

5축 혼합형 공작기계의 정밀도 향상 연구

Accuracy Improvement of a 5-axis Hybrid Machine Tool 김한성¹⁾

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(Abstract)

In this paper, a novel 5-axis hybrid-kinematic machine tool is introduced and the research results on accuracy improvement of the prototype machine tool are presented. The 5-axis hybrid machine tool is made up of a 3-DOF parallel manipulator and a 2-DOF serial one connected in series. The machine tool maintains high ratio of stiffness to mass due to the parallel structure and high orientation capability due to the serial-type wrist. In order to acquire high accuracy, the methodology of measuring the output shafts by additional sensors instead of using encoder outputs at the motor shafts is proposed. In the kinematic view point, the hybrid manipulator reduces to a serial one, if the passive joints in the U-P serial chain at the center of the parallel manipulator are directly measured by additional sensors. Using the method of successive screw displacements, the kinematic error model is derived. Since a ball-bar is less expensive than a full position measurement device and sufficiently accurate for calibration, the kinematic calibration method of using a ball-bar is presented. The effectiveness of the calibration method has been verified through the simulations. Finally, the calibration experiment shows that the position accuracy of the prototype machine tool has been improved from 153 to 86 μ m.

Keywords: Hybrid machine tool, Parallel manipulator, Double ball-bar, Kinematic calibration

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1. INTRODUCTION

A Conventional 5-axis machine tool provides high accuracy and large workspace. However, to the serial-kinematic structure, it due generally requires very massive structure to maintain high stiffness. In order to increase the of stiffness to mass. ratio the 3-DOF parallel-kinematic manipulator is employed as an arm and for high orientational capability, the 2-DOF serial-kinematic manipulator is used as a wrist. Hence, the proposed machine tool has a 5-DOF hybrid-kinematic structure as shown in Fig. 1. This machine tool will be applied for both machining and assembling tasks of automobiles' cvlinder blocks. Specifically, the parallel manipulator has three U-P-S legs at the side and one U-P leg at the center, where the prismatic joints in the U-P-S chains are controlled by linear actuators and the prismatic joint in the U-P chain is passive.

In design and control of a machine tool, to obtain high accuracy is one of the most important tasks to be accomplished. In order to guarantee high accuracy, the methodology of measuring the output shafts by additional sensors instead of using encoder outputs at the motor shafts is proposed. For the parallel manipulator, two angular encoders and one linear encoder at the U-P chain are additionally installed as shown in Fig. 1. In a similar manner, two angular encoders at the output shafts of the serial manipulator are installed. Therefore, the position and orientation of the tool tip can be calculated by the outputs of the five sensors connected in series. Hence, the hybrid manipulator can be considered as a serial manipulator, i.e.,

the U-P-R-R chain. In modeling kinematic errors, the method of successive screw displacements⁽¹⁾ are used instead of the Denavit-Hartenberg notations because the former is more general and straightforward.⁽²⁾

Since a ball-bar is less expensive than a full position measurement device calibration. sufficiently accurate for the calibration on the machine tool will be performed by using a ball-bar. For a length measurement, i.e., using a ball-bar, the kinematic calibration is reduced to a nonlinear least square method of minimizing the calculated and measured lengths of a ball-bar. The effectiveness of the kinematic calibration method with a ball-bar is verified through the simulations. Through calibration experiment, the accuracy has been improved from 153 to $86 \mu m$.

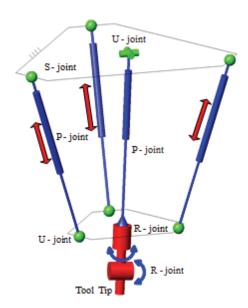


Fig. 1. Structure of the hybrid-kinematic machine tool.



2. Position Analysis

The forward kinematics of the machine tool can be obtained by considering the central leg, i.e., U-P-R-R serial chain in the middle if the U-P passive joints are measured. At a reference position, the kinematic parameters may be listed in Table 1, where \mathbf{s}_i and \mathbf{s}_{0i} denote the direction and location of the tth joint axis with respect to the fixed coordinate system A(x, y, z) when the machine tool is at the reference position.

Table 1 Screw axis locations and reference position.

