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# Sub-0.1 $\mu\text{m}$ MOSFET의 게이트전압 종속 캐리어 속도를 위한 정확한 RF 추출 방법

( Accurate RF Extraction Method for Gate Voltage-Dependent Carrier  
Velocity of Sub-0.1 $\mu\text{m}$  MOSFETs in the Saturation Region )

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요 약

Sub-0.1 $\mu\text{m}$ 로 스케일이 감소함에 따라 기생 저항 효과가 크게 발생하는 dc  $I_{ds}$  측정 데이터 없이 측정 S-파라미터로부터 얻어진 RF  $I_{ds}$ 를 사용하여 벌크 MOSFET의 포화영역에서 게이트 전압 종속 유효 캐리어 속도를 추출하는 새로운 방법이 개발되었다. 이 방법은 바이어스 종속 기생 게이트-소스 캐패시턴스와 유효 채널 길이의 복잡한 추출 없이 포화영역의 유효 캐리어 속도를 추출할 수 있게 한다. 이러한 RF 기술을 사용하여 벌크 포화 속도를 초과하는 전자 속도 overshoot 현상이 0.065 $\mu\text{m}$  게이트 길이의 벌크 N-MOSFET에서 관찰되었다.

## Abstract

A new method using RF  $I_{ds}$  determined from measured S-parameters is proposed to extract the gate-voltage dependent effective carrier velocity of bulk MOSFETs in the saturation region without additional dc  $I_{ds}$  measurement data suffering parasitic resistance effect that becomes larger with continuous down-scaling to sub-0.1 $\mu\text{m}$ . This method also allows us to extract the carrier velocity in the saturation region without the difficult extraction of bias-dependent parasitic gate-source capacitance and effective channel length. Using the RF technique, the electron velocity overshoot exceeding the bulk saturation velocity is observed in bulk N-MOSFETs with a polysilicon gate length of 0.065 $\mu\text{m}$ .

**Keywords** : MOSFET, CMOS, RF, carrier velocity, device modeling, S-parameter, parameter extraction

## I. INTRODUCTION

As successful down-scaling of channel length is continued below 0.1 $\mu\text{m}$  for MOSFETs, accurate values of experimentally determined effective carrier velocity  $v_{\text{eff}}$  in the saturation region are very important to determine the intrinsic speed and carrier transport

behavior in the channel region. Generally, the gate-voltage dependent  $v_{\text{eff}}$  is extracted by the following equation<sup>[1]</sup>:

$$\begin{aligned} v_{\text{eff}} &= \frac{I_{ds}}{WQ_{\text{in}}} \\ &= \frac{I_{ds}}{W \int_0^{V_{gs}} C_{gsd}(V_{gs}') dV_{gs}'} \\ &= \frac{I_{ds}}{\int_0^{V_{gs}} [C_{gsd}(V_{gs}') L_{\text{eff}}] dV_{gs}'} \end{aligned} \quad (1)$$

where  $L_{\text{eff}}$  is the effective channel length,  $W$  is the

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channel width and  $C_{gsd}' (= C_{gsd}/WL_{eff})$  is the gate-source-drain capacitance between gate and tied source and drain at  $V_{ds}=0V$  per unit channel area. However, the measurements of  $C_{gsd}$  at  $V_{ds}=0V$  using a very long-channel test device lead to velocity extraction errors, because the actual incremental charge  $dQ_{in}$  in the saturation region becomes smaller than that of  $C_{gsd}dV_{gs}$  at  $V_{ds}=0V$ . An another method using  $dQ_{in}$  at high  $V_{ds}$  is reported<sup>[2]</sup>, but  $dQ_{in}$  normalized by  $C_{ox}$  is still overestimated where  $C_{ox}$  is the oxide capacitance per unit channel area. Recently, a novel method<sup>[3]</sup> using  $g_{mi}/(WC_{gsi}') = g_{mi}/K$  at high  $V_{ds}$  where  $g_{mi}$  is the intrinsic transconductance,  $C_{gsi}'$  is the intrinsic gate-source channel capacitance per unit channel area, and  $K$  is the slope of the plot of  $C_{gs}$  versus  $L_{poly}$  is reported to avoid the errors in the traditional ones. However, this method produces the local carrier velocity at the point in the channel where  $\partial v_{eff}/\partial V_{gs} = 0$ <sup>[1,2]</sup>.

