

Minimum Number of Observation Points for LEO Satellite Orbit Estimation by OWL Network

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By using the Optical Wide-field Patrol (OWL) network developed by the Korea Astronomy and Space Science Institute (KASI) we generated the right ascension and declination angle data from optical observation of Low Earth Orbit (LEO) satellites. We performed an analysis to verify the optimum number of observations needed per arc for successful estimation of orbit. The currently functioning OWL observatories are located in Daejeon (South Korea), Songino (Mongolia), and Oukaïmeden (Morocco). The Daejeon Observatory is functioning as a test bed. In this study, the observed targets were Gravity Probe B, COSMOS 1455, COSMOS 1726, COSMOS 2428, SEASAT 1, ATV-5, and CryoSat-2 (all in LEO). These satellites were observed from the test bed and the Songino Observatory of the OWL network during 21 nights in 2014 and 2015. After we estimated the orbit from systematically selected sets of observation points (20, 50, 100, and 150) for each pass, we compared the difference between the orbit estimates for each case, and the Two Line Element set (TLE) from the Joint Space Operation Center (JSpOC). Then, we determined the average of the difference and selected the optimal observation points by comparing the average values.

Keywords: OWL-Net, LEO, TLE, optical observation, orbit estimation

1. INTRODUCTION

Currently, a number of Korean space assets are located in Low Earth Orbit (LEO) and Geo-Stationary Orbit (GEO). In Near Earth space, there are a large number of artificial space objects concentrated in LEO and GEO. This concentration is especially severe in LEO, to such levels that conjunction events occur frequently, including the collision between Iridium 33 and COSMOS 2251 in 2009. Accordingly, the Korea Astronomy and Space Science Institute (KASI) is developing an Optical Wide-field Patrol Network (OWL-Net) to monitor Korean space assets (Park et al. 2012). To anticipate and respond to space-object conjunctions effectively, the location and speed of proximal space objects

must be known.

Telescopes and observation time in Korea that could be utilized for space-object monitoring are limited. To use such limited resources effectively, it is important to find the minimum number of observation points that would allow estimation of orbits with an appropriate degree of precision. Choi et al. (2015) observed GEO satellites and estimated their orbits to determine the optimum number of observations. The numbers of observation points used for orbit estimation were 30, 60, 100, 150, 200, 300, 400, and 600. From these, the degrees of precision of the estimated orbits were compared. Moreover, the estimated orbits and Two Line Element set (TLE) were compared and it was found that the estimated orbit became closer to TLE when there

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were more observation points. In this study, the number of observation points for each pass (of LEO satellites) were 20, 50, 100, and 150 for orbit estimation, and estimation based on all the observation points (320). Comparison of the estimated orbits and the TLE were conducted afterwards. In this paper, a pass is defined as one passage of a satellite across the sky over the observatory. A shot refers to one image; one observation point is that obtained from the center point of a satellite streak.

Types of space-object monitoring systems include radar, laser, and optical observation methods. Lee et al. (2004) explained that the optical observation method has some advantages in identifying a situation in space, including in GEO. For this optical observation method, the monitoring of space objects is possible when the light reflected from space objects is brighter than the space background. Therefore, when sufficiently bright light reaches the observatory, recognizing the space condition is possible regardless of the distance. The optical observation method is advantageous in obtaining angular data including Right Ascension and Declination; however, it is not possible to obtain distance information directly, this way. Gauss and Laplace developed a method of determining distance and initial orbit of natural celestial bodies approximately 200 years ago.

Because we used an orbit estimation technique of an over-determined system, the initial orbit was not determined using the methods of Gauss or Laplace. Instead, TLE (provided by Space Track) was used as the initial orbit. For the orbit estimation of a satellite, the Orbit Determination Tool Kit (ODTK) program (developed by Analytical Graphics, Inc.: AGI), was utilized. In addition, the estimated orbit and TLE were compared using the System Tool Kit (STK) developed by AGI. Among the publicly available satellite orbits, TLE data provides the orbital data for most satellites. Regarding the accuracy of TLE, Vallado et al. (2013) showed that TLE, propagated with Simplified General Perturbations 4 (SGP4), maintained a degree of accuracy within 10 km of the actual orbits. Thus, with a Root Mean Squared (RMS) average distance of 10 km between the estimated orbit and the TLE, this method is considered appropriate for orbit estimation.

In this paper, orbit estimation was performed according to several groups of observation points of increasing number for each LEO satellite pass, and these were

compared with results obtained using TLE. Seven LEO satellites were observed including Gravity Probe B, Seasat 1, ATV-5, CryoSat-2, COSMOS 1455, COSMOS 1726, and COSMOS 2428. The orbit estimation results were compared with TLE to obtain the distance difference according to time. Moreover, the difference variation between the TLE and the orbit estimation results was analyzed according to the number of estimation points.

2. OPTICAL WIDE FIELD PATROL NETWORK (OWL-NET)

Currently operating observatories of OWL-Net are located in Daejeon (South Korea), Songino (Mongolia), and Oukaïmeden (Morocco), while observatories in Israel and the U.S. are under construction. The Daejeon Observatory is a test-bed that inspects each system and performs operation testing. Fig. 1 and Table 1 show the geographic locations and coordinates of each observatory.

