

# DVB-S3 시스템의 64-APSK 방식에 대한 연관정 비트 검출 기법

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## A Soft Demapping Method for 64-APSK in the DVB-S3 System

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### 요 약

본 논문에서는 DVB-S3 시스템에 정의되어 있는 64-APSK 변조 방식에 대한 연관정 비트 검출 기법을 제안한다. 본 논문에서 제안한 방식은 심볼을 구성하고 있는 각 비트에 대하여 경관정 경계(hard decision threshold; HDT) 선을 이용한 방법으로써, 수신단에서 검출된 심볼과 HDT 선과의 거리를 연관정 값으로 계산하는 것이다. HDT가 간단하게 결정될 경우 복잡도는 기존의 지수적 복잡도를 요구하는 최우(maximum likelihood; ML) 검출 기법에 비하여 매우 급격히 감소될 수 있다. 이러한 점을 고려하여, 본 논문에서는 먼저 64-APSK에 대한 각 구성 비트별 HDT 선을 유도하고, 이를 이용하여 연관정 비트 값을 계산할 수 있는 방법을 제안한다. 연관정 입출력을 필요로 하는 터보부호를 이용하여 ML 기법과 성능을 비교한 결과, 본 논문에서 제시한 방법은 ML 기법보다 적은 복잡도를 가지고 거의 유사한 성능을 도출할 수 있음을 보였다.

**Key Words** : satellite communication, soft demapping, 64-APSK, DVB-S3, satellite broadcasting.

### ABSTRACT

In this paper, we propose a soft demapping method for 64-ary APSK in the DVB-S3 system. The proposed method in this paper uses the hard decision threshold (HDT) line for each constituent bit in a symbol, and calculates the soft bit information with the distance between the HDT line and the detected symbol. If the HDT lines are defined in a simple manner, the complexity to estimate soft information can be largely reduced compared with the maximum likelihood detection (MLD) which has an exponential complexity. By considering this, we first derive HDT lines for each constituent bit for a 64-APSK symbol, and propose a method to calculate soft bit information. We simulate the BER performance of the proposed scheme by using a turbo codes which requires soft-input-soft-output information, and compare it that of the MLD. The result show that the proposed scheme produces approximating performance to MLD with largely reduced complexity.

## I. Introduction

Digital Video Broadcasting via Satellite-Second Generation (DVB-S2), was standardized by the European Telecommunications Standards in 2005 [1]. It specifies several advanced techniques to enhance the service quality, which enable two-way interactive service. For example, an adaptive coding and modulation techniques was adopted in combination with  $M$ -ary amplitude and phase shift keying (APSK) schemes up to 32-APSK and low density parity check (LDPC) codes. As an extension

of DVB-S2 standard, DVB-S3 defines 64-APSK modulation scheme [2]. The FEC scheme with LDPC codes produce excellent performance, approximating to the Shannon limit, mainly because of iterative decoding with soft-input-soft-output. For this reason, accurate soft bit information (SBI) should be provided to the decoder input.

A soft demapping scheme, more generally known as a soft decision demodulation (SDD) scheme, refers to the process of extracting soft bit information from a detected symbol at the receiver. A maximum-likelihood (ML) SDD scheme, can achieve the maximum performance. However,

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the complexity of ML SDD scheme increases in exponential order by the modulation order, and thus it is infeasible to implement for a high order modulation scheme.

An efficient soft demapping scheme with a linear order was proposed in order to solve the complexity problem [3]. In this schemes, the SBI is calculated by a liner metric, which is the distance between the hard decision threshold (HDT) line and the detected symbol, and thus computational complexity is largely reduced. In order to use this idea, we first propose the HDT lines for each constituent bit in a 64-APSK symbol, and subsequently derive equations to estimate SBI.

The remainder of this paper is organized as follows. Section II presents 64-APSK constellation in the DVB-S3 system, and presents conventional soft demapping methods based on exhaustive search. The ML soft demapping method using log-likelihood ratio (LLR) will be introduced first, and a Max LLR method for eliminating computations of exponential and log operations will be introduced. In section III, we define HDT lines for six constituent bits for a 64-APSK symbol, and derive the corresponding equation to calculate SBI. In section IV, we present simulation results. Finally, we draw conclusions in section V.

