

다중반응표면최적화 : 현황 및 향후 연구방향

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Multiresponse Optimization: A Literature Review and Research Opportunities

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Abstract

A common problem encountered in product or process design is the selection of optimal parameter levels which involves simultaneous consideration of multiple response variables. This is called a multiresponse problem. A multiresponse problem is solved through three major stages: data collection, model building, and optimization. Up to date, various methods have been proposed for the optimization, including the desirability function approach and loss function approach. In this paper, the existing studies in multiresponse optimization are reviewed and a future research direction is then proposed.

1. Introduction

Response surface methodology (RSM) consists of a group of techniques used in empirical study of the relationship between a response and a number of input variables. Consequently, the experimenter attempts to find the optimal setting for the input variables that maximizes (or minimizes) the response [Box and Draper, 1987; Khuri and Cornell, 1996; Myers and Montgomery, 2002].

In product or process development, it is quite common that several response variables are of interest. In this case, determination of optimum conditions on the input variables would require simultaneous consideration of all the responses. This is called a multiresponse problem [Khuri, 1996].

A multiresponse problem is solved through three stages: data collection (by the experimental design), model building, and optimization. In the optimization stage, two questions must be addressed: “what-to-optimize”(optimization goal) and “how-to-optimize-it”(solution technique). This paper focuses on the “what-to-optimize” aspect, assuming that the data have been collected and the response models have been fitted reasonably well. A multiresponse optimization (MRO) problem is formally defined as:

$$\begin{aligned} & \text{Optimize } [y_1(\mathbf{x}), y_2(\mathbf{x}), \dots, y_k(\mathbf{x})] \\ & \text{s.t. } \mathbf{x} \in \Omega, \end{aligned} \quad (1)$$

where $\hat{y}_i(\mathbf{x})$ denotes the estimated i th response ($i = 1, \dots, k$), \mathbf{x} is an input variable vector, and Ω is the experimental region.

Up to date, various methods have been proposed

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for MRO, including the desirability function 「Harrington, 1965; Derringer and Suich, 1980; Derringer, 1994」 and loss function approaches 「Pignatiello, 1993; Vining, 1998; Ko et al., 2005」. MRO problems often involve incommensurate and conflicting criteria in multiple responses. To obtain a satisfactory compromise in such a case, a decision maker (DM)'s preference information on the trade-offs among the responses should be incorporated into the problem. Recently, a few studies have proposed new methods to effectively extract the DM's preference information in MRO such as, for example, the interactive desirability function methods 「Jeong and Kim, 2003; Jeong and Kim, 2005; Jeong and Kim, 2009」 and posterior preference articulation methods 「Lee et al., 2010; Lee et al., 2011a」.

This paper aims at reviewing the existing studies in MRO and then proposing a future research direction. Specifically, it first reviews the numerous papers in the six MRO approaches each (Section 2), and then evaluates them via two aspects: statistics and preference information (Section 3). Finally, a promising research direction in MRO is presented (Section 4).

2. Review of the Existing Studies in MRO

The existing studies in MRO can be categorized into six approaches: graphical, priority-based, desirability function, loss function, process capability, and probability-based approaches. The last five approaches can be grouped into an analytical approach. They take a common strategy that reduces a multidimensional problem in Equation (1) into a one-dimensional problem and then solves it. Each approach is reviewed below.

2.1 Graphical approach

The graphical approach superimposes the response contour plots and determines an optimal

solution by a visual inspection 「Lind et al., 1960」. It had been widely used before analytical methods were developed 「Hill and Hunter, 1966」. This approach has a shortcoming that its usefulness is severely limited by the number of input variables and/or responses. Nevertheless, it has been utilized until recently due to its simplicity and intuitiveness 「Gupta et al., 2001; Hamed and Sakr, 2001; Theppaya and Prasertsan, 2004; Huang et al., 2004; Huang et al., 2005」.

2.2 Priority-based approach

The priority-based approach selects the most important response among a number of ones and then uses it as the objective function. The other responses are employed as constraints:

$$\begin{aligned} & \text{Optimize } \hat{y}_p(\mathbf{x}) \\ & \text{s.t. } \hat{y}_s(\mathbf{x}) \in \mathbf{R}_s, s = 1, \dots, k (s \neq p), \\ & \mathbf{x} \in \Omega, \end{aligned} \quad (2)$$

where $\hat{y}_p(\mathbf{x})$ and $\hat{y}_s(\mathbf{x})$ denote the estimated primary and secondary responses, respectively, and \mathbf{R}_s is a set of requirements for $\hat{y}_s(\mathbf{x})$.

Assuming there are only two responses of interest, Myers and Carter (1973) proposed an optimization formulation that maximizes (or minimizes) the primary response with an equality constraint on the other response. Biles (1975) extended this idea by allowing not only more than two responses, but also inequality constraints on the secondary responses. Del Castillo (1996) proposed an optimization formulation that treats the confidence regions for the stationary points of responses as constraints. More specifically, it first finds a stationary point of each response and then computes the confidence regions for the stationary points of responses. These confidence regions are used as constraints in Equation (2).

The priority-based approach has an advantage that it utilizes the typical formulation style in the optimization field as it is. However, it does not fulfill the philosophy of MRO that simultaneously cons

iders the multiple responses 「Kim et al., 2002」.

2.3. Desirability function approach

The desirability function approach transforms an estimated response (e.g., the i th estimated response \hat{y}_i) into a scale-free value, called a desirability (denoted as d_i for \hat{y}_i). It is a value between 0 and 1, and increases as the corresponding response value becomes more desirable. The overall desirability D , another value between 0 and 1, is defined by combining the individual desirability values (i.e., d_i 's). Then, the optimal setting is determined by optimizing D .