Joint	$oldsymbol{s}_i$	$oldsymbol{s}_{0i}$
1	(1,0,0)	(0,0,0)
2	(0,1,0)	(0,0,0)
3	(0,0,1)	(0,0,0)
4	(0,0,1)	(0,0,0)
5	(0,1,0)	$(0,0,L_0+L_1)$

Substituting the coordinates of the joint axes into the equation of the general spatial displacement, known as Rodrigues's formula, the screw transformation matrices are given by

$$A_{1} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & c\theta_{1} - s\theta_{1} & 0 \\ 0 & s\theta_{1} & c\theta_{1} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \quad A_{2} = \begin{bmatrix} c\theta_{2} & 0 & s\theta_{2} & 0 \\ 0 & 1 & 0 & 0 \\ -s\theta_{2} & 0 & c\theta_{2} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix},$$

$$A_{3} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & t_{3} \\ 0 & 0 & 1 \end{bmatrix}, \quad A_{4} = \begin{bmatrix} c\theta_{4} - s\theta_{4} & 0 & 0 \\ s\theta_{4} & c\theta_{4} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix},$$

$$A_{5} = \begin{bmatrix} c\theta_{5} & 0 & s\theta_{5} & -(L_{0} + L_{1})s\theta_{5} \\ 0 & 1 & 0 & 0 \\ -s\theta_{5} & 0 & c\theta_{5} & (L_{0} + L_{1})(1 - c\theta_{5}) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$(1)$$

where $c\theta_i = \cos\theta_i$, $s\theta_i = \sin\theta_i$ and t_3 denotes

the linear displacement of the prismatic joint in the middle of the machine tool.

The target position of the tool tip Q can be given by

$$\begin{bmatrix} R_q & \mathbf{q} \\ 0_{1\times 3} & 1 \end{bmatrix} = A_1(\theta_1) \cdots A_5(\theta_5) \begin{bmatrix} I_{3\times 3} & \mathbf{q_0} \\ 0_{1\times 3} & 1 \end{bmatrix}$$
(2)

where $\mathbf{q}_0 = [0,0,L_0+L_1+L_2]^T$ denotes the tool tip Q when the machine tool is at the reference position. At the reference position, the orientation of the moving frame coincides with that of the fixed frame.

For the inverse kinematics of the U-P-R-R serial chain, only 5 of the 12 parameters associated with the end-effector position vector and rotation matrix can be specified at will. This is because the manipulator has only 5 degrees of freedom. In this work, the position vector (\mathbf{q}) and the approach vector (\mathbf{w}_q) are specified and the other two unit vectors, \mathbf{u}_q and \mathbf{v}_q , are to be determined after the joint angles are found. The point M can be obtained by

$$\boldsymbol{m} = \boldsymbol{q} - L_2 \boldsymbol{w}_a \tag{3}$$

It is clear that the position of the point M depends only on the first three joint variables, θ_1 , θ_2 , and t_3 . From the geometry, the direction vector and the travel distance of the prismatic joint is determined by

$$oldsymbol{s}_3 = oldsymbol{m} \mid \mid oldsymbol{m} \mid \mid \quad \text{and} \quad t_3 = \mid \mid oldsymbol{m} \mid \mid -(L_0 + L_1) \quad \ (4)$$

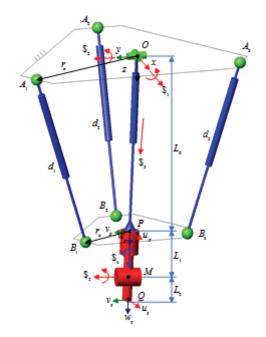


Fig. 2. Kinematic parameters of the machine tool.

Furthermore, the other two angles can be easily obtained in the following.

$$\mathbf{s}_3 = R_1 R_2 R_3 \mathbf{w}_{a0}$$
 where $\mathbf{w}_{a0} = [0,0,1]^T$ (5)

This equation reduces to

$$\begin{bmatrix} s_{3x} \\ s_{3y} \\ s_{3z} \end{bmatrix} = \begin{bmatrix} s\theta_2 \\ -s\theta_1 c\theta_2 \\ c\theta_1 c\theta_2 \end{bmatrix}$$
 (6)

Then,

$$\theta_2 = \sin^{-1}(s_{3x}), \ \theta_1 = \text{Atan2}[-s_{3y}/c\theta_{2}, s_{3z}/c\theta_{2}] \endaligned (7)$$

