

Study on Generation of Harmonic Voltage using Synchronous Machine with d-axis and q-axis Harmonic Field Windings

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Abstract – We examined the generation of harmonic voltage by a synchronous machine adding d-axis and q-axis harmonic field windings in order to reduce the harmonics in a power line. We derived the expressions of the armature voltage in the case of supplying the currents with the frequency $n\omega$ to the d-axis and q-axis harmonic field windings. We constructed the synchronous machine adding the harmonic windings. In this paper, the expressions and the experimental results on the generation of harmonic voltages by the synchronous machine are presented.

Keywords: Harmonic voltage, Synchronous machine, Harmonic field winding, Symmetric coordinate system

1. Introduction

With the popularization of equipment using power semiconductors, harmonics have become a significant problem in power systems. Harmonics in power systems cause undesirable effects in the electrical machinery and apparatus on the load side. In particular, it is very important to remove low order harmonics such as the 5th and 7th harmonics, because they have a large influence on the electrical machinery and apparatus.

An LC filter is generally used to reduce the harmonics, but the LC filter is subjected the influence of the impedance value, which changes with the load condition in the power system. The LC filter may also succumb to burnout by overload. Therefore, an active filter has been studied to avoid these disadvantages in the LC filter [1]. However, the active filter will generate other harmonics in a different order because of the switching of the semiconductor. Moreover, there is a problem of the costs involved in the enlargement.

An absorption method of the power line harmonics using a synchronous machine has recently been investigated [2]. A method for practical application, however, has not yet been realized. When the synchronous machine is used for

reducing the harmonics, the equipment using the synchronous machine is expected to be more advantageous than the LC filter and the active filter in terms of the cost.

In this paper, the armature voltages are presented in the case of applying an AC voltage with angular frequency $n\omega$ to the d-axis harmonic field winding of a synchronous machine. Then, it is shown that harmonic voltages with angular frequency $(n-1)\omega$ and $(n+1)\omega$ are induced in the armature winding. Moreover, the equations of the harmonic voltage generated in the armature winding are shown in the case of supplying simultaneously the currents to the d-axis and q-axis harmonic field windings.

We constructed a synchronous machine to ultimately demonstrate the reduction of the harmonics in a power line [3]-[4]. The structure of this experimental synchronous machine is different from a usual synchronous machine and the experimental machine has both d-axis and q-axis field windings.

The power spectrum of the armature voltage was measured in the case of supplying the AC currents with frequency f to the harmonic field windings of the experimental synchronous machine. Then, it was shown that the ratios of the amplitudes of harmonic voltages with frequency $(n-1)f$ and $(n+1)f$ have the possibility to change.

2. Model of Synchronous Machine

Fig. 1 shows the winding diagram of a synchronous

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machine with dual harmonic field windings d2 and q2.

In this figure, a, b and c are 3-phase armature windings to absorb the harmonics contained in the power line. The winding d1 on the d-axis is the ordinary field winding.

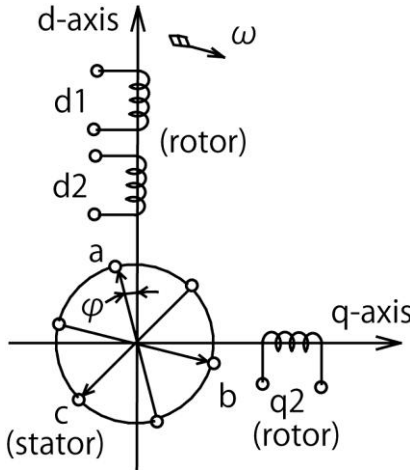


Fig. 1. Winding diagram of synchronous machine

In this figure, a, b and c are 3-phase armature windings to absorb the harmonics contained in the power line. The winding d1 on the d-axis is the ordinary field winding. φ is the electrical angle between the a-phase armature winding axis and the d-axis at $t = 0$. The DC voltage is applied to the field winding d1. Moreover, AC voltages with the frequency nf are applied to the harmonic field windings d2 and q2.

The design parameters of the experimental synchronous machine are given in Table 1.

Table 1. Design parameters of experimental synchronous machine

Frequency	60 Hz
Voltage	200 V
Current	1.9 A
Power	500 W
Number of Poles	4
Speed	1800 rpm

3. Expression on Harmonic Voltage of Armature Winding

In this section, the harmonic voltages of the armature winding are shown in the case of supplying AC currents to the harmonic windings d2 and q2.

