DHT).

**Assumption 1.** We suppose that  $\hat{e}$  can be effectively computed, so the co-DDH problem on  $(\mathbb{G}_1, \mathbb{G}_2)$  is easy to solve.

**Definition 4.** Computational co-Diffie–Hellman (co-CDH) problem on  $(\mathbb{G}_1, \mathbb{G}_2)$ : Given  $g_2, g_2^a \in \mathbb{G}_2$  and  $h \in \mathbb{G}_1$  as input, the solution of the problem is (to compute)  $h^a \in \mathbb{G}_1$ .

**Definition 5.** We say that an algorithm  $(t', \varepsilon')$ -breaks co-CDH on  $(\mathbb{G}_1, \mathbb{G}_2)$  if the algorithm runs in time (that is, within  $t'$ ) and successfully solves the co-CDH problem on  $(\mathbb{G}_1, \mathbb{G}_2)$  with a probability of at least  $\varepsilon'$ .

**Definition 6.** Two groups,  $(\mathbb{G}_1, \mathbb{G}_2)$ , are a  $(\lambda, t', \varepsilon')$  gap Diffie–Hellman group pair (co-GDH) if they satisfy the following properties:

- The group operation on both  $\mathbb{G}_1$  and  $\mathbb{G}_2$  and the map  $\psi$  from  $\mathbb{G}_2$  to  $\mathbb{G}_1$  can be computed in at most time  $\lambda$ .
- The co-DDH problem on  $(\mathbb{G}_1, \mathbb{G}_2)$  can be solved in at most time  $\lambda$ .
- No algorithm  $(t', \varepsilon')$  breaks the co-CDH problem on  $(\mathbb{G}_1, \mathbb{G}_2)$ .

**Assumption 2.** The two order- $q$  groups  $(\mathbb{G}_1, \mathbb{G}_2)$  in the public setting are a  $(\lambda, t', \varepsilon')$ -bilinear group pair; that is, they satisfy the following properties:

- The group operation on both  $\mathbb{G}_1$  and  $\mathbb{G}_2$  and the map  $\psi$  from  $\mathbb{G}_2$  to  $\mathbb{G}_1$  can be computed in at most time  $\lambda$ .
- A group  $\mathbb{G}_T$  of order  $q$  and a bilinear map  $\hat{e}: \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_T$  exist, and  $\hat{e}$  is computable in at most time  $\lambda$ .
- No algorithm  $(t', \varepsilon')$ -breaks the co-CDH problem on  $(\mathbb{G}_1, \mathbb{G}_2)$ .

Because we can efficiently solve the co-DDH problem by computing two bilinear maps, if two groups  $(\mathbb{G}_1, \mathbb{G}_2)$  are a  $(\lambda, t', \varepsilon')$ -bilinear group pair, then they are also a  $(2\lambda, t', \varepsilon')$ -co-GDH group pair.

Based on the above computational assumption, we propose a concrete and effective FS-UDS. The short signature scheme in

[22] and the forward-secure signatures generation technique in [23] are used as building blocks in the proposed scheme.

## 3. Algorithms

The proposed FS-UDS consists of seven algorithms; that is, *KGen*, *KUpd*, *UndSigFunGen*, *UndSig*, *UndVrfy*, *Sig*, and *Vrfy*, as follows:

**Algorithm. *KGen*** ( $1^k$ )

```

 $s_0 \xleftarrow{\$} Z_q^*; U_0 \leftarrow P^{s_0}$ 
For ( $j = 1; j \leq T; j++$ ) do
  ( $s_j \xleftarrow{\$} H_1(s_{j-1}); U_j \leftarrow P^{s_j}$ )
   $CERT_j \leftarrow \langle U_0, j, U_j, H_2(U_0, j, U_j)^{s_0} \rangle$ 
EndFor
erase  $s_j, j = 1, \dots, T$ ; store  $CERT_j, j = 1, \dots, T$ 
return  $\langle U_0, s_0 \rangle$ 

