

# Contact Parameter Computation and Analysis of Air Circuit Breaker with Permanent Magnet Actuator

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**Abstract** – An air circuit breaker (ACB) with novel double-breaker contact and permanent magnet actuator (PMA) is presented. Three-dimensional (3-D) finite element method (FEM) is employed to compute the electro-dynamic repulsion forces, including the Holm force and Lorentz force, which are acting on the static and movable contacts. The electro-dynamic repulsion forces of different contact pieces are computed, illustrating there is an optimal number of contact pieces for the ACB being studied. The electro-dynamic repulsion force of each contact, which varies from the outer position to the inner position, is also computed. Finally, the contacts of the double-breaker are manufactured according to the analyzed results to validate the simulations.

**Keywords:** Double-breaker contact, Permanent magnet actuator, Air circuit breaker, Electromagnetic repulsion force

## 1. Introduction

Circuit breaker (CB) is an indispensable element for switching on and off of power supply in a power system. The modern trend is to develop CBs which are compact in size and large in current interrupting capacity. Double-breaker CBs with two breaker contacts can interrupt higher short circuit or fault currents when compared to their single-breaker counterparts of similar size. However it is very difficult to drive the contacts of double-breaker CB using conventional spring actuator (SA). To reduce the size of CBs, permanent magnet actuator (PMA), which is becoming a key constituent of vacuum circuit breakers (VCB), is now being extensively developed [1-5]. As PMA is able to produce greater holding force than SA with the same physical size, PMA is finding increasing applications in the design and development of modern double-breaker CBs. Investigations and studies into the design of double-breaker CB with PMA, which includes the PMA design, PMA optimization, movement simulation [6], PMA control [7], short-time withstand current calculation, contact parameter computation and so on are challenging and topical issues facing the designers.

It is well known that computation of the electro-dynamic repulsion force is the key to optimal design of CBs. Indeed there is a wealth of work being reported on electro-

dynamic repulsion force computation. In [8], the short-time withstanding current of a spring operated double-breaker ACB is calculated. Ito and Li report their research on the blowout and electro-dynamic repulsion forces acting on the contacts of molded case circuit breakers [9-10]. Liu uses three-dimensional (3-D) finite element method (FEM) to study the electro-dynamic repulsion force of a single-breaker ACB driven by SA [11]. However, there is no literature that reports the computation of contact dynamics of double-breaker ACB with PMA.

The purpose of this paper is to present a new type of contacts with double-breaker in an ACB driven by PMA. 3-D FEM is employed to compute the electro-dynamic repulsion forces between the static and movable contacts. The electro-dynamic repulsion forces of different pieces of contacts are also computed, and each piece of contact is analyzed in details.

## 2. Mathematics Model

### 2.1 Holm force

To analyze the electro-dynamic repulsion force, it is assumed that either there is only one conducting zone, hereinafter referred as the conductive bridge in this paper, or all the conducting zones are focused at the center of the contact as shown in Fig. 1. Fig. 1(a) shows the cross-section of the contacts which include the movable contact, static contact and conductive bridge. Figs. 1(b) and 1(c) illustrate the cylindrical and rectangular contacts. Additionally, to simplify the computation, the conducting zone is considered as an equipotential superconducting ball with a radius  $r$  instead of being a plane. With these

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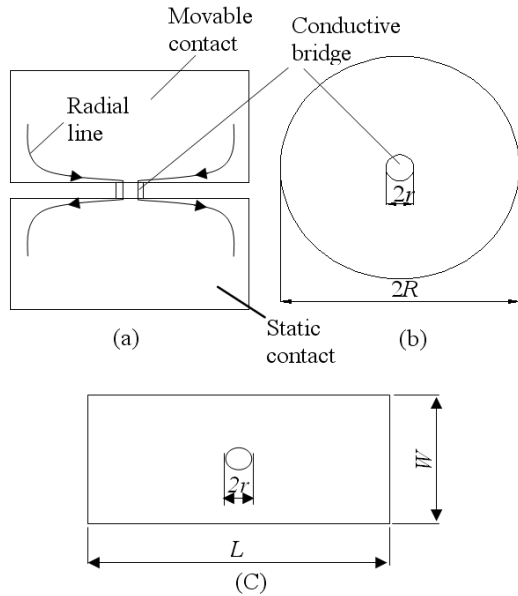
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assumptions, the shrink area is not an ellipsoidal surface but a series of spherical surfaces which are concentric with the superconducting ball, along the radial line in which the currents are flowing. The electro-dynamic repulsion force contributed by the shrink current is referred as the Holm force [12].