## II. Soft demapping for 64-APSK in DVB-S3

### 1. Constellation of 64-APSK

A constellation diagram of the 64-APSK defined in the DVB-S3 system is shown in Fig. 1, where there are four circles [2]. A complex 64-APSK symbol,  $s_{(\iota,i)}$  located at the  $i$ th point on the  $\iota$ th ring, can be represented as follows:

$$s_{(\iota,i)} = r_\iota e^{j(\frac{2\pi}{n_\iota})i + \theta_\iota}, \quad i = n_\iota - 1, \quad (1)$$

where  $n_\iota$ ,  $r_\iota$  and  $\theta_\iota$  are the number of symbols in the points  $\iota$ th ring, the radius and relative phase shift for the  $\iota$ th ring, respectively.

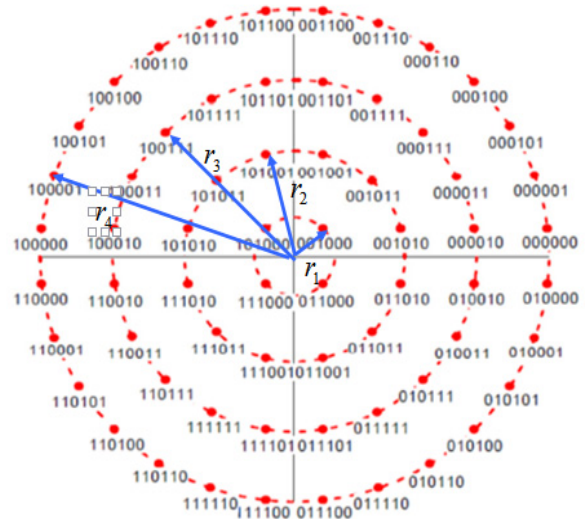


Fig. 1. 64-APSK Constellation

### 2. ML Detection with LLR Estimation

The objective of ML demodulator is to compute maximum a posteriori LLRs for all the information bits of the received symbol. We consider that  $P(b_i = 1) = P(b_i = 0) = 1/2$ , where  $b_i$  is the  $i$ th transmitted bit, then the LLR can be represented as follows:

$$L(b_i|r) = \log \left( \frac{\sum_{s:b_i=1} \exp(-\frac{1}{2\sigma^2} \|r - hs\|^2)}{\sum_{s:b_i=0} \exp(-\frac{1}{2\sigma^2} \|r - hs\|^2)} \right), \quad (2)$$

where  $s$  denotes an  $M$ -ary modulation symbol, and each element of  $s$  is composed of  $m = \log_2(M)$ , which is 6 for 64-APSK, information bits of  $b_i$ ,  $h$  is a channel gain,  $\sigma^2$  is the variance of additive white Gaussian noise (AWGN), and  $r$  is the received symbol.

In order to reduce the computational complexity, the idea is to approximate each of the sums in (1) by its largest term, which gives Max LLR values as follows:

$$L(b_i|r) \approx \frac{1}{2\sigma^2} [\min_{s:b_i=0} \|r - hs\|^2 - \min_{s:b_i=1} \|r - hs\|^2]. \quad (3)$$

Without losing generality, we assume a complex modulation scheme with in-phase (I) and quadrature-phase (Q) channels. Let us consider a BPSK scheme where a single bit is contained in a symbol and thus a real part of  $s$ ,  $R(s)$  is transmitted via the

I-channel. Assuming a detected symbol with perfect channel estimation, the detected symbol  $\hat{s}$  can be represented as follows[3][4]:

$$\hat{s} = \frac{h^*}{\|h\|^2} r. \quad (4)$$

Therefore, LLR value from ML detection in (2) for  $b_1$  can be derived:

$$\begin{aligned} L(b_1|r) &= \log \left( \frac{\exp(-\frac{1}{2\sigma^2} \|r-h\|^2)}{\exp(-\frac{1}{2\sigma^2} \|r+h\|^2)} \right) \\ &= \frac{1}{2\sigma^2} (\|r+h\|^2 - \|r-h\|^2) \\ &= \frac{1}{2\sigma^2} (\|h\hat{s}+h\|^2 - \|h\hat{s}-h\|^2) \\ &= \frac{4\|h\|^2}{2\sigma^2} R(\hat{s}) \\ &= \omega R(\hat{s}), \end{aligned} \quad (5)$$

where  $\omega = 2\|h\|^2/\sigma^2$ .