```

**Algorithm. *KUpd*** ( $s_{j-1}, CERT_j, j, U_0$ )

```

 $\langle U_0', j', U_j', \Lambda_j \rangle \leftarrow CERT_j; s_j \leftarrow H_1(s_{j-1}); U_j \leftarrow P^{s_j}$ 
If ( $\hat{e}(\Lambda_j, P) \neq \hat{e}(H_2(U_0, j, U_j), U_0)$ ) return  $\perp$ 
erase  $s_{j-1}$ 
return  $s_j$ 

```

**Algorithm. *UndSigFunGen*** ( $REQ\_C \parallel ID_C, sk_j, CERT_j$ )

```

 $H \leftarrow H_2(REQ\_C \parallel ID_C); K \leftarrow H^{sk_j}$ 
 $\sigma \leftarrow \langle CERT_j, \sigma' \rangle; \sigma_j \leftarrow \langle \sigma, j \rangle$ 
setup  $f(x) = H^x$   $f_{Signed_j}(x) = \langle \langle CERT_j, K^x \rangle, j \rangle$ 
return  $f(\cdot), f_{Signed_j}(\cdot)$ 

```

**Algorithm. *UndSig*** (*Msg*)

```

 $h = H_1(Msg);$  return  $f_{Signed_j}(h)$ 

```

**Algorithm. *UndVrfy*** ( $U_0, Z, j, Msg, REQ\_C \parallel ID_C$ )

```

 $\langle \langle CERT_j, Z' \rangle, j \rangle \leftarrow Z; \langle U_0', j', U_j', \Lambda_j \rangle \leftarrow CERT_j$ 
If ( $((U_0 \neq U_0') \vee (j \neq j'))$ ) return 0
If ( $Msg$  does not satisfy  $REQ\_C$ ) return 0
If ( $\hat{e}(\Lambda_j, P) \neq \hat{e}(H_2(U_0', j', U_j'), U_0)$ ) return 0
If ( $\hat{e}(Z', P) \neq \hat{e}(H_2(REQ\_C \parallel ID_C)^{H_1(Msg)}, U_j)$ ) return 0
else return 1

```

**Algorithm. *Sign*** ( $s_j, j, Msg$ )

```

 $\sigma' \leftarrow H_2(Msg)^{s_j}; \sigma \leftarrow \langle CERT_j, \sigma' \rangle; \sigma_j \leftarrow \langle \sigma, j \rangle$ 
return  $\sigma_j$ 

```

**Algorithm.**  $Vrfy(U_0, \sigma, j, Msg)$   
 $\langle CERT_j, \sigma' \rangle \leftarrow \sigma; \langle U_0', j', U_j', \Lambda_j \rangle \leftarrow CERT_j$   
 If  $((U_0 \neq U_0') \vee (j \neq j'))$  return 0  
 If  $(\hat{e}(\Lambda_j, P) \neq \hat{e}(H_2(U_0, j', U_j'), U_0))$  return 0  
 If  $(\hat{e}(\sigma', P) \neq \hat{e}(H_2(Msg), U_j))$  return 0  
 Else return 1

#### 4. Proof of Correctness

The following proposition shows that the proposed scheme is a “correct” FS-UDS scheme.

**Proposition 1.** Let  $Sig_{s_j, j}(x) = \langle \langle CERT_j, x^{s_j} \rangle, j \rangle$ , for each  $j \in \{1, 2, \dots, T\}$ , then the function pair  $f_{Signed_j}$  and  $f$  generated by  $UndSigFunGen$  satisfies (1).

**Proof.** For any  $j \in \{1, 2, \dots, T\}$ , we have

$$(Sig_{s_j, j} \circ f)(x) = Sig_{s_j, j}(H^x) = \langle \langle CERT_j, (H^x)^{s_j} \rangle, j \rangle \\ = \langle \langle CERT_j, (H^{s_j})^x \rangle, j \rangle = \langle \langle CERT_j, K^x \rangle, j \rangle = f_{Signed_j}(x).$$

It is not difficult to validate the correctness of  $UndVrfy$  and  $Vrfy$ , so we omit the proofs. ■

#### 5. Experimental Performance Analysis

We have implemented the algorithms in Java. Java has been used instead of C/C++ because many mobile agent platforms are developed in Java. An open-source Java Pairing-Based Cryptography Library (JPBC) [24] is used in our implementation. The performance is tested on both a portable PC and a server. The configurations of these platforms are listed in Table 2.

