# Low-Power and High-Efficiency Class-D Audio Amplifier Using Composite Interpolation Filter for Digital Modulators

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Abstract—This paper presents a high-efficiency digital class-D audio amplifier using a composite interpolation filter for portable audio devices. The proposed audio amplifier is composed of an interpolation filter, a delta-sigma modulator, and a class-D output stage. To reduce power consumption, the designed interpolation filter has an optimized composite structure that uses a direct-form symmetric and Lagrange FIR filters. Compared to the filters with homogeneous structures, the hardware cost and complexity are reduced by about half by the optimization. The coefficients of the digital deltasigma modulator are also optimized for low power consumption. The class-D output stage has gate driver circuits to reduce shoot-through current. The implemented class-D audio amplifier exhibited a high efficiency of 87.8 % with an output power of 57 mW at a load impedance of 16  $\Omega$  and a power supply voltage of 1.8 V. An outstanding signal-to-noise ratio of 90 dB and a total harmonic distortion plus noise of 0.03 % are achieved for a single-tone input signal with a frequency of 1 kHz.

*Index Terms*—Audio amplifier, digital class-D amplifier, composite interpolation filter, delta-sigma modulator, dead-time gate driver

#### I. INTRODUCTION

Interests in high-efficiency audio amplifiers with low power consumption have been increasing for portable applications, such as hearing instruments, wireless headsets, and mobile phones [1]. Since the peak-toaverage ratio (PAR) of an audio signal is 9 to 15 dB, linear amplifiers such as class-A or class–AB amplifiers have significantly reduced efficiency for the backed-off region from the peak output power and are not suitable for portable audio systems [2, 3]. Therefore, the class-D amplifier is preferred for portable applications because high efficiency can be maintained even at significantly backed-off power levels [4].

The architectures of the class-D amplifier can be classified into two types: 1) one based on pulse width modulation (PWM) method [5, 6] and 2) another based on pulse density modulation (PDM) method using a delta-sigma modulator (DSM) [7]. For an audio amplifier based on PWM method, a comparator is used to generate a pulse signal by comparing the input signal and a carrier signal which has a triangular or saw-tooth waveform. The carrier signal with a relatively low frequency leads to harmonics issues [5].

Alternatively, the class-D amplifiers based on PDM method using a DSM have a little lower power efficiency due to the relatively fast clock speed but have more linear output characteristics that can be achieved through the proper selection of oversampling ratio (OSR) and loop filter parameters [8]. The audio amplifiers based on PDM method are more suitable for digital audio

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applications, since they have digital input.

In this paper, we present a digital class-D audio amplifier, composed of a 16-bit digital interpolation filter (IF), a  $3^{rd}$ -order DSM, and a class-D output stage with gate driver circuits for a reduced shoot-through current. The IF has a composite structure with direct-form symmetric and Lagrange finite impulse response (FIR) filters for low power consumption. In addition, the noise gain of the DSM for a voice bandwidth of up to 8 kHz is optimized to minimize the current consumption.

# II. DESIGN OF DIGITAL CLASS-D AUDIO AMPLIFIER

Digital class-D audio amplifiers commonly comprise an IF, a modulator, and a class-D output stage. A typical structure of the designed digital class-D audio amplifier is shown in Fig. 1. As the 16-bit pulse-coded modulation (PCM) signal is applied to the IF, the filter oversamples the input signal with an OSR of 32. Then, the DSM converts the oversampled PCM signal to the 1-bit PDM signal and delivers it to the class-D output sage.

#### 1. Composite Structure of the IF

An FIR filter is a common type of IF. A cascaded 5stage IF is optimized with a composite structure for low power consumption, as shown in Fig. 2. Using multiple cascaded stages, a digital filter with a high OSR can have relatively mitigated hardware complexity, compared to the high-order single-stage filters for similar cut-off characteristics [9]. Due to the OSR of 32, the output digital signal of the IF has a sampling frequency of 1.024 MHz while that of the input is 32 kHz.

A 5-stage composite structure using a 14th-order direct-form symmetric FIR filter as the first stage and a Lagrange FIR filter for the following 4 stages is used to optimize power consumption and cost. The first stage has a high order of 14 to sharply cut off the image signal that is generated by the signal sampling.