From (5), we can clearly see that  $L(b_1|r)$  is equivalent to the distance between the HDT line and the detected symbol  $\hat{s}$  multiplied with a weighting factor,  $\omega$ . By extending this idea, SBI is the distance between HDT line multiplied with the factor  $\omega$ , i.e.,

$$L(b_i|r) = \omega \hat{b}_i(\hat{s}), \quad (6)$$

where  $\hat{b}_i(r)$  is the distance between  $\hat{s}$  and the  $i$ th HDT line.

### III. HDT based Soft demapping for 64-APSK

#### 1. HDT method for 64-APSK

We extend the concept of soft demapping using HDT to 64-APSK, so that SBI for the  $i$ th bit,  $L(b_i|r) = \omega \hat{b}_i(\hat{s})$ . In Fig. 2, the HDT lines for the first and second soft bits are represented, where  $H_i$  is the HDT line for the  $i$ th bit, and  $\hat{b}_i(\hat{s})$  can be written as:

$$\hat{b}_1 = -R(\hat{s}), \quad \hat{b}_2 = -I(\hat{s}), \quad (7)$$

where  $I(\hat{s})$  is the imaginary part of the detected symbol.

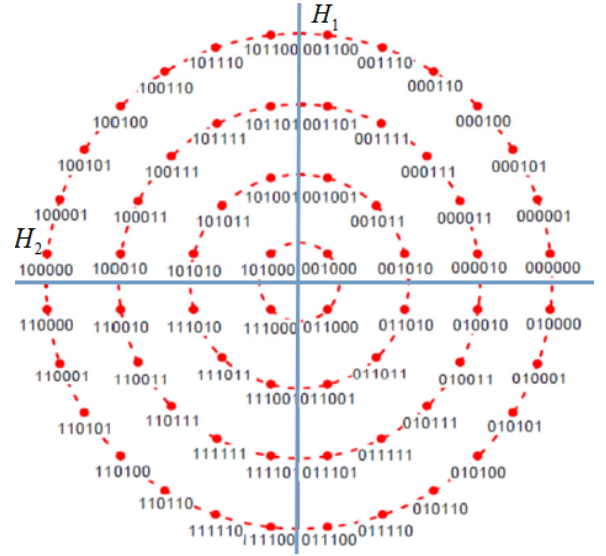


Fig. 2. HDT for the first and second bit of a 64-APSK symbol

In Fig. 3 and Fig. 4, the HDT lines for the third and fourth bits are represented. Because  $H_4$  is the rotated version of  $H_3$ , calculation of SBI for the third bit automatically provides the value for SBI for the fourth bit as expressed in (8) and (9), respectively.

