

# 압력커플링 정유압 변속기를 이용한 에너지 절감 유압시스템에 관한 연구

## A Study of Energy Saving Hydraulic System by A Pressure Coupling Hydrostatic Transmission

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**Abstract:** Nowadays, the demand of energy saving is increasing more and more while the natural resources have been exhausted. Besides, the emission gas caused by vehicles has been being a serious environment problem. Therefore, many studies have been carried out, especially focusing on braking energy regeneration, in order to save energy as well as reduce emission of mobile vehicles. In this paper, we propose a closed-loop hydrostatic transmission for braking energy regeneration with two configurations to reduce the energy consumption by recovering the braking energy. The effectiveness of the proposed system was verified by simulation. The simulation results indicated that the pressure coupling configuration gave better performance in comparison to flow coupling configuration about 40.8%, 61.7% and 53.8% reduction of fuel consumption in 10 mode, 10 mode modified profile and highway schedules, respectively.

### Nomenclature

$A_{r1,2}$  : valve throttling area  
 $C$  : viscous friction coefficient  
 $C_d$  : discharge coefficient  
 $D_{max}$  : max. Displacement of hydraulic machine  
 $J$  : moment of inertia of flywheel  
 $K_{sv}$  : DC gain of the mechanism  
 $E_{k,max}$  : max. Kinetic energy during deceleration  
 $n$  : adiabatic coefficient  
 $p_0$  : pre-charged pressure  
 $p_g$  : pressure of gas in accumulator  
 $p_i$  : pressure at port of accumulator  
 $p_{pvc1,2}$  : setting pressure of pilot check valve PCV1,2  
 $p_r$  : return line pressure  
 $p_s$  : driving/supply line pressure  
 $Q_b$  : boost flow rate  
 $Q_i$  : ideal flow rate of hydraulic machine

$Q_{ha}$  : flow rate into accumulator  
 $Q_l$  : loss flow rate of hydraulic machine  
 $Q_{mi}$  : flow rate into the inlet port of the motor  
 $Q_{mo}$  : flow rate from motor outlet port  
 $Q_{pm}$  : actual flow rate of hydraulic machine  
 $Q_{po}$  : output flow rate of the pump  
 $Q_{r1,2}$  : flow rate via relief valve RV1,2  
 $T_{ex}$  : external torque  
 $T_l$  : loss torque of hydraulic machine  
 $T_m$  : torque of hydraulic motor  
 $u(t)$  : electric signal control  
 $u_2$  : displacement ratio of pump/motor PM2  
 $V_0$  : volume of hydraulic accumulator  
 $V_f$  : fluid volume in the accumulator  
 $V_h$  : volume of fluid in the hose  
 $a$  : displacement ratio  
 $\Delta p$  : pressure difference  
 $\tau$  : time constant of DCM  
 $w$  : flywheel speed  
 $\delta$  : valve throttling area proportionality coefficient

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**Subscripts**

- u : upper
- l : lower

**1. Introduction**

Reduction of energy consumption is one of the most important topics in vehicle research. Many researches about saving energy have been done. In hydraulic systems, hydrostatic transmissions(HST), constant pressure systems(CPS), electro-hydraulic actuators(EHA) and secondary control systems with common pressure rails(CPR) have been considered for energy-saving. In a HST system, the velocity of the motor is continuously controlled by adjusting the pump flow rate. Thus, it is suitable for earth moving machines such as wheel loaders, tractors and forklifts, etc<sup>1)</sup>. However, the HST system cannot recover kinetic energy of the load, consequently, restricting its energy-saving potential. A CPS system employs a flywheel with an auxiliary hydraulic machine so that it is able to recover kinetic energy of the load and reuse recovered energy. The CPS system studies in 2) and 3) have shown that these systems are adequate for mobile applications, such as vehicles. However, the flywheel in CPS makes noise when operating and the kinetic energy of flywheel is gradually decreasing according to time. In an EHA system, batteries or super-capacitors are employed to store kinetic energy of the load<sup>4),14),15),16)</sup>. The EHA system has high recovery efficiency and good performance but its applicability is restricted due to its low specific power with batteries and high price with super-capacitors. In a CPR system, two common rails are employed: a high-pressure line connected with high-pressure accumulators and a low-pressure line connected directly to a tank. The CPR system is applied to vehicles and shows much reduction of energy consumption, according to 5) and 6). To utilize the advantage of the above hydraulic systems, a closed-loop hydrostatic transmission is proposed for braking energy regeneration with two hydraulic accumulators. The proposed system can be switched between two configurations: flow coupling configuration and pressure coupling configuration for the comparison of the effect