Harrington (1965) first proposed a simple form of a desirability function. Derringer and Suich (1980) extended Harrington's approach by suggesting a more systematic transformation scheme from \hat{y}_i to d_i . As an example, in the case of a nominal-the-best (NTB)-type, the desirability function is given as:

$$d_i(\hat{y}_i(\mathbf{x})) = \begin{cases} 0 & \text{if } \hat{y}_i(\mathbf{x}) \leq Y_i^{\min} \text{ or } \hat{y}_i(\mathbf{x}) > Y_i^{\max}, \\ \left[\frac{\hat{y}_i(\mathbf{x}) - Y_i^{\min}}{T_i^{\min} - Y_i^{\min}} \right]^{s_i} & \text{if } Y_i^{\min} < \hat{y}_i(\mathbf{x}) \leq T_i^{\min}, \\ \left[\frac{Y_i^{\max} - \hat{y}_i(\mathbf{x})}{Y_i^{\max} - T_i^{\max}} \right]^{t_i} & \text{if } T_i^{\max} < \hat{y}_i(\mathbf{x}) \leq Y_i^{\max}, \\ 1 & \text{if } T_i^{\min} < \hat{y}_i(\mathbf{x}) \leq T_i^{\max}, \end{cases} \quad (3)$$

where $d_i(\hat{y}_i(\mathbf{x}))$ is the desirability function of $\hat{y}_i(\mathbf{x})$, Y_i^{\min} and Y_i^{\max} are, respectively, the lower and upper bounds on the response, T_i^{\min} and T_i^{\max} ($T_i^{\min} \leq T_i^{\max}$) are, respectively, the lower and upper targets of the response, and s_i and t_i are the parameters that determine the shape of $d_i(\hat{y}_i(\mathbf{x}))$: if s_i (or t_i) = 1, the shape is linear; if s_i (or t_i) > 1, convex; and if $0 < s_i$ (or t_i) < 1, concave. It should be noted that, if $T_i^{\min} = T_i^{\max}$, the trapezoidal desirability function in Equation (3) reduces to a triangular one. For a definition on the desirability functions of larger-the-better (LTB)- and smaller-the-better (STB)-type responses, see Derringer and Suich (1980).

The desirability function proposed by Derringer and Suich (1980) contains non-differentiable points as shown in Equation (3). Del Castillo et al. (1996) proposed modified desirability functions that are everywhere differentiable so that an efficient gradient-based optimization method, which requires a differentiability assumption, can be used.

The overall desirability can be obtained by aggregating the individual desirability functions using the geometric mean:

$$D = (d_1 \times d_2 \times \dots \times d_k)^{1/k}. \quad (4)$$

Later, different forms of aggregation have been proposed. For example, Derringer (1994) proposed the use of a weighted geometric mean. Kim and Lin (2000) suggested maximizing the lowest d_i , which is equivalent to maximizing the overall degree of satisfaction of all the responses.

Most of the studies in the desirability function approach have been focused mainly on the location effects (i.e., means) of responses. However, as the Taguchi's robust design concept became more popular, the desirability function approach tried to consider the dispersion effects (i.e., variances) as well as the location effects 「Tong et al., 2001; Ribardo and Allen, 2003; Wu, 2005; Kwon et al., 2005; Kim and Lin, 2006」.

The most important advantage of the desirability function approach is easy to use in practice. Moreover, it incorporates the DM's preference information through various channels. However, the acquisition of such information may be quite difficult because he/she provides the information assumptively without recognizing the tradeoffs among the multiple conflicting responses. To overcome this limitation, Jeong and Kim (2003, 2005, 2009) proposed interactive desirability function methods to incorporate the DM's preference information well. The methods adjust the shape, bound, and, target of a desirability function using the preference information extracted from the DM in an interactive manner.

2.4. Loss function approach

The loss function approach aims to find the optimal parameter setting by minimizing the expected loss function. Pignatiello (1993) first proposed the use of a squared error loss function in MRO:

$$L(\mathbf{y}(\mathbf{x})) = (\mathbf{y}(\mathbf{x}) - \boldsymbol{\theta})' \mathbf{C}(\mathbf{y}(\mathbf{x}) - \boldsymbol{\theta}), \tag{5}$$

where $\mathbf{y}(\mathbf{x})$ is a vector of response variables, $\boldsymbol{\theta}$ is the target vector of responses, and \mathbf{C} is the cost matrix representing the relative importance of each response. Then, the expected loss, which is to be minimized, can be derived as:

$$E[L(\mathbf{y}(\mathbf{x}))] = (E(\mathbf{y}(\mathbf{x})) - \boldsymbol{\theta})' \mathbf{C} (E(\mathbf{y}(\mathbf{x})) - \boldsymbol{\theta}) + \text{trace}[\mathbf{C}\boldsymbol{\Sigma}_y(\mathbf{x})], \tag{6}$$

where $\boldsymbol{\Sigma}_y(\mathbf{x})$ is the variance-covariance matrix of the responses. Tsui (1999) extended the Pignatiello's model, which was developed only for an NTB-type response, to the cases for LTB-and STB-type responses.

Vining (1998) proposed a modification to the Pignatiello's model by employing a vector of the estimated responses $\hat{\mathbf{y}}(\mathbf{x})$ in loss function, instead of $\mathbf{y}(\mathbf{x})$. Consequently, the expected loss can be expressed as:

$$E[L(\hat{\mathbf{y}}(\mathbf{x}))] = (E(\hat{\mathbf{y}}(\mathbf{x})) - \boldsymbol{\theta})' \mathbf{C} (E(\hat{\mathbf{y}}(\mathbf{x})) - \boldsymbol{\theta}) + \text{trace}[\mathbf{C}\boldsymbol{\Sigma}_y(\mathbf{x})], \tag{7}$$

where the $\boldsymbol{\Sigma}_y(\mathbf{x})$ is the variance-covariance matrix of the predicted responses. The Vining's approach includes Khuri and Conlon (1981)'s method using the generalized distance concept as a special case.

