

# Double Sieve Collision Attack Based on Bitwise Detection

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## Abstract

Advanced Encryption Standard (AES) is widely used for protecting wireless sensor network (WSN). At the Workshop on Cryptographic Hardware and Embedded Systems (CHES) 2012, Gérard *et al.* proposed an optimized collision attack and break a practical implementation of AES. However, the attack needs at least 256 averaged power traces and has a high computational complexity because of its byte wise operation. In this paper, we propose a novel double sieve collision attack based on bitwise collision detection, and an improved version with an error-tolerant mechanism. Practical attacks are successfully conducted on a software implementation of AES in a low-power chip which can be used in wireless sensor node. Simulation results show that our attack needs 90% less time than the work published by Gérard *et al.* to reach a success rate of 0.9.

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**Keywords:** AES, wireless sensor network, collision attack, power analysis, side-channel attack

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## 1. Introduction

Wireless sensor networks (WSN) provide promising solutions in a wide range of applications, such as military, healthy care, industrial monitoring, target localization and tracing. Sensor nodes that consist the WSN are usually placed in potentially hostile environment and face various kinds of challenges [1]-[3]. For the needs of security, cryptographic algorithms are used to implement authentications and encrypted communications in WSN. Advanced Encryption Standard (AES), adopted by USA government in 2002 [4], is ideal for the resources-constrained sensor nodes because of its high speed and low cost. As a standard encryption algorithm in wireless communication [5], AES is widely used in current WSN platforms.

However, wireless sensor nodes are vulnerable to side-channel attacks. Since proposed by Kocher *et al.* [6], side-channel attacks have been known as efficient to recover the key by eavesdropping the physical information (e.g., power consumption, electro-magnetic radiation) leaked by target devices [7]-[10]. These attacks are more efficient than traditional cryptanalysis. They do not interrupt operations of the target device, so they can be conducted stealthily on wireless sensor nodes without being detected [11],

Side-channel collision attack, as a combination of side-channel attack and cryptanalysis, was proposed in 2003 by Schramm *et al.* against DES [12], and was applied to AES [13] soon after that. Improved collision attacks were presented subsequently [14]-[17]. Most collision attacks are highly sensitive to errors, namely false positives of collision detections [18], which usually happen when the noise level is high. Gérard *et al.* [18] introduced Low Density Parity Check (LDPC) decoding approach to deal with errors, which made their work more efficient than previous methods. However, there are two problems for LDPC method. First, the computational complexity of the offline stage is high, due to its framework. Second, the online stage (power acquisition stage) is very time-consuming, because all the acquired power traces need to be saved.

In this paper, we propose an efficient and error robust collision attack. The new framework of our approach is based on a double sieve model, which ensures the efficiency and success rate of attacks. A bitwise collision detection method is proposed, which greatly reduces the time for online stage by reducing the number of saved traces. The computational complexity of the framework is low, so the key can be recovered very fast. Practical attacks on AES and experimental results show that our approach is more efficient than previous methods.

The rest of this paper is organized as follows. In Section 2, we briefly introduce the notations and recall previous collision attacks. In Section 3, we propose the framework of our new collision attack. In Section 4, we describe the bitwise collision detection method. In Section 5, we present the experiments of our new attack. An error-tolerant version of our attack is presented in Section 6, and the efficiency is analyzed in Section 7. Finally, Section 8 concludes the paper.

## 2. Preliminary

### 2.1 Notations

The cryptographic algorithm we focus on in this paper is AES. The 16-bytes plaintext and first-round sub key are denoted as  $P = \{p_1, \dots, p_{16}\}$  and  $K = \{k_1, \dots, k_{16}\}$ . Plaintexts and power

traces are numbered by superscript, and the  $i$ th plaintext and power trace are written as  $P^i$  and  $T^i$ . The operations of 16 S-Boxes are handled sequentially, so a power trace can be cut into 16 sections, each of which is composed of  $l$  points. The section corresponding to the  $a$ th S-Box is denoted as  $T_a = \{t_{a,1}, t_{a,2}, \dots, t_{a,l}\}$ . Averaged power traces are used in our attack, denoted as  $\bar{T} = \{\bar{T}_1, \dots, \bar{T}_{16}\}$ .

