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# Implementation of a Robust Fuzzy Adaptive Speed Tracking Control System for Permanent Magnet Synchronous Motors

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### **Abstract**

This paper presents a fuzzy adaptive speed controller that guarantees a fast dynamic behavior and a precise trajectory tracking capability for surfaced-mounted permanent magnet synchronous motors (SPMSMs). The proposed fuzzy adaptive control strategy is simple and easy to implement. In addition, the proposed speed controller is very robust to system parameter and load torque variations because it does not require any accurate parameter values. The global stability of the proposed control system is analytically verified. To evaluate the proposed fuzzy adaptive speed controller, both simulation and experimental results are shown under motor parameter and load torque variations on a prototype SPMSM drive system.

Key words: Adaptive control, Fuzzy control, Permanent magnet synchronous motor (PMSM), Speed control, Uncertainties

### NOMENCLATURE

 $\theta$ : Electrical rotor position;

 $\theta_d$ : Desired electrical rotor position;

 $\omega$ : Electrical rotor angular speed;

 $\omega_d$ : Desired electrical rotor angular speed;

 $e_1: \theta - \theta_d = \int_0^t (\omega - \omega_d) d\tau;$ 

 $e_2$ :  $\omega - \omega_d$ ;

 $i_{as}$ : q-axis current;

 $i_{qsd}$ : Desired q-axis current;

 $i_{ds}$ : d-axis current;

 $i_{dsd}$ : Desired d-axis current;

 $V_{as}$ : q-axis control input voltage;

 $V_{ds}$ : d-axis control input voltage;

 $T_L$ : Load torque;

*p* : Number of poles;

 $R_s$ : Stator resistance;

 $L_s$ : Stator inductance;

J: Rotor equivalent inertia;

B: Viscous friction coefficient;

 $\lambda_m$ : Magnetic flux;

# I. INTRODUCTION

Permanent magnet synchronous motor (PMSM) drives have been used for various industrial applications such as electric vehicles (EV, Plug-in Hybrid EV, Fuel Cell EV), CNC machine tools, hard disk drives, and industrial robots since they have some excellent characteristics [1]-[17], such as high efficiency, low noise, low inertia, robustness, high torque to current ratio, etc. Unfortunately, PMSMs are not easy to control because they have nonlinearities due to nonlinear magnetic materials and coupling of the state variables (currents and speed) in the dynamic model. To guarantee a fast transient response and an excellent trajectory tracking capability, various nonlinear control methods such as [4]-[13] have been reported. These methods include robust control [4], disturbance observer based control [5]-[7], adaptive control [8]-[9], nonlinear feedback linearization [10]-[11], and neural network control [12], [13]. However, most of the previous control algorithms have been established on the assumption that knowledge of the PMSM parameters is available. In recent years, some PMSM control schemes based on the fuzzy control theory [14]-[17] have also been presented. These fuzzy PMSM control methods

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[14]-[17] may give a satisfactory performance. However, there have been no systematic and consistent design techniques to prove the stability of closed-loop fuzzy control systems because they are based on the heuristics-based fuzzy approach [18]. In addition, the control performance of the PMSM can be seriously affected by system parameter variations and external disturbances. Consequently, most previous control strategies may not satisfy the requirements for closed-loop system stability under uncertainties such as motor parameter and load torque variations.

Meanwhile, the fuzzy adaptive control design has been an alternative solution which can control uncertain nonlinear systems [18], [19]. The fundamental design procedure of the fuzzy adaptive control system is as follows: first, a fuzzy model is constructed to identify the input/output behaviors of an uncertain system; next, a controller for the uncertain system is designed; and then adaption control laws are decided to tune the parameters of the fuzzy model.

This paper proposes a fuzzy adaptive speed controller which can ensure a fast transient response and an accurate tracking surfaced-mounted capability for permanent synchronous motors (SPMSMs). The proposed fuzzy adaptive control algorithm is simple and easy to implement. Furthermore, the proposed control method is very robust to variations of the motor parameters and load torque since it does not require exact system parameter and load torque values. The proposed speed control law consists of two terms: a feedback term and a fuzzy adaptive compensating term. That is, the feedback term stabilizes the error dynamics, while the fuzzy adaptive compensating term makes up for model parameter and load torque variations. In this paper, the global stability of the proposed fuzzy adaptive control system is analytically proven. To validate the feasibility of the proposed fuzzy adaptive speed controller, simulation and experimental results are presented under uncertainties (i.e., motor parameter and load torque variations) with a prototype SPMSM drive system.