A structure of the designed direct-form symmetric FIR filter for the first stage is shown in Fig. 3(a). Since the direct-form symmetric structure has been adopted instead of just a direct form, the hardware cost decreases by approximately half. Additionally, the following stages can have rather simple structure, which can reduce the

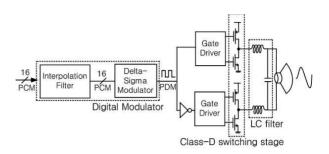
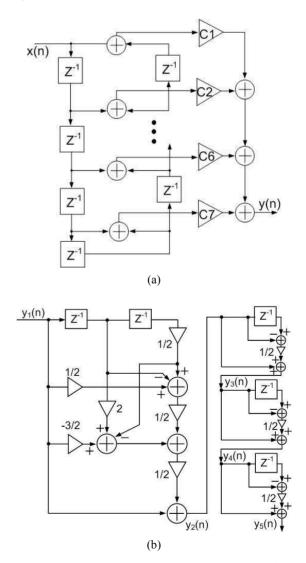


Fig. 1. A structure of the digital class-D audio amplifier based on PDM method.

<i>.</i>		Cascade interpolation filter				
DF: 14 <sup>th</sup> o (21	S 16 rder 2fs	Lagrange 2 <sup>nd</sup> order (21)	16 4fs	Lagrange ▲ 1 <sup>st</sup> order (8↑)	16	

**Fig. 2.** A structure of the proposed 5-stage composite interpolation filter.



**Fig. 3.** Schematic diagrams of the IF stages (a) 14<sup>th</sup>-order direct-form symmetric FIR filter for the first stage, (b) cascaded Lagrange FIR filter for the 2<sup>nd</sup> to 5<sup>th</sup>-stages.

 Table 1. Coefficients for the 14<sup>th</sup>-order direct-form symmetric

 FIR filter

Coefficient	Value
C1	-0.009796142578125
C2	-0.000335693359375
C3	0.034820556640625
C4	-0.0152587890625
C5	-0.095367431640625
C6	0.10394287109375
C7	0.4795989990234375

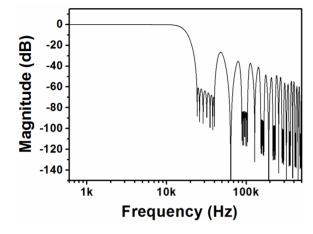


Fig. 4. Amplitude response of the designed filter.

power consumption caused by the higher clock speed. Table 1 shows the coefficients based on 16-bit finite length word for the 14<sup>th</sup>-order direct-form symmetric FIR filter.

A Lagrange filter, as shown in Fig. 3(b), is adopted for the  $2^{nd}$  to  $5^{th}$  stages. The  $2^{nd}$  stage has  $2^{nd}$ -order structure, and the other three stages have  $1^{st}$ -order structure. The amplitude response of the designed 5-stage IF is plotted in Fig. 4. Low ripple characteristics within ±0.09 dB are obtained up to a given audio bandwidth of 8 kHz.

The characteristics of the proposed composite IF are compared to the IF filters with homogeneous structures, which are optimized to have performance similar to that of the proposed composite IF structure, as shown in Table 2. In comparison, the hardware cost is reduced by about half due to the optimized composite structure. Furthermore, the simulated power consumption simulated using Design Compiler is as low as  $1.33 \mu$ W.

#### 2. Digital DSM

The digital DSM is composed of integrators, a

 Table 2. Comparison of the proposed IF to the IF's with homogeneous structures

	direct-form symmetric	Lagrange	This work	
Ripple (dB) @ 0 Hz-8 kHz	±0.11	±0.09	±0.09	
Attenuation (dB) @ 32 kHz	-66	-76	-66	
Tap/multiplier/adder	40/40 /34	14/84 /78	16/24 /25	
Power (µW)	5.21	3.6	1.33	

\*fs: 1.024 MHz, VDD: 1.8 V with 0.18 μm process

Table 3. The extracted coefficients for the DSM

Coefficients	Value	Coefficient	Value
al	1/24+1/26	c1	1/23+1/25
a2	1/23+1/25	c2	1/22+1/23
a3	1/22+1/24	c3	1
b1	1/24+1/26	g1	1/28

\* b2=b3=b4=0

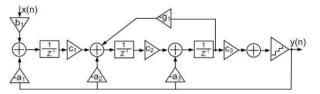


Fig. 5. A schematic diagram of the designed DSM.

quantizer, and feedback loops, as shown in Fig. 5. The coefficients, which are connected to each node, determine the transfer characteristics and the out-band noise gain [10]. The extracted coefficients are presented in Table 3.