Fig. 2 shows the OWL-Net dome, which is a fully open system. Table 2 shows that the optical telescope diameter is 50 cm, with a Field of View (FOV) of 1.10 degree of arc, and an Alt-Azi type mount. Fig. 3 shows the chopper installed in front of the CCD camera to obtain numerous observation points with a single exposure. When the CCD camera receives an exposure command, the chopper initiates rotation and the CCD camera opens and closes by means of the chopper blade. When the CCD camera is open, satellite streaks are obtained. The series of streaklets for satellites appear as dotted lines in the obtained images.



Fig. 1. Locations of the operating OWL-Net observatories: Songino, Mongolia; Oukaïmeden, Morocco; and Daejeon, Korea (test-bed).

Table 1. Locations of OWL-Net Observatories

| # | Country | City | Latitude | Longitude | height(km) |
|----------|---------|------------|-----------------|------------------|------------|
| Test bed | Korea | Daejeon | 36:23:51.4851 N | 127:22:32.4453 E | 0.139 |
| OWL 1 | Mongol | Songino | 47:53:10.0538 N | 106:20:05.1414 E | 1.674 |
| OWL 2 | Morocco | Oukaïmeden | 31:12:23.3000 N | -07:51:59.4000 E | 2.725 |



Fig. 2. The optical tube assembly on an Alt-Azi mount at the test-bed of OWL-Net.

Table 2. Specifications of the OWL-Net optical telescope

| Item | Value |
|------------------------|-------------|
| Diameter | 50 cm |
| Effective focal length | 1,493.46 mm |
| F/number | 2.99 |
| FOV | 1.10 deg |
| Mount | Alt-Azi |

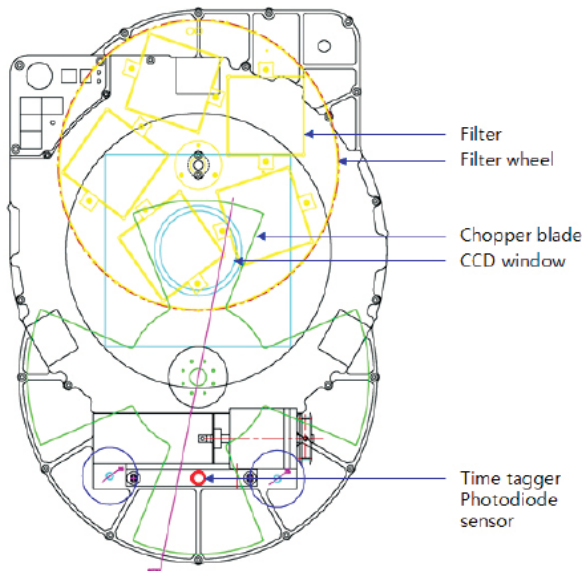


Fig. 3. Design of the wheel station housing of a CCD camera, a chopper system, and a filter wheel of OWL-Net (Park et al. 2013).

The OWL-Net can use different observation modes when monitoring LEO and GEO satellites. For the LEO satellite observation mode, the chopper is used because stars are tracked using a sidereal clock drive (derotator). Therefore, stars are detected as points and satellites are detected as streaks. For the GEO satellite observation mode, neither the chopper nor the tracking function may be used. Normally, the OWL-Net satellite observation-mode detects stars as

points and satellites as streaks. The observation strategy for GEO satellite was studied by Choi et al. (2011, 2015). In this study, to establish an effective observation strategy for LEO satellites, an LEO satellite observation mode was employed.

The observation images were processed using a preprocessing program developed by Park et al. (2013). This preprocessing program detects satellite streaks in the images to determine the satellite streak epoch time, right ascension, and declination. Currently, this preprocessing program is subject to detection errors, such as occasionally failing to detect satellites or misidentifying stars as satellites. With this program, the time and coordinates are obtained using different methods. The time information is obtained through the time history of the CCD camera’s observation window opening and closing due to the action of the chopper, while the right ascension and declination are obtained using the acquired streak coordinates and absolute coordinates of the background stars. According to Son et al. (2015), the time information of the OWL-Net can be synchronized to the order of 0.001 s using the Network Time Protocol (NTP). The obtained time and coordinates are sequentially recorded. For example, as can be seen in Fig. 4, the small circle is the detected satellite’s coordinates, as obtained using the preprocessing program, the white boxes are the sequentially recorded time data, and the black boxes are the sequentially recorded coordinate data. Black No. 3 is a misidentification of a star near a streak as a satellite. In the recordings, the satellites are recorded as being at the coordinates of Black No. 3 for the time of White No. 3, and at the coordinates of Black No. 4 for the time of White No. 4. As a result, the time and coordinate data become mismatched, causing error in the orbit determination using this observation data. This problem is similar to that described by Jo et al. (2015). Such detection error causes mismatches between the time and coordinate data. Therefore, the recorded time information and the corresponding satellite streak must be accurately re-matched to compensate for the detection error.

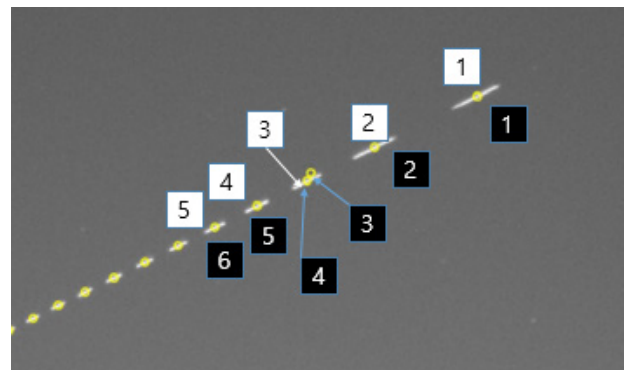


Fig. 4. Partial shot of Gravity Probe B observed 2 October 2014 at the test-bed.