The carrier velocity extracted from  $g_{mi}/(WC_{gsi}')$  is overestimated when  $\partial v_{eff}/\partial V_{gs} > 0$  because  $g_{mi}/(WC_{gsi}') = v_{eff} + (Q_{in}/C_{gsi}')(\partial v_{eff}/\partial V_{gs})$  obtained by differentiating (1) in terms of  $V_{gs}$ <sup>[2]</sup>. Thus, the best way to extract the average carrier velocity in the saturation region is to use  $I_{ds}/(WQ_{in})$  at high  $V_{ds}$  directly.

It is well known that the measured dc  $I_{ds}$  is degraded by the reduction of internal  $V_{gsi}$  due to the potential drop between source resistance of MOSFETs. This degradation may be negligible in typical submicron MOSFETs, but it becomes much larger due to the increase of  $I_{ds}$  per unit width as channel length is scaled down to the sub-0.1 $\mu\text{m}$  regime. Thus, the previous methods<sup>[1-2]</sup> using  $I_{ds}/(WQ_{in})$  lead to underestimated extraction of  $v_{eff}$  due to a degraded dc  $I_{ds}$  value in sub-0.1 $\mu\text{m}$  devices.

Thus, in this paper, a new RF method based on the removal of the  $I_{ds}$  degradation effect using measured S-parameters is proposed to extract the effective carrier velocity of actual sub-0.1 $\mu\text{m}$  bulk MOSFETs accurately in the saturation region.

## II. NEW EXTRACTION METHOD

S-parameters are measured on typical bulk N-MOSFETs with different polysilicon gate length  $L_{poly}$  and 10 gate fingers of 5 $\mu\text{m}$  unit finger width. To remove RF probe pad parasitics, the accurate de-embedding technique was carried out by subtracting parasitics of open and short test structures from measured device S-parameters<sup>[4]</sup>. In order to reduce  $v_{eff}$  extraction error due to the overestimated  $Q_{in}$  in the conventional methods using (1) at  $V_{ds}=0V$ , the following equation in the saturation region is used:

$$v_{eff}(V_{gs}, V_{ds}) = \frac{I_{ds}}{\int_0^{V_{gs}} [C_{gsi}(V_{gs}', V_{ds})/L_{eff}] dV_{gs}'} \quad (2)$$

where  $C_{gsi}$  is the intrinsic gate-source capacitance in the saturation region.

To obtain  $C_{gsi}$  and  $L_{eff}$  accurately using C-V measurements, the parasitic overlap and fringe capacitance  $C_{gso}$  should be subtracted from the extracted gate-source capacitance  $C_{gs}$ . However, the accurate determination of  $C_{gso}$  that contains the voltage-dependent component is very difficult in sub-0.1 $\mu\text{m}$  CMOS technology.

In order to extract  $v_{eff}$  without the difficult extraction of voltage-dependent  $C_{gso}$  and  $L_{eff}$ , the following new equation is derived by substituting  $C_{gsi} = KL_{eff}$  into (2):

$$v_{eff}(V_{gs}, V_{ds}) = \frac{I_{ds}}{\int_0^{V_{gs}} K(V_{gs}', V_{ds}) dV_{gs}'} \quad (3)$$

In (3),  $K$  can be obtained by the slope of the plot of  $C_{gs}$  versus  $L_{poly}$ , because  $C_{gs} = C_{gso} + K(L_{poly} - \Delta L)$  where  $\Delta L$  is the channel length reduction.

Since dc  $I_{ds}$  in the saturation region is degraded by source resistance, a RF value of  $I_{ds}(rf)$  determined by the following voltage-integral of  $g_{mi}$  and the output conductance  $g_{ds}$  is used for removing the source resistance effect:

$$I_{ds(rf)}(V_{gs}, V_{ds}) =$$

$$\int_0^{V_{ds}} g_{ds}(0, V_{ds}') dV_{ds}' + \int_0^{V_{gs}} g_{mi}(V_{gs}', V_{ds}) dV_{gs}' \quad (4)$$

In order to extract  $C_{gs}$ ,  $g_{mi}$ , and  $g_{ds}$  from the measured S-parameters, a direct extraction technique<sup>[5-7]</sup> using a small-signal MOSFET equivalent circuit model in Fig. 1 has been applied.