Ko et al. (2005) proposed an improvement over the Pignatiello's and Vining's models. They employ a vector of the newly estimated responses $\hat{\mathbf{y}}_n(\mathbf{x})$ in the loss function, as opposed to $\mathbf{y}(\mathbf{x})$ in the Pignatiello's or $\hat{\mathbf{y}}(\mathbf{x})$ in Vining's model. Then, the expected loss is expressed as:

$$E[L(\hat{\mathbf{y}}_n(\mathbf{x}))] = (E(\hat{\mathbf{y}}_n(\mathbf{x})) - \boldsymbol{\theta})' \mathbf{C} (E(\hat{\mathbf{y}}_n(\mathbf{x})) - \boldsymbol{\theta}) + \text{trace}[\mathbf{C}\boldsymbol{\Sigma}_{\hat{\mathbf{y}}_n}(\mathbf{x})] + \text{trace}[\mathbf{C}\boldsymbol{\Sigma}_y(\mathbf{x})], \tag{8}$$

The expected loss in Equation (8) includes both the variance of the estimated and the variance of the estimated responses. Thus, the Ko et al.'s model is a more generalized model and includes both the Pignatiello's and Vining's models as special cases.

The loss function approach originates from the Taguchi's robust design concept. Therefore, it necessarily considers the dispersion effects of responses (i.e., $\boldsymbol{\Sigma}_y(\mathbf{x})$ in Equations (6) and (8)). The loss function approach is statistically good, but it requires strong statistical assumptions as a consequence.

2.5. Process capability approach

The process capability approach derives a process capability index using the estimated mean and standard deviation of a response. The overall capability index is obtained by combining the individual process capability indices. Then, the optimal setting is determined by maximizing the overall capability index.

Barton and Tsui (1991) proposed a performance centering as a process capability index:

$$PC_i = \min \left\{ \frac{\hat{\mu}_i(\mathbf{x}) - Y_i^{\min}}{\hat{\sigma}_i(\mathbf{x})}, \frac{Y_i^{\max} - \hat{\mu}_i(\mathbf{x})}{\hat{\sigma}_i(\mathbf{x})} \right\}, \tag{9}$$

where PC_i , $\hat{\mu}_i(\mathbf{x})$, and $\hat{\sigma}_i(\mathbf{x})$ are the performance centering measure, the estimated mean, and the estimated standard deviation of the i th response variable, respectively. Then, they suggested maximizing the minimum of PC_i 's. Plante (1999) extended the Barton and Tsui's approach by developing several multicriteria models based on the performance centering. Plante (2001) proposed the use of two typical process capability indices, Cpk and Cpm :

$$Cpk_i = \min \left\{ \frac{\hat{\mu}_i(\mathbf{x}) - Y_i^{\min}}{3\hat{\sigma}_i(\mathbf{x})}, \frac{Y_i^{\max} - \hat{\mu}_i(\mathbf{x})}{3\hat{\sigma}_i(\mathbf{x})} \right\}, \tag{10}$$

$$Cpm_i = \frac{Y_i^{\max} - Y_i^{\min}}{6\sqrt{(\hat{\sigma}_i(\mathbf{x}))^2 + (\mu_i(\mathbf{x}) - \theta_i)^2}}, \quad (11)$$

where θ_i is the target of the i th response variable. As shown in Equations (9) and (10), PC_i and Cpk_i are fundamentally the same index. Then, he suggested maximizing the (weighted) geometric mean of Cpk_i 's (or Cpm_i 's). Ch'ng et al. (2005) proposed to maximize the weighted sum of Cpm_i 's. Köksalan and Plante (2003) proposed an interactive optimization method to incorporate the DM's preference information in their proposed method.

The major advantage of the process capability approach is that its objective function, namely, Cpk and Cpm , are familiar to quality practitioners and it considers the dispersion effects of responses via the variance term (i.e., $\hat{\sigma}_i(\mathbf{x})$ in Equations (9)-(11)).

2.6. Probability-based approach

The probability-based approach assumes a multivariate probability distribution of a multivariate response \mathbf{Y} . It first models the distributional parameters in terms of input variables and then finds the optimal setting which maximizes the probability that all responses simultaneously meet their specifications.

Chiao and Hamada (2001) assumed the multivariate normal distribution with mean $\boldsymbol{\mu} = (\mu_1, \mu_2, \dots, \mu_k)'$ and variance-covariance matrix $\boldsymbol{\Sigma}$ (the diagonal elements of which are the variances $\sigma_1^2, \sigma_2^2, \dots, \sigma_k^2$ and the off-diagonal elements of which are the covariances $\rho_{ij}\sigma_i\sigma_j$ ($1 \leq i < j \leq k$), where ρ_{ij} is the correlation between the i th and j th responses). The joint probability density function, $f(\mathbf{Y}; \boldsymbol{\mu}, \boldsymbol{\Sigma})$, is given as:

$$f(\mathbf{Y}; \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \frac{1}{(2\pi)^{(k/2)}|\boldsymbol{\Sigma}|^{1/2}} e^{-(1/2)(\mathbf{Y}-\boldsymbol{\mu})'\boldsymbol{\Sigma}^{-1}(\mathbf{Y}-\boldsymbol{\mu})}. \quad (12)$$

The distributional parameters are modeled as a function of \mathbf{x} : $\hat{\mu}_i(\mathbf{x})$, $\hat{\sigma}_i(\mathbf{x})$, and $\hat{\rho}_{ij}(\mathbf{x})$. Then, they

suggested maximizing the proportion of conformance, $P(\mathbf{Y} \in \mathbf{S} | \mathbf{x})$, where \mathbf{S} is a set of specifications for the responses. Peterson (2004) and Miró-Quesada et al. (2004) estimated the distributional parameters in the multivariate t distribution using a Bayesian approach.

The major advantage of this approach is that it stands on the solid statistical basis. However, it has some shortcomings that it makes a strong statistical assumption and allows no interaction with the DM.