## 2.2 Linear Collision Attack

Collision attack proposed by Schramm *et al.* [12] is based on the concept of internal collision, where a function produces the same output for two inputs:  $\phi(x_1) = \phi(x_2) = y$ . Linear collision attack [17] describes how to recover the key from internal collisions based on linear equations. In AES, if a collision between the computations of S-Box  $a$  and  $b$  in the first round is detected, the attackers will have the following relation:

$$Sbox(p_a \oplus k_a) = Sbox(p_b \oplus k_b). \quad (1)$$

A linear equation can be deduced:

$$k_a \oplus k_b = p_a \oplus p_b = \Delta k_{a,b}. \quad (2)$$

A series of linear equations can be built with more collisions detected. Eventually, once 1 key byte is determined, the other 15 key bytes can be decided immediately. As a result, the size of key space is reduced to  $2^8$ .

## 2.3 Correlation-Enhanced Collision Attack

Two main approaches have been proposed to detect side-channel collisions [18]: the binary test and the correlation-enhanced method [19]. The former one computes the distance between two power traces. Euclidean distance and absolute deviation [20] are usually used here. A Collision is confirmed if the distance is less than a threshold. However, this technique is a byte wise operation. A collision only indicates  $HW(p_a \oplus k_a) = HW(p_b \oplus k_b)$ , and (2) is not necessarily established. This method is also sensitive to false detections of collisions. The correlation-enhanced technique compares two series of (instead of two) power traces with correlation coefficient, and returns a score list of all the guessed value of  $\Delta k_{a,b}$ . This allows an improvement: By testing several highest-scored candidates instead of only the first one, the probability of finding a correct collision can be increased. But this approach needs to compute correlation coefficient for every guessed value of  $\Delta k_{a,b}$ , so the efficient is a problem.

## 2.4 LDPC Decoding Problem in Collision Attack

Gérard *et al.* [18] pointed out that the linear collision attack can be re-written as a LDPC decoding problem, since there exists a relationship:

$$\Delta k_{a,b} \oplus \Delta k_{b,c} = \Delta k_{a,c}, \quad \forall 1 \leq a \neq b \neq c \leq 16 \quad (3)$$

The set  $\Delta K = \{\Delta k_{a,b} \mid 1 \leq a \neq b \leq 16\}$  can be regarded as a LDPC code, and (2) as parity-check nodes. Finding the correct  $\Delta K$  is equivalent to decode the LDPC code.

It is noteworthy that (3) provides a solution to find out errors in collision detections. In this paper, we exploit (3) as an error-checking criterion, and detail the procedure in the next section.

### 3. A Novel Framework for Linear Collision Attack

In this section, we propose a new framework of collision attack. As shown in Fig. 1, the main body of the framework is a loop. Each iteration, called a partial attack, is based on a double sieve model, and contributes a part of information of the key. The loop iterates and accumulates the information until all the bytes of  $\Delta K$  are determined. Finally  $2^8$  candidate keys that are compatible to the set  $\Delta K$  are tested.

The double sieve model includes two screenings: 1) Collision detection sieves the probable candidate of the  $\Delta K$ , and saves the result in a  $1 \times 120$  array *DeltaKey1*. 2) Error detection screens out the false part of *DeltaKey1*, and saves the survivals in a  $1 \times 120$  array *DeltaKey2*. Accumulated information of  $\Delta K$  is kept in *DeltaKey3*.

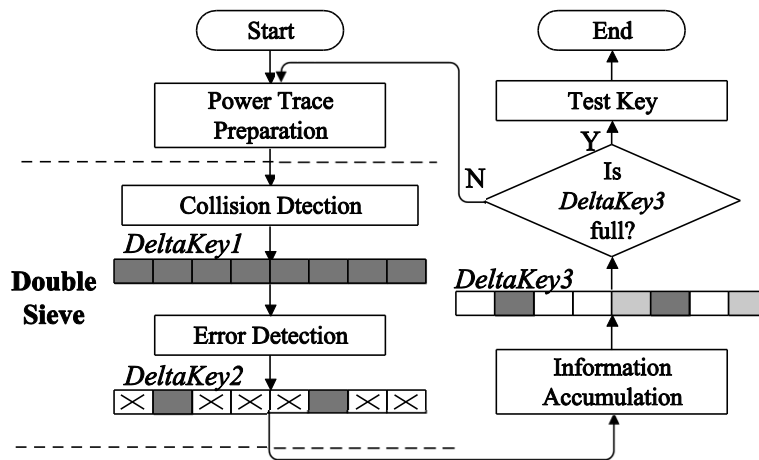


Fig. 1. Work flow of the new framework.