This paper is organized as follows. Section II describes the design problem. The design and stability analysis of the proposed fuzzy adaptive controller are fully illustrated in Section III. Section VI gives simulation and experimental results to prove the effectiveness of the proposed control algorithm. Finally, conclusions are presented in Section V.

# II. DESIGN PROBLEM DESCRIPTION

The dynamic model of a surface-mounted PMSM (SPMSM) where the *d*-axis of the synchronously rotating reference frame is oriented to the rotor flux vector is given by:

$$\dot{\omega} = k_1 i_{qs} - k_2 \omega - k_3 T_L 
i_{qs} = -k_4 i_{qs} - k_5 \omega + k_6 V_{qs} - \omega i_{ds} 
i_{ds} = -k_4 i_{ds} + k_6 V_{ds} + \omega i_{qs}$$
(1)

where:

$$k_1 = \frac{3}{2} \frac{1}{J} \frac{p^2}{4} \lambda_m, \ k_2 = \frac{B}{J}, \ k_3 = \frac{p}{2J},$$
$$k_4 = \frac{R_s}{L_s}, \ k_5 = \frac{\lambda_m}{L_s}, \ k_6 = \frac{1}{L_s}$$

Note that the load torque disturbance  $T_L$  as well as the uncertainties of the parameters  $k_i$  can directly affect the control performance.

To design a robust fuzzy adaptive speed controller, the following assumptions are made:

A1:  $\omega$ ,  $i_{qs}$ , and  $i_{ds}$  are measurable.

A2: The desired speed  $\omega_d$  is constant.

Most of the previous PMSM control schemes use the assumptions A1-2, and almost all of the previous methods are based on the restrictive assumption that  $k_i$  is accurately known. Fig. 1 shows a block diagram of a general vector-controlled SPMSM control system. As shown in Fig. 1, the position or speed controller outputs the desired q-axis current  $i_{asd}$  which is used as the input of the current controller. Then from the desired and measured qd currents, the current controller properly generates control inputs  $(V_{qs}, V_{ds})$  that can regulate the motor speed  $(\omega)$  and the electromagnetic torque. Note that the desired d-axis current  $i_{dsd}$  is usually set to zero. There is an exception for a field-weakening operation over rated speed. For field-oriented control (FOC), the two actual phase currents  $(i_a, i_b)$  are measured and then transformed into q-axis and d-axis currents  $(i_{qs}, i_{ds})$  using coordinate transformation formulas (i.e., Park's and transformations).

Using the FOC system, the PMSM drive system can be reduced to the following first-order dynamic equation [6], [9]:

$$\dot{\omega}(t) = k_1 i_{as}(t) - k_2 \omega(t) - k_3 T_L \tag{2}$$

It should be noted that many previous FOC methods such as [6], [9] were developed by using the above first-order equation (2). Considering this fact, the focus of this paper will be on proposing a fuzzy adaptive speed controller that produces a q-axis command current  $i_{qsd}$  for the speed dynamic model (2) under the assumptions A1-2. Furthermore, a conventional PI current controller will be adopted to evaluate the overall performance of the proposed speed controller.

The following lemmas will be used to prove the stability of the proposed control system.

Lemma 1 [20]: Consider the following linear system:

$$\dot{x}(t) = Ax(t) + Bu(t), \qquad y(t) = Cx(t)$$

where  $x \in \mathbb{R}^n$ ;  $u \in \mathbb{R}^m$ ;  $y \in \mathbb{R}^p$ ; and A, B, and C are constant matrices with appropriate dimensions. Assume that the control input u(t) belongs to  $L_2$  and the transfer function

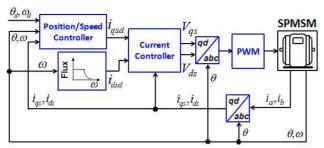


Fig. 1. Block diagram of a general vector-controlled SPMSM control system.

 $C(sI-A)^{-1}B$  is stable and strictly proper. Then y(t) is continuous and it converges to zero.

Lemma 2 [20]: Let f(t) be a differentiable function of t. If f(t) is bounded and f(t) has a finite limit as time approaches infinity, then f(t) converges to zero.