3. POST CORRECTION OF OPTICAL OBSERVATION DATA BY OWL-NET

In this study, LEO satellites ATV-5, Gravity Probe B, CryoSat-2, Seasat 1, COSMOS 1455, COSMOS 1726, and COSMOS 2428 were observed. The observation subjects were LEO satellites observed for over three days by OWL-Net. Of note, ATV-5 was observed through international cooperation with the Defense Advanced Research Projects Agency (DARPA) and performed re-entry on 15 February 2015. Table 3 shows the North American Aerospace Defense Command Catalogue Number (NORAD ID), perigee altitude, apogee altitude, and eccentricity of the satellites from Space Track.

In this study, data from the Songino OWL-Net observatory and the Daejeon OWL-Net test-bed were used. The data, after compensation for detection error, are shown in Tables 4 and 5. Only passes with more than 145 observation points were used. For ATV-5, two passes obtained on 15 February 2015, were used.

4. METHODS OF ORBIT DETERMINATION AND RESULTS

In this study, we focused on determining the minimum number of effective observations per pass, needed to maximize the efficiency of the OWL-Net observation

Table 3. Orbital characteristics of the observed satellites

| Observation Target | | Orbit(km) | | |
|--------------------|----------|-----------|--------|--------------|
| Satellite | NORAD ID | Perigee | Apogee | Eccentricity |
| ATV 5 | 40103 | 368 | 405 | 0.0013728 |
| COSMOS 1455 | 14032 | 516 | 543 | 0.0019497 |
| COSMOS 1726 | 16495 | 507 | 526 | 0.0013828 |
| COSMOS 2428 | 31792 | 845 | 857 | 0.0007984 |
| CryoSat-2 | 36508 | 712 | 726 | 0.0009476 |
| Gravity Probe B | 28230 | 635 | 638 | 0.0002320 |
| SEASAT 1 | 10967 | 747 | 749 | 0.0001213 |

Table 4. Orbital characteristics of the observed satellites

| Satellite | Date | Points per pass | Points per shot | | | | | | | | | | | | | | | | | | | | |
|-----------------|----------|-----------------|-----------------|----|----|----|----|-----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|
| | | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| CryoSat-2 | 20150524 | 453 | 69 | 76 | 50 | 62 | 94 | 102 | | | | | | | | | | | | | | | |
| | 20150525 | 1,595 | 56 | | 43 | | 71 | 122 | 119 | 109 | 108 | 103 | 100 | 94 | 91 | 85 | 80 | 74 | 73 | 70 | 70 | 71 | 56 |
| | 20150528 | 256 | | | | | | | | 69 | 86 | 101 | | | | | | | | | | | |
| | 20150603 | 706 | | | | | | | | | | 99 | 92 | 87 | 81 | 77 | 73 | 70 | 66 | | 61 | | |
| Gravity Probe B | 20141104 | 279 | | | | | 52 | 56 | | 78 | 93 | | | | | | | | | | | | |
| | 20141105 | 575 | | 89 | 81 | 67 | 54 | 46 | | | | 65 | 79 | 94 | | | | | | | | | |
| | 20141106 | 94 | | | | | | | | | 94 | | | | | | | | | | | | |
| Seasat 1 | 20141117 | 223 | 67 | 50 | 20 | | | | | 21 | | 65 | | | | | | | | | | | |
| | 20141119 | 209 | | | | 82 | 69 | 58 | | | | | | | | | | | | | | | |
| | 20141120 | 104 | | | | | | | | 104 | | | | | | | | | | | | | |

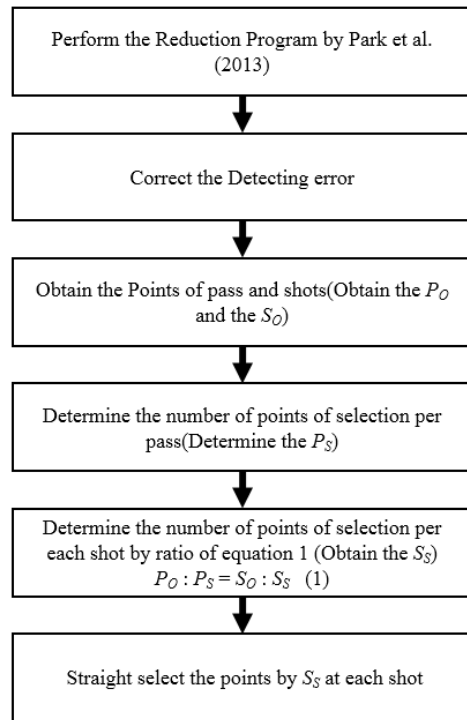


Fig. 5. Selection process of points in each shot.

strategy. Several sets of observation points of increasing number (20, 50, 100, and 150), as well as all points together (320), were used for each pass in the orbit-estimation experiment. For this experiment, both detected streaks and non-detected streaks were considered to reflect the effect of detection error when selecting observation points. When the satellite passed over the sky above the observatory, one observation pass was completed and this pass was observed (recorded) in numerous shots. The number of observation points obtained from a pass (P_O) and the number of observation points obtained from a shot (S_O) were determined. Fig. 5 shows the process of determining the observation points from each shot. In the figure, P_S is the number of observation points that could be selected from a pass and S_S is the number of observation points that could