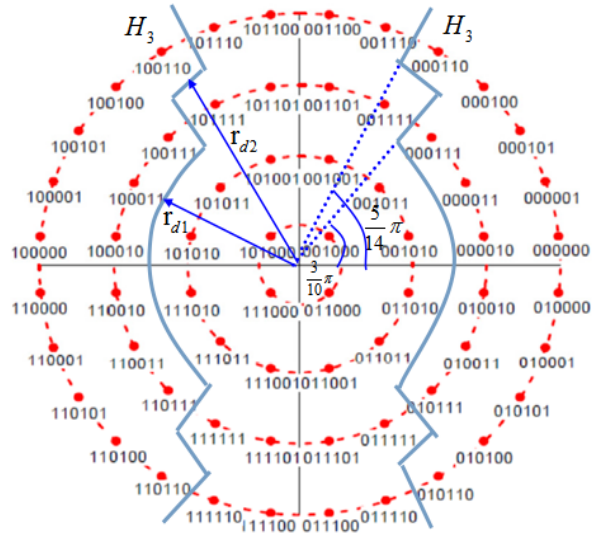


Fig. 3. HDT for the third bit of a 64-APSK symbol

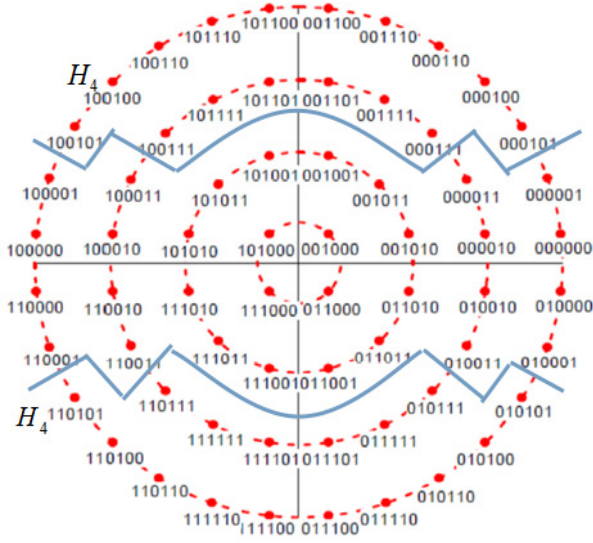


Fig. 4. I HDT for the fourth bit of a 64-APSK symbol

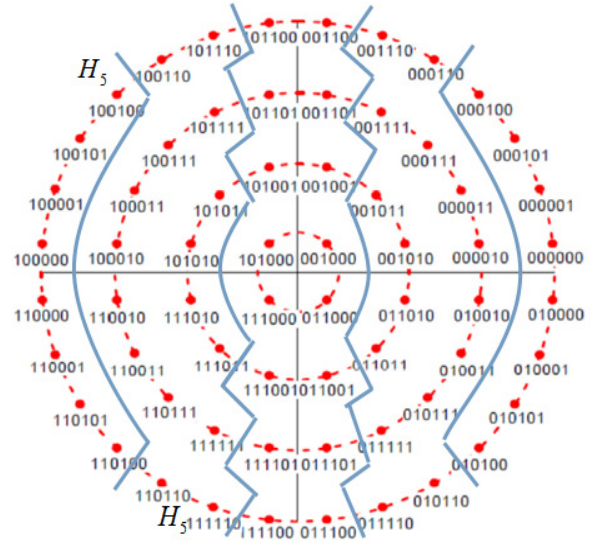


Fig. 5. HDT for the fifth bit of a 64-APSK symbol

$$\hat{b}_3(r) = \begin{cases} r_{d_1} - \|r\|, & \text{if } \theta_r \leq \frac{3}{10}\pi, \|r\| \leq r_{d_2}, \\ \left\| r - r_{d_1} e^{j\frac{3}{10}\pi} \right\|, & \text{if } \theta_r > \frac{3}{10}\pi, \|r\| \leq r_{d_2}, \\ -\min\{\|r\| - r_{d_1}, \|r\| \sin(\frac{3}{10}\pi - \theta_r)\}, & \text{if } \theta_r \leq \frac{3}{10}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ \min\{r_{d_2} - \|r\|, \|r\| \sin(\theta_r - \frac{3}{10}\pi)\}, & \text{if } \frac{3}{10}\pi < \theta_r \leq \frac{5}{14}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ \left\| r - r_{d_2} e^{j\frac{5}{14}\pi} \right\|, & \text{if } \frac{5}{14}\pi < \theta_r, r_{d_2} < \|r\| \leq r_{d_3}, \\ -\min\{\|r\| - r_{d_1}, \left\| r - r_{d_2} e^{j\frac{3}{10}\pi} \right\|\}, & \text{if } \theta_r < \frac{3}{10}\pi, \|r\| > r_{d_3}, \\ -\min\{\|r\| - r_{d_2}, \|r\| \sin(\frac{5}{14}\pi - \theta_r)\}, & \text{if } \frac{3}{10}\pi < \theta_r \leq \frac{5}{14}\pi, \|r\| > r_{d_3}, \\ \|r\| \sin(\theta_r - \frac{5}{14}\pi), & \text{if } \theta_r > \frac{5}{14}\pi, \|r\| > r_{d_3}. \end{cases} \quad (8)$$