of each configuration. The high pressure accumulator (HPA) plays an important role in the system, as discussed in 7). It functions as power source as well as energy storage to absorb the braking energy from the hydraulic pump/motor in braking time.

This paper is organized as follows: section 2 describes the proposed system and its operation; section 3 presents the mathematical model of the system; section 4 presents the simulation and analysis of the simulation results. Finally, conclusions are presented in the last section.

**2. System description**

The proposed system is a hydrostatic drive which transmits the power from the electric motor to the load, the flywheel FW. In comparison with a traditional HST, a directional control valve and two hydraulic accumulators (HPA, LPA) are added (Fig. 1). The high-pressure accumulator HPA functions as a storage system or a power supply, while the low-pressure accumulator LPA functions as a low-pressure, high-flow source for the hydraulic machine pump/motor during decelerating, and boosts the system during accelerating. The flywheel FW simulates external load. The secondary unit, the hydraulic pump/motor, could function as a hydraulic pump or a hydraulic motor depending on velocity, displacement and pressure difference between two ports of pump/motor.

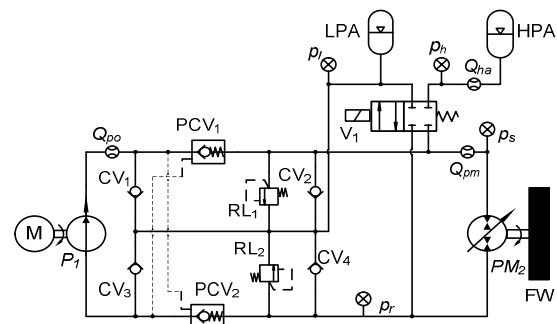


Fig. 1 Schematic diagram of the proposed system

The proposed system can operate in two distinguished configurations of hydraulic systems that are flow coupling configuration and pressure coupling configuration by controlling the directional control valve.

### 2.1 Flow coupling configuration

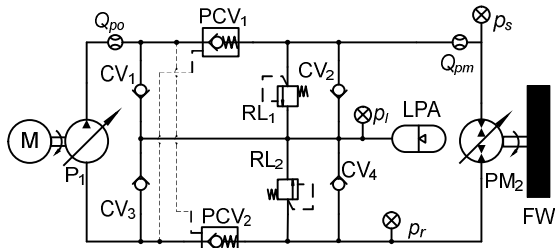


Fig. 2 Flow coupling configuration

When  $V_1$  is OFF, the system operates as a closed-loop flow coupling hydrostatic transmission with over-velocity protection mechanisms, as in Fig. 2. The velocity of the flywheel FW is controlled by adjusting the displacement of pump  $P_1$  while the displacement of hydraulic machine  $PM_2$  is fixed. When the velocity of the flywheel is greater than reference velocity, the pressure in return line  $p_r$  becomes high, while the pressure in the driving/supply line  $p_s$  becomes low. Pilot check valve  $PCV_2$  is then closed, and hydraulic energy in the form of high-pressure fluid is dissipated via the relief valve  $RL_2$ . This function is similar to that of a hydraulic brake, which reduces the velocity of the flywheel FW under the reference velocity. As the velocity of the flywheel in an HST is reduced, the kinetic energy of the flywheel is dissipated by braking. In the application of hydraulic vehicles, regenerative braking energy is substantial, so the recovery of regenerative energy may significantly reduce total energy consumption.