Table 5. Statistics of satellite observation at the OWL-Net Songino Observatory

| Satellite | Date | Points per pass | Points per shot | | | | | | | | | | | | | | | | | | | | |
|-----------------|----------|-----------------|-----------------|-----|-----|-----|-----|-----|----|----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|
| | | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| ATV-5 | 20150215 | 506 | | 52 | 52 | 81 | 70 | 61 | 50 | 45 | | | 43 | 52 | | | | | | | | | |
| | 20150215 | 155 | | | 48 | 51 | | | 56 | | | | | | | | | | | | | | |
| COSMOS 1455 | 20141101 | 375 | 93 | 76 | 51 | 26 | | | | 13 | 45 | 71 | | | | | | | | | | | |
| | 20141104 | 341 | | 74 | 61 | 42 | 29 | 32 | 45 | 58 | | | | | | | | | | | | | |
| | 20141106 | 86 | | | | | | | | | | 86 | | | | | | | | | | | |
| COSMOS 1726 | 20141101 | 272 | | 68 | 38 | 15 | | | | | | 62 | 89 | | | | | | | | | | |
| | 20141102 | 145 | | 53 | 17 | | | 21 | | 54 | | | | | | | | | | | | | |
| | 20141103 | 354 | 87 | 80 | | 21 | 15 | | 30 | 48 | 73 | | | | | | | | | | | | |
| | 20141105 | 250 | | | | | | | 39 | 55 | 70 | 86 | | | | | | | | | | | |
| | 20141106 | 84 | | | | | | | | | | 84 | | | | | | | | | | | |
| COSMOS 1455 | 20150210 | 825 | | | | | 99 | 90 | 84 | 82 | 83 | 89 | 99 | 102 | 97 | | | | | | | | |
| | 20150211 | 178 | | | | | | | | | | | 45 | 121 | 12 | | | | | | | | |
| | 20150212 | 994 | | 110 | 129 | 118 | 109 | 101 | 96 | | 99 | 111 | 121 | | | | | | | | | | |
| | 20150213 | 1,133 | | 142 | 130 | 119 | 109 | 103 | 99 | 98 | 100 | 112 | 121 | | | | | | | | | | |
| | 20141105 | 250 | | | | | | | 39 | 55 | 70 | 86 | | | | | | | | | | | |
| | 20141106 | 84 | | | | | | | | | | 84 | | | | | | | | | | | |
| Gravity Probe B | 20141101 | 819 | 113 | 97 | 82 | 68 | 54 | 41 | 33 | 44 | 61 | 78 | 95 | 53 | | | | | | | | | |
| | 20141102 | 731 | 113 | 99 | 55 | 68 | 68 | 70 | 77 | 85 | 96 | | | | | | | | | | | | |
| | 20141103 | 287 | | 83 | 95 | 109 | | | | | | | | | | | | | | | | | |
| | 20141104 | 442 | | | | 43 | 54 | 45 | 43 | 51 | 62 | 77 | 67 | | | | | | | | | | |
| | 20141105 | 366 | 112 | 91 | 87 | 76 | | | | | | | | | | | | | | | | | |
| | 20141106 | 553 | 115 | 90 | | 81 | 80 | 85 | | | 102 | | | | | | | | | | | | |
| Seasat 1 | 20141121 | 380 | | | | | | | | 51 | 59 | 72 | | 99 | 99 | | | | | | | | |
| | 20141123 | 130 | | | | | | | 50 | | | | | 80 | | | | | | | | | |
| | 20141127 | 252 | | | | | | | | | | 74 | 85 | 93 | | | | | | | | | |

be selected from a shot.

Orbit estimation was performed using the ODTK developed by AGI. Table 6 shows the input values, which were changed for the ODTK setup. When the position and speed uncertainty were reduced, the problem of non-convergence occurred for ODTK, so the values for position and speed uncertainty were set to be relatively large.

To establish a precise dynamics model, all acceleration terms supported by ODTK were set as shown in Table 7. Two largest values among the satellite height, width, and depth were multiplied, and set as the satellite surface area.

Compensation of the observation data was performed with regard to diurnal and annual aberrations, detection error, and Light Travel Time. The detection error and Light Travel Time compensations were applied when the ODTK input file was created, while the compensation for diurnal and annual aberrations was directly applied within ODTK.

The steps for using ODTK were, in the order used for initial orbit determination, least square method, filter, and smoother. In this study, we found frequent occurrence of the least square method tracking the wrong local minimum. Thus, instead of using the least square method results as the initial value for the filter, TLE was used as the initial value for the filter. The TLE used here was obtained from Space Track.