$$F_H = \frac{\mu_0}{4\pi} I^2 \ln \frac{R}{r} = \begin{cases} \frac{\mu_0}{4\pi} I^2 \ln \left( \frac{\xi H \pi R^2}{P} \right)^{1/2} \\ \frac{\mu_0}{4\pi} I^2 \ln \left( \frac{\xi H W L}{P} \right)^{1/2} \end{cases} \quad (1)$$

where,  $I$  is the current flowing through the contact,  $R$  is the contact radius of the cylindrical contact,  $W$  and  $L$  are the respective width and length of the rectangular contact,  $r$  is the radius of the conductive bridge,  $\xi$  is the surface conditioning coefficient which varies within the range [0.3-0.6],  $H$  is the Brinell hardness,  $P$  is the contact force.



**Fig. 1.** Contact model, (a) cross-section of the movable contact, static contact and conductive bridge (b) cylindrical contact (c) rectangular contact

## 2.2 Lorentz force

Since the eddy current has little effect on the electro-dynamic repulsion force, the static electromagnetic field equation can be employed to solve the current density and flux density distributions. The electric vector potential  $T$  is used to calculate the current density using

$$\mathbf{J} = \nabla \times \mathbf{T} \quad (2)$$

where  $T$  satisfies the governing equation

$$\nabla \times \left( \frac{1}{\sigma} \nabla \times \mathbf{T} \right) = 0 \quad (3)$$

where  $\sigma$  is the electric conductivity. The current constrain condition is

$$\oint_s \mathbf{T} \cdot d\mathbf{l} = \mathbf{I} \quad (4)$$

Once the current density  $\mathbf{J}$  is obtained, the magnetic vector potential  $\mathbf{A}$  is employed to decide the flux density  $\mathbf{B}$

$$\mathbf{B} = \nabla \times \mathbf{A} \quad (5)$$

In the whole field region,  $\mathbf{A}$  satisfies the following governing equation:

$$\nabla \times \left( \frac{1}{\mu} \nabla \times \mathbf{A} \right) = \mathbf{J} \quad (6)$$

where  $\mu$  is the permeability.

The contact force density  $f$  is dependent on the current density and flux density, and the electromagnetic force is calculated by

$$\mathbf{F} = \int_v f dV = \int_v \mathbf{J} \times \mathbf{B} dV \quad (7)$$

where  $V$  is the contact volume. Using the conductive bridge model, the Holm force and Lorentz force acting on the contact can be computed using FEM.

## 3. Computation of the Contact Electro-Dynamic Repulsion Force and Movement Simulation

### 3.1 The contact system of the ACB with PMA

Fig. 1 shows the proposed contact model for the ACB with PMA. The main mechanical motion system mainly consists of the PMA, a rotating shaft, a cam, insulated plastic, a guide track and a movable contact. When either the making coil or breaking coil of the PMA is excited, the movable iron of the PMA will move up or down to realize the making or breaking operation. The cam is driven by a movable iron, and the rotating shaft transmits the movement of the cam to the insulated plastic in the horizontal direction as shown in Fig. 2. Since the movable contact is latched together with the insulated plastic, it moves along the guide track.

Fig. 3 shows the open and closed positions of the static

contact and movable contact. Fig. 3(a) shows the open position between the static contact and the movable contact. In this CB, the distance  $d$  between the static and movable contacts is 22 mm. Fig. 3(b) shows the closed position and depicts the forces acting on the static and movable contacts. When the movable contact realizes the making operation, the current passes through the static and movable contacts as shown by the arrows in Fig. 3. The whole contact system is acted upon by the Holm force, Lorentz force, spring anti-force and thrust force which are generated by the PMA. Additionally, the movable parts are also acted upon by frictional forces as the contact moves.