The performance results of the proposed algorithms on the platforms are listed in Table 3. The input and output sizes of the algorithms are also provided. Moreover, results of another undetectable digital signature scheme [16] without forward security is appended at the end of the table for comparison.

According to Table 3, all the algorithms in both schemes work fine on either a PC or a server. For algorithms that are frequently used in both schemes (that is,  $Sign$ ,  $Vrfy$ ,  $UndSigFunGen$ ,  $UndSig$ , and  $UndVrfy$ ), although the time and space cost of the proposed algorithms are a little more than the ones in [16], the largest difference is only 45 ms on time cost and 387 bytes on space cost. Importantly, the sacrifice of these small costs brings the forward-security. The new forward-secure signature scheme is capable of protecting the signing key in both the original signer’s host and the remote servers. As for the  $KeyGen$  algorithm, it is only used once for

each user in the initialization stage. Therefore, it brings little burden to the mobile agent system, even though the  $KeyGen$  algorithm needs more time than the one in [16].

#### 6. Theoretical Security Analysis

In this subsection, we prove the security of the proposed scheme based on Assumption 2. The co-CDH problem is computationally infeasible in many algebra structures, such as Weil pairings; so, Assumption 2 is widely used in security schemes. We use this assumption as a mathematical basis for the proposed FS-UDS scheme.

**Theorem 1.** Suppose that Assumption 2 is true, then for the proposed FS-UDS scheme, and for any  $\tau < t'$ , the insecurity function that is defined in (3) satisfies (4).

$$\text{InSec}(FSUndSig, 1^k, \dots, T; \tau, q_s, q_u) \\ \leq e(q_s^{(1)} + q_s^{(2)} + q_u^{(1)} + q_u^{(2)} + 1) \cdot \varepsilon'. \quad (3)$$

**Proof.** The first step of this proof is to adapt the forgery experiments to the proposed concrete construction as follows:

Table 2. Configurations of testing platforms.

Platform	CPU	RAM	OS	JDK
PC	1.7 G 2Cores	4 GB	Win7	7.0
Server	2.5 G 6Cores × 2	96 GB	WinServ2008	7.0

Table 3. Results of performance tests.

Algorithm		Time (ms)		Size (byte)	
		PC	Server	Input	Output
Ours	$KGen (T=10)$	663	610	2	148
	$KUpd$	66	65	534	20
	$Sign$	46	44	149	514
	$Vrfy$	101	101	771	1
	$UndSigFunGen$	46	43	535	642
	$UndSig$	15	13	128	514
	$UndVrfy$	115	114	901	1
[16]	$KGen$	17	15	2	148
	$Sign$	52	50	148	128
	$Vrfy$	57	56	384	1
	$UndSigFunGen$	56	51	150	256
	$UndSig$	16	15	128	128
	$UndVrfy$	76	72	514	1

Game  $FU\text{-ForgeSig}(FSUndSig[1^k, r, T], F_1)$ ,  
 $\langle U_0, s_0 \rangle \leftarrow KGen(1^k, r, T); j \leftarrow 0$   
Repeat  
 $j \leftarrow j+1; s_j \leftarrow KUpd(s_{j-1});$   
 $d \leftarrow F_1 \left[ \begin{array}{l} O^{FSUndSig.Sig_{s_j}(\cdot)} \\ O^{FSUndSig.UndSigFunGen_{s_j}(\cdot)} \end{array} \right] (CMA - CRA, U_0)$   
Until  $((d = \text{breakin}) \vee (j = T))$   
If  $((d \neq \text{breakin}) \wedge (j = T)) \quad j \leftarrow T+1$   
 $(\langle \sigma, b \rangle, M) \leftarrow F_1(\text{forge}, s_j)$