### 2.2 Pressure coupling configuration

When  $V_1$  is ON, the system operates as a closed-loop pressure coupling hydrostatic transmission, as shown in Fig. 3. In this configuration, pump  $P_1$  is ON/OFF controlled to compensate the pressure of HPA. The velocity of the flywheel is controlled directly by adjusting the displacement of the hydraulic machine  $PM_2$ .

In accelerating time, Fig. 3a, the driving line is connected to HPA while the return line is directly connected to LPA. The hydraulic machine  $PM_2$  functions as a hydraulic motor that transfers the potential energy in the HPA into the kinetic energy of

the flywheel. To accelerate the flywheel, the displacement of  $PM_2$  is increased, and vice versa. In decelerating time, Fig. 3b, the hydraulic machine  $PM_2$  functions as a hydraulic pump that pumps fluid from LPA to HPA. The kinetic energy of the flywheel is transformed to hydraulic energy stored in HPA. When the displacement of the hydraulic machine  $PM_2$  increases, the impeded torque in the shaft of  $PM_2$  also increases, so that the velocity of the flywheel decreases rapidly.

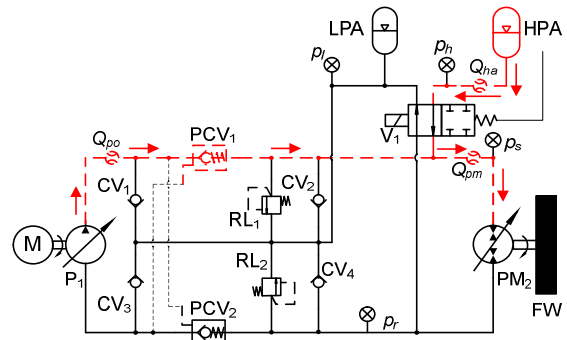


Fig. 3a Accelerating time in pressure coupling configuration

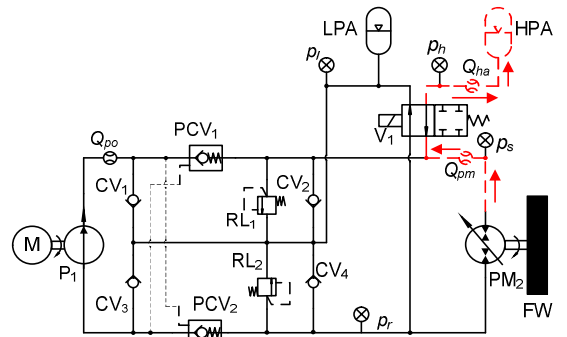


Fig. 3b Decelerating time in pressure coupling configuration

## 3. Mathematical Model

### 3.1 Analysis of efficiency

The ideal flow rates, volumetric and mechanical efficiencies of the piston hydraulic pump are expressed in Eq. (1), (2) and (3), respectively:

$$Q_i = \alpha \omega D_{\max} \quad (1)$$

$$\eta_{vP} = \frac{Q_i - Q_l}{Q_i} \quad (2)$$

$$\eta_{iP} = \frac{\alpha D_{\max} \Delta p}{\alpha D_{\max} \Delta p + T_i} \quad (3)$$

The actual output flow rate and input torque of the pump are expressed in Eq. (4) and (5), respectively:

$$Q_o = Q_i \eta_{pV} \quad (4)$$

$$T_i = \alpha \Delta p D_{\max} \eta_{iPM} \quad (5)$$

### 3.1.1 Motor mode

The volumetric efficiency, mechanical efficiency, actual flow rate and actual output torque of the piston hydraulic motor are expressed by Eq. (6) ~ (9), respectively.