The work flow of our framework is showed in Algorithm 1. Each partial attack consists of 4 steps. First, power traces are collected and preprocessed in the **PreparePowerTraces** step. Then in **DetectCollision** step, these power traces are used to detect collisions. These two steps will be detailed in Section 4.

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#### Algorithm 1 New Framework for Linear Collision Attack

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**Input:** 8 power traces  $\bar{T}^1, \dots, \bar{T}^8$  for each partial attack.

**Output:** The guessed key  $K$ .

```

1:   Clear DeltaKey3
2:   while (DeltaKey3 is not full)
3:        $(\bar{T}^1, \dots, \bar{T}^8) \leftarrow \mathbf{PreparePowerTraces}()$ 
4:        $\Delta Key1 \leftarrow \mathbf{DetectCollision}(\bar{T}^1, \dots, \bar{T}^8)$ 
5:        $\Delta Key2 \leftarrow \mathbf{DetectError}(\Delta Key1)$ 
6:        $\Delta Key3 \leftarrow \mathbf{Accumulate}(\Delta Key2, \Delta Key3)$ 
7:   end
8:   for every candidate key  $K$  compatible to DeltaKey3
9:       if ( $\mathbf{TestKey}(K)$ ) return ( $K$ )
10:  end
  
```

---

In the **DetectError** step, as described in Algorithm 2, we use (3) to check every elements of *DeltaKey1*. A  $1 \times 120$  array *Errorlist* is used to record how many times (3) is not satisfied for every  $\Delta k_{a,b}$ . If an equation of (3) is not satisfied, the three involved  $\Delta k$ 's will be marked. If  $Errorlist((a,b))$  is larger than a threshold  $Th_{EL}$ ,  $\Delta k_{a,b}$  will be erased. Because there are 14 possible values of  $c$  which satisfy the condition  $(a \neq c \neq b) \wedge (1 \leq c \leq 16)$ , every  $\Delta k_{a,b}$  has 14 relative equations in (3), so the maximum of  $Errorlist((a,b))$  is 14. A wrong guess of  $\Delta k_{a,b}$  tends to fail in most of the checks, whereas a correct guess has few failures. So we set  $Th_{EL}$  as a middle value, for example 7.

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**Algorithm 2 DetectError ( )**


---

**Input:** *DeltaKey1*, a set of  $\Delta K$  to be checked.

**Output:** The error-eliminated *DeltaKey1*.

```

1:   Errorlist ((a,b)) ← 0 (1 ≤ a ≠ b ≤ 16)
2:   for (each (a, b, c), 1 ≤ a ≠ b ≠ c ≤ 16)
3:       if ( DeltaKey1((a,b)) ⊕ DeltaKey1((b,c)) ≠ DeltaKey1((a,c)))
4:           Errorlist ((a,b)) ← Errorlist ((a,b)) + 1
5:           Errorlist ((a,c)) ← Errorlist ((a,c)) + 1
6:           Errorlist ((b,c)) ← Errorlist ((b,c)) + 1
7:       end
8:   end
9:   for (each (a, b), 1 ≤ a ≠ b ≤ 16)
10:      if (Errorlist ((a,b)) > ThEL)      erase DeltaKey1((a,b))
11:   end
12:   return (DeltaKey1)

```

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**Accumulate** step compares the newly obtained information in *DeltaKey2* and the accumulated information in *DeltaKey3*. Then *DeltaKey3* is refreshed with the union of *DeltaKey2* and *DeltaKey3*. An exception is that for some  $\Delta k_{a,b}$ , the corresponding values kept in *DeltaKey2* and *DeltaKey3* are different. Then they should be erased.

#### 4. Bitwise Collision Detection

Here we detail the bitwise collision detection and the related **PreparePowerTraces** step. The essential idea is to find the 1-bit collision between two bytes, and to treat other bits as noise by choosing plaintexts and acquiring power traces properly. The input of S-Box, (i.e.,  $K \oplus P$ ), is chosen as the attack target, and Hamming Weight is used as the power model. We denote the bits in a plaintext byte and a key byte with  $u$  and  $v$  :

$$\begin{aligned}
 P_j &= u_{j,8} \| u_{j,7} \| u_{j,6} \| u_{j,5} \| u_{j,4} \| u_{j,3} \| u_{j,2} \| u_{j,1} \\
 k_j &= v_{j,8} \| v_{j,7} \| v_{j,6} \| v_{j,5} \| v_{j,4} \| v_{j,3} \| v_{j,2} \| v_{j,1}
 \end{aligned}$$