If  $\left( (FSUndSig.Vrfy(U_0, \langle \sigma, b \rangle, M) = 1) \wedge (1 \leq b < j) \wedge (M \notin L_b^{Sign}) \wedge (M \notin L_b^{UndSigFunGen}) \right)$  return 1  
Else return 0  
Game  $FU\text{-ForgeUndSig}(FSUndSig[1^k, r, T], F_2)$   
 $\langle U_0, s_0 \rangle \leftarrow KGen(1^k, r, T); j \leftarrow 0$   
Repeat  
 $j \leftarrow j+1; s_j \leftarrow KUpd(s_{j-1});$   
 $d \leftarrow F_2 \left[ \begin{array}{l} O^{FSUndSig.Sig_{s_j}(\cdot)} \\ O^{FSUndSig.UndSigFunGen_{s_j}(\cdot)} \end{array} \right] (CMA - CRA, U_0)$

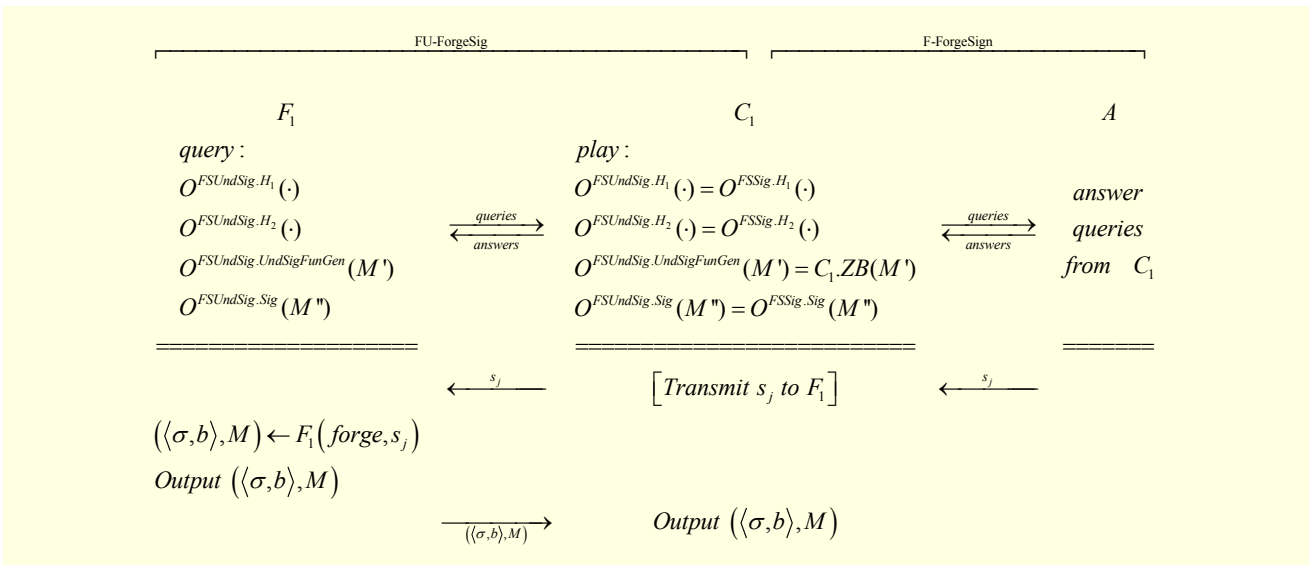


Fig. 3.  $C_1$  plays between  $F_1$  and  $A$ .