In the high-frequency region, resistances and inductances are extracted from y-intercepts of Z-parameter equations<sup>[5]</sup> at  $V_{gs}=0V$  as a function of  $\omega^{-2}$ . The drain junction capacitance is determined at  $V_{gs}=0V$  using the following low-frequency equation in Fig. 2:

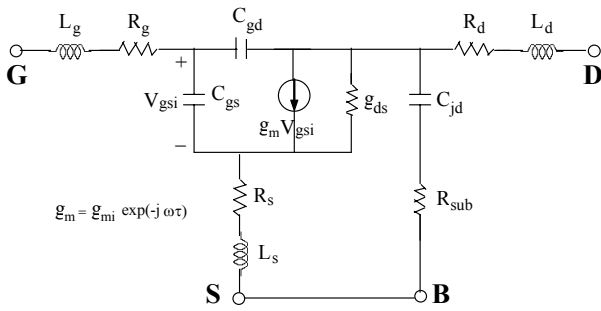


그림 1. 소스와 벌크가 연결된 소신호 MOSFET 등가회로.

Fig. 1. A small-signal MOSFET equivalent circuit with tied source and bulk.

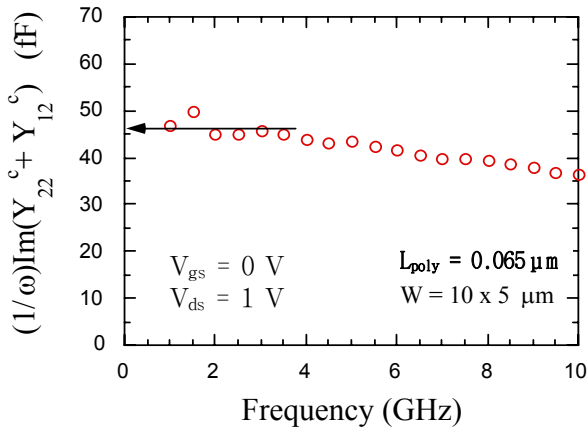


그림 2. 측정된  $(1/\omega)Imag(Y_{22}^c + Y_{12}^c)$  대 주파수 데이터

Fig. 2. The measured data of  $(1/\omega)Imag(Y_{22}^c + Y_{12}^c)$  versus frequency.

$$C_{jd} \approx \frac{1}{\omega} Imag(Y_{22}^c + Y_{12}^c) \quad (5)$$

where  $Y^c$ -parameters are obtained by subtracting extracted  $R_d$ ,  $R_g$ ,  $L_d$ , and  $L_g$  from measured S-parameters.

The substrate resistance  $R_{sub}$  is determined by  $k_1/C_{jd}^2$  at  $V_{gs}=0$  where  $k_1$  is the slope of  $Real(Y_{22}^c + Y_{12}^c)$  versus  $\omega^2$  at low-frequencies<sup>[6,7]</sup>. The values of  $C_{gs}$ ,  $g_m$ , and  $g_{ds}$  are extracted by the following equations:

$$C_{gs} = \frac{1}{\omega} Imag(Y_{11}^i + Y_{12}^i) \quad (6)$$

$$g_m = |Y_{21}^i - Y_{12}^i| \quad (7)$$

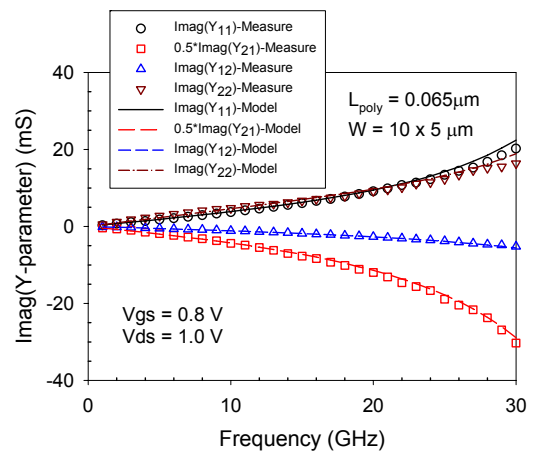
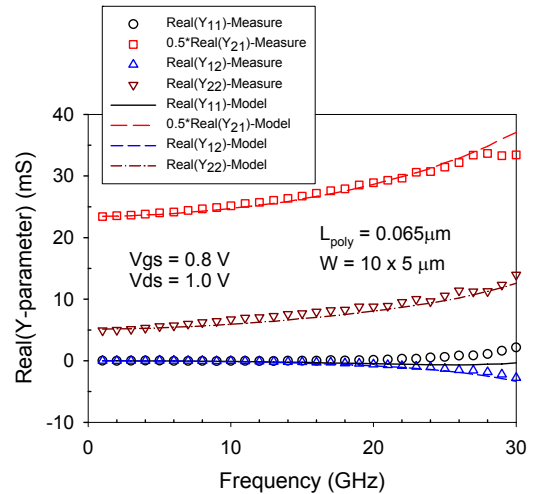