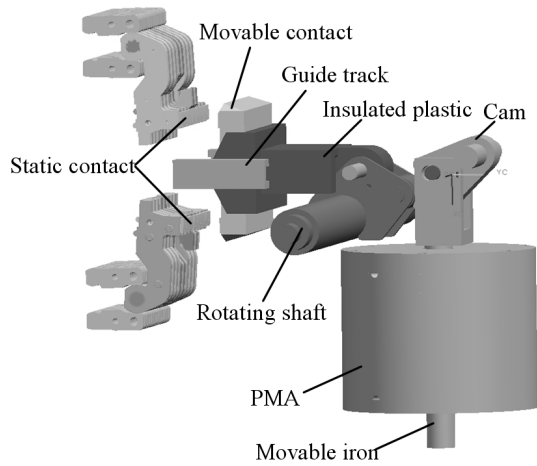


Fig. 2. Assembly of the contact located on the ACB

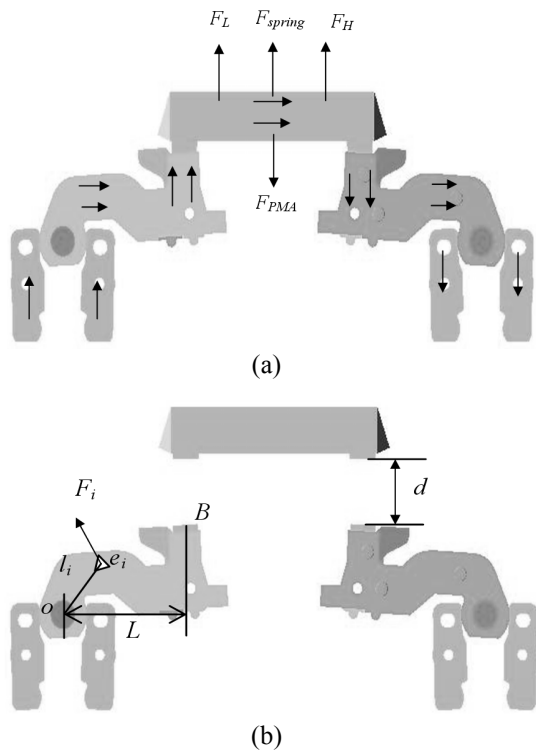


Fig. 3. The static contact and movable contact position: (a) At the open position; (b) At the closed position

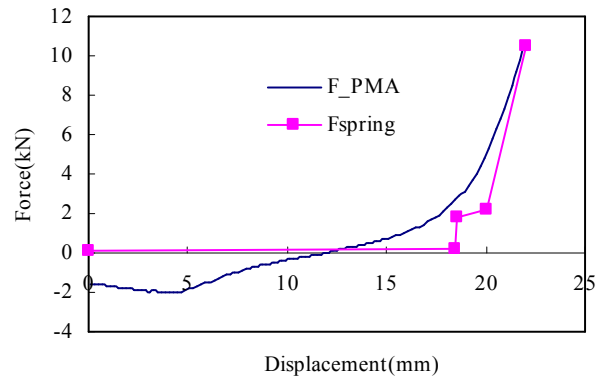
For each element  $e_i$  as shown in Fig. 3(b), the electrodynamic repulsion force to the conductive bridge center (point  $B$ ) can be computed from

$$F = \sum F'_i = \sum \frac{F_i \cdot l_i}{L} \quad (9)$$

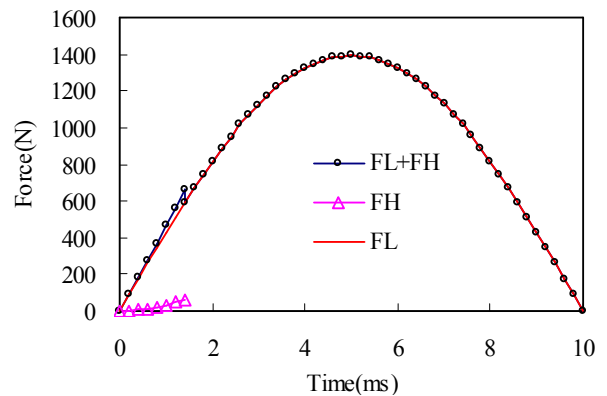
where  $F_i$  is the electromagnetic force of the static contact element,  $l_i$  is the distance between the element center and the rotor axis center (point  $O$ ),  $L$  is the distance between point  $O$  and point  $B$  and  $L=50\text{mm}$ ,  $F'_i$  is the converted electro-dynamic repulsion force of each element between point  $O$  and point  $B$ .