From Eq. (2),

$$\mathbf{w}_{q} = R_{1} R_{2} R_{3} R_{4} R_{5} \mathbf{w}_{q0} \tag{8}$$

Since θ_1 , θ_2 , and t_3 are already known, the above equation can be reduced to

$${}^{3}\boldsymbol{w}_{a} = R_{4}R_{5}\boldsymbol{w}_{a0} \tag{9}$$

where ${}^{3}\boldsymbol{w}_{q} = R_{3}^{T}R_{2}^{T}R_{1}^{T}\boldsymbol{w}_{q}$. Each component can be obtained by

$$\begin{bmatrix} {}^{3}w_{qx} \\ {}^{3}w_{qy} \\ {}^{3}w_{qz} \end{bmatrix} = \begin{bmatrix} c\theta_{4}s\theta_{5} \\ s\theta_{4}s\theta_{5} \\ c\theta_{5} \end{bmatrix}$$
 (10)

Then,

$$\theta_5 = \cos^{-1}(^3w_{qx}), \theta_4 = \text{Atan2}[^3w_{qy}/s\theta_{5,} ^3w_{qx}/s\theta_{5}](1$$

It is noted that two solution sets are possible in the working range, i.e., $\theta_5 = \theta_5^*$ or $-\theta_5^*$.

The inverse kinematics of the 3-DOF parallel manipulator is simply determined by

$$d_i = || R_p \boldsymbol{b}_i + \boldsymbol{p} - \boldsymbol{a}_i ||$$
 for $i = 1, 2, 3$ (12)

where $\mathbf{p}_0 = [0,0,L_0]^T$, $\begin{bmatrix} R_q & \mathbf{q} \end{bmatrix}$

$$\begin{bmatrix} R_q & \mathbf{q} \\ 0_{1\times3} & 1 \end{bmatrix} = A_1(\theta_1) A_2(\theta_2) A_3(t_3) \begin{bmatrix} I_{3\times3} & \mathbf{p_0} \\ 0_{1\times3} & 1 \end{bmatrix},$$

$$\mathbf{a}_1 = r_a \begin{bmatrix} 1/2 \\ \sqrt{3}/2 \end{bmatrix}, \quad \mathbf{a}_2 = r_a \begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{a}_3 = r_a \begin{bmatrix} -\frac{1/2}{\sqrt{3}}/2 \\ 0 \end{bmatrix},$$

$$\mathbf{b}_1 = r_b \begin{bmatrix} 1/2 \\ \sqrt{3}/2 \end{bmatrix}, \quad \mathbf{b}_2 = r_b \begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{b}_3 = r_b \begin{bmatrix} -\frac{1/2}{\sqrt{3}}/2 \\ 0 \end{bmatrix}.$$



3. Error Model

When there some kinematic errors exist in the U-P-R-R serial chain, the kinematic parameters for an actual model can be summarized in Table 2. For a revolute joint, four kinematic errors (two for the direction of joint axis and two for location error) can be considered, however, for a prismatic joint, only two kinematic errors for the joint direction exist. The total kinematic errors associated with directions and locations of joint axes are 18 and there are 5 joint offsets $(\delta\theta_1, \delta\theta_2, \delta t_3, \delta\theta_4, \delta\theta_5)$. Therefore, 23 kinematic errors should be estimated by the following kinematic calibration.

Once the kinematic errors in the serial chain are determined, the relation between the U-P chain and three S-P-U chains needs to be investigated. The kinematic errors in the S-P-U chains are summarized as follow:

Joint location errors: $\delta \boldsymbol{a}_i$ and $\delta \boldsymbol{b}_i$ for i=1,2,3

Table 2 Kinematic parameters for an actual model.

Joint	$oldsymbol{s}_i$	$oldsymbol{s}_{0i}$		
1	$(\sqrt{1-u_{1y}^2-u_{1z}^2},u_{1y},u_{1z})$	$(0,\!\delta y_1,\!\delta z_1)$		
2	$(u_{2x},\sqrt{1-u_{2x}^2-u_{2z}^2},u_{2z})$	$(\delta x_2, 0, \delta z_2)$		
3	$(u_{3x}, u_{3y}, \sqrt{1 - u_{3x}^2 - u_{3y}^2})$	(0,0,0)		
4	$(u_{4x},u_{4y},\sqrt{1-u_{4x}^2-u_{4y}^2})$	$(\delta x_4, \delta y_4, 0)$		
5	$(u_{5x},\sqrt{1-u_{5x}^2-u_{5z}^2},u_{5z})$	$(\delta x_5, 0, L_0 + L_1 + \delta z_5)$		

Length offset errors: δd_i for i = 1,2,3

The kinematic errors will be determined by using Eq. (12).