#### 4.1 Preparation of Power Traces

For a partial attack, 8 power traces will be prepared. We use the most significant bit (i.e., bit 8) as an example to illustrate the process flow of the preparation of power traces:

- 1) Generate plaintexts of which the 8th bits of all the bytes are fixed (to zero for example). Other bits are random (e.g.,  $p_j = 0 \| u_{j,7} \| u_{j,6} \| u_{j,5} \| u_{j,4} \| u_{j,3} \| u_{j,2} \| u_{j,1}$  ( $1 \leq j \leq 16$ )).
- 2) Acquiring power traces with an oscilloscope that can average power traces in a real-time mode. Then only 1 power trace will be saved, denoted as  $T^8$ .
- 3) To further reduce the noise, the newly acquired power trace will be averaged along with those acquired in previous partial attacks. For the  $n$ th partial attack we have:

$$\bar{T}^{8,n} = (T^8 + \bar{T}^{8,n-1} (n-1)) / n \quad (4)$$

- 4) Cut  $\bar{T}^{8,n}$  into 16 sections:  $\bar{T}^8 = \{\bar{T}_1^8, \dots, \bar{T}_{16}^8\}$ . (The superscript  $n$  is omitted for simplicity.)

#### 4.2 Bitwise Collision Detection

As presented in Algorithm 3, we use  $\bar{T}_a^i$  and  $\bar{T}_b^i$  to detect the  $i$ th-bit collision between  $k_a$  and  $k_b$  ( $1 \leq a \neq b \leq 16$ ). Function **Distance** is the Euclidean distance of  $\bar{T}_a^i$  and  $\bar{T}_b^i$ :

$$\text{Distance}(\bar{T}_a^i, \bar{T}_b^i) = \sum_{j=1}^l (\bar{T}_{a,j}^i - \bar{T}_{b,j}^i)^2 \quad (5)$$

If (5) is less than  $Th_{CD}$ , we can guess that  $u_{a,i} \oplus v_{a,i} = u_{b,i} \oplus v_{b,i}$ . Since  $u_{a,i} = u_{b,i} = 0$ , we have  $D(i) = v_{a,i} \oplus v_{b,i} = 0$ .

---

#### Algorithm 3 Bitwise Collision Detection

---

**Input:** 8 power traces  $\bar{T}^1, \dots, \bar{T}^8$

**Output:** *DeltaKey1*, the most probable candidate of  $\Delta K$ .

```

1:   for (each (a, b), 1 ≤ a ≠ b ≤ 16)
2:       for (i=1, ... 8)
3:           if (Distance ( $\bar{T}_a^i, \bar{T}_b^i$ ) <  $Th_{CD}$ )    D(i) = 0
4:           else    D(i) = 1
5:           end
6:       end
7:       DeltaKey1((a,b)) = D
8:   end
9:   return (DeltaKey1)

```

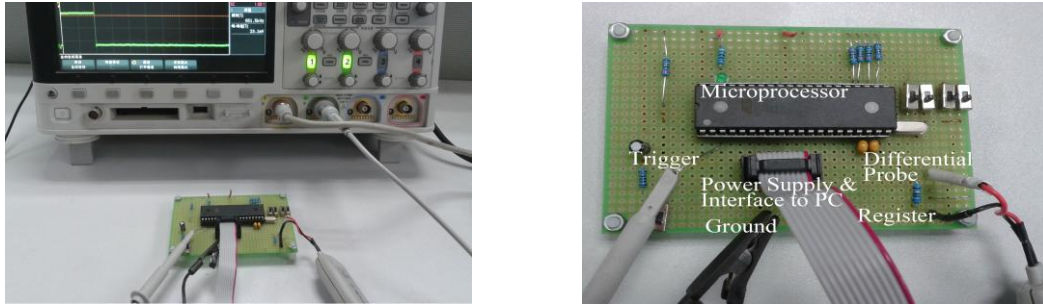
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$Th_{CD}$  should be chosen carefully to ensure the accuracy of collision detection. Since the result of **Distance** follows a chi-square distribution,  $Th_{CD}$  is relevant to the noise level. Here is an adaptively strategy to determine it: the median of the results of **Distance** can be chosen as  $Th_{CD}$  to make sure that they are divided into two groups with the similar sizes.

