# Prediction of Speed in Urban Freeway Having More Freight Vehicles - Based in I-696 in Michigan -

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**Abstract**: Generally an urban freeway means a primary arterial which provides road users with a free-flow speed, except for ramp junctions during rush hours. However, most road users suffer from traffic congestion in the basic segments as well as in the ramp junctions of urban freeway during rush hours, because most road users prefer urban freeways to local roads in the urban areas. This study then intends to analyze lane traffic characteristics of urban freeway basic segments having more freight vehicles during rush hours, find the lane showing a high correlation with the segment speed between lane speeds, and finally suggest a segment-speed predictive model by the lane speed of urban freeway basic segments during rush hours.

Key words : urban freeway, lane traffic characteristics, segment speed, correlation analysis, regression modeling

# 1. Introduction

#### 1.1 Background

Generally, an urban freeway, as a primary arterial which is capable of carrying high traffic volumes with no more than 4 through lanes in one direction(AASHTO, 2005), must provide high-speed road users with a high level of efficiency and safety except for rush hours. In recent years urban freeways are not, however, playing a key role in high-speed road travel due to rapidly increased travel demand both at rush hours and non-rush hours. So, it is absolutely needed to improve the efficiency of use in existing urban freeways instead of building new ones.

#### 1.2 Objectives

Most urban freeway users suffer from serious traffic congestion due to more travel demand and shorter travel length when compared to expressway. So, the purpose of this study is to suggest an appropriate segment-speed predictive model in the urban freeway basic segments having more freight vehicles. To do that, it is needed to investigate the lane traffic characteristics in urban freeway during the morning rush hour, identify the appropriate lane-speed that highly correlated with segment-speed, and finally specify the relationship between the lane-speed and segment-speed.

## 1.3 Data Collection

A Michigan urban freeway(I-696), a divided ground-level freeway having 4 lanes in each direction and having more freight vehicles (10% or higher) in lanes 3 and 4, was divided into 8 basic segments for data collection, as shown in Fig. 1. Its geometry is summarized in Table 1.



Fig. 1 Basic segment on urban freeway I-696

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Table 1 Geometry of basic segment

Item	Geometric data
No. of lanes	4
Lane width	3.6m
Speed limit	112km/h
Right shoulder	≥1.5m
Left shoulder	≥1.5m
Segment length	150m

Data collection was conducted during the morning peak period hour of 06:30 to 07:30, and a master data-set for analysis of the basic segments under study was generated every 2 minutes.

# 2. Analysis of traffic characteristics

## 2.1 Flow rate

Flow rate, as the number of vehicles per a unit time, is converted into an hourly flow rate as follows(TRB, 1975);

$$q_i = \frac{n}{t} \tag{1}$$

$$q = \sum_{i=1}^{30} q_i \tag{2}$$

Where, n: No. of vehicles observed for a unit time(veh)

t : Observed time(2min)

- $q_i$ : Flow rate for 2 minutes(veh/2min)
- q : Flow rate for 1 hour(veh/h)



Fig. 2 Flow rate distribution

There did not seem to be a significant difference in the average flow rate between segments, but there was a distinct difference between lanes except for lane 2, as shown in Fig. 2.

Table 2 Flow rate statistics at segment(veh/h/l)

	Segment	Lane 1	Lane 2	Lane 3	Lane 4
Average	1,540	1,130	1,680	2,190	1,170
	(-)	(-27%)	(+9%)	(+42%)	(-24%)

The average flow rate of lanes appeared to decrease by about 20% in lanes 1 and 4, but to increase by about 40% in lane 3 when compared to the average flow rate of segments, as summarized in Table 2.

## 2.2 Speed

Speed, as the kilometers per hour, is represented by the space mean speed as follows(May, 1990);

$$u_s = \frac{n}{\sum_{i=1}^n \frac{1}{u_i}} \tag{3}$$

Where,  $u_s$ : Average speed(km/h)

 $u_i$ : Speed of individual vehicle(km/h)

n : No. of vehicles observed for a unit time(veh)



Fig. 3 Speed distribution

Similarly, the speed analysis showed that there was not a big difference in the average speed between segments, but there was a distinct difference between lanes except for lane 2, as shown in Fig. 3.