Finally, using the STK developed by AGI, the filter result

Table 6. List of ODTK configurations

| Object | Properties | Value |
|-------------|---------------------------------|-------------------------|
| Satellite | Initial orbit state | TLE of Space Track |
| | Mass | Obtained from reference |
| | Area | Obtained from reference |
| | Cd | 2.2 |
| | R | 1,000 m |
| | I | 2,000 m |
| | C | 100 m |
| | dot R | 1 m/s |
| | dot I | 1 m/s |
| | dot C | 1 m/s |
| Observatory | Measurement Statistics Elements | RA, Dec |
| | Sigma | 20 arcsec |
| | Half Life | 1 min |
| | White Noise Sigma | 3 arcsec |
| | Estimation bias | TRUE |
| Filter | Antenna Type | Optical |
| | Aberration | all |
| | Start Time | First observation time |
| | Nominal Sigma | 100 |

from the ODTK was compared with the TLE propagation result. The TLE provided by JSpOC and the orbit estimation results were compared to determine the precision of the orbit estimation. With TLE as the reference, the distance differences for the radial, in-track, and cross-track coordinates of the estimated orbit were set as the precision indicators. In addition, the RMS average was obtained for the distance difference. Figs. 6–19 and Table 8 show the

Table 7. List of acceleration terms applied in ODTK to estimate orbits

| Perturbation | Acceleration term |
|--------------------------|--|
| Gravity force | EGM 96, 70 X 70 |
| | Gravity force of Sun, Moon and other Planets |
| | Tide force by ground and ocean |
| | General relative effect |
| Drag | CIRA 1972 Model Ballistic Coefficient(BC)=Cd*A/m ¹) |
| Solar radiation pressure | Spherical Radiation Model Shadow of Earth and Moon |

¹The dimension and mass of each satellite were obtained from eoPortal Directory (2015a, b), ESA (2015), Kosmonavtika (2015), and Everitt & Parkinson (2006).

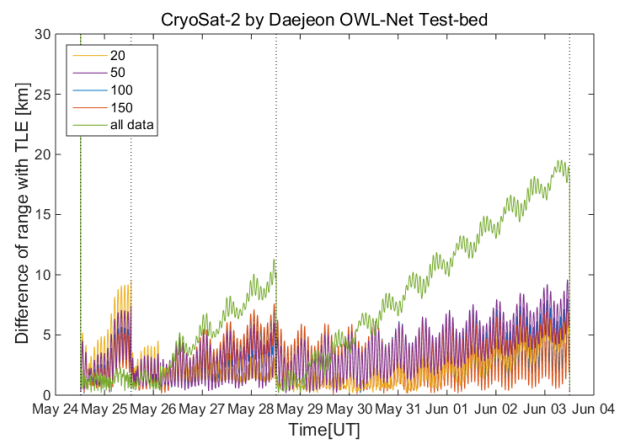


Fig. 6. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of CryoSat-2 observed on 24 May–03 June 2015 at the Daejeon OWL-Net Test-bed, with sets of differing number of observations, and TLE with 11 epochs as a reference orbit (The vertical solid lines represent an observation epoch, and the result of each set is distinguished with colors, as shown in the box at the upper left corner of the figure).

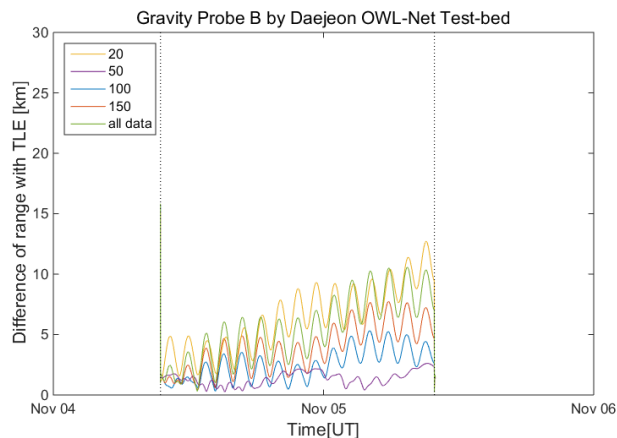


Fig. 7. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Gravity Probe B observed on 04–05 November 2014 at the Daejeon OWL-Net Test-bed, with sets of differing number of observations, and TLE with five epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors, as shown in the box at the upper left corner of the figure).

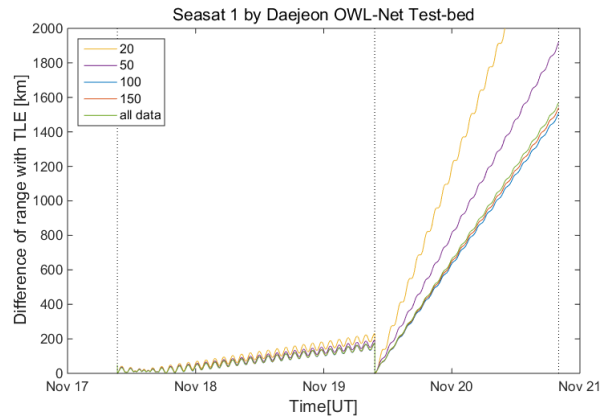


Fig. 8. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 17–20 November 2014, at the Daejeon OWL-Net Test-bed, with sets of differing number of observations, and TLE with five epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in box at the upper left corner of the figure).

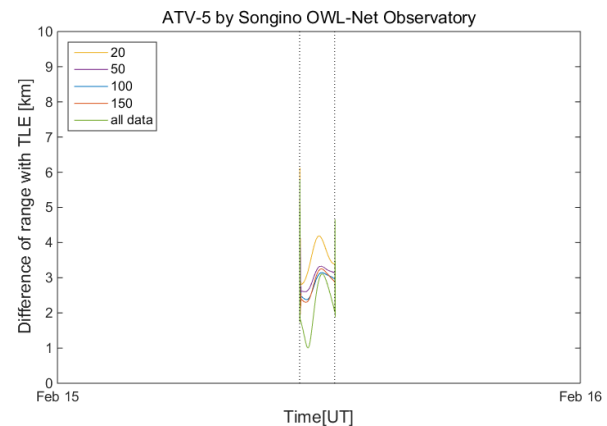


Fig. 9. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of ATV-5 observed on 15 February 2015 at the Songino OWL-Net Observatory, with sets of differing number of observations, and TLE with three epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors, as shown in the box at the upper left corner of the figure).