We set the following assumptions:

- (1) The windings of the synchronous machine under consideration are circumferentially distributed for the sinusoid.

- (2) The rotor is rotating with the constant angular velocity ω .

- (3) The initial phase difference ψ between the d-axis and the a-phase armature winding is zero for the simplicity.

The AC voltage v_{d2n} with angular frequency ω is applied to the winding d2, and then the current i_{d2n} as shown in (1) flows into the winding d2.

$$i_{d2n} = I_{d2n} \cos(n\omega t + \phi_{nd}) \tag{1}$$

where I_{d2n} is the maximum value of i_{d2n} and Ψ_{nd} is the initial electrical angle at $t = 0$.

This AC current i_{d2n} can be resolved into two rotating currents i_{d2F} (positive-phase-sequence component) and i_{d2B} (negative-phase-sequence component) as (2), and each amplitude of the currents is one-half the maximum amplitude of i_{d2n} .

$$i_{d2n} = i_{d2F} + i_{d2B} \tag{2}$$

As shown in Fig. 2, i_{d2F} rotates with angular velocity $n\omega$ toward the revolution of the rotor and i_{d2B} reversely rotates with $n\omega$.

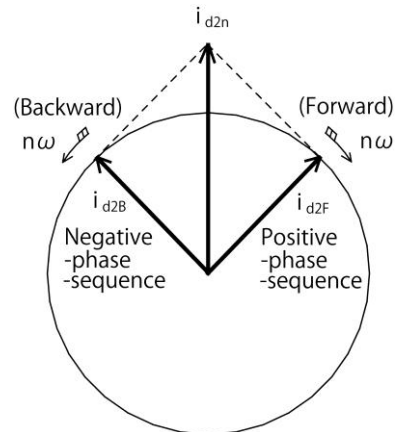


Fig. 2. Resolved currents into positive- and negative-phase-sequence components

Since the magnetic flux due to i_{d2F} rotates in the same direction as the rotor revolution, it is observed on the armature winding as magnetic flux rotating with $(n+1)\omega$ as shown in Fig. 3 (a). Therefore, voltage with angular frequency $(n+1)\omega$ is generated in the armature winding.

The harmonic voltage $v_{ad(n+1)}$ of the a-phase armature winding is expressed as the following equation.

$$v_{ad(n+1)} = (n+1)\omega \cdot M_{ad2} \cdot (I_{d2n}/2) \times \cos\{(n+1)\omega t + \phi_{nd}\} \tag{3}$$

where M_{ad2} is the mutual inductance between the a-phase armature winding and the winding d2.

In contrast, since the magnetic flux due to i_{d2B} rotates in the inverse direction to the rotor revolution, it is observed on the armature winding as magnetic flux rotating with $(n-1)\omega$ as shown in Fig. 3 (b). Therefore, the harmonic voltage with angular frequency $(n-1)\omega$ is generated in the armature winding.

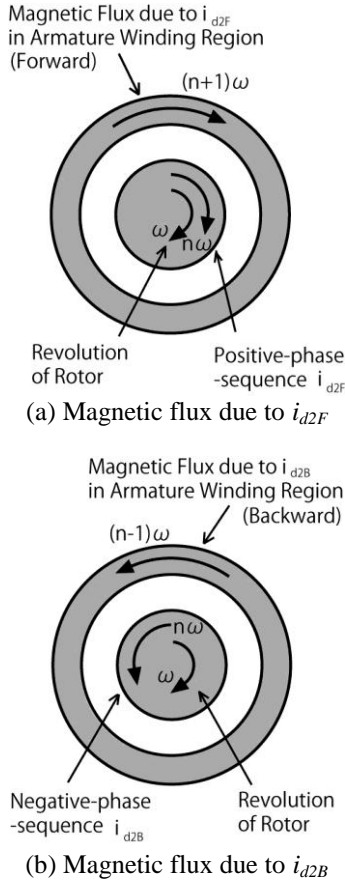


Fig. 3. Magnetic flux in armature winding region

The harmonic voltage $v_{ad(n-1)}$ of the a-phase armature winding is expressed as the following equation.

$$v_{ad(n-1)} = (n-1)\omega \cdot M_{ad2} \cdot (I_{d2n}/2) \times \cos\{(n-1)\omega t + \phi_{nd}\} \quad (4)$$

Consequently, by supplying the AC current with angular frequency $n\omega$ to the winding d2, the two harmonic voltages with angular frequency $(n+1)\omega$ and $(n-1)\omega$ are generated in the a-phase armature winding.