# III. FUZZY ADAPTIVE CONTROLLER DESIGN AND STABILITY ANALYSIS

By introducing the error vector  $e = [e_1, e_2]^T$  where  $e_1 = \int_0^t e_2 d\tau$  and  $e_2 = \omega - \omega_d$ , the following error dynamics can be obtained from (2):

$$\dot{e}_1 = e_2 
\dot{e}_2 = k_1 i_{as} - k_2 \omega - k_3 T_L$$
(3)

The error dynamics (3) is rearranged as:

$$\dot{e}_1 = e_2 
\dot{e}_2 = -\gamma e_2 + k_1 [i_{ee} - \eta(t)]$$
(4)

where  $\eta(t)$  is defined as:

$$\eta(t) = \frac{1}{k_1} (k_2 \omega + k_3 T_L - \gamma e_2)$$
 (5)

and  $\gamma > 0$  is a design parameter.

Theorem 1: Assume that the term  $\eta(t)$  of (5) is accurately known. Let  $i_{qs} = i_{qsd}$  be given by:

$$i_{as} = i_{asd} = -\delta\sigma + \eta(t) \tag{6}$$

where  $\delta > 0$ ,  $\sigma = \gamma e_1 + e_2$ , and  $\gamma > 0$ . Then, e converges to zero.

Proof: Define the Lyapunov functional as:

$$V_0 = \frac{1}{2} [\kappa e_1^2 + \sigma^2]$$
 (7)

where  $\kappa$  is a sufficiently small positive constant satisfying:

$$4\delta \gamma k_1 > \kappa > 0 \tag{8}$$

The time derivative of (7) along the error dynamics (4) is written by:

$$\dot{V}_0 = \kappa e_1 \dot{e}_1 + \sigma \dot{\sigma} \tag{9}$$

The error dynamics (4) implies that:

$$\dot{\sigma} = \gamma \dot{e}_1 + \dot{e}_2 = \gamma e_2 - \gamma e_2 + k_1 [i_{qs} - \eta(t)]$$

$$= \gamma e_2 - \gamma e_2 + k_1 [-\delta \sigma + \eta(t) - \eta(t)] = -k_1 \delta \sigma$$
(10)

Thus, (9) can be reduced to:

$$\dot{V}_0 \le \kappa e_1(\sigma - \gamma e_1) - k_1 \delta \sigma^2 = -e_r^T Q e_r \tag{11}$$

where  $e_r = [e_1, \sigma]^T$  and Q is a  $2 \times 2$  matrix given by:

$$Q = \begin{bmatrix} \kappa \gamma & -0.5\kappa \\ -0.5\kappa & k_1 \delta \end{bmatrix}$$
 (12)

which is positive definite as long as the inequality (8) is satisfied. This completes the proof.  $\nabla\nabla\nabla$ 

The term  $i_{qsd}$  of (6) requires accurate knowledge of  $\eta(t)$ . Because  $\eta(t)$  is not known accurately, a r-rule fuzzy model  $\eta_f(t)$  is applied to approximate  $\eta(t)$ . The ith fuzzy rule of  $\eta_f(t)$  is of the following form:

Rule i for 
$$\eta_f(t)$$
: IF  $e_1$  is  $F_{1i}$  and  $e_2$  is  $F_{2i}$ , THEN  $\eta_f(t)$  is  $G_i$ .

where  $F_{1i}$  and  $F_{2i}$  ( $i=1,\cdots,r$ ) denote the fuzzy sets associated with  $e_1$  and  $e_2$ , where r is the number of fuzzy rules and  $G_i$  are the fuzzy singletons for  $\eta_f(t)$ . The fuzzy sets  $F_{1i}$  and  $F_{2i}$  are characterized by the membership functions  $m_{1i}(e_1)$  and  $m_{2i}(e_2)$ . Based on the standard fuzzy inference method (using a singleton fuzzifier, a product fuzzy inference and a weighted average defuzzifier), the final output  $\eta_f(t)$  of the above fuzzy model can be represented as follows:

$$\eta_f = \xi^T h(e) = \sum_{i=1}^r \xi_i h_i(e)$$
(13)

where  $\xi = [\xi_1, \dots, \xi_r]^T$  is the adjustable parameter vector, and  $h = [h_1, \dots, h_r]^T$  is the fuzzy basis function vector given by:

$$h_{i}(e) = \frac{\prod_{j=1}^{2} m_{jk}(e_{j})}{\sum_{k=1}^{r} \prod_{j=1}^{2} m_{jk}(e_{j})}, i = 1, 2, \dots, r$$

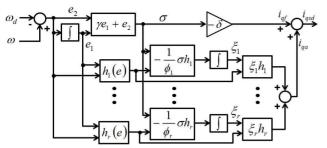


Fig. 2. Block diagram of the proposed fuzzy adaptive control algorithm.