그림 3. Y-파라미터 측정치(symbol)와 모델(lines)값의 비교

Fig. 3. Comparison between and measured (symbol) and modeled (lines) Y-parameters.

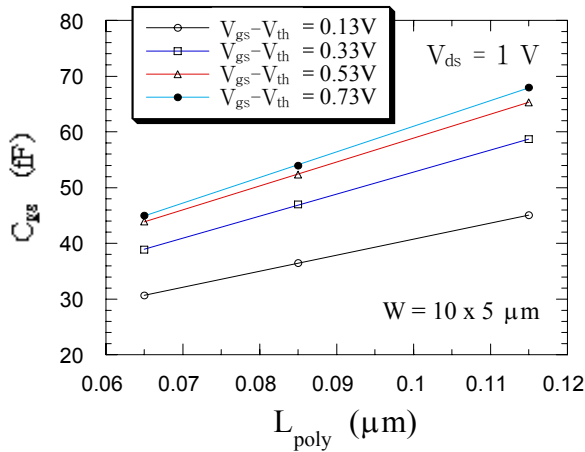


그림 4. 다양한  $V_{gs} - V_{th}$ 에서 추출된  $C_{gs}$  대  $L_{poly}$  데이터

Fig. 4. The extracted data of  $C_{gs}$  versus  $L_{poly}$  at various  $V_{gs} - V_{th}$ .

$$g_{ds} = \text{Real}(Y_{22}^i) \quad (8)$$

where  $Y^i$ -parameters are obtained by subtracting  $C_{jd}$ ,  $R_{sub}$ ,  $R_s$ , and  $L_s$  from the  $Y^c$ -parameters sequentially.

The accuracy of the parameter extraction has been demonstrated by observing excellent agreements between measured and modeled  $Y$ -parameters up to 30 GHz in Fig. 3. The values of  $K$  at various  $V_{gs}$  are determined from the slope of the best regression lines for  $C_{gs}$  versus  $L_{poly}$  in Fig. 4.

### III. RESULTS AND DISCUSSION

In Fig. 5, gate-voltage dependent data of  $v_{eff}$  at  $L_{poly} = 0.065\mu\text{m}$  obtained from the conventional method of (3) using  $I_{ds}(dc)$  are lower than those of the new one using  $I_{ds}(rf)$  in (4). The large extraction error of the conventional method is generated by degraded  $I_{ds}(dc)$  caused by the potential drop across  $R_s$ . Fig. 6 shows the current degradation effect that  $I_{ds}(dc)$  is about 19% smaller than  $I_{ds}(rf)$  due to the gate-source voltage reduction of  $I_{ds}R_s=0.08\text{V}$  at  $V_{gs}=0.9\text{V}$ . This indicates the current degradation effect should be eliminated to extract an accurate value of  $v_{eff}$  in deep sub-0.1- $\mu\text{m}$  devices. It is observed that  $v_{eff}$  exceeds the bulk saturation velocity ( $v_{sat} = 10^7\text{cm/s}$ ) for bulk