$$\eta_{vM} = \frac{\alpha D_{\max} \omega}{\alpha D_{\max} \omega + Q_{loss}} \quad (6)$$

$$\eta_{iM} = \frac{\alpha D_{\max} \Delta p - T_{loss}}{\alpha D_{\max} \Delta p} \quad (7)$$

$$Q_m = \frac{Q_i}{\eta_{vM}} \quad (8)$$

$$T_m = \alpha \Delta p D_{\max} \eta_{iM} \quad (9)$$

### 3.1.2 Electro-hydraulic displacement control mechanism (DCM)

An electro-hydraulic mechanism is employed to regulate the angle of the swash plate for control the displacement of the hydraulic pump/motor. A full order model of the system is a fifth-order system with voltage input and the angle of the swash plate or the displacement of the pump/motor. However, in practical application of hydraulic systems, a reduced first-order is often used instead of the full order model<sup>(9-11)</sup>. In this study, a first-order model of the electro-hydraulic mechanism is used and expressed as:

$$u(t) = \frac{\tau}{K_{sv}} \dot{\alpha} + \frac{1}{K_{sv}} \alpha \quad (10)$$

### 3.2 Model of hydraulic accumulator

High pressure accumulator plays an important role in the switching closed loop HST. Its volume must be large enough to absorb the kinetic energy of vehicle during decelerating time but its size should be small because of the limit of space in vehicle. In such system, we employed bladder accumulator, which filled with nitrogen gas. According to 12), the nitrogen gas is

assumed to compress and expand based on the adiabatic gas law:

$$pV^n = p_0V_0^n = p_{\max}V_{\min}^n \quad (11)$$

Then the fluid volume in the hydraulic accumulator HPA is derived as:

$$V_f = \begin{cases} 0, & \text{if } p_i \leq p_0 \\ V_0(1 - \frac{p_0}{p_i})^{\frac{1}{n}}, & \text{else} \end{cases} \quad (12)$$

The energy that can be absorbed by HPA is calculated as:

$$E = \frac{p_{\max}^{\frac{1}{n}} V_0}{n-1} \left[ \lambda_p^{\frac{1}{n}} - \lambda_p \right] \quad (13)$$

where,

$$\lambda_p = \frac{p}{p_{\max}} \quad (14)$$

The optimal pre-charged pressure for maximum energy capacity of HPA is given by:

$$p_0 = n^{n/(1-n)} p_{\max} \quad (15)$$

And the maximum energy stored in HPA is given by:

$$E_{\max} = p_{\max} V_0 n^{n/(1-n)} \quad (16)$$

Then the volume of HPA is derived as:

$$V_0 = \frac{E_{k,\max}}{p_{\max} n^{n/(1-n)}} \quad (17)$$

### 3.3 Model of connecting line

#### 3.3.1 Flow coupling configuration

For simplicity, the pressure drop in the check valves is neglected, so the pressure before and after check valves is the same. Hydraulic accumulator LPA is large enough to make the pressure of accumulator constant. The dynamic response of the valves can be ignored when compared with that of the flywheel or system pressures. In the driving line, pressure  $p_s$  is expressed as:

$$\frac{dp_s}{dt} = \frac{\beta}{V_h} (Q_{p0} + Q_b - Q_{r1} - Q_{mi}) \quad (18)$$

The return line is more sophisticated because the pressures at motor outlet  $p_r$  and pump inlet  $p_{pi}$  may be different depending on the state of the pilot check valve PCV<sub>2</sub>. The pressure at the pump inlet port is expressed

as:

$$p_{pi} = \begin{cases} p_r & \text{if } p_s > p_{pcv2} \\ p_l & \text{if } p_s \leq p_{pcv2} \end{cases} \quad (20)$$