It should be noted that  $h_i$  can be regarded as the normalized weight of each IF-THEN rule and that they satisfy  $h_i \geq 0$  and  $\sum_{i=1}^r h_i = 1$ .

Let the optimal parameter vector be defined as  $\xi_*$ . Then the minimum approximation error is expressed as:

$$\varepsilon = \eta - \eta_f = \eta - \xi_*^T h(e) = \sum_{i=1}^r \xi_{i*} h_i(e)$$
 (14)

It should be noted that standard results such as [19] imply that a fuzzy system can uniformly approximate nonlinear functions to arbitrary accuracy. Thus if the searching space for  $\eta_i(t)$  is sufficiently big, it can be assumed that  $\epsilon = 0$ .

The q-axis current reference command  $i_{qsd}$  can be decomposed as the feedback term  $i_{qf}$  and the fuzzy adaptive compensating term  $i_{qa}$ :

$$i_{asd} = i_{af} + i_{aa} \tag{15}$$

where:

$$i_{af} = -\delta \gamma e_1 - \delta e_2 = -\delta \sigma \tag{16}$$

$$i_{qa} = \sum_{i=1}^{r} \xi_i h_i(e) \tag{17}$$

$$\xi_{i} = -\frac{1}{\phi_{i}} \int_{0}^{t} \sigma h_{i} d\tau \tag{18}$$

and  $\delta > 0$ ,  $\gamma > 0$ , and  $\phi_i > 0$ . Fig. 2 shows a block diagram of the proposed fuzzy adaptive control algorithm.

Theorem 2: Assume that the searching space for  $\eta_j(t)$  is sufficiently big and that  $\epsilon = 0$ . Let  $i_{qs} = i_{qsd}$  be given by (15) with (16), (17), and (18). Then, e converges to zero, and  $\xi = [\xi_1, \dots, \xi_s]^T$  are bounded, respectively.

**Proof**: Define the Lyapunov functional as:

$$V = \frac{1}{2} [\kappa e_1^2 + \sigma^2 + \sum_{i=1}^r \varsigma_i \tilde{\xi}_i^2]$$
 (19)

where  $\zeta_i = \phi_i k_l$ ,  $\xi_i = \xi_{i^*} - \xi_i$ , and  $\kappa$  is a sufficiently small

positive constant satisfying the inequality (8). Its time derivative along the error dynamics (4) is given by:

$$\dot{V} = \kappa e_1 \dot{e}_1 + \sigma \dot{\sigma} - \sum_{i=1}^r \varsigma_i \tilde{\xi}_i \ \dot{\xi}_i$$
 (20)

The equations (4), (14),  $\epsilon = 0$ , and (15) imply that:

$$\dot{e}_{2} = -\gamma e_{2} + k_{1} \left[ -\delta \sigma + \sum_{i=1}^{r} \xi_{i} h_{i} - \varepsilon - \eta(t) \right]$$

$$= -\gamma e_{2} + k_{1} \left[ -\delta \sigma + \sum_{i=1}^{r} \xi_{i} h_{i} - \varepsilon - \sum_{i=1}^{r} \xi_{i*} h_{i} \right]$$

$$= -\gamma e_{2} - k_{1} \delta \sigma + k_{1} \sum_{i=1}^{r} \widetilde{\xi}_{i} h_{i}$$
(21)

The time derivative of  $e_2$  leads to:

$$\dot{\sigma} = -\gamma \dot{e}_1 + \dot{e}_2 = -k_1 \delta \sigma + k_1 \sum_{i=1}^r \widetilde{\xi}_i h_i$$
 (22)