2.7. Other approaches

There are a few studies that are not directly included in, but closely related to the desirability function approach. Kumar and Goel (2002) and Lai and Chang (2004) proposed a fuzzy modeling approach, which can be viewed as the desirability function approach. Peterson (2000) proposed a combined approach of the desirability function and probability-based approaches.

Several variants of the loss function approach have also appeared in the literature. Ribeiro et al. (2000), Teeravaraprug and Cho (2002), and Savage and Seshadri (2003) added a "cost-of-loss" concept to the loss function approach. Tong and Su (1997), Su and Tong (1997), Antony (2000), Yang and Chou (2005), Wang and Tong (2005), and Liao (2006) considered a new variable called "quality loss" as a response. Chen (1997), Lu and Antony (2002), Maghsoodloo and Chang (2001), Wu (2002), and Tong et al. (2004a, 2004b) considered the "signal-to-noise" ratio as a response. Romano et al. (2004) proposed a loss function method integrating both robust parameter design and tolerance design. Logothetis and Haigh (1988), Artiles-Leon (1996), Tong et al. (1997), and Jayaram and Ibrahim (1997) also modified the conventional loss function approach or introduced a new concept into it.

Reddy et al. (1997) and Xu et al. (2004) proposed a goal programming approach. Kumar et al. (2000)

proposed to apply a utility concept to the Taguchi method.

3. Evaluation of the Existing Studies

In this section, the existing studies in MRO are evaluated in two aspects: statistics and preference information. The statistics-based evaluation identifies whether an existing study considers the important statistical properties (which will be described in detail in Subsection 3.1) for MRO and how many. The preference information-based evaluation finds how many channels an existing approach holds in order to represent the DM's preference information and at which timing, namely, before, during, or after solving the problem, the preference information are specified.

The evaluation results will show the limitations of the existing studies and present some insights on a further research direction in MRO. It should be noted that the papers in the analytical approach in Section 2 are used in the evaluation. Therefore, the graphical approach is excluded for evaluation. It should be also noted that the framework of this evaluation refers to Kim et al. (2002).

3.1. Statistics-based evaluation

In this subsection, the existing studies in MRO are evaluated depending on whether or not it considers the following three statistical properties: (i) correlation structure among responses, (ii) robustness of response, and (iii) quality of response models.

3.1.1. Correlation structure among responses

The correlation structure means the strength of relationships among responses. The first column of Table 1 shows the evaluation results on the correlation structure. All the studies in the priority-based and process capability approaches do not consider the correlation structure at all. Few studies in the desirability function approach consider

the correlation structure among responses. Wu (2005) is the only study considering the correlation structure in this approach.

On the other hand, nearly half the studies in the loss function approach and all the studies in the probability-based approach consider the correlation structure through variance-covariance matrix. In the loss function approach, Elsayed and Chen (1993), Ribeiro and Elsayed (1995), Ames et al. (1997), and Lamghabbar et al. (2004) did not consider the correlation structure.

3.1.2. Robustness of response

The robustness refers to the low sensitivity of the response to other factors, that is, the small dispersion effects. Two types of sensitivity have been addressed: robustness to uncontrollable (noise) factors and robustness to parameter fluctuation. The robustness to uncontrollable factors means how large the variance of a response is at specific setting of input variables. On the other hand, the robustness to parameter fluctuation means how large the variance of a response is amplified by the parameter fluctuation of input variables.

The second column of Table 1 shows the results of evaluation on the robustness of response. All the studies in the priority-based approach and most of the studies in the desirability function and probability-based approaches do not consider the robustness. But, several papers in the desirability function approach consider the robustness. Tong et al. (2001), Ribardo and Allen (2003), Wu (2005), and Kim and Lin (2006) considered the robustness to uncontrollable factors, while Kwon (2005) considered both the robustness to uncontrollable factors and the robustness to parameter fluctuation.

On the other hand, all the studies in the process capability approach and most of the studies in the loss function approach, including Wu and Chyu (2004), consider the robustness. This is because the loss function approach originates from the Taguchi's robust design concept and the process capability

approach uses the indices involving the estimated standard deviation of a response.

3.1.3. Quality of response models

The quality of response models refers to how reliable the estimated response models are. Two approaches have been proposed in this regard: quality of description and quality of prediction. The quality of description measures how well the estimated response models explain data. The R^2 , adjusted R^2 , or mean squared error can be employed as measures of the quality of description. On the other hand, the quality of prediction measures how large the variance of a model itself is at specific setting of input variables.

The last column of Table 1 shows the results of evaluation on the quality of response models. Most of the studies in all the approaches do not consider the quality of response models. But, a couple of papers in the desirability function, loss function, and probability-based approaches each consider the quality of response models. Kim and Lin (2000, 2006) in the desirability function approach proposed a method to adjust the desirability function shape by incorporating the levels of the quality of description. Vining (1998) and Ko et al. (2005) in the loss function approach considered the quality of prediction by employing the variance-covariance matrix of the predicted responses (i.e., $\Sigma_y(\mathbf{x})$ in Equations (7) and (8), respectively). Peterson (2004) and Miró-Quesada et al. (2004) in the probability-based approach also employed the variance-covariance matrix of the predicted responses.

3.1.4. Summary

Table 1 shows that the robustness is the most considered property by the existing studies in MRO, while the quality of response models is not much considered. Many studies in the loss function and probability-based approaches seem to consider two properties. The ratios of papers considering two properties amount to 56% in the loss function approach and 67% in the probability-based approach, respectively. All the studies in the process

capability approach and most of the studies in the desirability function approach consider only the robustness. The only paper considering all the properties is Ko et al. (2005). In the future, a newly conducted study in MRO needs to consider all the three statistical properties.