Fig. 4 shows the three forces acting against permanent magnet force  $F_{PMA}$ . Fig. 4(a) are  $F_{PMA}$  and the spring force with respect to displacement. Fig. 4(b) presents the variation of the Lorentz force  $F_L$  and Holm force  $F_H$  acting on phase A as a function of time. In the closed position, the contact system satisfies the following equation:

$$F_{PMA} = F_L + F_H + F_{spring} \quad (8)$$



(a)



(b)

Fig. 4. Three forces which are, namely  $F_{spring}$ ,  $F_L$  and  $F_H$  are acting against permanent magnet force: (a) permanent magnet force  $F_{PMA}$  and spring force  $F_{spring}$ ; (b) Lorentz force  $F_L$  and Holm force  $F_H$  for the phase A.

### 3.2 Computation of the contact electro-dynamic repulsion Force

The electro-dynamic force is computed by the conductive bridge model proposed in [9], in which the superconductive balls are substituted by cylindrical elements. The Holm force and Lorentz force acting on the movable contacts are computed by 3-D finite element analysis. The computed model is firstly built in the Unigraphics (UG) software and saved in parasolid format to allow the model to be recognized by the ANSYS finite element software. With this proposed arrangement, the finite element preprocessing time is substantially reduced. The detailed computation flow chart of this algorithm is shown in Fig. 5. In this study the force of one phase with constant direct current is evaluated by solving the current density  $J$  of each element with FEM. The  $J$  of each element is then loaded in order to compute the magnetic flux density  $B$ . Once  $J$  and  $B$  are obtained, the contact force can be computed using Eq. (7).

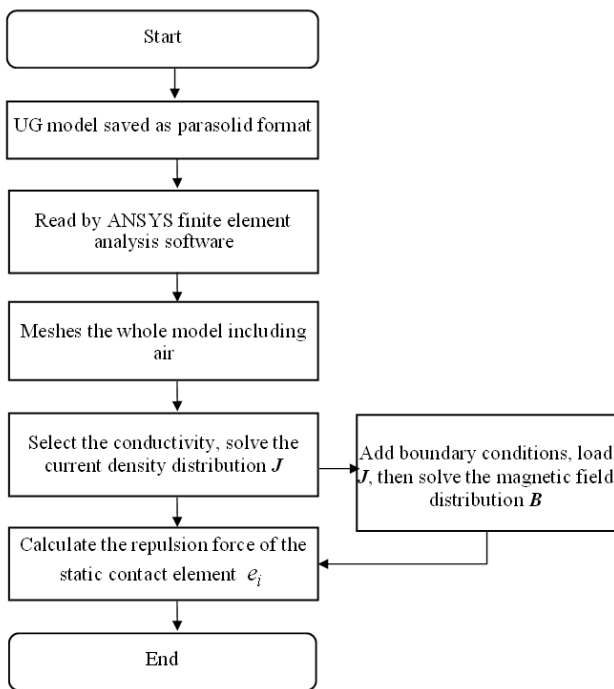


Fig. 5. Computation flow chart

### 3.3 Movement simulation of the contact

The movement of the contact can be co-simulated in the finite element analysis as well as in the Adams and Matlab software. The magnetic field is computed using FEM to find out the relationship among the flux linkage, displacement and current, and such information is stored in a look-up table. The control model, which is built in Matlab, is connected with the Adams model via input and output interfaces. Detailed movement simulation can be

referred to the work of our research group and hence is not repeated here [7]. Fig. 6 shows the result of the movement simulation of the contact.