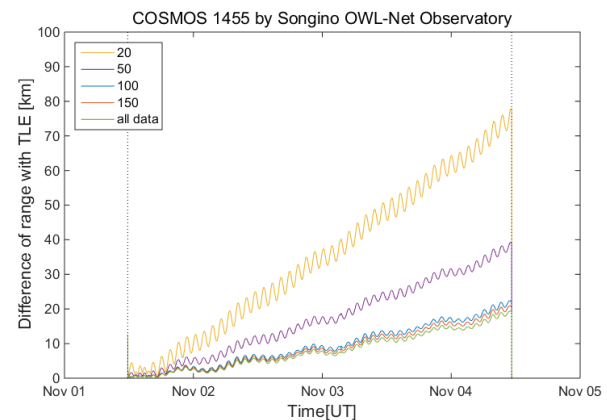


Fig. 10. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of COSMOS 1455 observed on 01–04 November 2014 at the Songino OWL-Net Observatory, with sets of differing number of observations, and TLE with six epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

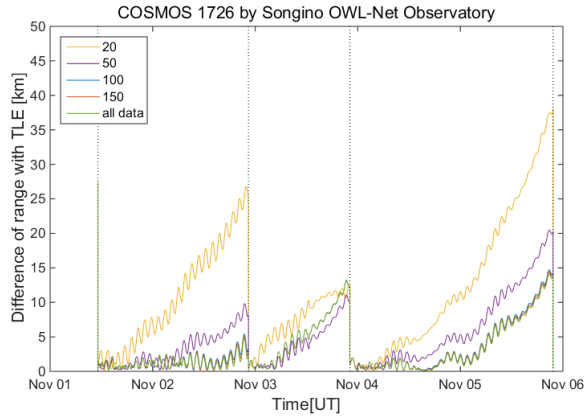


Fig. 11. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of COSMOS 1726 observed on 01–05 November 2015 at the Songino OWL-Net Observatory, with sets of differing number of observations, and TLE with six epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

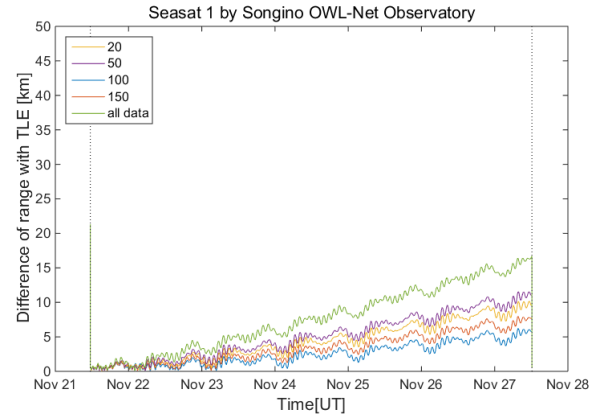


Fig. 14. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 21–27 November 2014 at the Songino OWL-Net Observatory, with sets of differing number of observations, and TLE with seven epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

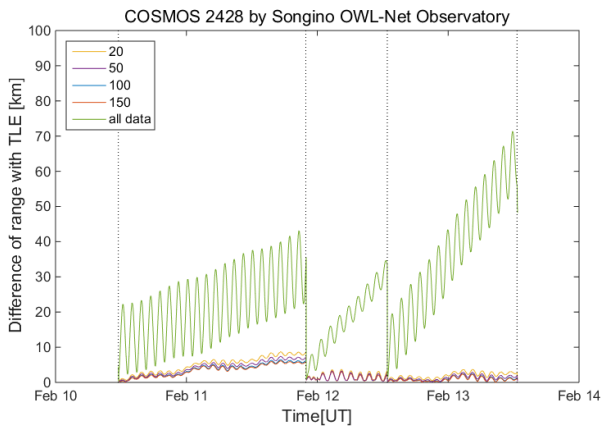


Fig. 12. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of COSMOS 2428 observed on 10–13 February 2015 at the Songino OWL-Net Observatory, with sets of different number of observations, and TLE with thirteen epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

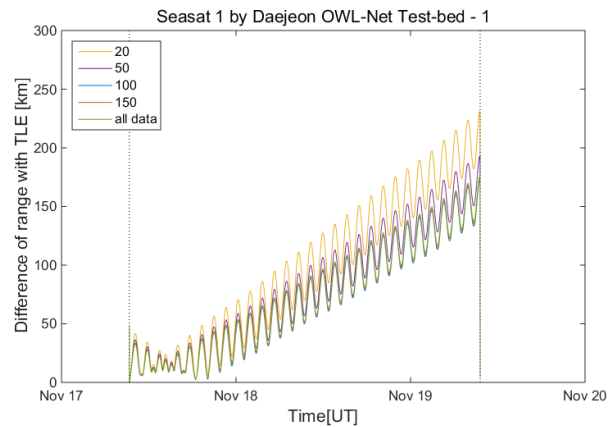


Fig. 15. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 17–19 November 2014 at the Daejeon OWL-Net test-bed with sets of differing number of observations, and TLE with three epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