From (3) and (4), the ratio $|v_{ad(n+1)}|/|v_{ad(n-1)}|$ is as follows.

$$\left| \frac{v_{ad(n+1)}}{v_{ad(n-1)}} \right| = (n+1)/(n-1) \quad (5)$$

Therefore, the ratio depends on only n , and it becomes constant value.

In order to change separately the amplitudes and the phases of the two harmonic voltages with angular frequency $(n+1)\omega$ and $(n-1)\omega$, the AC voltage v_{q2n} with angular frequency $n\omega$ is applied to the winding q2. Then, the current i_{q2n} as shown in (6) flows into the winding q2.

$$i_{q2n} = I_{q2n} \cos(n\omega t + \phi_{nq}) \quad (6)$$

where I_{q2n} is the maximum value of i_{q2n} and ϕ_{nq} is the initial electrical angle at $t = 0$.

As well as the current i_{d2n} in the winding d2, i_{q2n} is resolved into the positive-phase-sequence component i_{q2F} and the negative-phase-sequence component i_{q2B} .

$$i_{q2n} = i_{q2F} + i_{q2B} \quad (7)$$

The harmonic voltages generated by i_{q2F} and i_{q2B} are made to be $v_{aq(n+1)}$ and $v_{aq(n-1)}$, respectively. The angular frequency of $v_{aq(n+1)}$ is $(n+1)\omega$ and that of $v_{aq(n-1)}$ is $(n-1)\omega$.

These harmonic voltages are derived as the following equations, when the spatial phase difference $\pi/2$ of the winding q2 for the d2 winding is considered.

$$v_{aq(n+1)} = (n+1)\omega \cdot M_{aq2} \cdot (I_{q2n}/2) \times \cos\{(n+1)\omega t + \phi_{nq} + \pi/2\} \quad (8)$$

$$v_{aq(n-1)} = (n-1)\omega \cdot M_{aq2} \cdot (I_{q2n}/2) \times \cos\{(n-1)\omega t + \phi_{nq} - \pi/2\} \quad (9)$$

where M_{aq2} is the mutual inductance between the a-phase armature winding and the winding q2.

By assuming that winding d2 and winding q2 are symmetrical two-phase winding, $M_{ad2} = M_{aq2} = M_{a2}$ is set in the following. From (3) and (8), the total voltage $v_{a(n+1)}$ with angular frequency $(n+1)\omega$ in the a-phase armature winding is given as the following equation.

$$v_{a(n+1)} = v_{ad(n+1)} + v_{aq(n+1)} = (n+1)\omega \cdot M_{a2} \cdot \left[(I_{d2n}/2) \cos\{(n+1)\omega t + \phi_{nd}\} + (I_{q2n}/2) \cos\{(n+1)\omega t + \phi_{nd} + \pi/2\} \right] \quad (10)$$

Moreover, from (4) and (9), the total voltage $v_{a(n-1)}$ with angular frequency $(n-1)\omega$ in the a-phase armature

winding is given as the following equation.

$$\begin{aligned} V_{a(n-1)} &= V_{ad(n-1)} + V_{aq(n-1)} \\ &= (n-1)\omega \cdot M_{a2} \cdot \left[\left(\frac{I_{d2n}}{2} \right) \cos\{(n-1)\omega t + \phi_{nd}\} \right. \\ &\quad \left. + \left(\frac{I_{q2n}}{2} \right) \cos\{(n-1)\omega t + \phi_{nd} - \pi/2\} \right] \end{aligned} \quad (11)$$

By substituting the value of $2\pi f$ for ω in (10) and (11), it is possible to use them as the relational expressions of the frequency f .

Similarly, the harmonic voltages on the b-phase and the c-phase can be obtained.

