

# Supervoxel-based Staircase Detection from Range Data

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**Abstract:** In this paper, we propose a supervoxel clustering-based staircase extraction algorithm to obtain poses and dimensions of staircases from a point cloud. In order to effectively reduce the candidate points and accelerate supervoxel clustering, large planes in the scene, such as walls, floors, and ceilings, are eliminated while scanning the environment. Next, staircase candidates with small planes are initially estimated using supervoxel clustering. Then, parameter values for the staircases are refined, and higher staircases that remain undetected due to occlusion are predicted and generated virtually. Experimental results show that staircases are detected accurately and predicted successfully.

**Keywords:** Staircase, Plane detection, Supervoxel clustering, Prediction, Point cloud

## 1. Introduction

Mobile robots have become more commonplace in commercial and industrial settings. Mobile robots that perform human tasks move around their environment. Robots have been used in hospitals to move materials for many years. Recently, mobile robots have begun operating in multi-floor indoor environments where staircases are common features. However, mobile robots often encounter difficulties in identifying and navigating staircases. The ability to safely identify and navigate staircases is important for the prevention of serious injury to people and damage to the mobile robots [1]. In order to perform human tasks in multi-floor indoor environments, it is important to have a detection method for stairs that are present when moving to a target location.

To detect staircases, a method using random sample consensus (RANSAC) was proposed [1]. This method uses the Microsoft Kinect to find staircases in the same interval. But the results from detection include points that correspond to walls connected to staircases. Therefore, elimination of points for other components is needed. To solve this problem, it is necessary for the points of walls, ceilings, and floors to be eliminated. To eliminate these objects, a method of plane detection is needed.

An et al. proposed a fast plane-detection method that detects planes during data gathering [3]. While scanning the environment, points are converted into line segments and clustered onto planes. It is effective for calculations to be processed during point cloud acquisition. However, this method easily fails to detect planes for small areas.

In this paper, we propose a supervoxel clustering-based staircase extraction algorithm to accurately obtain poses and dimensions of staircases. For stairs that are undetected due to occlusion, a method to predict undetected stairs is also presented.

## 2. Proposed Method

Fig. 1 shows a flow chart of our proposed algorithm. At first, we eliminate points of large planes, like walls, floors and ceilings, to reduce the processing time of the method and eliminate unrelated points that exist. In this process, we apply a plane detection method, which is processed per scan [3]. For the remaining points, we extract staircase parameters using a supervoxel clustering-based staircase extraction algorithm, and create virtual steps by predicting ascent staircases by using the extracted parameters. In Section 1, we reviewed a detection method [3], and in the

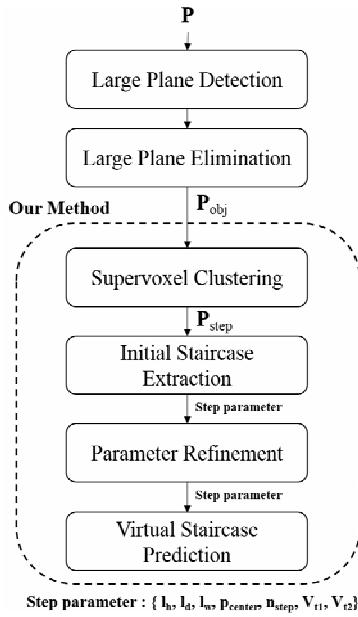


Fig. 1. Flow chart of the proposed stair-detection method.

next section, we introduce the proposed stair detection algorithm.

## 2.1 Large Plane Detection

### 2.1.1 Line Segment Extraction

In each scan, points  $p_i$  can be described by range and bearing from light detection and ranging (LIDAR), so  $(\rho_i, \theta_i)$  is obtained.  $p_i$  can be converted to 2D Cartesian coordinates  $(\rho_i \cos \theta_i, \rho_i \sin \theta_i)$ . To extract line segments, a breakpoint representing discontinuities in the sequence of scan points is detected per scan. A breakpoint detection algorithm examines the distance between two consecutive points  $(p_i, p_{i-1})$  using the following condition:

$$\|p_i - p_{i-1}\| < D_0, \quad (1)$$

where  $D_0$  is a threshold. If Eq. (1) is satisfied,  $p_i$  and  $p_{i-1}$  are considered to be in the same cluster. Otherwise,  $p_i$  and  $p_{i-1}$  are considered breakpoints and are put into different clusters. The distance between two consecutive points is proportional to  $\rho_{i-1}$ . So,  $D_0$  should be dependent on  $\rho_{i-1}$ . An intuitive method for  $D_0$  was proposed [4]:

$$D_0 = \rho_{i-1} \cdot \sin(\Delta\phi) / \sin(\lambda_u - \Delta\phi) + 3\sigma_d, \quad (2)$$

where  $\varphi$  is the sensor resolution, and  $\lambda_u$  is chosen on the basis of user experience. The term  $3\sigma_d$  is added in order to account for noise associated with  $\rho_i$  when  $p_i$  is close to the sensor frame origin. Quantitative determination of  $\lambda$  is an unresolved problem, but in mobile robot applications  $\lambda = 10^\circ$  has been reported to be satisfactory.

After finding the breakpoint process, clusters include a polygonal line. To include only the line segment, a

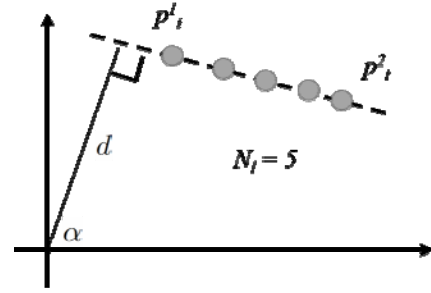


Fig. 2. Parameters of a line.

splitting process that divides the polygonal line into line segments is performed. To do this, iterative end-point fitting (IEPF) was adopted. This method has been used in many vision and robotics applications. First, the line segment  $li$  is generated by the end of two points of a cluster. Next, the distances  $h_j$  between the line and points included in a cluster are calculated. The maximum value of  $h_j$  is compared with threshold  $h_0$ . If  $h_{j(\max)}$  is bigger, the cluster is divided into two clusters at the point corresponding to  $h_{j(\max)}$ .

Each cluster after the splitting process can be expressed by line parameters, as shown in Fig. 2.  $p_i^1, p_i^2$  is two end points of a line, and  $N_i$  is the number of points included in the line segment. After extraction of the line segment, a merging process is performed to combine short line fragments by checking the following condition:

$$|\alpha_i - \alpha_j| < \alpha_0 \wedge \|p_i^2 - p_j^1\| < d_0. \quad (3)$$

Also, lines that are not effective in the detection of a plane are eliminated. These are lines that are found to be less than threshold  $L_{\min}$ , or that have too few scan points.

$$\|p_i^2 - p_j^1\| < L_{\min} \vee n_i < N_e. \quad (4)$$

The line segment extracted in each scan step is represented by two-dimensional (2D) coordinates, and it has to be converted into 3D coordinates. Dimensions of two 2D end points of a line segment are converted into 3D points represented by  $W = (u, v)$  by using scan information of the end point and the angle of actuator  $\psi$ .

$$\begin{aligned} W_x &= \rho \cos \theta, \\ W_y &= \rho \sin \theta \cdot \cos(\psi - \frac{\pi}{2}), \\ W_z &= \rho \sin \theta \cdot \sin(\psi - \frac{\pi}{2}). \end{aligned} \quad (5)$$

Also, direction vector  $\delta_i$ , which is defined by  $(u_i^k - v_i^k) / \|u_i^k - v_i^k\|$ , is generated.

### 2.1.2 Line Clustering

After extraction of line segments, clustering is processed to group lines that belong to the same plane. If the

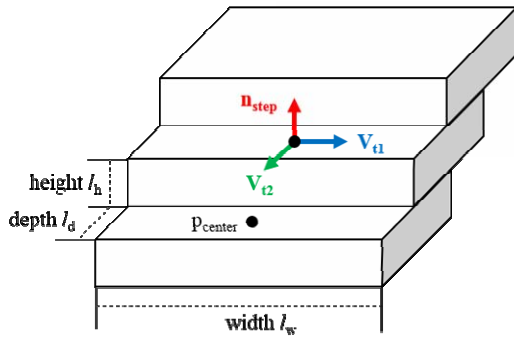


Fig. 3. Parameters of staircases.

points of a plane are obtained by our scanning system, the directions of the lines are similar. The line extracted in each scan is compared with representative direction  $\delta_j$  using the following condition:

$$|\delta_j \cdot \delta_m| > \delta_c \quad (6)$$

where  $\delta_m$  is the direction vector that represents each cluster. If Eq. (6) is satisfied, the line is included in the cluster, and  $\delta_m$  is recalculated by simple moving average (SMA):

$$\delta'_m = (N_m \delta_m + \delta_j) / (N_m + 1) \quad (7)$$

where  $N_m$  represents the number of lines included in the cluster.