4. Kinematic Calibration

In this work, the kinematic calibration method will be performed by using a length measurement, i.e., ball-bar. (3-7) In the following derivation, the superscripts, "c" and "m" are used to denote the calculated and measured values, respectively, and the subscript, "j" is employed to indicate the measurement number. As illustrated in Fig. 3, the calibration methods using length measurement is to find the set kinematic parameters satisfying the following equation:

$$\parallel \boldsymbol{q}^{c}(\boldsymbol{\theta}_{j}^{m} + \delta\boldsymbol{\theta}, \boldsymbol{\beta}) - \boldsymbol{c} \parallel = l_{j}^{m}$$
 (13)

where $\mathbf{q}(\cdot)$ denotes the forward kinematics function of the U-P-R-R serial chain, $\boldsymbol{\theta}_i^m$ and $\delta \boldsymbol{\theta}$ denote the measured joint angle and the joint offset vectors, $\boldsymbol{\beta}$ is the kinematic error vector in Table 2 to be updated, $\mathbf{c} = \mathbf{c} + \delta \mathbf{c}$ and and l_i^m denote the position vector of the fixed center of a ball-bar and the measured length of a ball-bar, respectively.

The purpose of this work is to develop and to verify the effectiveness of a kinematic calibration method suitable for the prototype of a 5-axis hybrid machine tool being developed as shown in Fig. 4. The main kinematic parameters of the machine tool are listed in Table 3.

Prior to a real calibration experiment in future, a virtual prototype with realistic kinematic errors is assumed. The error bound is determined from the information on machining and assembling tolerances and its direction is generated by the random function in MATLAB. It is also assumed that the prototype machine will be calibrated by a ball-bar, specifically, the QC10 ball-bar of Renishaw with the accuracy, $\pm 0.5 \,\mu$ m. For the collection of measurement data, one center of the ball-bar is fixed $\bar{c} = [0.0.1500 \,\mathrm{mm}]^T$ at expressed in the reference frame. The n=32 measurement points are selected on the hemisphere surfaces with 150mm radius. The n sets of encoder values from the three linear actuators and the U-P-R-R serial chain and the corresponding n ball-bar lengths are measured at the same time, which are actually calculated from the virtual prototype for numerical simulations.

Using Eq. (13) and "Isqnonlin" function of MATLAB, the kinematic parameters and the

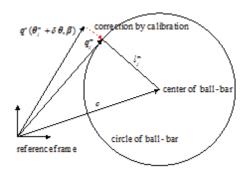


Fig. 3. Outline of the calibration methods using a ball-bar.

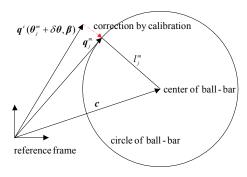


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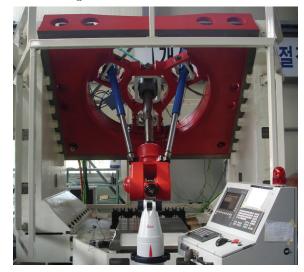


Fig. 4. Prototype of a 5-axis hybrid machine tool.

position error of the ball center are updated so as to minimize the error between the calculated and measured lengths of the ball-bar.

It is assumed that the maximum error bounds for angle and length are $\pm 25 \, \mu \, \text{m}$, respectively. The assumed kinematic errors for a virtual prototype are written in parentheses of Table 4.

The estimated kinematic parameters by the suggested calibration method are also in Table

4. It is noted that estimated values are close

Table 3 Parameters for a prototype machine tool.

Parameters	Unit [mm]	
Radius of the fixed $plate(r_a)$	600	
Radius of the moving $plate(r_b)$	250	
Reference $height(L_0)$	840	
Distance between A and $\mathrm{C}(L_1)$	291	
Tool length(L_2)	340	
Initial length of an $actuator(d_{i0})$	910	
Linear actuator $stroke(\Delta d_i)$	800	

to the assumed ones and at least the signs are identical. It is also noted that estimated values does not necessarily following the assumed ones.