4. Experiment on Harmonic Voltage of Armature Winding

Fig. 4 shows the circuit diagram for an experiment on the generation of harmonic voltages using the experimental synchronous machine. The frequency f of the power line is 60 (Hz). The windings d2 and q2 are connected to an oscillator (frequency: nf). The phases of both currents are able to change separately by the phase shifters shown in Fig. 4. The amplitudes of both currents are also able to be adjusted separately by the power amplifiers.

Fig. 5 shows the power spectrums of the armature winding voltage obtained by an FFT analyzer in the case of supplying currents with the frequency $4f$ and $6f$ to only the winding q2 ($I_{d2n} = 0$ A, $I_{q2n} = 0.2$ A). For the frequency of $4f$ (Fig. 5(a)), it is confirmed that harmonic voltages of $3f$ and $5f$ are generated in the armature winding. Moreover, for the frequency $6f$ (Fig. 5(b)), harmonic voltages of $5f$ and $7f$ are confirmed.

(4) is also applicable for the case of supplying the current to the q-axis winding. By substituting 4 for n in this equation, the ratio of harmonic voltage becomes $5/3 \approx 1.67$. Moreover, the ratio is $7/5 = 1.4$ for $n = 6$. These values almost agree with the experimental result.

When an AC current with frequency nf is supplied to the winding d2, induced current flows in the winding d1 on the same d-axis and the magnetic flux due to the current in the winding d2 greatly decreases. Therefore, in order to prevent induced current, the reactor shown in Fig. 4 is connected to a circuit for the winding d1.

However, the reduction of the magnetic flux due to the induced current is occurred, since the inductance value of the reactor is finite.

The maximum value I_{d2n} of AC current i_{d2n} in the

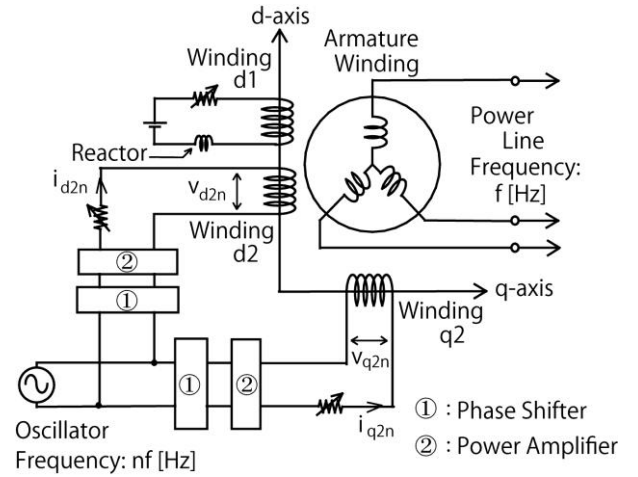


Fig. 4. Circuit Diagram for Experiment

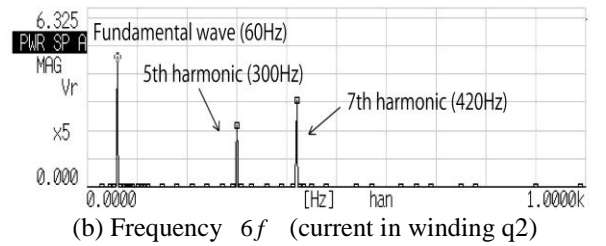
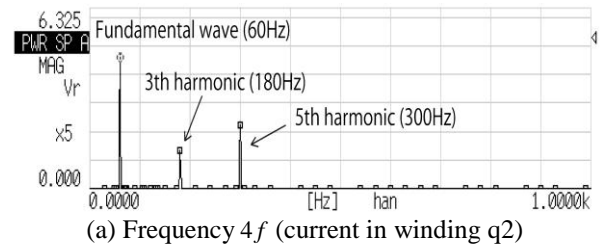


Fig. 5. Power spectrum of voltage of armature winding ($I_{d2n}/\sqrt{2} = 0$ A, $I_{q2n}/\sqrt{2} = 0.2$ A)

winding d2 can be separated as the following equation.

$$I_{d2n} = I_{d2ne} + I_{d2ni} \quad (12)$$

where, I_{d2ne} is effective component, which generates the magnetic flux and I_{d2ni} is non-effective component of which the magnetic flux is canceled by the magnetic flux due to the induced current of the winding d1.