Pressure  $p_r$  plays an important role in the system dynamics, and is expressed by:

$$\frac{dp_r}{dt} = \frac{\beta}{V_h} (Q_{mo} + Q_b - Q_{r2} - Q_{pi}) \quad (21)$$

$$Q_{r1,2} = \begin{cases} 0, & \text{if } \Delta p \leq p_{rv} \\ K_{1,2}(\Delta p - p_{rv})\sqrt{\Delta p}, & \text{if } p_{rv} \leq \Delta p \leq p_{max} \end{cases} \quad (22)$$

where

$$K_{1,2} = C_d \delta \frac{A_{r1,2}}{k} \sqrt{\frac{2}{\rho}} \quad (23)$$

The reference velocity of the flywheel at each instant is determined by the flow coupling principle expressed as:

$$\omega_{fl} = \frac{\omega_p D_p \eta_{vp} \eta_{vm}}{D_m} \quad (24)$$

### 3.3.2 Pressure coupling configuration

In the accelerating line pressure  $p_s$  is expressed as:

$$\frac{dp_s}{dt} = \frac{\beta}{V_h} (Q_{po} + Q_b - Q_{ha} - Q_{r1} - Q_{pm}) \quad (25)$$

where,

$Q_{pm}$  is expressed by Eq. (8) in accelerating time and Eq. by (4) in decelerating time.

$$Q_{ha} = \begin{cases} 0, & \text{if } p_i \leq p_0 \\ \frac{d}{dt} \left[ V_0 \left( 1 - \frac{p_0}{p_i} \right)^{\frac{1}{k}} \right], & \text{if } p_i > p_0 \end{cases} \quad (26)$$

$$\Delta p = p_s - p_r \quad (27)$$

where  $p_r$  is the returning line pressure, which is considered as the pressure in LPA in pressure coupling configuration.

### 3.3.3 Model of load

The dynamic equation of the flywheel FW is obtained by applying Newton's second law, as:

$$T_m = J\dot{\omega} + C\omega + T_{ex} \quad (28)$$

where  $T_{ex}$  is external load torque.

## 4. Simulation and Results

To analyze the response of the proposed system for vehicle applications, this system was applied to a 2000kg vehicle. Final reduction gear ratio is 3.55 and the radius of wheel is 0.28m. We employed 10-mode profile schedule, one of the typical driving schedules for vehicle testing, as a velocity reference to evaluate the performance of the proposed system. Setting parameters of the system model for simulations are shown in Table 1.

Table 1 Setting parameters of the system

Components	Capacity	Unit
<b>Hydraulic machine</b>		
displacement	[-55 55]	cc/rev
max pressure	250	bar
<b>Flywheel</b>		
inertial moment	4.5	kgm <sup>2</sup>
viscous friction coef.	0.01	Nm/(RPM)
<b>HPA</b>		
volume	20	liter
gas-pre-charge	120	bar
max pressure	280	bar
<b>LPA</b>		
volume	50	liter
gas-pre-charge	2	bar
<b>Electric motor</b>		
power	25	HP
speed	1160	rpm

The simulations have been carried out in the following two cases: flow coupling configuration and pressure coupling configuration, using a PID controller for velocity control in both cases.

Firstly, simulation was carried out in flow coupling configuration. Fig. 4 shows the velocity response, error and displacement ratio of pump P<sub>1</sub>, respectively in flow coupling configuration. This figure shows good performance in velocity response. The displacement  $\alpha_1$  of pump P<sub>1</sub> was regulated to achieve the reference velocity while the displacement  $\alpha_2$  of motor PM<sub>2</sub> was fixed at 0.9. The supply pressure and return pressure in flow coupling configuration are shown in Fig. 5. The supply pressure increases during the acceleration time and decreases during the deceleration time. In the contrary, return pressure increases during deceleration time or braking time and decreases during acceleration time. Fig. 6 shows the flow rate and fluid volume via hydraulic machine PM<sub>2</sub>. In flow coupling configuration,

this flow rate proportional to the velocity of flywheel FW as shown in Eq.(24). The total fluid volume via PM<sub>2</sub> during 10 mode profile schedule is 61 liters. Fig. 7 indicates the supplied power and supplied energy by pump P<sub>1</sub>. The supplied power varies to meet the demand of hydraulic machine PM<sub>2</sub> in accelerating and decelerating time. The sum energy supplied to 10 mode profile is 307.8kJ.