### 2.1.3 Plane Fitting

To parameterize the plane of each cluster, a line segment of cluster  $\lambda_i$  is selected randomly. And we select the two line segments,  $\lambda_{i-1}, \lambda_{i+1}$ , that are closest and second closest to  $\lambda_i$ . The plane parameters  $n_j$  and  $d_j$  are determined by calculating the singular value decomposition (SVD) on six end points of three selected line segments.

## 2.2 Large Plane Elimination

After large planes, such as walls, floors, and ceilings, are detected, a partial point cloud,  $\mathbf{P}_{obj}$ , is obtained by removing from  $\mathbf{P}$  the points belonging to the large planes. Our proposed method detects staircases from  $\mathbf{P}_{obj}$ , and extracts several parameters, including dimensions ( $l_d, l_h, l_w$ ) and poses ( $n_{step}$ ) of the staircases, as shown in Fig. 3. This large-plane elimination process reduces the number of points significantly, and thus, improves efficiency of the proposed staircase detection method.

## 2.3 Staircase Detection

In the proposed method, the approximate positions of steps are extracted using supervoxel clustering. Then, the detected stairs are refined to optimize the parameters of the staircases. Finally, the staircases that have not been detected due to occlusion are predicted and generated virtually.

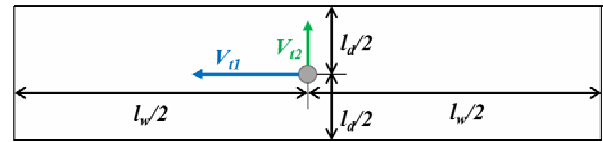


Fig. 4. Parameters of a step.

### 2.3.1 Supervoxel Clustering

In order to find the approximate position of a staircase, supervoxel clustering is employed. Supervoxel clustering groups points into perceptually meaningful regions that are homogeneous with respect to location and normal vectors. Supervoxel  $V_i$  is generated by using supervoxel clustering. Based on the fact that the plane of each step is parallel to the floor plane, we eliminate supervoxels where normal vector  $n_{vi}$  does not satisfy the following condition:

$$|n_{floor} \cdot n_{vi}| > \delta_n, \quad (8)$$

where  $n_{floor}$  represents the normal vector of the floor plane.

In order to get rid of supervoxels corresponding to other objects, rather than staircases, supervoxels having similar height with respect to the floor plane are merged into the same cluster. A cluster corresponding to a step usually consists of several supervoxels. Therefore, a cluster having a small number of supervoxels is eliminated. Points belonging to each cluster are denoted by  $\mathbf{P}_{step}$ .

### 2.3.2 Initial Staircase Extraction

To extract the parameters from each cluster, principal component analysis (PCA) is applied to  $\mathbf{P}_{step}$ . Then, eigenvectors represent two tangential vectors and one normal vector, as shown in Fig. 3.

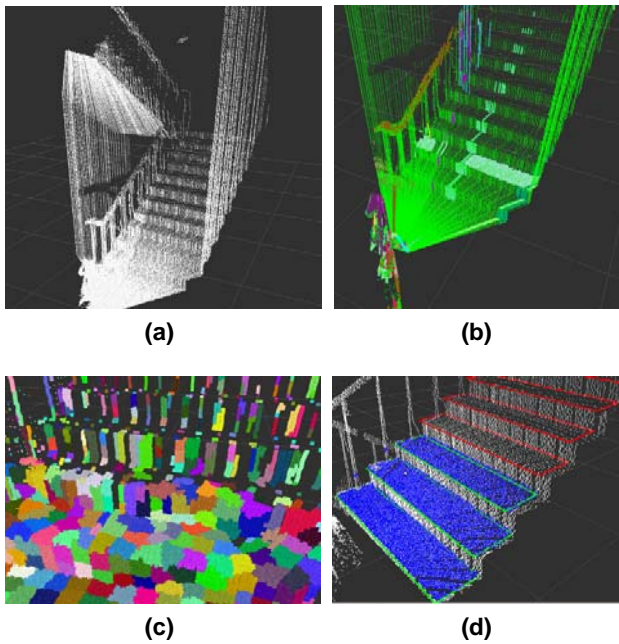
To calculate  $l_w$ , we first calculate signed distances of all the points in  $\mathbf{P}_{step}$  to a plane that has a normal vector of  $V_{t1}$  and that passes through the center of mass for  $\mathbf{P}_{step}$ , as shown in Fig. 4. Because only points of the staircase are projected, the maximum value of the projection distance is part of a width. So,  $l_w$  is calculated by addition of a projection distance using  $V_{t1}$  and  $V_{t2}$ . Calculation of  $l_d$  is similar to that of  $l_w$ .