The equation (18) means that:

$$\dot{\xi}_i = -\frac{1}{\phi_i} \sigma h_i \tag{23}$$

Therefore, (19) can be reduced to:

$$\dot{V} \le \kappa e_1(\sigma - \gamma e_1) - k_1 \delta \sigma^2 = -e_r^T Q e_r \tag{24}$$

where Q is already defined in (12) and it is positive definite. This implies that:

$$\lambda_{\min}(Q) \int_0^\infty e_r^T e_r dt \le V(0) - V(\infty) \le V(0)$$
 (25)

where  $V(t) \ge 0$  is used. Since the smallest eigenvalue of Q,  $\lambda_{\min}(Q)$ , is positive,  $\int_0^\infty e_r^T e_r dt \le \infty$  can be obtained. This leads to  $e_r \in L_2 \cap L_\infty$  (i.e.  $e_1 \in L_2 \cap L_\infty$ ,  $e_2 \in L_2 \cap L_\infty$ ,  $\sigma \in L_2 \cap L_\infty$ .), and  $\xi_i \in L_\infty$ . From  $\sigma = \gamma e_1 + e_2$ , the following transfer function relationship between  $e_1$  and  $\sigma$  can be obtained.

$$H_{e_{l}\sigma}(s) = \frac{1}{s + \gamma} \tag{26}$$

where s is the Laplace variable. Because  $H_{e_i\sigma}(s)$  is strictly positive real and  $\sigma \in L_2$ , Lemma 1 can be used to state that  $e_1(t)$  converges to zero. Lemma 2 indicates that  $e_2(t)$  converges to zero if  $\dot{e}_2 = \ddot{e}_1$  is bounded. Since  $e_2 \in L_\infty$ ,  $\sigma \in L_\infty$ ,  $\xi_i \in L_\infty$ , and  $0 \le h_i \le 1$ , by using (21) the following inequality can be known:

 $\label{eq:Table I} \mbox{\sc Parameters of a Prototype SPMSM}$ 

Number of poles ( <i>p</i> )	12
Stator resistance $(R_s)$	$0.99 [\Omega]$
Stator inductance $(L_s)$	5.82 [mH]
Magnetic flux $(\lambda_m)$	7.92×10 <sup>-2</sup> [V·sec/rad]
Equivalent inertia ( <i>J</i> )	$1.21 \times 10^{-3} [kg \cdot m^2]$
Viscous friction coefficient (B)	$0.3\times10^{-3}$ [N·m·sec/rad]

$$|\dot{e}_{2}| \leq \gamma |e_{2}| + k_{1}\delta |\sigma| + k_{1}\sum_{i=1}^{r} |\widetilde{\xi}_{i}| \cdot |h_{i}|$$

$$(27)$$

i.e.,  $\dot{e}_2$  is bounded, and thus it can be concluded that  $e_2$  also converges to zero.

### IV. PERFORMANCE EVALUATION

To present simulation and experimental results that can support the proposed control scheme, the parameters of a prototype SPMSM drive system are listed in Table I. Thus, (2) can be rewritten as the following dynamic equation:

$$\dot{\omega} = 3539.6i_{as} - 0.2484\omega - 4968.8T_L \tag{28}$$

The following membership functions with r = 9 are chosen to build the fuzzy model  $\eta_t(t)$  given in (13):

$$h_i = m_{1i} / \sum_{j=1}^r m_{1j}, m_{1i} = e^{-\mu_i (\omega - \omega_d - W_i)^2}$$
(29)

where  $W_1 = -W_0$ ,  $W_2 = 3W_1/4$ ,  $W_3 = W_1/2$ ,  $W_4 = W_1/4$ ,  $W_5 = 0$ ,  $W_9 = W_0$ ,  $W_8 = 3W_9/4$ ,  $W_7 = W_9/2$ ,  $W_6 = W_9/4$ ,  $\mu_i = 1/W_0^2$ , and  $W_0 = 50$ .