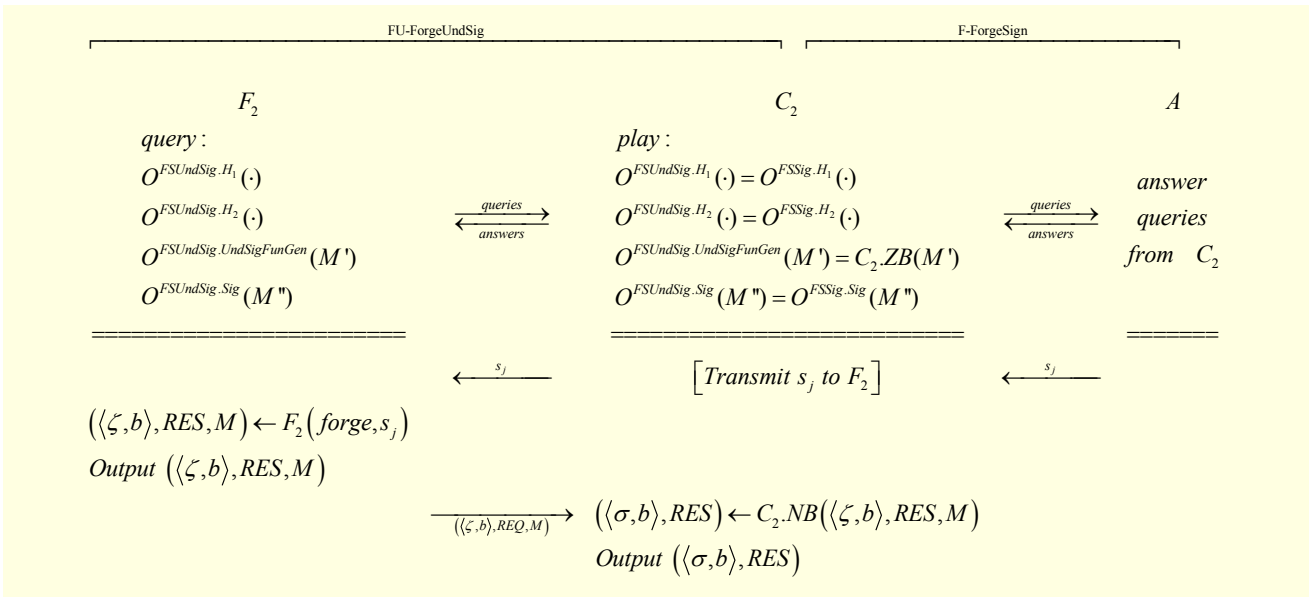


Fig. 4.  $C_2$  plays between  $F_2$  and  $A$ .

```

Until((d = breakin) ∨ (j = T))
If((d ≠ breakin) ∧ (j = T))  j ← T + 1
((ζ, b), RES, M) ← F2(forge, sj)
If(
  (UndVrfy(U0, ⟨ζ, b⟩, RES, M) = 1) ∧ (1 ≤ b < j)
  ∧ (RES ∉ TbSign) ∧ (RES ∉ TbUndSigFunGen)
) return 1
Else return 0

```

The second step proceeds with the help of some intermediate players and transitivity security games. An intermediate player  $C_1$  plays the game FU-ForgeSig with  $F_1$  as shown in the left part of Fig. 3 and plays the game F-ForgeSig with another intermediate player  $A$  as shown in the right part of Fig. 3. Similarly, an intermediate  $C_2$  plays the game FU-ForgeUndSig with  $F_1$  as shown in the left part of Fig. 4 and plays the game F-ForgeSig with another intermediate player  $A$  as shown in the right part of Fig. 4.

As shown in Figs. 3 and 4, the intermediate players  $C_1$  and  $C_2$  have some algorithms that help them to play the games. The descriptions of these algorithms are as follows:

**Algorithm.**  $C_2.NB(\langle \zeta, b \rangle, RES, M)$   
 $\langle \langle CERT_j, \zeta^1 \rangle, j \rangle \leftarrow \zeta; h \leftarrow O^{H_1}(M);$   
 $\sigma \leftarrow \langle \langle CERT_j, h^{-1} \cdot \zeta^1 \rangle, j \rangle$   
 return  $(\langle \sigma, b \rangle, RES)$

**Algorithm.**  $C_i.ZB(RES, sk_j, CERT_j) \quad i = 1, 2$   
 $H \leftarrow O^{FSSig.H_2}(RES); \Delta \leftarrow O^{FSSig.Sig}(RES);$   
 $\langle CERT_j, K, j \rangle \leftarrow \Delta$   
 setup  $f(x) = H^x \quad f_{Signed}(x) = \langle \langle CERT_j, K^x \rangle, j \rangle$   
 return  $f(\cdot), f_{Signed}(\cdot)$

Moreover, the game F-ForgeSign is the normal security game that is widely used in the research of forward-secure signature schemes. F-ForgeSign proceeds as follows:

```

Game F-ForgeSign(FSSig[1k, r, T], Ci) // i = 1, 2
⟨U0, s0⟩ ← FSSig.KGen(1k, r, T); j ← 0
Repeat
  j ← j + 1; sj ← FSSig.KUpd(sj-1);
  d ← Ci[OFSSig.Sigsj(·)](CMA, U0)
Until((d = breakin) ∨ (j = T))
If((d ≠ breakin) ∧ (j = T))  j ← T + 1
((σ, b), M) ← Ci(forge, sj)
If((FSSig.Vrfy(U0, ⟨σ, b⟩, M) = 1) ∧ (1 ≤ b < j) ∧ (M ∉ VbSig))