The speed analysis of lanes showed that the average speed decreased by about 10% in lanes 3 and 4, but increased by about 20% in lane 1 when compared to the average speed of segments, as summarized in Table 3.

Table 3 Speed statistics at basic segment(km/h)

	Segment	Lane 1	Lane 2	Lane 3	Lane 4
Average	94	119	97	83	82
	(-)	(+27%)	(+3%)	(-12%)	(-13%)

#### 2.3 Density

Density, as the number of vehicles per kilometer, is computed by the reciprocal of the distance headway as follows(May, 1990);

$$\overline{d_h} = \frac{\sum_{i=1}^n d_{hi}}{n} \tag{4}$$

$$k = \frac{3,600}{\overline{d_h}} \tag{5}$$

Where,  $d_{hi}$  : Distance headway of individual vehicle(m)

 $d_h$ : Average distance headway(m)

k : Density(veh/km)

Likewise, the average density was not shown to be a significant difference between segments, but there was a considerable difference between lanes except for lane 2, as shown in Fig. 4.

The average density of lanes was shown to decrease by about 10% to 40% in lanes 1 and 4, but to increase by about 20% to 70% in lanes 2 and 3 when compared to the average density of segments, as summarized in Table 4.

Table 4 Density statistics at basic segment(veh/km)

	Segment	Lane 1	Lane 2	Lane 3	Lane 4
Average	18	13	23	33	16
	(-)	(-28%)	(+28%)	(+83%)	(-11%)



Fig. 4 Density distribution

#### 3. Correlation analysis of traffic characteristics

### 3.1 Correlative characteristics of Q-K

Flow rate and density appear to fall into a parabolic curve except for the outlier, as shown in Fig. 5 and 6. In particular, the maximum flow  $rates(Q_m)$  and the optimal densities( $K_M$ ) in the Q-K curves of lanes appear to be about 2,390vph and 20vpk in lane 1, about 2,250vph and 22vpk in lane 2, about 2,990vph and 34vpk in lane 3, and finally about 1,640vph and 16vpk in lane 4, as summarized in Table 5 respectively.



Fig. 5 Q-K correlative characteristics at segment



Fig. 6 Q-K correlative characteristics at lanes

Table 5 Correlation results of  $\mathsf{Q}\!-\!\mathsf{K}$ 

	Q <sub>m</sub>	$Q_{1m}$	$Q_{2m}$	Q <sub>3m</sub>	$Q_{4m}$
K <sub>M</sub>	2,140 20				
$K_{1M}$		2,390 20			
$K_{2M}$			2,250 22		
K <sub>3M</sub>				2,990 34	
$\mathrm{K}_{\mathrm{4M}}$					1,640 16

## 3.2 Correlation analysis of Q-Us

Flow rate and speed appear to fall into a parabolic curve except for the outlier, as shown in Fig. 7 and 8. In particular, the maximum flow rates( $Q_m$ ) and the optimal speeds( $U_{sM}$ ) at the  $Q-U_s$  curves of lanes appear to be about 2,390vph and 113kph in lane 1, about 2,250vph and 106kph in lane 2, about 2,990vph and 90vpk in lane 3, and finally about 1,640vph and 99vpk in lane 4, as summarized in Table 6 respectively.