## 4. Finite Element Analysis

Since the contacts are symmetrical both on the left and right and they are connected in series, a quarter of the model suffices for the computation of the repulsion force. The analyzed FEM domain is shown in Fig. 7. Two layers of air including Air I and Air II are used to build the model being studied. Air I is fine-meshed, while for the Air II

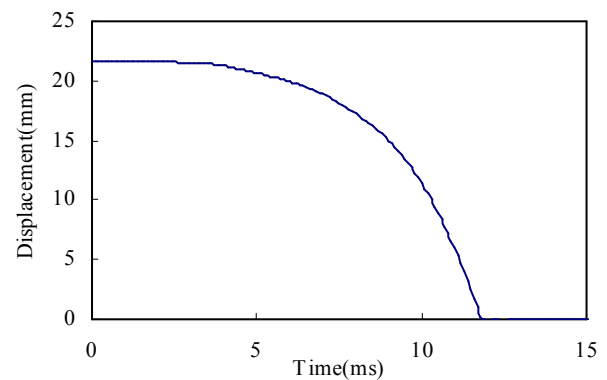


Fig. 6. The movement simulation of the contact

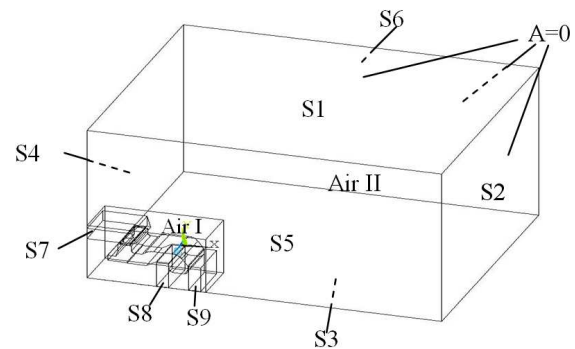


Fig. 7. The analyzed model in ANSYS

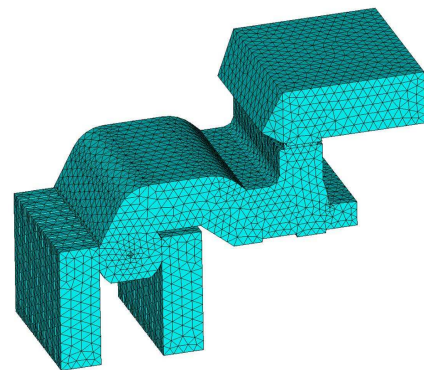


Fig. 8. Meshes of the contact for a quarter of the model

layer, the domain is coarse-meshed to reduce the computing time. The magnetic vector potential  $A$  of the boundaries S1, S2 and S6 is set to zero in the ANSYS model. 3-D FEM is employed to analyze the electro-dynamic repulsion force of the contacts. When computing the current density  $J$ , the freedom of VOLT in ANSYS is coupled to S7, S8 and S9. A node is chosen from S7 and supplied with a current of 50 kA; S8 and S9 are coupled with VOLT=0. Consequently, the current would circulate in

the contacts and their corresponding current density  $J$  is distributed automatically. Fig. 8 shows the meshes of a quarter of the model for the contacts. The element and node numbers are 46539 and 53925, respectively. Fig. 9 shows the current density distributions, including those in the parallel and single contacts. Since the short circuit current focuses on the conductive bridge between the movable contact and the static one, the maximum magnetic flux density can be above 4T as shown in Fig. 10.