$$\hat{b}_4(\hat{s}) = -\hat{b}_3(\|\hat{s}\| e^{j(\frac{\pi}{2} - \theta_r)}). \quad (9)$$

where  $\theta_r = \tan^{-1}(|I(\hat{s})|/|R(\hat{s})|)$ ,  $r_{d_1} = (r_1 + r_2)/2$ ,  $r_{d_2} = (r_2 + r_3)/2$ , and  $r_{d_3} = (r_3 + r_4)/2$ . When we estimate  $\hat{b}_4(\hat{s})$ , we can use the symmetry characteristics of  $H_3$  and  $H_4$ . Therefore, we rotate  $\|r\| e^{\theta}$  by  $\pi/2 - 2\theta_r$  anticlockwise, resulting in a simplified estimation using  $\hat{b}_3$  which is in (9).

In Fig. 5 and Fig. 6, there are HDT lines for the fifth and sixth bits,  $H_5$  and  $H_6$ . The discontinuities of  $H_5$  and  $H_6$  incur comparatively complex comparison operations for estimation of  $\hat{b}_5$  and  $\hat{b}_6$ . Thus, the SBI for the fifth and sixth bit can be represented as (10) and (11), respectively. In here, we also can use the symmetry characteristics of  $H_5$  and  $H_6$ .