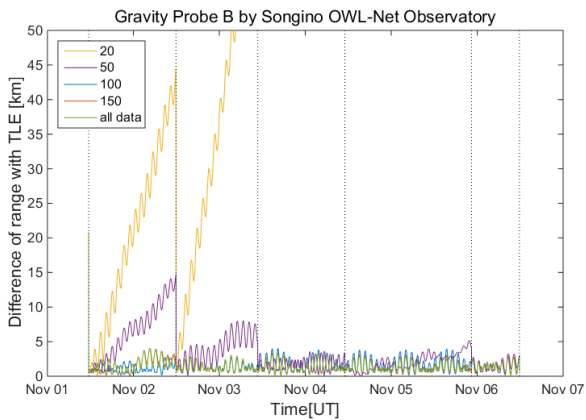


Fig. 13. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Gravity Probe B observed on 01–06 November 2015 at the Songino OWL-Net Observatory, with sets of different number of observations, and TLE with seven epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

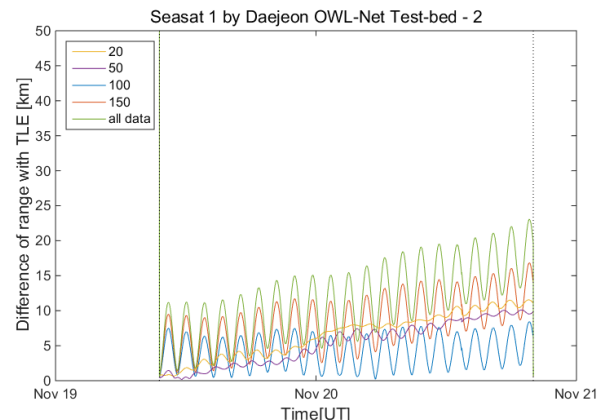


Fig. 16. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 19–20 November 2014 at the Daejeon OWL-Net test-bed with sets of differing number of observations, and TLE with three epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

Table 8. Difference between TLE and RMS mean range of estimated orbit

| Observatory | Satellite | Difference between TLE and RMS mean range of estimated orbit (km) | | | | |
|-------------|-----------------|---|--------|--------|--------|--------|
| | | 20 | 50 | 100 | 150 | all |
| Testbed | CRYOSAT_2 | 3.25 | 3.64 | 2.82 | 2.61 | 8.10 |
| | Gravity_Probe_B | 6.15 | 1.39 | 2.46 | 3.62 | 4.26 |
| | Seasat_1 | 646.13 | 451.71 | 362.65 | 372.12 | 400.97 |
| Songino | ATV-5 | 3.49 | 2.99 | 2.79 | 2.70 | 2.48 |
| | Gravity_Probe_B | 390.66 | 3.12 | 1.46 | 1.42 | 1.53 |
| | COSMOS_1455 | 34.75 | 16.87 | 9.03 | 8.25 | 7.13 |
| | COSMOS_1726 | 10.93 | 4.72 | 3.21 | 3.12 | 3.02 |
| | COSMOS_2428 | 3.34 | 2.63 | 2.17 | 1.99 | 23.40 |
| | Seasat_1 | 4.33 | 5.02 | 2.44 | 3.29 | 7.17 |

obtained results. In Figs. 6–19, the black vertical line refers to the time of observation. Fig. 15 shows the result that was obtained using the optical observation data of Seasat 1 on 17 and 19 November 2014, by the Daejeon OWL-Net test-bed. Fig. 16 shows the results obtained using optical observation data of the same subject and by the same observatory but for different dates (19 and 20 November 2014). Figs. 17–19 show results obtained using only the optical observation data of the Daejeon OWL-Net test-bed for Seasat 1 on 17, 19, and 20 November 2014.

5. SUMMARY

Comparing the orbit estimation results according to the observation point numbers for 7 LEO satellites revealed that the use of more observation points led to more accurate estimations of orbits, except for Seasat 1 and Gravity Probe B, as shown in Figs. 6–14. When comparing the orbit estimation results for Seasat 1 and Gravity Probe B with those of the other satellites, it was difficult to explain the abnormality of the orbit estimation results with anything other than errors in the observation data or errors in the orbit estimation filter (shown in Figs. 7–8 and Figs. 13–14). In addition, comparison between the orbit estimation conditions of the other satellites, except for the two satellites in question, shows that the possibility of an error in the orbit estimation filter is very low. Thus, the source of the errors was thought to be in the observation data obtained from the optical observations of Seasat 1 and Gravity Probe B.

Though the Gravity Probe B and Seasat 1 had similar observation periods, the estimated orbits obtained from each observatory were clearly different. It is thought that there is a measurement time bias in one of the two observatories, or in both observatories. The presence of significant error in many observation points is recognized by ODTK due to the measurement time bias, resulting in

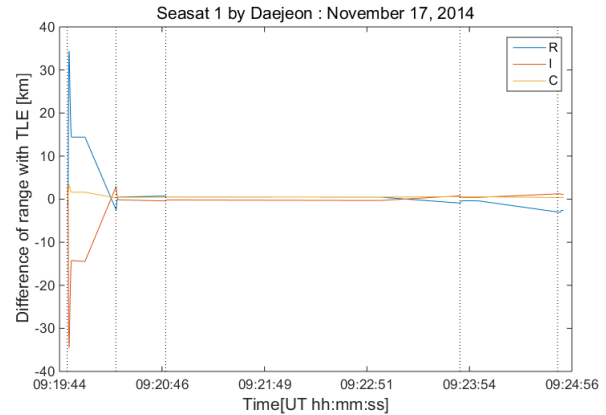


Fig. 17. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 17 November 2014 at the Daejeon OWL-Net test-bed, with sets of different number of observations, and TLE with two epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