3.2. Preference information-based evaluation

Most of the MRO approaches require the DM's preference information on the tradeoffs among multiple responses. The preference information is represented through preference parameters. The shape, bound, and target of a desirability function or the cost matrix of a loss function are examples of such preference parameters. The preference information can be extracted at one of the following timings: before, during, and after solving the problem. In this subsection, the existing MRO approaches are evaluated in terms of: (i) the number of preference parameters and (ii) the timing of extracting the DM's preference information.

3.2.1. Number of preference parameters

In general, the preference parameters in MRO include the target (of a response), specifications (of a response), and relative weights (among responses). The priority-based approach considers the target and specifications. The desirability function approach considers not only all those parameters, but also the pattern or curve of the desirability (of a response). The loss function approach considers the target and relative weights. The process capability approach considers all the parameters, but it does not consider any additional parameter unlike the desirability function approach. The probability-based approach considers only the specifications.

As of now, the desirability function approach considers the most preference parameters among the MRO approaches. This means that the desirability function approach enables the DM to have flexible options to provide his/her preference information in various ways. Therefore, this approach is ex-

<Table 1> The results of evaluation based on statistical properties

Approach	Existing Studies	Correlation	Robustness	Quality
Priority-based approach	Myers and Carter (1973)			
	Biles (1975)			
	Del Castillo (1996)			
Desirability function approach	Derringer and Suich (1980)			
	Derringer (1994)			
	Del Castillo et al. (1996)			
	Kim and Lin (2000)			●
	Tong et al. (2001)		○	
	Jeong and Kim (2003)			
	Ribardo and Allen (2003)			○
	Wu (2005)	○	○	
	Kwon et al. (2005)		◎	
	Jeong and Kim (2005)			
Kim and Lin (2006)			○	●
Loss function approach	Pignatiello (1993)	○	○	
	Elsayed and Chen (1993)		○	
	Ribeiro and Elsayed (1995)		◎	
	Ames et al. (1997)			
	Vining (1998)	○		○
	Tsui (1999)	○	○	
	Lamghabbar et al. (2004)		○	
	Wu and Chyu (2004)	○	○	
	Ko et al. (2005)	○	○	○
	Process capability approach	Barton and Tsui (1991)		○
Plante (1999)			○	
Plante (2001)			○	
Köksalan and Plante (2003)			○	
Ch'ng et al. (2005)			○	
Probability-based approach	Chiao and Hamada (2001)	○	○	
	Peterson (2004)	○		○
	Miró-Quesada et al. (2004)	○		○

In the Robustness column, the symbol ◎ represents that the corresponding paper considers both the robustness to uncontrollable factors and the robustness to parameter fluctuation, while the symbol ○ only the robustness to uncontrollable factors.

In the Quality column, the symbol ● represents that the corresponding paper considers only the quality of description, while the symbol ○ only the quality of prediction.

pected to have a good potential to effectively extract the DM preference information.

3.2.2. Timing of extracting the DM's preference information

Existing MRO methods can be categorized through the multiobjective optimization (MOO) classification system. Generally, the MOO literature classifies various optimization methods into three categories by the timing of the DM's preference information into a model: prior, progressive, and posterior preference articulation methods [Hwang et al., 1979; Zeleny, 1982; Steuer, 1986; Miettinen, 1999; Collette and Siarry, 2003; Figueira et al., 2005].

The prior method requires that all the preference information of the DM be extracted prior to solving the problem. The progressive method, often referred to as the interactive method, requires that the DM input his/her preference information into a model during the problem solving process. The posterior method first finds all (or most) of the efficient solutions without any substantial articulation of the DM's preference information. The DM then chooses the best one from the set of efficient solutions a posteriori.

Most of the studies in the MRO approaches are categorized into the prior method in terms of MOO [Park et al., 2000; Park and Kim, 2005]. However, a few studies, for example, Montgomery and Bettecourt (1977), Mollaghasemi and Evans (1994), Boyle and Shin (1996), Köksalan and Plante (2003), Jeong and Kim (2003, 2005, 2009), Park and Kim (2005), proposed an interactive method to MRO problems.

Montgomery and Bettencourt (1977) and Park and Kim (2005) applied the GDF algorithm [Geoffrion et al., 1972] to a battle tank crew-training problem and a polymer design problem, respectively. Mollaghasemi and Evans (1994) applied a modified version of STEM [Benayoun et al., 1971] to a job shop simulation problem. Köksalan and Plante (2003) proposed to use the parametric Achievement-Scalaring Program [Korhonen and Laakso, 1986] to

solve an MRO problem.

The studies employing the posterior method in solving MRO problems have scarcely been found. Recently, Lee et al. (2010) and Lee et al. (2011a) proposed a posterior method to MRO. Both studies adopt the ϵ -constraint method [Haimes et al., 1971] to generate a good number of efficient solutions. However, they proposed a different method in selecting the best solution. Lee et al. (2010) proposed a "graphically" interactive selection method focusing on the two-response case. Lee et al. (2011a) proposed to use the Köksalan and Sagala (1995)'s interactive selection method for the multi-response case.

The prior method is conceptually easy to understand, but the DM may have difficulties in specifying all the required preference information in advance. The posterior method requires minimal cognitive efforts of the DM in the beginning, but it is impractical to generate a good representative set of efficient solutions. Moreover, it may require an excessive cognitive effort of the DM after all in selecting the best solution, especially when the solution space is represented with a large number of solutions [Lee et al., 2011b]. The interactive method is more realistic in that it requires the DM's preference information progressively rather than requiring all preference information in advance, although the DM has only to provide his/her preference information by a local level due to the "one-solution-at-a-time" scheme. This method would be highly effective and efficient in searching the DM's preference structure for a satisfactory compromise as stated in Steuer (1986).

4. Conclusions and a Future Research Direction

This paper has reviewed the existing studies in MRO under the categories of the graphical, priority-based, desirability function, loss function, process capability, and probability-based approaches. Then, it has evaluated them in two aspects: sta-

tistics and preference information.