The feedback loops reduce quantization noise in the low frequency region for noise shaping characteristics [11]. The coefficients at each node and order of the DSM are optimized for the audio band of 8 kHz for better noise shape. The designed DSM transforms the 16-bit input signal into a 1-bit PDM signal with a clock frequency of 1.024 MHz.

A power consumption of 13  $\mu$ W was achieved with the designed modulator, including the composite IF, in simulations using Design Compiler. Fig. 6 shows the measured output power spectral density (PSD) of the designed modulator, including the IF and DSM. As shown in Fig. 7, the measured THD+N of the designed modulator is lower than -72 dB. The circuits were implemented on a vertex-5 FPGA board. Measurements

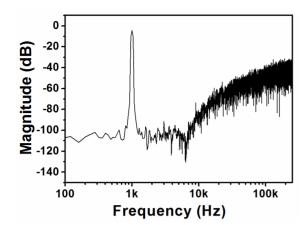


Fig. 6. The measured output PSD of the designed DSM.

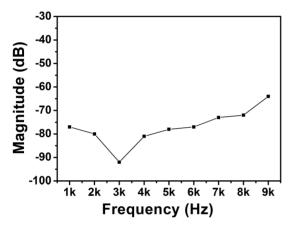


Fig. 7. The measured THD+N of the designed DSM.

**Table 4.** Maximum stable input scale and THD+N according to the out-band noise gain of the DSM

Out-band noise gain	1.1	1.2	1.3	1.4
Max. stable input (FS)	0.966	0.897	0.862	0.793
THD+N (dB)	70.8	79.0	83.2	86.0

were done using a Chipscope.

For an input signal of a 1-kHz sine wave, which has a full-scale (FS) magnitude of 0.8, an outstanding SNR of 90 dB was achieved. As the out-band noise gain of the DSM becomes larger, the allowable scale of the input signal should be smaller for unconditional stability. Table 4 shows the maximum stable input scale and THD+N characteristics according to the out-band noise gain of the DSM. The designed modulator has an out-band noise gain of 1.2 and operates with a reasonable maximum stable input signal scale of 0.897.

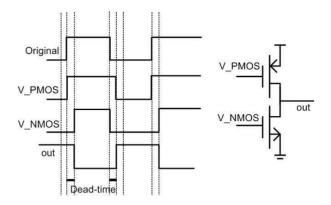


Fig. 8. Timing diagram of the dead-time for the gate driver.

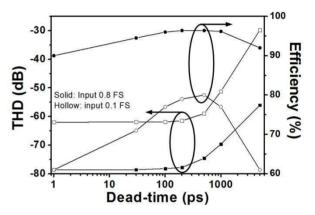


Fig. 9. Simulated THD and power efficiency according to the dead-time.

#### 3. Full-bridge class-D output stage

For low even-order harmonic distortion, full-bridge class-D structure is adopted as the output stage of the amplifier (see Fig. 1). The full-bridge structure has low even-order harmonic distortion and does not require a DC blocking capacitor. After passing the low-pass filter at the output of the amplifier, the in-band audio signal can be restored.

For class-D amplifiers, efficiency degradation comes from switching loss, conduction loss, and shoot-through current loss [12]. The shoot-through current loss can be reduced using a gate driver with an appropriate deadtime. The dead-time prevents from simultaneous turn-on of the PMOS and NMOS switches, so that the shootthrough current can be removed. A timing diagram of the dead-time is shown in Fig. 8. To make a dead-time properly, the ON state of the PMOS switch should be extended at its falling edge, and the OFF state for the NMOS switch should be shortened at its falling edge.

The simulated THD and efficiency according to the

dead-time are shown in Fig. 9. As the dead-time increases, the power efficiency and THD increase. If the dead-time becomes too long, the power efficiency decreases due to the decreased output power. Before having too much of an increase in THD, a dead-time of 150 ps was chosen for optimal efficiency improvement.