In order to show the effectiveness of the suggested calibration method, the well-known circular test on the XY plane with the radius of 150mm is presented in Fig. 5. From the kinematic calibration and error compensation, the maximum absolute kinematic error has been reduced from 214.5 to $48.2\,\mu\,\text{m}$. Using the proposed algorithm and verified calibration procedure through simulation, calibration experiment has been performed on the prototype machine tool as shown in Fig. 6.

Table 4 Assumed and estimated kinematic errors.

i	\boldsymbol{s}_i	Estimated (Assumed)	$oldsymbol{s}_{0i}$	Estimated (Assumed)	$\delta\theta_i$	Estimated (Assumed)
1	u_{1y}	14.6132 (22.5065)	δy_1	-22.1156 (-16.1867)	$\delta\theta_1$	3.6879 (5.7716)
	u_{1z}	-4.7791 (-13.4431)	δz_1	-12.6657 (-4.7147)	001	
2	u_{2x}	13.2356 (5.3421)	δx_2	37.9109 (21.7735)	$\delta\theta_2$	9.8016 (14.5969)
	u_{2z}	-1.0796 (-0.7009)	δz_2	12.9004 (20.8452)	002	
3	u_{3x}	15.6955 (19.5649)	-	-	$\delta\theta_3$	7.7064 (15.6583)
	u_{3y}	13.4825 (13.1048)	-	-	003	
4	u_{4x}	-6.1924 (-2.1766)	δx_4	12.5541 (-4.4865)	$\delta \theta_4$	-1.3791 (21.0906)
	u_{4y}	-22.605 (-24.0748)	δy_4	6.9893 (19.6825)	004	
5	u_{5x}	1.3792 (16.0704)	δx_5	-29.9936 (-22.1054)	$\delta\theta_5$	1.5168
	u_{5z}	-3.5677 (-2.7648)	δz_5	-7.3568 (-7.3566)	005	(11.9104)
	δc_x	-46.8734 (-15.5173)	δc_y	11.9864 (-15.3284)	δc_z	-7.9520 (9.1112)

[Unit: [arc sec] for angle and $[\mu m]$ for length]

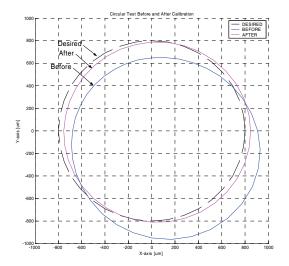


Fig. 5. Circular test before and after calibration.

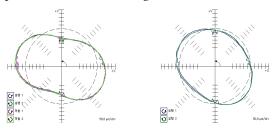




Fig. 6. Calibration experiment using a ball-bar.

In the experiment, The Renishaw QC10 ball-bar with $\pm 0.5 \,\mu$ m is used. The n = 32points on the hemisphere surface with radius 150mm are collected for updating kinematic parameters. The major errors were firstly calibrated, for example, the offset lengths of linear actuators.

Then, the well-known circular test was performed (refer to Fig. 7(a)). The circular



(b) after calibration (a) before calibration Fig. 7. Circular tests with radius 150mm.

test result after calibration experiment is shown in Fig. 7(b). From the two tests, it is verified that position accuracy of the prototype machine tool has been improved from 153 to 86μ m.

5. Conclusions

In this paper, a new hybrid-kinematic structure for both machining and assembling is proposed. By attaching additional sensors to passive joints in the central leg, the hybrid structure can be considered as a pure serial manipulator. Using the successive screw displacements, the kinematics analysis is performed and a kinematic error model is developed for the 5-DOF serial chain. The 5-DOF serial chain is calibrated by using a length measurement, i.e., ball-bar. Once all kinematic parameters in the serial chain are determined, the kinematic parameters associated with the parallel-kinematic manipulator will be estimated. In order to verify the effectiveness of this suggested method, the simulation results of the kinematic calibration for a virtual prototype have been presented. The calibration experiment on the prototype machine tool was performed. From the kinematic calibration and error compensation, the maximum kinematic error has been reduced from 153 to $86 \mu m$.

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