In the future, a new study is required to consider the following two points. First, it should consider all the three important statistical properties for MRO: correlation structure among responses, robustness of response, and quality of response models. Second, it should try to effectively extract the DM's preference information on the multiple conflicting responses.

The second requirement can be well resolved by a combination of the desirability function approach and the interactive method. As mentioned in Subsection 3.2.1, the desirability function approach has the most preference parameters, namely, the target, specifications, shape, and relative weights. Such a good number of preference parameters allow the DM to have flexible options to provide his/her preference information in various ways. As mentioned in Subsection 3.2.2, an interactive method is the most realistic alternative in effectively searching the DM's preference structure for a satisfactory compromise. Therefore, the combined approach is certainly believed to be a very promising alternative for MRO.

References

- [1] Ames, A., Mattucci, N., McDonald, S., Szonyi, G., and Hawkins, D.(1997), "Quality Loss Function for Optimization Across Multiple Response Surfaces", *Journal of Quality Technology*, Vol. 29, pp. 339-346.
- [2] Antony, J.(2000), "Multi-Response Optimization in Industrial Experiments Using Taguch's Quality Loss Function and Principal Component Analysis", *Quality and Reliability Engineering International*, Vol. 16, pp. 3-8.
- [3] Artiles-Leon, N.(1996), "A Pragmatic Approach to Multiple-Response Problems Using Loss Functions", *Quality Engineering*, Vol. 9, pp. 213-220.
- [4] Barton, R. S. and Tsui, K. L.(1991), "Multivariate Yield Maximization Using CAD/CAE Models: Efficient Approximations Based on Mean and Variance", *Design Theory and Methodology (ASME)*, Vol. 31, pp. 31-35.
- [5] Benayoun, R., de Montgolfier, J., Tergny, J., and Larichev, O.(1971), "Linear Programming with Multiple Objective Functions: Step Method (STEM)", *Mathematical Programming*, Vol. 1, pp. 366-375.
- [6] Biles, W. E.(1975), "A Response Surface Methods for Experimental Optimization of Multi-Response Processes", *Industrial and Engineering Chemistry Process Design and Deployment*, Vol. 14, pp. 152-158.
- [7] Box, G. E. P. and Draper, N. R.(1987), *Empirical Model Building and Response Surfaces*, John Wiley & Sons, New York.
- [8] Boyle, C. R. and Shin, W. S.(1996), "An Interactive Multiple-Response Simulation Optimization Method", *IIE Transactions*, Vol. 28, pp. 453-462.
- [9] Chen, L.(1997), "Designing Robust Products with Multiple Quality Characteristics", *Computer and Operations Research*, Vol. 24, pp. 937-944.
- [10] Chiao, C. and Hamada, M.(2001), "Analyzing Experiments with Correlated Multiple Responses", *Journal of Quality Technology*, Vol. 33, pp. 451-465.
- [11] Ch'ng, C. K., Quah, S. H., and Low, H. C.(2005), "Index Cpm* in Multiple Response Optimization", *Quality Engineering*, Vol. 17, pp. 165-171.
- [12] Collette, Y. and Siarry, P.(2003), *Multiobjective Optimization: Principles and Case Studies*, Springer-Verlag, Berlin.
- [13] Del Castillo, E.(1996), "Multiresponse Process Optimization via Constrained Confidence Regions", *Journal of Quality Technology*, Vol. 28, pp. 61-70.
- [14] Del Castillo, E., Montgomery, D. C., and McCarville, D. R.(1996), "Modified Desirability Functions for Multiple Response Optimization", *Journal of Quality Technology*, Vol. 28, pp. 337-345.
- [15] Derringer, G. and Suich, R.(1980), "Simultaneous Optimization of Several Response Variables", *Journal of Quality Technology*, Vol. 12, pp. 214-219.
- [16] Derringer, G.(June 1994), "A Balancing Act: Optimizing a Product's Properties", *Quality Progress*, pp. 51-57.
- [17] Elsayed, E. and Chen, A.(1993), "Optimal Level of Process Parameters for Products with Multiple Characteristics", *International Journal of Production Research*, Vol. 31, pp. 1117-1132.
- [18] Figueira, J., Greco, S., and Ehrgott, M.(2005), *Multiple Criteria Decision Analysis: State of the Art Surveys*, Springer, New York.