### 2.3.3 Parameter Refinement

Unfortunately, the parameter values obtained in the previous process are incorrect, because  $\mathbf{P}_{step}$  contains outliers as well. In order to refine the parameters of steps, a range for staircase  $R_1$  is calculated using the  $l_w$  and  $l_d$ .

$$R_1 = \sqrt{l_w^2 + l_d^2} \quad (9)$$

Then,  $\mathbf{P}_{refined}$  is obtained, which has points within the range of  $R_1$  with respect to the center of mass of  $\mathbf{P}_{step}$ . In this process, points of other objects connected with the staircases, including fences and handrails, can be



**Fig. 5. The environment of stair detection: (a) The entire point cloud, (b) The plane extracted via line-based method [3], (c) The result of supervoxel clustering, (d) The staircases that are detected (green) and predicted (red).**

eliminated. Next,  $\mathbf{P}_{\text{refined}}$  is projected to  $n_{\text{step}}$  and extracts points  $\mathbf{P}_{\text{step}}$ , which can determine a step. To calculate the parameter of a step, we use the same process as in subsection 2.3.2.

### 2.3.4 Virtual Staircase Prediction

Due to occlusion and viewing angle, a small number of points are sensed for higher steps, and thus, a few steps are detected. Thereafter, we generate virtual steps to use the information effectively. Because each parameter of a step is similar, we can calculate predicted parameters using a mean of the calculated parameters.

## 3. Experimental Results and Conclusions

To implement our proposed method, we used a rotating 2D scanning LIDAR with an actuator in the environment, as shown in Fig. 5(a). At first, we applied a line segment-based plane detection method [3], as shown in Fig. 5(b). With the parameter values to extract planes of small sizes, the method cannot find large planes because of noise. In addition, an incorrect plane segmenting the steps vertically was also detected.

The result of supervoxel clustering is shown in Fig. 5(c). Compared with lower steps, supervoxels corresponding to upper steps do not have enough information to calculate parameters because of sparsity of points.

The green rectangles shown in Fig. 5(d) represent the staircase calculated by our proposed method. For the

higher steps, we generated virtual steps represented by red rectangles using calculated parameter values.

We proposed a supervoxel clustering-based stair detection method to obtain the position and orientation of staircases. Before applying our method, we eliminate large planes, including walls, floors, and ceilings. Then, staircases are initially detected by using supervoxel clustering. Finally, unextracted staircases are predicted. As a result, staircases are calculated and predicted successfully.

## References

- [1] T. Tang, W. Lui and W. Li, "Plane-based detection of staircases using inverse depth", in Proc. Of ACRA 2012, Dec. 2012. [Article \(CrossRef Link\)](#)
- [2] M. Y. Yang and W. Forstner, "Plane detection in point cloud data", Technischer Reprort, Institute of Geodesy and Geoinformation, Dept. of Photogrammetry, 2010. [Article \(CrossRef Link\)](#)
- [3] S. Y. An, L. K. Lee and S. Y. Oh, "Line segment-based fast 3D plane extraction using nodding 2D laser range finder", Robotica, pp. 1-24, September 2014. [Article \(CrossRef Link\)](#)
- [4] G. A. Borges and J. J. Aldon, "Line extraction in 2D range images for mobile robotics", Journal of Intelligent and Robotics Systems, Vol. 40, pp. 267-297, Jul. 2004, doi:10.1023/B:JINT.0000038945.55712.65 [Article \(CrossRef Link\)](#)