Secondly, simulation was carried out in pressure coupling configuration. Fig. 8 shows the velocity response, error and displacement ratio of hydraulic machine PM<sub>2</sub>, respectively. This figure shows that the velocity response is better in comparison with it in flow coupling configuration. The displacement of motor PM<sub>2</sub> is regulated to reach the required torque and velocity as the system pressure changes while the displacement ratio pump P<sub>1</sub> was ON/OFF controlled to maintain the pressure in the high pressure accumulator HPA in a specified interval.

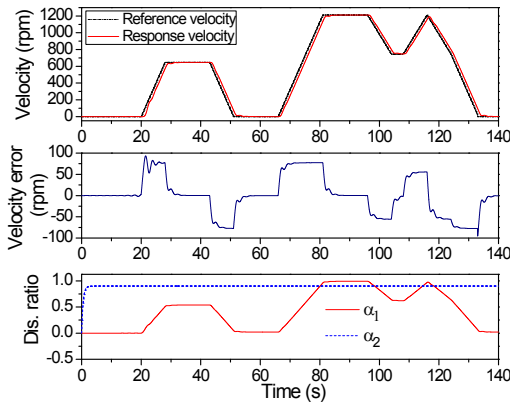


Fig. 4 Velocity, error and displacement ratio of pump P<sub>1</sub> in flow coupling configuration

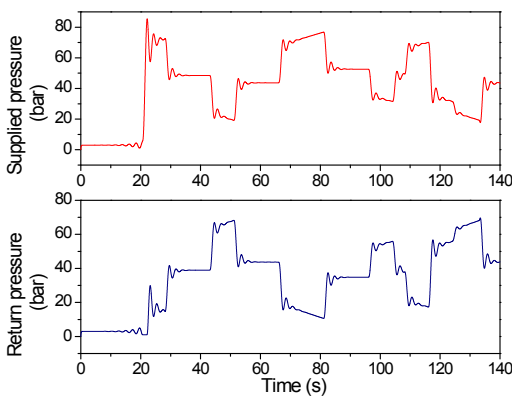


Fig. 5 Supplied pressure and return pressure in flow coupling configuration

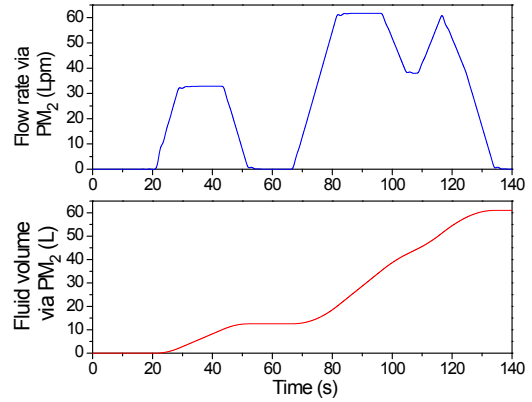


Fig. 6 Flow rate and fluid volume via hydraulic machine PM<sub>2</sub> in flow coupling configuration