```

```

return 1
Else return 0

```

Similar to the second step, the third step involves the intermediate player  $A$  playing the game F-ForgeSign with  $C_i$  ( $i = 1$  or  $2$ ) as shown in the left part of Fig. 5 and playing the game CMA with another player  $S$  as shown in the right part of Fig. 5. CMA is a standard message attack game, so we omit the description of this game. As shown in Fig. 5, the intermediate player  $A$  has some algorithms to help him play the games. The descriptions of these algorithms are as follows:

**Algorithm.**  $A.Init(T, 1^k)$   
 $t \xleftarrow{\$} \{1, \dots, T\}; b \xleftarrow{\$} \{1, \dots, t\}$   
 $HashList \leftarrow \emptyset; SKeyList \leftarrow \emptyset; PKeyList \leftarrow \emptyset$   
 For( $i = 0, i \leq t; i++$ ) do  
 $SKeyList[i] \xleftarrow{\$} Z_q^*; PKeyList[i] \leftarrow P^{SKeyList[i]}$   
 EndFor  
 $U_b \leftarrow U^*$   
 For( $i = t + 1, i \leq T; i++$ ) do  
 $SKeyList[i] \leftarrow B.ZB\_H(s_{i-1}); PKeyList[i] \leftarrow P^{SKeyList[i]}$   
 EndFor  
 store all  $SKeyList, PKeyList$

**Algorithm.**  $A.ZB\_S(j, Msg)$   
 If( $b^1 = j$ ) return  $O^{Sign.Sig}(Msg)$   
 Else return  $H_2(Msg)^{SKeyList[j]}$

**Algorithm.**  $A.ZB\_H(x)$   
 If( $\exists y, \langle x, y \rangle \in HashList$ ) return  $y$   
 $y \xleftarrow{\$} Z_q^*; HashList \leftarrow HashList \cup \{\langle x, y \rangle\};$  return  $y$

After these steps, we can immediately find that a successful forgery of  $F$  can be reduced to a successful forgery of the BLS signature. Finally, we estimate the cost and probability of a successful forgery.

Suppose that  $F_i$  ( $i = 1$  or  $2$ ) can win the game that queries  $O^{FSUndSig.H_1(\cdot)}, O^{FSUndSig.H_2(\cdot)}, O^{DSig}(\cdot, \cdot), O^{H_3(\cdot)}$ , and  $O^{H_2(\cdot)}$  at most  $q_{H_1}^{(i)}, q_{H_2}^{(i)}, q_u^{(i)}$ , and  $q_s^{(i)}$  times, respectively, and has a running time of  $\tau_i$  and an advantage  $\varepsilon_i$ . That is,  $F_1$  is a  $\langle \tau_1, \varepsilon_1, q_{H_1}^{(1)}, q_{H_2}^{(1)}, q_s^{(1)}, q_u^{(1)} \rangle$ -forger of  $FSUndSig.Sig$  or  $F_2$  is a  $\langle \tau_2, \varepsilon_2, q_{H_1}^{(2)}, q_{H_2}^{(2)}, q_s^{(2)}, q_u^{(2)} \rangle$ -forger of  $FSUndSig.UndSig$ .

Let  $c_{exp}$  be the time of computing an exponentiation in  $\mathbb{G}_1$  or  $\mathbb{G}_2$ , and let  $c_{mg}$  be the time of generating a random element of  $Z_q^*$ . We obtain the main result as follows, by calculating the