With  $\delta = 0.2$ ,  $\phi_i = 0.1$ , and  $\gamma = 1$ , the *q*-axis current reference command  $i_{qsd}$  can be expressed as the following control law:

$$i_{qsd} = -0.2\sigma + \sum_{i=1}^{9} \xi_i h_i$$
 (30)

where  $\sigma$  is represented by:

$$\sigma = \int_0^t (\omega - \omega_d) d\tau + (\omega - \omega_d)$$
 (31)

Also,  $\xi_i$  is continuously updated by the following adaptation law:

$$\xi_i(t) = -10 \int_0^t \sigma h_i(e) d\tau \tag{32}$$

Fig. 3 shows an overall block diagram of the proposed control system. As illustrated in Fig. 3, the rotor position ( $\theta$ ) and the two phase currents ( $i_a$ ,  $i_b$ ) are measured to carry out

the closed-loop control. In addition, the overall control system is composed of two control loops: a proposed fuzzy adaptive speed controller in an outer loop and a conventional PI current controller in an inner loop. It is noted that the PI gains  $(K_{Pc}, K_{Ic})$  of the PI current controller are determined by the following gain tuning rule [21], [22]:

$$K_{Pc} = L_s \omega_c = 1.82, \quad K_{Ic} = R_s \omega_c = 311.02$$
 (33)

where the bandwidth  $\omega_c = 2\pi \cdot 50$  rad/s. In this paper, a Texas Instruments TMS320F28335 DSP is used to implement the proposed control algorithm as software. In both the simulation and the experiment, the PWM frequency is selected as 5[kHz], and a space vector pulse-width modulation (SVPWM) method is employed to adjust the motor speed and torque according to the control input ( $V_{qs}$  and  $V_{ds}$ ).

Figs. 4 and 6 show the simulation results of the proposed fuzzy adaptive speed controller using Matlab/Simulink under three conditions: speed transient response under nominal parameters, speed transient response and torque transient response under 200% variations of the stator resistance  $(R_s)$ and the stator inductance  $(L_s)$ , respectively. In Figs. 4 to 5, the desired motor speed ( $\omega_d$ ) is changed from 125.66 [rad/sec] to 251.32 [rad/sec] and then from 251.32 [rad/sec] to 125.66 [rad/sec]. However, the load torque  $(T_L)$  remains at 1 [N·m]. Fig. 4 shows the simulation results ( $\omega_d$ ,  $\omega$ ,  $i_{asd}$ ,  $i_{as}$ ,  $i_{ds}$ ,  $V_{an}$ ,  $i_a$ ) of the speed transient response under nominal condition. On the other hand, Fig. 5 shows the simulation results of the speed transient response under 200% variations of the stator resistance  $(R_s)$  and the stator inductance  $(L_s)$ . Fig. 6 shows the simulation results of the torque transient response under 200% variations of the stator resistance  $(R_s)$  and the stator inductance  $(L_s)$  when the load torque  $(T_I)$  abruptly increases from 1  $[N \cdot m]$  to 2  $[N \cdot m]$  and then vice versa. However, the desired motor speed ( $\omega_d$ ) remains at 251.32 [rad/sec]. In Figs. 4 to 6, it is clearly shown that the proposed fuzzy adaptive speed controller is very robust to uncertainties such as system parameter and load torque variations.

Figs. 7 and 8 show the experimental results of the proposed control method for the speed transient response and the torque transient response, respectively. Figs. 7 (a) and 8 (a) illustrate the desired speed  $(\omega_d)$  and measured speed  $(\omega)$ , while Figs. 7 (b) and 8 (b) show the desired q-axis current  $(i_{qsd})$ , the measured q-axis current  $(i_{qs})$ , and the measured d-axis current  $(i_{ds})$ . Figs. 7 (c) and 8 (c) show the phase a voltage  $(V_{an})$  and the phase a current  $(i_a)$ . The simulation and experimental results demonstrate that the proposed fuzzy adaptive speed controller can guarantee outstanding speed control performance (i.e., fast transient behavior, accurate trajectory tracking capability, and robustness) without accurate information on the motor parameter and load torque values.

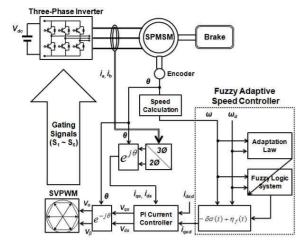


Fig. 3. Overall block diagram of the proposed control system.

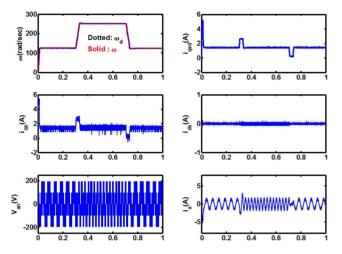


Fig. 4. Simulation results of speed transient response under nominal parameters when the desired speed  $(\omega_d)$  suddenly changes.