Fig. 7  $Q-U_s$  correlative characteristics at segment



Fig. 8  $Q-U_s$  correlative characteristics at lanes

Table 6 Correlation results of  $Q - U_s$ 

	$Q_{m}$	$Q_{1m}$	$Q_{2m}$	$Q_{3m}$	$Q_{4m}$
$\mathrm{U}_{\mathrm{sM}}$	2,140 105				
u <sub>s1M</sub>		2,390 113			
u <sub>s2M</sub>			2,250 106		
u <sub>s3M</sub>				2,990 90	
u <sub>s4M</sub>					1,640 99

## 3.3 Correlation analysis of $U_s - K$

Speed and density appear to fall into a cubic curve except for the outlier, as shown in Fig. 9 and 10. In particular, the optimal speeds( $U_{sM}$ ) and densities( $K_M$ ) at the  $U_s-K$  curves of lanes appear to be about 113kph and 20vpk in lane 1, about 106kph and 22vpk in lane 2, about 90kph and 34vpk in lane 3, and finally about 99kph and 16vpk in lane 4, as summarized in Table 7 respectively.



Fig. 9  $U_s - K$  correlative characteristics at segment



Fig. 10  $U_s - K$  correlative characteristics at lanes

Table 7 Correlation results of  $U_s - K$ 

	K <sub>M</sub>	K <sub>1M</sub>	K <sub>2M</sub>	K <sub>3M</sub>	${ m K}_{4{ m M}}$
U <sub>sM</sub>	20 105				
u <sub>s1M</sub>		20 113			
u <sub>s2M</sub>			22 106		
u <sub>s3M</sub>				34 90	
u <sub>s4M</sub>					16 99

# 4. Model Development and Verification

#### 4.1 Model Development

	Segment L=150m							
L1	*		Usı	•		*		
L2	*		Us2			*		
L3	*		Usa	09		*		
L4	*		Us4	•		*		
				Detector				
In	Independent variable							
u	u <sub>si</sub> : Average speed in the lanes (i=1, 2, 3, 4)							
D	Dependent variable							
U	U <sub>s</sub> : Average speed in the segments							

Fig. 11 Variables selected for model development

Assuming that the average speed in the segments would be influenced by the lane-speeds in the segments, correlation analysis was conducted between the average speed( $U_s$ ) of segments and lane-speeds( $u_{si}$ ) in the segments. It is summarized in Table 8.

Гable	8	Correlation	results	of	U <sub>s</sub> -u <sub>si</sub> at	basic	segments
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Segn	La nent-sp	ane-speed beed	u <sub>s1</sub>	u <sub>s2</sub>	u <sub>s3</sub>	u <sub>s4</sub>
C1	TT	r	0.858	0.969	0.954	0.968
51	Us	Model	CUB	EXP	CUB	CUB
<b>C</b> 2	TT	r	0.868	0.974	0.949	0.968
52	Us	Model	QUA	EXP	CUB	CUB
<u></u>	TT	r	0.891	0.979	0.961	0.950
50	U <sub>s</sub>	Model	EXP	EXP	CUB	CUB
C 4	TT	r	0.914	0.984	0.957	0.965
54	Us	Model	EXP	CUB	CUB	CUB
05 II	TT	r	0.934	0.977	0.968	0.978
50	0 <sub>s</sub>	Model	CUB	CUB	CUB	CUB
C.C.	TT	r	0.964	0.971	0.975	0.963
50	Us	Model	EXP	CUB	CUB	CUB
67	TT	r	0.953	0.970	0.967	0.956
51	Us	Model	EXP	CUB	CUB	CUB
00	TT	r	0.923	0.978	0.963	0.948
58	Us	Model	EXP	POW	CUB	CUB
No. of the highest r		0	6	1	1	

Note: CUB is cubic model, EXP is exponential model, QUA is quadratic model, POW is power model

With the speed of lane  $2(u_{s2})$  selected as a dependent variable and the average speed(U<sub>s</sub>) of segments selected as the independent one, segment-speed predictive models  $(U = f(u_{s2}))$  are suggested as follows;

$$CUB : U = \beta_0 + \beta_1 \times u_{s2} + \beta_2 \times u_{s2}^2 + \beta_3 \times u_{s2}^3$$
(8)

$$EXP : U = \beta_0 \times e^{\beta_1 \times u_{s2}}$$
(9)

$$POW : U = \beta_0 \times u_{s2}^{\beta_1}$$
(10)

Where, U : Segment-speed predictive model in the segments

- u<sub>s2</sub>: Speed of lane 2(km/h)
- $\beta_j$  : Coefficients of function(j=0, 1, 2, 3)

A multiple regression analysis was used to build the segment-speed predictive model, which was developed by all-possible-regression selection procedures for the purpose of identifying the important independent variables with the criteria of  $R^2$ . In particular, multi-collinearity was avoided by the trial-and-error process.