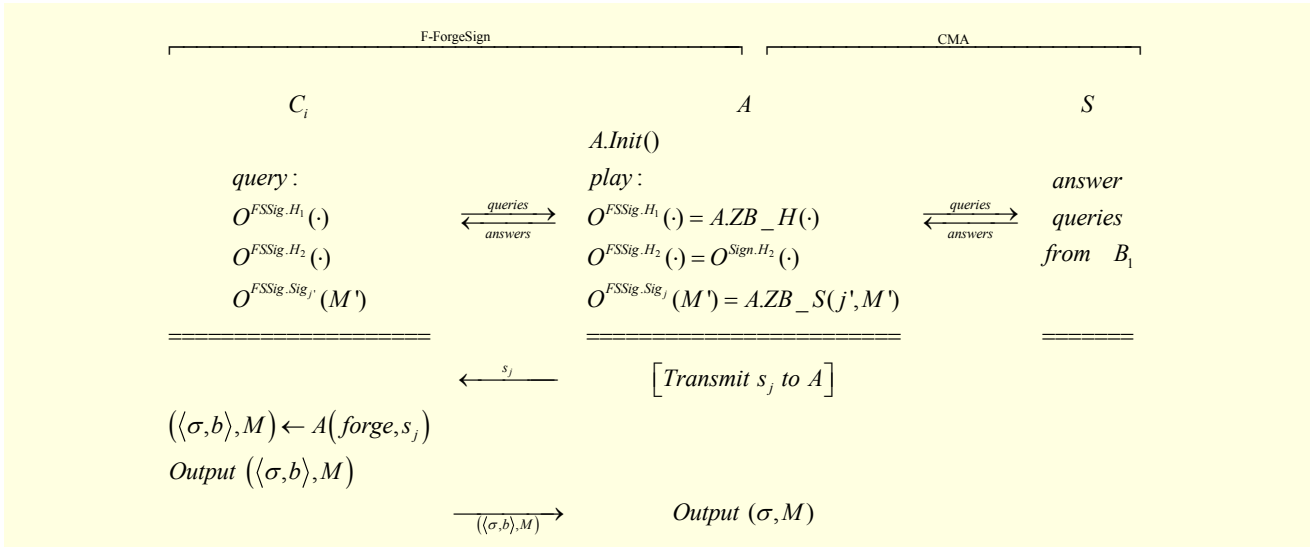


Fig. 5. A plays between  $C_i$  and  $S$ .

number of operations in the game:  
 For any  $\tau$ , if

$$\tau \leq \left( t' - c_{\text{exp}} \left( 2(q_{H_2}^{(1)} + q_{H_2}^{(2)} + q_u^{(1)} + q_u^{(2)}) + 3(q_s^{(1)} + q_s^{(2)} + q_u^{(1)} + q_u^{(2)}) + 2T \right) - (2T + q_{H_1}^{(1)} + q_{H_1}^{(2)}) \cdot c_{\text{rng}} \right)$$

then

$$\text{InSec}(FSUndSig, 1^k, \dots, T; \tau, q_s, q_u) \leq e(q_s^{(1)} + q_s^{(2)} + q_u^{(1)} + q_u^{(2)} + 1) \cdot \varepsilon'$$

to show that a forgery of the BLS signature can support someone else to solve the co-CDH problem. The sketch of

```
#####
# U0: [2359,7664,0]
# sigma: <CERTj,sign:[465,4107,0]>
# j: 6
# Msg: "a good deal"
# REQ_C: "a Note III mobile phone, price <= $1000000"
# CERTj: < <U0:[2359,7664,0], Uj:[2359,7664,0], j:0>,
# sig:[14590,6660,0]>
#####
```

Fig. 7. Successful forgery of  $CERT_j$ .

### 7. Experimental Security Analysis

Besides the theoretical proof of security, experimental security analysis is provided to show that the security of the proposed scheme relies on the difficulty in solving the co-CDH problem. Actually, the analysis consists of two experiments. We firstly perform an experiment to show that if an attacker can break our scheme (that is, successfully forge an undetachable signature that can pass the verification of the undetachable signature verification algorithm  $UndVrfy$ ), then the attacker is also capable of breaking the BLS signature scheme (that is, successfully forge a signature generated by the BLS signing algorithm). Secondly, we perform an experiment

```
#####
# U0: [12276,9226,0]
# Z: <CERTj,sign:[11679,11471,0]>
# J: 6
# Msg: A good deal
# x=H1(msg): 160
# REQ_C|IDc: a Note III MP, price <= $10000000|Customer001
# K (=K^x^(1/x)): 17115,11024,0
# the output of sign_j(REQ_C|IDc): 17115,11024,0
#####
```

Fig. 8. Successful forgery of  $K$ .