Since the peak-to-average ratio (PAR) of the audio signal is about 10 dB [13], the efficiency at an output level of 0.1 FS significantly improves from an initial value of around 60 % to around 80 %.

## **III. EXPERIMENTAL RESULTS**

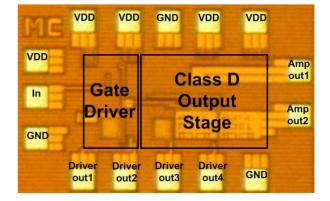
The designed IF and DSM are implemented using a vertex-5 FPGA board and the full-bridge class-D output stage including the gate driver was fabricated using Magnachip's CMOS 0.18  $\mu$ m process. The transistor cell sizes of the class-D switch are optimized for efficiency at a load impedance of 16  $\Omega$ . The PMOS and NMOS switching transistors have widths of 24000 and 12000  $\mu$ m, respectively. Fig. 10 shows a micro-photograph of the fabricated class-D output stage including the gate driver. The chip size is 0.4 mm<sup>2</sup>. An APx525 audio analyzer from Audio Precision was used to measure the THD+N performance.

The fabricated class-D audio amplifier exhibited power efficiency as high as 87.8 % for the 1-kHz input signal with 0.8 FS and a very low THD+N of 0.03 % for the 1-kHz input signal with 0.1 FS. The implemented audio amplifier has an output power of 57 mW with a load impedance of 16  $\Omega$  and a supply voltage of 1.8 V. The measured output PSD of the designed audio amplifier for the 1-kHz input signal with a FS of 0.1 is shown in Fig. 11. The measured efficiency and THD+N performances are shown in Fig. 12.

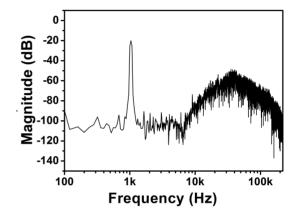
Table 5 summarizes the output performance of the class-D audio amplifier in this work compared to previously published results. The proposed audio amplifier demonstrates excellent power efficiency and THD+N performance.

## **IV. CONCLUSIONS**

A class-D audio amplifier with a composite IF, a DSM, and a class-D output stage has been proposed. The proposed digital IF has a composite structure to reduce



**Fig. 10.** Micro-photograph of the implemented class-D output stage with the gate driver (size: 0.4 mm<sup>2</sup>).



**Fig. 11.** The measured output PSD of the designed audio amplifier for the 1-kHz input signal with a FS of 0.1.

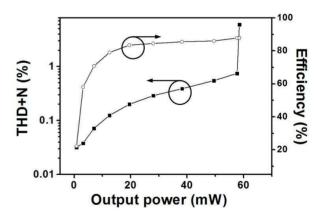


Fig. 12. The measured efficiency and THD+N of the class-D audio amplifier.

power consumption and hardware cost. In addition, a full-bridge class-D output stage with a gate driver featuring an optimized dead-time was presented to enhance power efficiency without considerable degradation of the THD.

The fabricated class-D audio amplifier showed power

Parameter	[2]	[11]	[14]	[15]	This work
Modulator architecture	Analog $\Delta\Sigma$	Digital $\Delta\Sigma$	Analog PWM*	Analog PWM**	Digital $\Delta\Sigma$
Process (µm)	CMOS 0.18	CMOS 0.18	CMOS 0.5	CMOS 0.5	CMOS 0.18
Power supply (V)	3.0	1.8	2.7	2.5	1.8
Pout (mW)	N/A	N/A	250	450	57
Sampling frequency (MHz)	3.2	N/A	0.45	0.2	1.024
Load impedance $(\Omega)$	32	36	8	8	16
Peak SNR (dB)	98.5	71	92	80	90
THD+N (%)	0.022	0.07 (THD)	0.05	0.07	0.03
Efficiency (%)	77	79	90	92	87.8
Bandwidth (kHz)	20	20	20	20	8

Table 5. Performance comparison

\* Sliding mode control

\*\* Rectangular-wave delta modulator

efficiency as high as 87.8 % and low THD+N of 0.03 % for a 1-kHz sinusoidal input signal. It has an output power of 57 mW with a load impedance of 16  $\Omega$  and a supply voltage of 1.8 V.

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