## 5. Experiments

### 5.1 Measurement Setup

As shown in **Fig. 2**, we built an experimental environment to mount the side-channel collision attacks. The target AES is implemented in a low-power, high-performance microcontroller AT89S52, which is suitable for various applications of WSN. A resistance of 10 Ohm is put in the power supply path of the microcontroller. An Agilent MSO-X 3054A oscilloscope with a differential probe is employed to acquire the voltage difference over the resistance which is related to the current consumed by the AT89S52. In our case, each raw power traces contains 10 000 points. For each partial attack, one power trace is averaged from  $m$  raw power traces. Here we set  $m$  to be 300.



**Fig. 2.** Measurement setup of collision attacks on AT89S52.

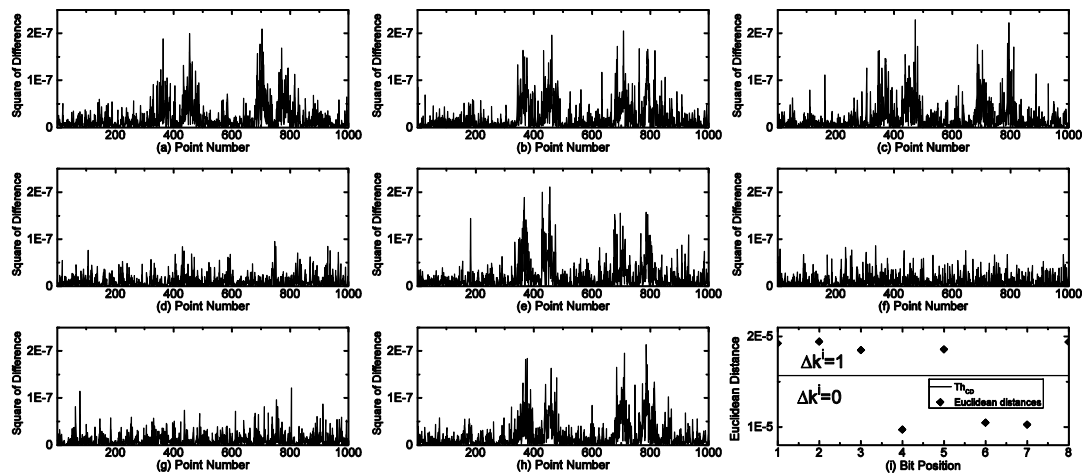
## 5.2 Bitwise Collision Detection

For each pair of key bytes  $(k_a, k_b)$ , we use bitwise collision detection method to find out  $\Delta k_{a,b}$ . Here we use  $(k_1, k_2)$  as an example to detail how it works, where

$$k_1 = \alpha_8 \parallel \alpha_7 \parallel \alpha_6 \parallel \alpha_5 \parallel \alpha_4 \parallel \alpha_3 \parallel \alpha_2 \parallel \alpha_1 = 01110010$$

$$k_2 = \beta_8 \parallel \beta_7 \parallel \beta_6 \parallel \beta_5 \parallel \beta_4 \parallel \beta_3 \parallel \beta_2 \parallel \beta_1 = 10011011$$

**Fig. 3** shows the detection results. **Fig. 3(a)-(h)** correspond to the collision detection results of bit 8-1. For example, **Fig. 3(a)** shows  $(\bar{T}_1^8 - \bar{T}_2^8)^2$ . There exist obvious peaks, because  $\alpha_8 \neq \beta_8$ . In **Fig. 3(d)**, the curve  $(\bar{T}_1^5 - \bar{T}_2^5)^2$  is close to zero, suggesting that  $\alpha_5 = \beta_5$ . Finally, the Euclidean distances of 8 bits and a threshold line ( $Th_{CD}$ ) are plotted in **Fig. 3(i)**. Here we have  $\Delta k_{1,2} = 11101001$ .