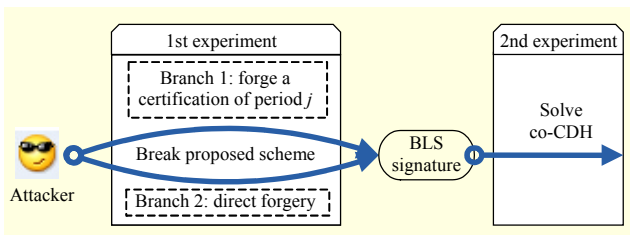


Fig. 6. Sketch of security experiments.

experimental security analysis is illustrated in Fig. 6.

In practical applications, sufficiently large security parameters should be used. In fact, in performance testing, we also use sufficiently large security parameters. However, to enable “an attacker” to successfully break the proposed scheme, very small security parameters (toy parameters) are used in the attacking experiments. Only in this way can the attacker break the scheme by brute-force guessing with limited computational capability.

The first experiment can be divided into two branches. One branch is where the attacker has forged a certification of the fake underlying public key of period  $j$ , then the attacker uses the fake signing key to generate a “valid” undetachable digital

signature. A screen capture of the output is shown in Fig. 7. It is easy to verify that the value of “sig” in the blue rectangle is just a BLS signature on the hash value of the message in the upper rectangle. Another branch is where the attacker directly generates an undetachable digital signature. The certification of period  $j$ ,  $CERT_j$ , is “real and valid.” Thus, the attacker must generate a “valid”  $K$  that is used inv, otherwise the verification process would fail. Note that  $K$  is also a BLS signature on  $REQ\_C \parallel ID_C$ . A screen capture of the output is shown in Fig. 8.

According to the series of experiments, if an attacker is capable of breaking the proposed scheme, then the co-CDH problem could be solved. Hence, for sufficiently large security parameters, the proposed scheme is secure.

## V. Comparison with Relative Works

The first implementation of an undetachable signature is the RSA-based version presented by Kotzanikolaou and others [13]. This was improved by Lee and others in [17] and by Shi and others in [15]. Han and others proposed a security scheme for e-Transactions using mobile agents with an agent broker [14]. They gave an undetachable signature function pair but did not present the signing function Sig subject to (1). Another undetachable signature scheme from pairings was proposed by Shi and others in [16], which is also based on the short signature scheme proposed in [22]. However, this proposed scheme provides forward security, which is not provided by the scheme in [16]. The latest published undetachable signature scheme was presented in 2013. The scheme [18] uses a cryptosystem based on conic curves and is in the form of a threshold digital signature.

As shown in Table 4, different schemes are based on different problems; however, most significantly, only the proposed scheme is forward-secure.

**Table 4.** Comparison of proposed scheme with other undetachable signature schemes.

Scheme	Computational infeasible problem	Forward-secure
[13]	Factorization of big integer	No
[17]	Factorization of big integer	No
[14]	$q$ -Strong Diffie-Hellman problem	No
[15]	Discrete logarithm on elliptic curves	No
[16]	co-CDH	No
[18]	Factorization of big integer and discrete logarithm on conic curves	No
Ours	co-CDH	Yes

## VI. Conclusion

In this paper, we proposed the idea of a forward-secure undetachable digital signature (FS-UDS) so that mobile agents can perform forward-secure signing operations on behalf of the original signers securely, even while they are running in a malicious host. We gave the formal definition of an FS-UDS scheme. Then, we provided the security notion of forward-secure undetachable signature schemes as a theoretical basis. A concrete scheme with provable security was proposed for protecting mobile agents in electronic commerce. The proposed scheme is constructed on co-GDH group pairs, and its security relies on the infeasibility in solving computational co-Diffie–Hellman problems.

An implementation of the proposed undetachable signature algorithm can securely migrate with mobile agents from one host to another without the signing algorithm being at risk from misuse or the signing key being compromised. Moreover, even though a customer’s signing key (in a given time period) has been compromised, any adversary cannot forge any contracts that were signed before the compromising because this scheme is forward-secure.

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