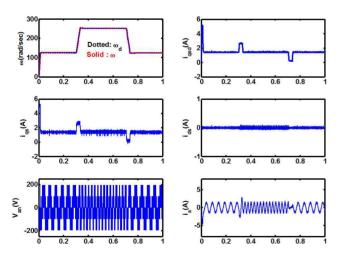


Fig. 5. Simulation results of speed transient response under 200% variations of some parameters ( $R_s$  and  $L_s$ ) when the desired speed ( $\omega_d$ ) suddenly changes.

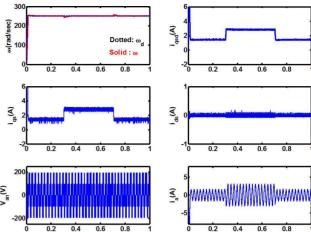
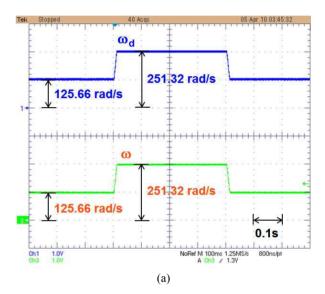
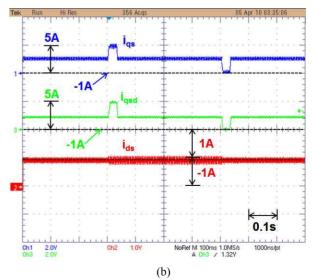


Fig. 6. Simulation results of torque transient response under 200% variations of some parameters ( $R_s$  and  $L_s$ ) when the load torque ( $T_L$ ) suddenly changes.





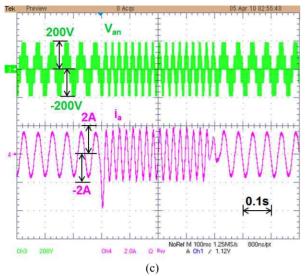
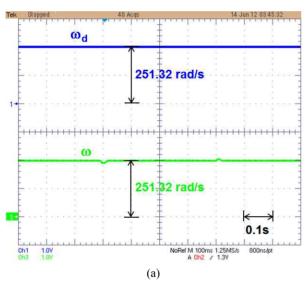
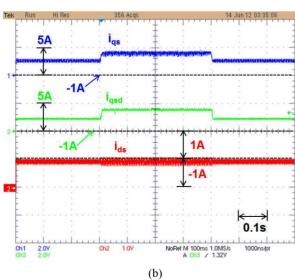


Fig. 7. Experimental results when the desired speed  $(\omega_d)$  suddenly changes. (a)  $\omega$  and  $\omega_{d}$ . (b)  $i_{qsd}$ ,  $i_{qs}$ , and  $i_{ds}$ . (c)  $V_{an}$  and  $i_{a}$ .





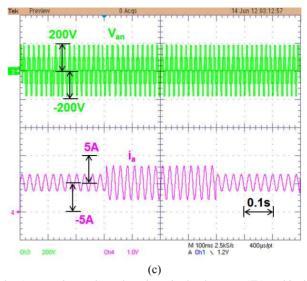


Fig. 8. Experimental results when the load torque  $(T_L)$  suddenly changes. (a)  $\omega$  and  $\omega_d$ . (b)  $i_{qsd}$ ,  $i_{qss}$ , and  $i_{ds}$ . (c)  $V_{an}$  and  $i_a$ .

### V. CONCLUSIONS

This paper proposed a fuzzy adaptive speed control strategy that can guarantee a fast transient behavior and a precise trajectory tracking capability for surfaced-mounted permanent magnet synchronous motors (SPMSMs). The proposed speed controller is very robust with respect to system uncertainties such as motor parameter and load torque variations. As a result, it does not require accurate parameter values. In addition, it was analytically proven that the proposed control system is asymptotically stable. In this paper, a conventional PI current controller was used together with the proposed fuzzy adaptive speed controller to examine the overall control performance. From the verification results, it can be seen that the proposed fuzzy adaptive control algorithm can be simply and easily implemented, and that it can assure excellent control performance such as fast dynamic response, accurate tracking capability, and robustness.

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