**Fig. 3.** The result of bitwise collision detection between  $k_1$  and  $k_2$ .



### 5.3 Error Detection

After collision detection, a guessed  $\Delta K$  is produced and kept in *DeltaKey1*. Then the error detection method is used to screen out the wrong part of  $\Delta K$ . For the sake of simplicity, we focus on the triplet  $\Delta k_{1,2}$ ,  $\Delta k_{1,3}$ , and  $\Delta k_{2,3}$  to illustrate the workflow of our framework, where

$$\Delta k_{1,2} = 11101001 \quad \Delta k_{1,3} = 11101000 \quad \Delta k_{2,3} = 00000001.$$

As shown in Fig. 4, the triplet  $\Delta k_{1,2}$ ,  $\Delta k_{1,3}$ , and  $\Delta k_{2,3}$  are recovered within 2 partial attacks. In partial attack 1, the wrong guessed  $\Delta k_{2,3}$  is discarded after error detection, and  $\Delta k_{1,2}$ ,  $\Delta k_{1,3}$  are delivered to *DeltaKey2*. Similarly, in partial attack 2, the false guess of  $\Delta k_{1,3}$  is discarded. In the **Accumulate** step, the information of two partial attacks is merged together, then  $\Delta k_{1,2}$ ,  $\Delta k_{1,3}$ , and  $\Delta k_{2,3}$  are revealed. All the other parts of  $\Delta K$  are recovered in the same way, and finally the key of AES is recovered.

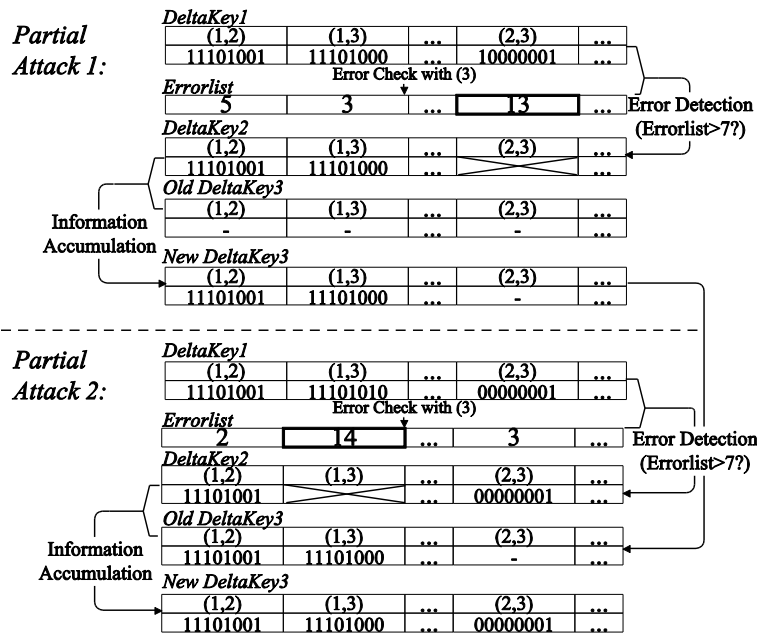


Fig. 4. Recovery process of  $\Delta k_{1,2}$ ,  $\Delta k_{1,3}$ , and  $\Delta k_{2,3}$ .

## 6. Improved Framework with Error-Tolerant Mechanism

Here we propose an error-tolerant version of our approach. Our original approach is a binary test and has a low cost of computation. The correlation-enhanced method produces a list of candidates of  $\Delta k_{a,b}$ , and increases the success rate at the expense of larger computation amount. Our improved approach uses the concept of list to realize an error-tolerant mechanism and keeps the computation amount at a reasonable level. Improvements are mainly made in **DetectCollision** and **DetectError** steps:

### 6.1 Modified Bitwise Collision Detection

To increase the number of candidates of each  $\Delta K$ , the most straight forward idea is to include the 8 hypothetical values which are one-bit different from the most probable one. The output of



the **DetectCollision** step,  $\Delta Key1$ , then becomes a  $9 \times 120$  matrix. The elements of the matrix are denoted as  $\Delta Key1(i, (a, b))$  ( $1 \leq i \leq 9, 1 \leq a \neq b \leq 16$ ).

## 6.2 Modified Error Detection

There are two main changes in the modified error detection method as presented in Algorithm 4: 1) The input  $\Delta Key1$  becomes a  $9 \times 120$  matrix, and the first row of  $\Delta Key1$  is checked in loop 1 (step 2-6); 2) In loop 2, if  $Errorlist((a, b)) > Th_{EL}$ , other 8 candidates will be checked in turn, as shown in Algorithm 5. Only if no candidate passes the check will  $\Delta Key1(1, (a, b))$  be erased, or it will be replaced by the candidate which leads to the minimum  $Errorlist((a, b))$ .

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### Algorithm 4 DetectError ( ) (Modified)

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**Input:**  $\Delta Key1$ , a  $9 \times 120$  matrix, including 9 candidates of  $\Delta K$ .