- [19] Geoffrion, A. M., Dyer, J. S., and Feinberg, A.(1972), "An Interactive Approach for Multi-Criterion Optimization with an Application to the Operation of an Academic Department", *Management Science*, Vol. 19, pp. 357-368.
- [20] Gupta, V. K., Assmus, M. W., Beckert, T. E., and Price, J. C.(2001), "A Novel pH- and Time-Based Multi-Unit Potential Colonic Drug Delivery System. II. Optimization of Multiple Response Variables", *International Journal of Pharmaceutics*, Vol. 213, pp. 93-102.
- [21] Haimes, Y. Y., Lasdon, L. S., and Wismer, D. A.(1971), "On a Bicriterion Formulation of the Problems of Integrated System Identification and System Optimization", *IEEE Transactions on Systems, Man, and Cybernetics*, Vol. 1, pp. 296-297.
- [22] Hamed, E. and Sakr, A.(2001), "Application of Multiple Response Optimization Technique to Extended Release Formulations Design", *Journal of Controlled Release*, Vol. 73, pp. 329-338.
- [23] Harrington, E., Jr.(1965), "The Desirability Function", *Industrial Quality Control*, Vol. 21, pp. 494-498.
- [24] Hill, W. J. and Hunter, W. G.(1966), "A Review of Response Surface Methodology: A Literature Survey", *Technometrics*, Vol. 8, pp. 571-590.
- [25] Huang, Y., Tsai, Y., Lee, S., Chang, J., and Wu, P.(2005), "Optimization of pH-Independent Release of Nicardipine Hydrochloride Extended-Release Matrix Tablets using Response Surface Methodology", *International Journal of Pharmaceutics*, Vol. 289, pp. 87-95.
- [26] Huang, Y., Tsai, Y., Yang, W., Chang, J., Wu, P., and Takayama, K.(2004), "Once-Daily Propranolol Extended-Release Tablet Dosage Form: Formulation Design and In Vitro/In Vivo Investigation", *European Journal of Pharmaceutics and Biopharmaceutics*, Vol. 58, pp. 607-614.
- [27] Hwang, C. L., Masud, A. S. M., Paidy, S. R., and Yoon, K.(1979), *Multiple Objective Decision Making-Methods and Applications (Lecture Notes in Economics and Mathematical Systems)*, Springer-Verlag, Berlin.
- [28] Jayaram, J. S. R. and Ibrahim, Y.(1997), "Robustness for Multiple Response Problems Using a Loss Model", *International Journal of Quality Science*, Vol. 2, pp. 199-205.
- [29] Jeong, I. and Kim, K.(2003), "Interactive Desirability Function Approach to Multi-Response Surface Optimization", *International Journal of Reliability, Quality and Safety Engineering*, Vol. 10, pp. 205-217.
- [30] Jeong, I. and Kim, K.(2005), "D-STEM: A Modified Step Method with Desirability Function Concept", *Computers and Operations Research*, Vol. 32, pp. 3175-3190.
- [31] Jeong, I. and Kim, K.(2009), "An interactive desirability function method to multiresponse optimization", *European Journal of Operational Research*, Vol. 195, pp. 412-426.
- [32] Khuri, A. I.(1996), "Multiresponse Surface Methodology", *Handbook of Statistics: Design and Analysis of Experiment (Vol. 13) (eds. A. Ghosh and C. R. Rao)*, pp. 377-406.
- [33] Khuri, A. I. and Conlon, M.(1981), "Simultaneous Optimization of Multiple Responses Represented by Polynomial Regression Functions", *Technometrics*, Vol. 23, pp. 363-375.
- [34] Khuri, A. I. and Cornell, J.(1996), *Response Surfaces: Designs and Analyses*, Dekker, New York.
- [35] Kim, K., Byun J., Min, D., and Jeong, I.(2002), "Multiresponse Surface Optimization: Concept, Methods, and Future Directions", *Proceedings of the International Conference on Quality Management and Motivation for Organizational Development (QMOT)*, pp. 506-515.
- [36] Kim, K. and Lin, D.(2000), "Simultaneous Optimization of Mechanical Properties of Steel by Maximizing Exponential Desirability Functions", *Journal of Royal Statistical Society-Series C*, Vol. 49, pp. 311- 325.
- [37] Kim, K. and Lin, D.(2006), "Optimization of Multiple Responses Considering Both Location and Dispersion Effects", *European Journal of Operational Research*, Vol. 169, pp.133-145.
- [38] Ko, Y., Kim, K., and Jun, C.(2005), "A New Loss Function-Based Method for Multiresponse Optimization", *Journal of Quality Technology*, Vol. 37, pp. 50-59.
- [39] Korhonen, P. J. and Laakso, J.(1986), "A Visual Interactive Method for Solving the Multiple Criteria Problem", *European Journal of Operational Research*, Vol. 24, pp. 277-287.
- [40] Köksalan, M. and Plante, R. D.(2003), "Interactive Multicriteria Optimization for Multiple-Response Product and Process Design", *Manufacturing and*