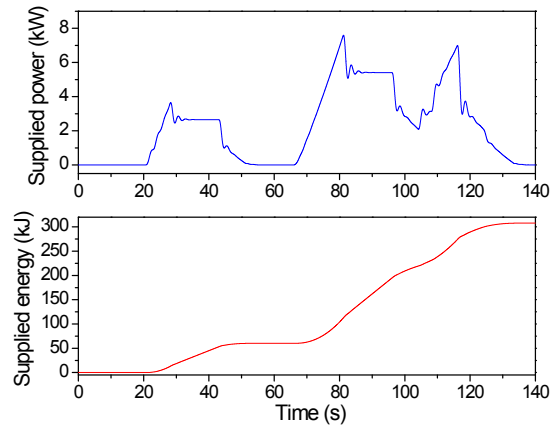


Fig. 7 Supplied power and energy in flow coupling configuration

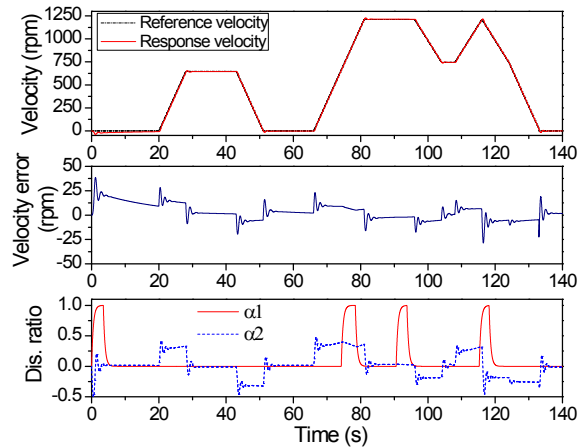


Fig. 8 Velocity, error and displacement ratio of PM<sub>2</sub> in pressure coupling configuration

The flow rate into the high accumulator is maximum until the pressure of HPA reaches to 160 bar and it is zero until the pressure decreases to 135bar (Fig. 9 ~ 10). The displacement of PM<sub>2</sub> is regulated to make driving or braking torque as in Eq. (9). Therefore, its

flow rate is positive in accelerating time and negative in decelerating time, and the sum of fluid via PM<sub>2</sub> is less than that of flow coupling configuration. The high pressure accumulator HPA stores energy from P<sub>1</sub>, supplies hydraulic energy to hydraulic machine PM<sub>2</sub> in accelerating time and absorbs it from PM<sub>2</sub> in decelerating time. The flow rate of HPA increases as the flow rate of P<sub>1</sub> increases or the flow rate of PM<sub>2</sub> is negative, and it decreases as the flow rate of PM<sub>2</sub> increases. HPA power and energy are shown in Fig. 11. The supplied power and energy of pump P<sub>1</sub> are shown in Fig. 12. The supplied power is switched between zero and maximum value due to the displacement ratio of P<sub>1</sub>. The sum energy supplied to 10 mode profile schedule in this configuration is 182.2kJ. It means that 125.6kJ or 40.8% supplied energy was reduced compared to that of flow coupling configuration.

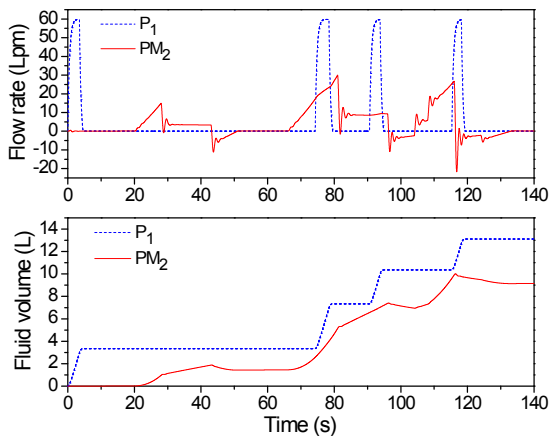


Fig. 9 Flow rate and fluid volume of P<sub>1</sub> and PM<sub>2</sub> in pressure coupling configuration

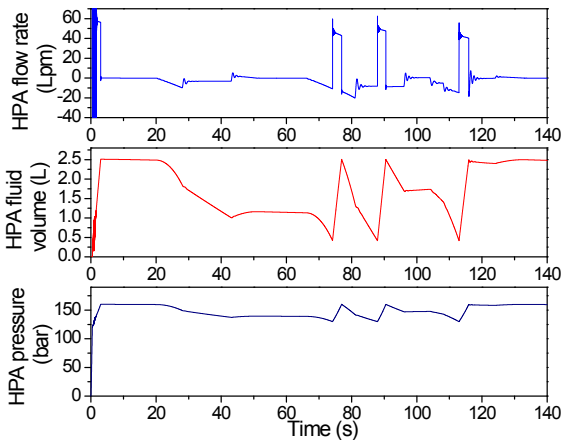


Fig. 10 Input flowrate, fluid volume and pressure of HPA in pressure coupling configuration