**Output:** The error-eliminated  $\Delta Key1$  ( $1 \times 120$ ).

```

1:   Errorlist((a,b)) ← 0 (1 ≤ a ≠ b ≤ 16)
2:   for (each (a, b, c), 1 ≤ a ≠ b ≠ c ≤ 16)
3:       if ( ΔKey1(1,(a,b)) ⊕ ΔKey1(1,(b,c)) ≠ ΔKey1(1,(a,c)))
4:           Errorlist((a,b)) ← Errorlist((a,b)) + 1
           Errorlist((a,c)) ← Errorlist((a,c)) + 1
           Errorlist((b,c)) ← Errorlist((b,c)) + 1
5:       end
6:   end
7:   for (each (a, b), 1 ≤ a ≠ b ≤ 16)
8:       if (Errorlist((a,b)) > ThEL) EnumerateCheck(ΔKey1(i,(a,b)), (1 ≤ i ≤ 9))
9:   end
10:  return (the first row of ΔKey1)

```

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### Algorithm 5 EnumerateCheck ( )

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**Input:**  $\Delta Key1(i, (a, b))$  ( $1 \leq i \leq 9$ ), candidates of  $\Delta k_{a,b}$

```

1:   temp1 ← Errorlist(a, b), temp2 ← 1
2:   for (i = 2, ..., 9)
3:       Errorlist(a, b) ← 0
4:       for (1 ≤ c ≤ 16, c ≠ a, c ≠ b)
5:           if ( ΔKey1(i,(a,b)) ⊕ ΔKey1(1,(b,c)) ≠ ΔKey1(1,(a,c)))
6:               Errorlist(a, b) ← Errorlist(a, b) + 1
7:           end
8:       end
9:       if (Errorlist((a,b)) < temp1)   temp1 ← Errorlist((a,b)), temp2 ← i
10:  end
11:  if (temp1 < ThEL)   ΔKey1(1,(a,b)) ← ΔKey1(temp2,(a,b))
12:  else   erase ΔKey1(1,(a,b))
13:  end
14:  return

```

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## 7. Efficiency Comparison

We do simulations in MATLAB to compare the efficiency of our attack and the LDPC method. The comparisons include the success rate and time (online time and offline time).

### 7.1 Online Time vs. Success Rate

We denote the time for the oscilloscope to capture and average a power trace as  $\tau_A$ , and the time to save a trace as  $\tau_S$ . In our case where one power trace contains 10 000 sample points,  $\tau_S$  is roughly 50 times of  $\tau_A$ . Let  $m$  be the number of power traces to be averaged,  $n$  be the number of partial attacks, the total online time  $\tau_{OL}$  is

$$\tau_{OL} = 8n(m\tau_A + \tau_S) = 8n(0.02m + 1)\tau_S. \quad (6)$$

In Our original version, we fix  $m = 300$ , so

$$\tau_{OL} = 56n\tau_S. \quad (7)$$

In the error-tolerant version, we set  $m = 50$ , so

$$\tau_{OL} = 16n\tau_S. \quad (8)$$

In order to assess the efficiency, we plot the success rates of attacks as a function of online time  $\tau_{OL}$ , rather than the number of raw power traces, by sweeping the upper limit of  $n$ . As shown in Fig. 5, our original approach (denoted as DS) is more efficient than the LDPC method when the online time is less than  $900\tau_S$ . The error-tolerant version (denoted as DS-ET) achieves an obvious gain in efficiency. The online time needed to reach a success rate of 0.9 is 90% less than that of LDPC method.

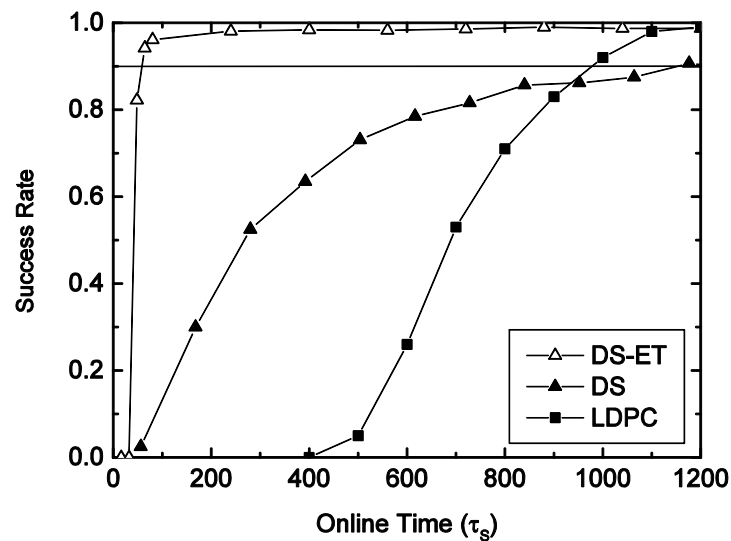


Fig. 5. The success rates as a function of online time  $\tau_{OL}$ .