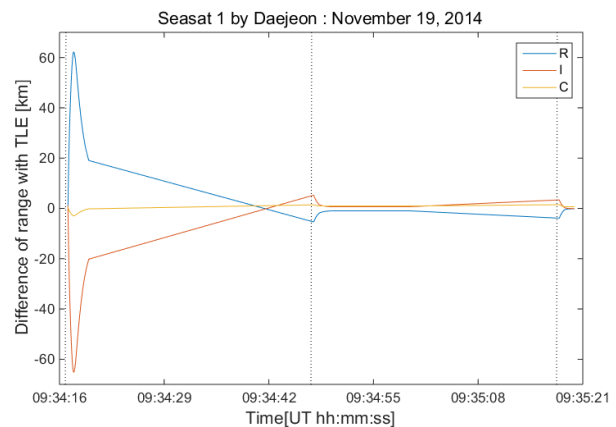


Fig. 18. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed on 19 November 2014 at the Daejeon OWL-Net test-bed, with sets of differing number of observations, and TLE with two epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

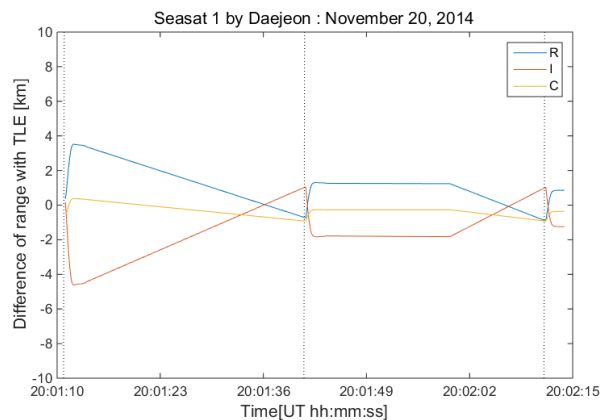


Fig. 19. Differences of the range in Radial-In track-Cross track coordinates between the estimated orbits of Seasat 1 observed 20 November 2014 at the Daejeon OWL-Net test-bed, with sets of differing number of observations, and TLE with two epochs as a reference orbit (The vertical solid lines represent observation epochs, and the result of each set is distinguished with colors as shown in the box at the upper left corner of the figure).

the rejection of these points, and their not being used in the orbit estimation. When Seasat 1 observation data for three days was processed as 1 degree of arc, the result shown in Fig. 8 was obtained; however, when the same observation data were processed in relation to a daily base, the orbit estimation results shown in Figs. 17–19 were obtained. This shows that when the observation data for Seasat 1 is used on a daily base, there is no significant deviation from TLE. In Fig. 15, it can be observed that the estimated orbit of Seasat 1 deviated greatly from TLE. However, when data for a specific day is processed, as shown in Fig. 16, the orbit accuracy is fairly well maintained. In this case, there is no close correlation between the number of observation points used for the data processing, and the improvement in accuracy. From the above results, it was determined that an adequate orbit was obtainable through orbit estimation using individual arcs; however, due to the presence of very different levels of measurement time-bias between the Seasat 1 observation data on 17 and 19 November 2014 at the Daejeon OWL-Net test-bed, orbit estimation failed when it was attempted using observation data as one long arc.

In Table 8, it can be seen that regardless of the number of observation points for CryoSat-2, ATV-5, and COSMOS 2428, the RMS average difference in distance from TLE was within 10 km. In the cases of COSMOS 1455 and COSMOS 1726, the RMS average difference in distance from TLE was within 10 km when the numbers of observation points were 100 and 50, respectively. Thus, when the number of observation points is greater than 100, the RMS average distance difference between the estimated orbit and TLE is within 10 km. For COSMOS 2428, the distance difference with TLE is greater when using all the observation points, than when using 150 points. This is thought to be due to not selecting an observation point that significantly includes observation errors.

The observation periods for Gravity Probe B and Seasat 1 at the test-bed and Songino Observatories were either similar or overlapped. The Gravity Probe B observed from the test-bed, and Seasat 1 observed from the Songino Observatory showed tendencies of varying orbit estimation accuracy, regardless of the number of observation points. Therefore, Gravity Probe B and Seasat 1 used the observations of both observatories, and orbit estimations were not performed.

In conclusion, the distance between the estimated orbit and TLE for LEO satellites was within 10 km when the number of observation points for each pass was greater than 100, in most cases. When the number of observation points per pass increased, the estimated orbit and TLE converged. Unlike for generally known orbit estimation theory, using

all the observation points for orbit estimation resulted, in some cases, in the reduction of the accuracy of orbit estimation. Moreover, the exceptionally unacceptable orbit estimation results obtained when using observation data from a specific observatory on a specific date are thought to be due to the presence of measurement-time bias for each observatory that cannot be estimated, and that has temporal variation in its magnitude. Therefore, until the problem of measurement-time bias for each observatory can be clearly addressed and resolved, using all observation points for orbit estimation will not necessarily lead to improved results.

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