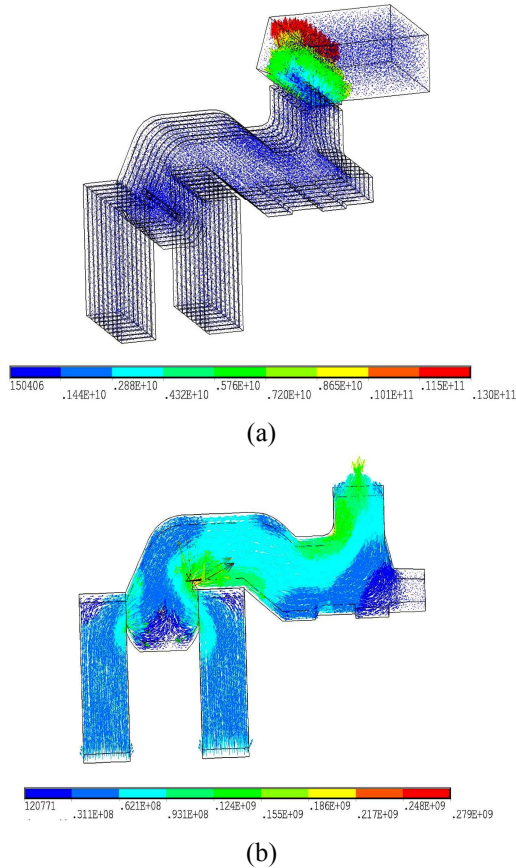


Fig. 9. Current density distribution (a) Parallel contact (b) Single contact

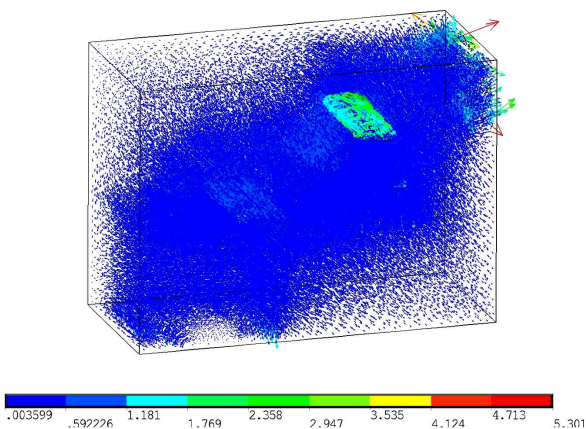


Fig. 10. Magnetic field distribution

## 5. Contact Parameter Analysis

### 5.1 The best pieces choice of static contact

Assuming the width ( $W$ ) of the static contact is constant in the low voltage ACB being designed, one has

$$W = w \cdot N \quad (10)$$

where,  $w$  is the width of each piece,  $N$  is the number of pieces and  $W=89.5\text{mm}$ . The electro-dynamic repulsion force for 2 to 20 contact pieces is computed as shown in Fig. 11. It can be seen that the electro-dynamic repulsion force acting on the static contacts decreases as the number of contact piece increases. The figure shows there is an optimal number of contact pieces. If the number of contact pieces is too large, the contact intensity will be weakened. On the other hand, if the number is too small, the electro-dynamic repulsion force will increase substantially. The computed profile also shows that the change from 12 to 20 pieces is not substantial. Thus for the double-breaker CB, the best number of static contact pieces is 16 if both the intensity and electro-dynamic repulsion force are taken into consideration collectively.

### 5.2 Electromagnetic repulsion force distribution analysis

The paper computes the electro-magnetic repulsion of double-breaker contacts. The computed results are found to concur with those of the single-break circuit breaker proposed in [11]. During the short circuit withstand test, the contacts are supplied with a direct current of 100 kA. Since the contacts are symmetrical on both left and right, the current intensity in the finite element analysis for the quarter model is taken as 50 kA. Fig. 11 depicts the electro-dynamic repulsion force of all the contact pieces. It can be observed that the electro-dynamic repulsion forces increases from the outermost piece (denoted as 1 in Fig.12) to the inner pieces (denoted as 5, 6, 7 and 8 in Fig. 12). The maximum value is larger than the minimum value by about 23.3% and such factor should be taken into consideration when designing the anti-force spring and PMA. The variation of electromagnetic repulsion force coincides with that of single contact circuit breaker, which explains why

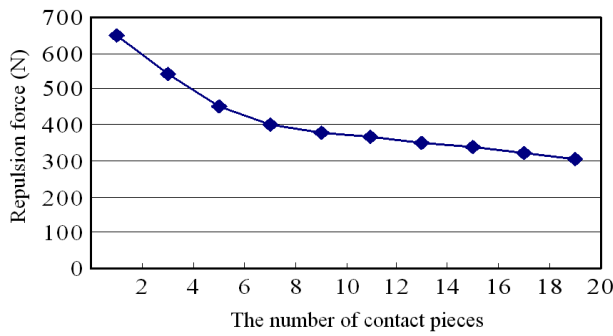


Fig. 11. The electro-dynamic repulsion force for different number of contact pieces with a current  $i=50\text{kA}$