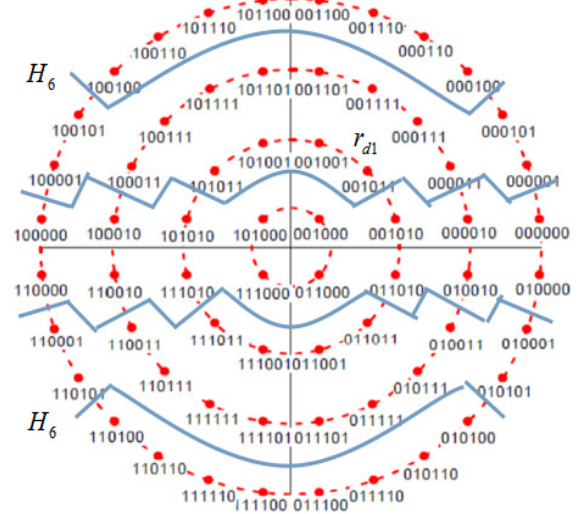


Fig. 6. HDT for the sixth bit of a 64-APSK symbol

$$\hat{b}_5(r) = \begin{cases} -(r_{d_1} - \|r\|), & \text{if } \theta_r < \frac{1}{3}\pi, \|r\| < r_{d_1}, \\ -\left\| r - r_{d_1} e^{j\frac{1}{3}\pi} \right\|, & \text{if } \theta_r > \frac{1}{3}\pi, \|r\| \leq r_{d_1}, \\ \min\{\|r\| - r_{d_1}, \|r\| \sin(\frac{1}{3}\pi - \theta_r)\}, & \text{if } \theta_r \leq \frac{1}{3}\pi, r_{d_1} < \|r\| \leq r_{d_2}, \\ -\min\{r_{d_2} - \|r\|, \|r\| \sin(\theta_r - \frac{1}{3}\pi)\}, & \text{if } \frac{1}{3}\pi < \theta_r \leq \frac{4}{10}\pi, r_{d_1} < \|r\| \leq r_{d_2}, \\ -\left\| r - r_{d_2} e^{j\frac{4}{10}\pi} \right\|, & \text{if } \theta_r > \frac{4}{10}\pi, r_{d_1} < \|r\| \leq r_{d_2}, \\ r_{d_3} - \|r\|, & \text{if } \theta_r \leq \frac{4}{14}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ \min\left\{ \left\| r - r_{d_2} e^{j\frac{4}{10}\pi} \right\|, \left\| r - r_{d_2} e^{j\frac{1}{3}\pi} \right\| \right\}, & \text{if } \frac{4}{14}\pi < \theta_r \leq \frac{1}{3}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ \min\{\|r\| - r_{d_2}, \|r\| \sin(\frac{4}{10}\pi - \theta_r)\}, \left\| r - r_{d_2} e^{j\frac{4}{10}\pi} \right\|, & \text{if } \frac{1}{3}\pi < \theta_r \leq \frac{4}{10}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ -\min\{r_{d_3} - \|r\|, \|r\| \sin(\theta_r - \frac{4}{10}\pi)\}, & \text{if } \frac{4}{10}\pi < \theta_r \leq \frac{6}{14}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ -\left\| r - r_{d_3} e^{j\frac{6}{14}\pi} \right\|, & \text{if } \theta_r > \frac{6}{14}\pi, r_{d_2} < \|r\| \leq r_{d_3}, \\ -\min\{r_{d_3} - \|r\|, \|r\| \sin(\frac{4}{14}\pi - \theta_r)\}, & \text{if } \theta_r \leq \frac{4}{14}\pi, \|r\| > r_{d_3}, \\ \min\left\{ \left\| r\right\| \sin(\frac{6}{14}\pi - \theta_r), \left\| r - r_{d_3} e^{j\frac{6}{14}\pi} \right\|, \left\| r\right\| \sin(\theta_r - \frac{4}{14}\pi) \right\}, & \text{if } \frac{4}{14}\pi < \theta_r \leq \frac{6}{14}\pi, \|r\| > r_{d_3}, \\ \min\{\|r\| - r_{d_3}, \|r\| \sin(\theta_r - \frac{4}{14}\pi)\}, \left\| r\right\| \sin(\frac{6}{14}\pi - \theta_r), & \text{if } \frac{4}{10}\pi < \theta_r \leq \frac{6}{14}\pi, \|r\| > r_{d_3}, \\ -\|r\| \sin(\theta_r - \frac{6}{14}\pi), & \text{if } \theta_r > \frac{6}{14}\pi, \|r\| > r_{d_3}. \end{cases} \quad (10)$$

$$\hat{b}_6(\hat{s}) = -\hat{b}_5(\|\hat{s}\| e^{(\frac{\pi}{2}-\theta_s)}). \quad (11)$$

### IV. Simulation results

We simulated the BER performance of the proposed soft demapping scheme for 64-APSK and compared to that of the MLD scheme. We used duo-binary turbo code with an information block size  $N$  of 192 symbols (384bits), and a code rate,  $R$  of 1/2 to verify the performance of the soft demapping schemes.

The BER performance comparison shown in Fig. 7 demonstrated that the performance of the proposed HDT method scheme can achieve an approximating performance of the MLD scheme.

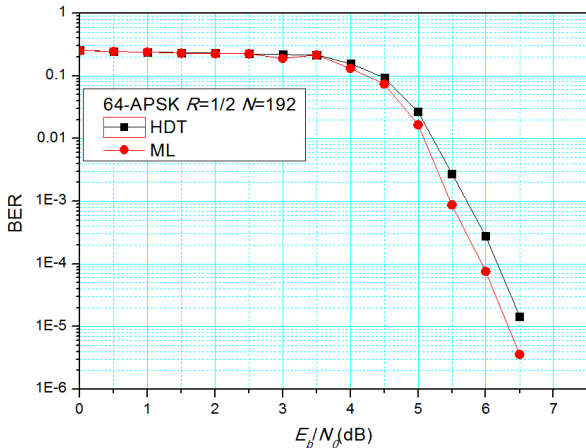


Fig. 7. BER performance of the soft demapping schemes for 64-APSK

### VI. Conclusion

In this paper, we proposed an efficient soft demapping method for 64-APSK in the DVB-S3 system. Based on the HDT lines, SBI can be estimated in a linear complexity. Simulation results showed that the performance of our proposed method can approximate to that of the ML method.

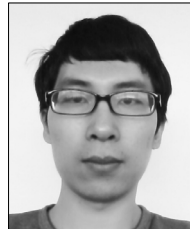
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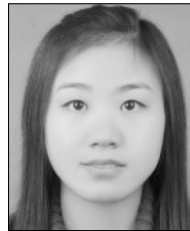
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