## 7.2 Online Time vs. Offline Time

Offline time reflects the computational complexity of the attack algorithm. We examined the operation time for three algorithms (LDPC, DS, and DS-ET) to carry out 1000 attacks. As shown in Fig. 6, the computational complexity of LDPC method is significantly higher than our approaches. The error-tolerant version of our attack needs least offline time to recover the key.

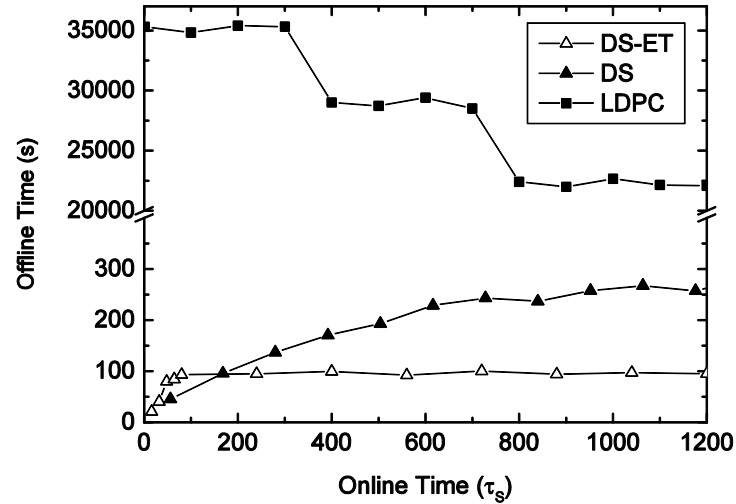


Fig. 6. The offline time as a function of online time  $\tau_{OL}$ .

## 7.3 Selection of Parameters

The former experiments are done with a fixed  $m$ . Here we focus on the impacts of  $m$  on the success rates of attacks.

As shown in Fig. 7, the success rate curves reach to a larger upper limit with larger  $m$ . However, increasing  $m$  also increases the time for each partial attack. So there is no need to increase  $m$  once the upper limit of success rate is close to 1. In our case (the error-tolerant version),  $m = 50$  is reasonable.

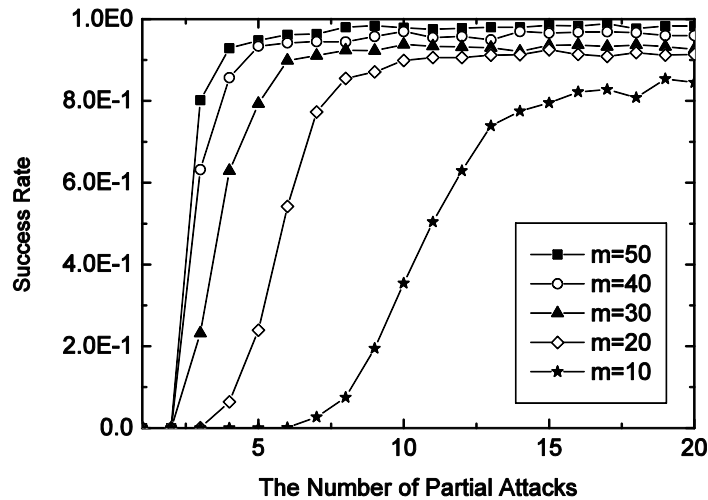


Fig. 7. The success rates with different average times  $m$  as a function of  $n$  (the number of partial attacks).

## 8. Conclusion

We propose a double sieve collision attack based on bitwise collision detection in this paper, and give an error-tolerant version which significantly reduces the time of online stage. Practical attacks are successfully mounted on AES implemented in a real chip which can be used in WSN. We also compare the efficiency of our attack with the work published by Gérard *et al.* [18]. The experiment result shows our attack saves 90% of time to reach a success rate of 0.9.

Although AES is the target algorithm in this paper, our work can be extended to other symmetry cryptography algorithms that are vulnerable to collision attack.

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