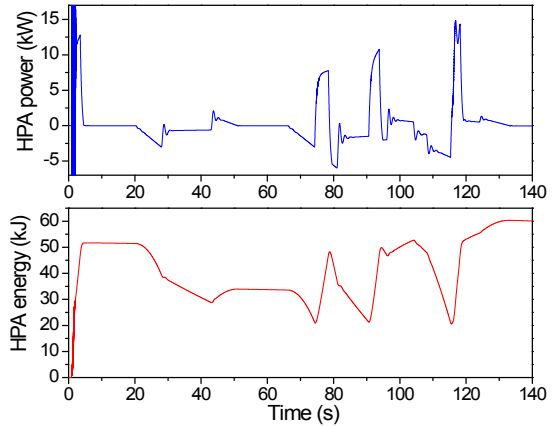


Fig. 11 Power and energy of HPA in pressure coupling configuration

Besides 10 mode profile schedule, simulation was also carried out in case of modified 10 mode profile and highway schedule in the same way.

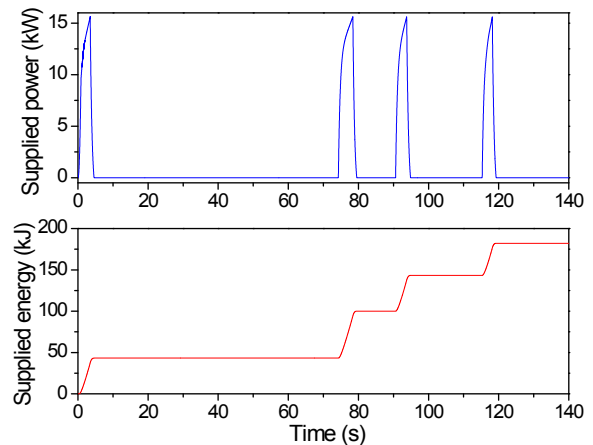


Fig. 12 Supply power and energy in pressure coupling configuration

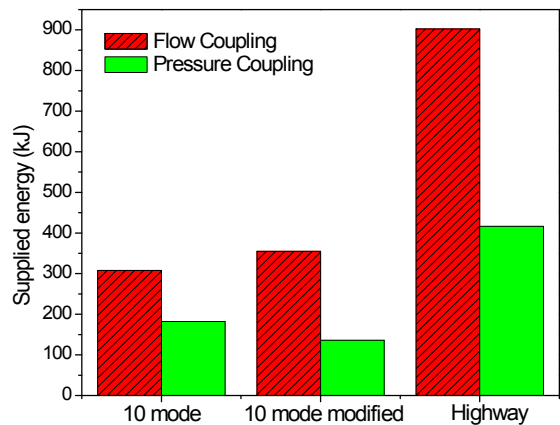


Fig. 13 Supply energy in 10 mode, 10 mode modified profile and highway schedule

The supplied energy for these three schedules is compared in Fig. 13. 61.7% and 53.8% of energy among the supply energy are reduced in 10 mode modified profile and highway schedule, respectively. This result means that the proposed pressure coupling hydrostatic transmission is superior in energy consumption reduction in three road driving schedules.

## 5. Conclusions

A closed-loop hydrostatic transmission with two different configurations (flow coupling and pressure coupling) was proposed and investigated in this research. All hydraulic components were mathematically modeled based on parameters of a real hydraulic system.

This simulation results proved that the pressure coupled hydrostatic transmission had better energy efficiency compared to that of flow coupling one and from the simulation results, 40.8%, 61.7% and 53.8% supplied energy was reduced in 10 mode, modified 10 mode and highway profile, respectively when pressure coupling configuration was adopted.

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