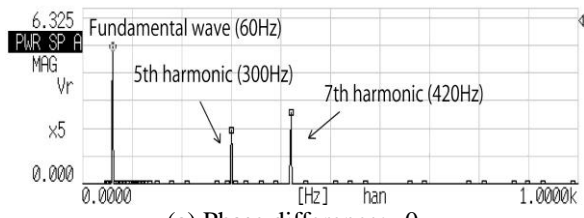
Fig. 6 shows the power spectrums of the armature voltage in the case of the frequency $6f$ and the current $I_{d2ne}/\sqrt{2} = I_{q2n}/\sqrt{2} = 0.15$ A.

Fig. 6 (a) shows the power spectrum in the case of $\phi_{dn} = \phi_{qn}$. In addition, Figs. 6(b) - 6(d) show the power spectrum in changing the phase of i_{d2n} by the phase shifter. These figures indicate that the ratio to the 5th and 7th harmonic voltages changes with the phase difference

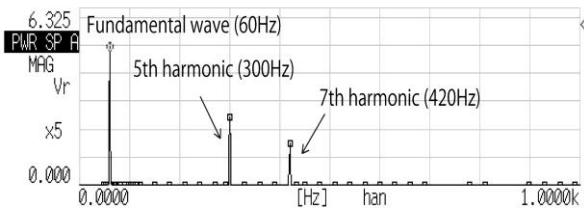
between i_{d2n} and i_{q2n} .

In Fig. 6(c), the 5th harmonic is large compared with the value in other figures, and the 7th harmonic becomes almost 0. This is confirmed by substituting $\phi_{dn} = \phi_{qn} + \pi/2$ for (10) and (11).

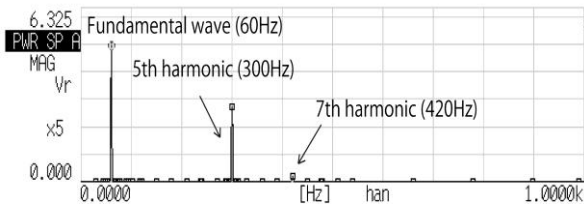
In contrast, in Fig. 6(d), the 7th harmonic is large compared with the value in other figures, and the 5th harmonic becomes almost 0. Similarly, this can also be confirmed by substituting $\phi_{dn} = \phi_{qn} - \pi/2$ for (10) and (11).



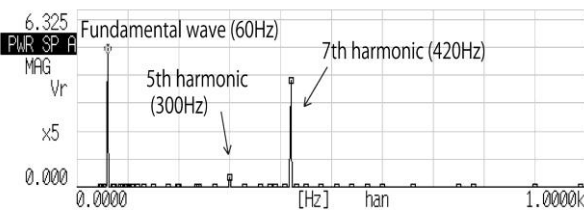
(a) Phase difference: 0
(i_{d2n} and i_{q2n} are equal to the same phase.)



(b) Phase difference: $\pi/6$ (i_{d2n} is leading from i_{q2n} .)



(c) Phase difference: $\pi/2$ (i_{d2n} is leading from i_{q2n} .)



(d) Phase difference: $-\pi/2$ (i_{d2n} is lagging from i_{q2n} .)

Fig. 6. Power spectrum of voltage of armature winding
($I_{d2n} / \sqrt{2} = I_{q2n} / \sqrt{2} = 0.15$ A)

5. Conclusions

In this paper, the equations of the harmonic voltage generated in the armature winding are shown in the case of

supplying currents with angle frequency $n\omega$ (frequency nf) to the d-axis and the q-axis harmonic field windings.

We constructed a synchronous machine to demonstrate finally the reduction of the harmonics in a power line. The power spectrum of the armature voltage was measured in the case of supplying the AC currents with frequency nf to the harmonic field windings of the experimental synchronous machine.

The results obtained are as follows:

- (1) By supplying AC current with frequency nf to the harmonic field winding, harmonic voltages with frequency $(n-1)f$ and $(n+1)f$ are generated in the armature winding.
- (2) The equations of harmonic voltages generated in the armature winding were derived in the case of supplying AC currents with frequency nf to the d-axis and q-axis harmonic windings.
- (3) The theory and the experiment clarified that the ratios of the amplitudes of the harmonic voltages in the armature winding can be changed in the case of supplying AC currents to the d-axis and q-axis harmonic windings.

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