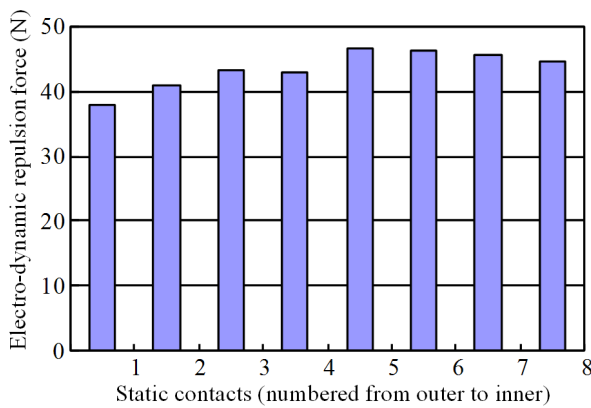


Fig. 12. Electro-dynamic repulsion force distribution of each pieces contact with a current  $i=50\text{ kA}$

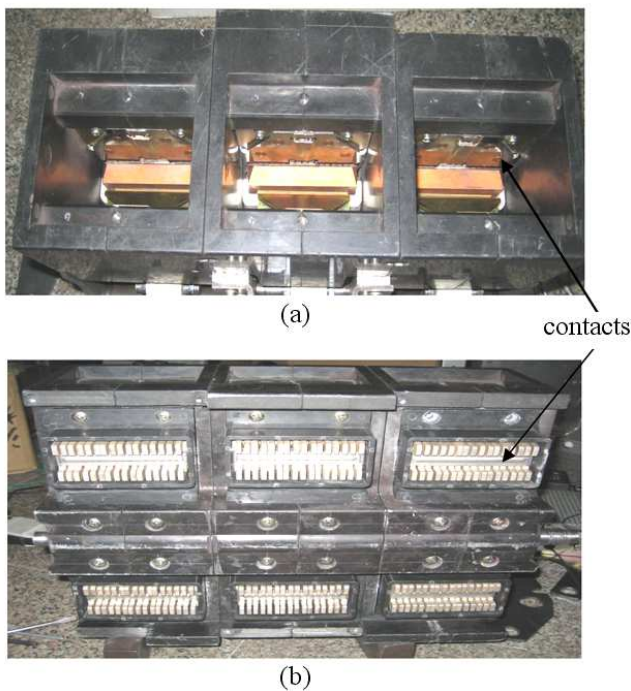


Fig. 13. Prototype and contacts: (a) Top overview; (b) Back overview

the outer contacts are ablated more readily when compared with those in the inner contacts as reported in [11] during the short circuit withstand test. Fig. 13 shows the prototype of a double-breaker contact for the ACB with PMA. The double-breaker contact of ACB driven by PMA is manufactured according to the analyzed results.

## 6. Conclusion

An air circuit breaker (ACB) with novel double-breaker contact and permanent magnet actuator (PMA) is presented in this paper. 3-D FEM is used to compute the electro-dynamic repulsion forces of double-breaker contact for an ACB with PMA successfully. For the proposed ACB it is found that, within limits, the electro-dynamic repulsion force acting on the static contact decreases as the number of the contact pieces increases. Additionally, it is found that the repulsion forces on the static contacts of the outermost pieces are lower than those in the inner pieces by about 23.3% and this factor must be taken into consideration in the optimal design of the double-breaker contact.

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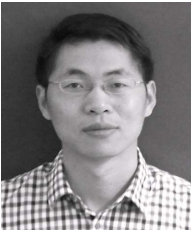


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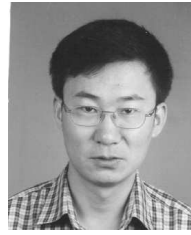
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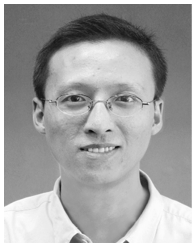
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