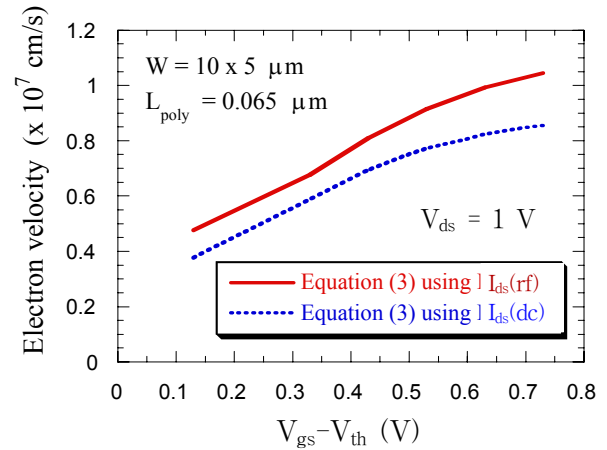


그림 5. 새로운 방법으로  $I_{ds}(rf)$ 를 사용하여 추출된 식(3)의  $V_{gs}$  증속  $v_{eff}$  곡선과  $I_{ds}(dc)$ 를 사용한 기존 방법 곡선과의 비교

Fig. 5. The  $V_{gs}$ -dependent curve of  $v_{eff}$  extracted from the new method of (3) using  $I_{ds}(rf)$ , compared with the conventional one of (3) using  $I_{ds}(dc)$ .

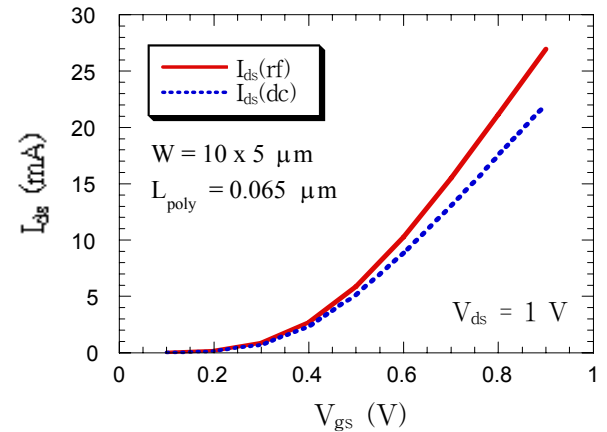


그림 6. 식 (4)의 RF  $I_{ds}(rf)$  데이터와 DC  $I_{ds}(dc)$  데이터를  $V_{gs}$  함수로 그린 그래프

Fig. 6. RF  $I_{ds}(rf)$  data of (4) and DC  $I_{ds}(dc)$  data as a function of  $V_{gs}$ .

N-MOSFETs with  $L_{poly} = 0.065\mu\text{m}$ , because of carrier acceleration due to velocity overshoot near the drain side<sup>[1, 8]</sup>.

Physically, the drain-source saturation voltage  $V_{ds}(sat)$  at the drain end of the inversion channel is expressed by  $V_{gs} - V_{th}$ . Thus, to analyze gate-voltage dependence of velocity in the saturation region, the effect of lateral channel electric field due to the  $V_{gs}$  increase should be incorporated together with that of vertical one. In particular, in sub-0.1 $\mu\text{m}$  bulk N-MOSFETs, the rising rate of lateral channel electric field with  $V_{gs} - V_{th}$  becomes larger due to

very short channel length. In Fig. 5, the linear increase of  $v_{eff}$  at low  $V_{gs} - V_{th}$  is primary due to the rise of lateral field, but the reduction of the increasing rate at high  $V_{gs} - V_{th}$  is due to velocity saturation and the rise of vertical field. This analysis will be very helpful to understand the gate-voltage dependent behavior of the cutoff frequency  $f_T$  and the maximum oscillation frequency  $f_{max}$  for deep sub-0.1- $\mu m$  devices in the saturation region.

#### IV. CONCLUSIONS

A new RF method using the RF value of  $I_{ds}$  obtained by the voltage-integral of  $g_{mi}$  and  $g_{ds}$  from measured S-parameters is proposed to extract  $V_{gs}$ -dependent  $v_{eff}$  of actual sub-0.1 $\mu m$  bulk MOSFETs in the saturation region accurately. This new method is developed to avoid the extraction error in conventional ones due to dc  $I_{ds}$  degradation that can't be neglected in sub-0.1 $\mu m$  MOSFETs. This technique based on the slope extraction of  $C_{gs}$  versus  $L_{poly}$  is more accurate than previous methods, because the difficult extraction of bias-dependent  $C_{gso}$  and  $L_{eff}$  is not needed. It is observed that electron velocity enhancement exceeding  $v_{eff}$  occurs in bulk N-MOSFETs with  $L_{poly} = 0.065\mu m$ .

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