Туре	Models						
CUB	$U = 29.8335 + 0.0374u_{s2} + 0.0109u_{s2}^2 - 0.00005u_{s2}^3$						
COD	$R^2$	0.957	F-sig.	0.000			
FYP	$U = 28.5348e^{0.0118u_{s2}}$						
LAF	$R^2$	<u>0.964</u>	F-sig.	0.000			
POW	$U = 7.8153 u_{s2}^{0.5485}$						
POW	$R^2$	0.927	F-sig.	0.000			

Table 9 Results of segment-speed predictive models

Thus, the segment-speed predictive model appeared as an exponential model to be in a higher explanatory power  $(R^2)$  with the speed of lane 2 than the cubic or power ones, as shown in Table 9.

# 4.2 Model Verification

There were two approaches applied to ensure the validity of the models developed. One approach was to conduct the paired t-tests between the observed and expected speeds, whether the p-values were greater than the significance level ( $\alpha/2$ =0.025) or not at the 95% confidence level.

Segment	Model	t-value	p-value	Result
S5	CUB	-7.366	0.000	Reject
	EXP	-0.692	0.494	<u>Accept</u>
	POW	-0.850	0.402	<u>Accept</u>
S6	CUB	-7.221	0.000	Reject
	EXP	-0.824	0.416	<u>Accept</u>
	POW	-1.512	0.141	<u>Accept</u>
S7	CUB	-7.510	0.000	Reject
	EXP	-0.953	0.348	<u>Accept</u>
	POW	-2.382	0.024	Reject
S8	CUB	-7.510	0.000	Reject
	EXP	-0.953	0.348	Accept
	POW	-2.382	0.024	Reject

In the paired t-tests, the p-values of the exponential model (0.0.348, 0.416 and 0.494) were higher than those of the power model (0.024, 0.141 and 0.402) and of the cubic model (0.000) respectively, as shown in Table 10. Another approach was to test the utility of the regression models with traffic data that was unused. The results (r) of the correlation analysis were shown to be 0.951 or higher in the segments regardless of the models, as shown in Figure

12. So, the exponential model proved to be very effective in predicting segment-speed in the segments.



Fig. 12 Verification at segment 5

## 4.3 Model Evaluation

Statistics were applied to evaluate the measures of effectiveness (MOE) between the EXP model, the POW model, and the CUB model. They were to compare the root mean square error (RMSE) between the observed and expected speeds by the models. Particularly, there was less difference in the root mean square error (RMSE) of this model ( $6.211 \sim 7.666$ ) than in that of the POW model ( $6.450 \sim 8.148$ ) and the CUB model ( $8.453 \sim 10.095$ ) respectively, as shown in Table 13. So, the EXP model proved to have a higher predictability than the POW and CUB models in the segments.

Model Segment	CUB	EXP	POW
S5	8.453	<u>6.211</u>	6.450
S6	9.443	7.247	7.446
S7	10.095	7.666	7.970
S8	8.861	6.623	8.148

Table 11 Results of RMSE analysis

# 5. Conclusions

From these traffic characteristics analyses, and the development and validation of the segment–speed predictive model in the urban freeway basic segments having more freight vehicles, the following conclusions were drawn;

- 1) Average speeds in the urban freeway basic segments were shown to have a higher correlation with the speed of lane 2 than lanes 3 or 4 in the basic segments
- 2) The exponential model proved to be suitable for predicting the mean speed in the urban freeway basic segments with a high explanatory power and validity

It was concluded that this study needs to be continued concerning the various geometric characteristics of urban freeways having more freight vehicles for the purpose of proving the reliability of the segment-speed predictive model.

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