- Service Operations Management*, Vol. 5, pp. 334-347.
- [41] Köksalan, M. and Sagala, P. N. S.(1995), "Interactive approaches for discrete alternative multiple criteria decision making with monotone utility functions", *Management Science*, Vol. 41, pp. 1158-1171.
- [42] Kumar, P., Barua, P. B., and Gaindhar, J. L.(2000), "Quality Optimization (Multi-Characteristics) through Taguchi's Technique and Utility Concept", *Quality and Reliability Engineering International*, Vol. 16, pp. 475-485.
- [43] Kumar, P. and Goel, P.(2002), "Product Quality Optimization Using Fuzzy Set Concepts: A Case Study", *Quality Engineering*, Vol. 15, pp. 1-8.
- [44] Kwon, J., Lee, J., Lee, S., Jun, C., and Kim, K.(2005), "Multiresponse Optimization through A New Desirability Function Considering Process Parameter Fluctuation", *Journal of the Korean Operations Research and Management Science Society*, Vol. 30, pp. 95-104.
- [45] Lai, Y. and Chang, S.(1994), "A Fuzzy Approach for Multiresponse Optimization: An Off-Line Quality Engineering Problem", *Fuzzy Sets and Systems*, Vol. 63, pp. 117-129.
- [46] Lamghabbar, A., Yacout, S., and Ouali, M. S.(2004), "Concurrent Optimization of the Design and Manufacturing Stages of Product Development", *International Journal of Production Research*, Vol. 42, pp. 4495-4512.
- [47] Lee, D., Jeong, I., and Kim, K.(2010), "A Posterior Preference Articulation Approach to Dual Response Surface Optimization", *IIE Transactions*, Vol. 42, pp. 161-171.
- [48] Lee, D., Kim, K., and Köksalan, M.(2011a), "A Posterior Preference Articulation Approach to Multiresponse Surface Optimization", *European Journal of Operational Research*, Vol. 210, pp. 301-309.
- [49] Lee, D., Kim, K., and Köksalan, M.(2011b), "An Interactive Method to Multiresponse Surface Optimization Based on Pairwise Comparisons", *IIE Transactions* (To appear).
- [50] Liao, H.(2006), "Multi-Response Optimization using Weighted Principal Component", *International Journal of Advanced Manufacturing Technology*, Vol. 26, pp. 720-725.
- [51] Lind, E. E., Goldin, J., and Hickman, J. B.(1960), "Fitting Yield and Cost Response Surfaces", *Chemical Engineering Progress*, Vol. 56, pp. 62-68.
- [52] Logothetis, N. and Haigh, A.(1988), "Characterizing and Optimizing Multi-Response Processes by the Taguchi Method", *Quality and Reliability Engineering International*, Vol. 4, pp. 159-169.
- [53] Lu, D. and Antony, J.(2002), "Optimization of Multiple Responses using a Fuzzy-Rule Based Inference System", *International Journal of Production Research*, Vol. 40, pp. 1613-1625.
- [54] Maghsoodloo, S. and Chang, C.(2001), "Quadratic Loss Functions and Signal-to-Noise Ratios for a Bivariate Response", *Journal of Manufacturing Systems*, Vol. 20, pp. 1-12.
- [55] Miettinen, K. M.(1999), *Nonlinear Multiobjective Optimization*, Kluwer, Boston.
- [56] Miró-Quesada, G., Del Castillo, E., and Peterson, J. J.(2004), "A Bayesian Approach for Multiple Response Surface Optimization in the Presence of Noise Variables", *Journal of Applied Statistics*, Vol. 31, pp. 251-270.
- [57] Mollaghasemi, M. and Evans, G. W.(1994), "Multicriteria Design of Manufacturing Systems through Simulation Optimization", *IEEE Transactions on Systems, Man, and Cybernetics*, Vol. 24, pp. 1407-1411.
- [58] Montgomery, D. C. and Bettencourt, V. M., Jr.(1977), "Multiple Response Surface methods in Computer Simulation", *Simulation*, Vol. 29, pp. 113-121.
- [59] Myers, R. H. and Carter, W. H.(1973), "Response Surface Techniques for Dual Response Systems", *Technometrics*, Vol. 15, pp. 301-317.
- [60] Myers, R. H. and Montgomery, D. C.(2002), *Response Surface Methodology*, 2nd Edition, John Wiley & Sons, New York.
- [61] Park, K. and Kim, K.(2005), "Optimizing Multi-Response Surface Problems: How to Use Multi-Objective Optimization Techniques", *IIE Transactions*, Vol. 37, pp. 523-532.
- [62] Park, K., Kim, K., and Moskowitz, H.(2000), "Multi-Response Surface Optimization and Multi-Objective Optimization: Relationships and Directions", *New Frontiers of Decision Making for the Information Technology Era* (Eds. Shi and Zeleny), pp. 289-303, World Scientific Publishing, Singapore.
- [63] Peterson, J. J.(2000), "A Probability-Based Desirability Function for Multiresponse Optimization",

- Proceedings of the Section on Quality and Productivity (Annual Meeting of the American Statistical Association).*
- [64] Peterson, J. J.(2004), "A Posterior Predictive Approach to Multiple Response Surface Optimization", *Journal of Quality Technology*, Vol. 36, pp. 139-153.
- [65] Pignatiello, J.(1993), "Strategies for Robust Multiresponse Quality Engineering", *IIE Transactions*, Vol. 25, pp. 5-15.
- [66] Plante, R. D.(1999), "Multicriteria Models for the Allocation of Design Parameter Targets", *European Journal of Operational Research*, Vol. 115, pp. 98-112.
- [67] Plante, R. D.(2001), "Process Capability: A Criterion for Optimizing Multiple Response Product and Process Design", *IIE Transactions*, Vol. 33, 497-509.
- [68] Reddy, P., Nishina, K., and Babu, S.(1997), "Unification of Robust Design and Goal Programming for Multiresponse Optimization: A Case Study", *Quality and Reliability Engineering International*, Vol. 13, pp. 371-383.
- [69] Ribeiro, J. L. and Elsayed, E. A.(1995), "A Case Study on Process Optimization Using the Gradient Loss Function", *International Journal of Production Research*, Vol. 33, pp. 3233-3248.
- [70] Ribeiro, J. L., Fogliatto, F. S., and ten Caten, C. S.(2000), "Minimizing Manufacturing and Quality Costs in Multiresponse Optimization", *Quality Engineering*, Vol. 13, pp. 191-201.
- [71] Ribardo, C. and Allen, T.(2003), "An Alternative Desirability Function for Achieving 'Six Sigma' Quality", *Quality and Reliability Engineering International*, Vol. 19, pp. 227-240.
- [72] Romano, D., Varetto, M., and Vicario, G.(2004), "Multiresponse Robust Design: A General Framework Based on Combined Array", *Journal of Quality Technology*, Vol. 36, pp. 27-37.
- [73] Savage, G. J. and Seshadri, R.(2003), "Minimizing Cost of Multiple Response Systems by Probabilistic Robust Design", *Quality Engineering*, Vol. 16, pp. 67-74.
- [74] Steuer, R. E.(1986), *Multiple Criteria Optimization: Theory, Computation, and Application*, John Wiley & Sons, New York.
- [75] Su, C. and Tong, L.(1997), "Multi-Response Robust Design by Principal Component Analysis", *Total Quality Management*, Vol. 8, pp. 409-416.
- [76] Teeravaraprug, J. and Cho, B.(2002), "Designing the Optimal Process Target Levels for Multiple Quality Characteristics", *International Journal of Production Research*, Vol. 40, pp. 37-54.
- [77] Theppaya, T. and Prasertsan, S.(2004), "Optimization of Rubber Wood Drying by Response Surface Method and Multiple Contour Plots", *Drying Technology*, Vol. 22, pp. 1637-1660
- [78] Tong, L. and Su, C.(1997), "Optimizing Multi-Response Problems in the Taguchi Method by Fuzzy Multiple Attribute Decision Making", *Quality and Reliability Engineering International*, Vol. 13, pp. 25-34.
- [79] Tong, L., Su, C., and Wang, C.(1997), "The Optimization of Multiresponse Problems in the Taguchi Method", *International Journal of Quality and Reliability Management*, Vol. 14, pp. 367-380.
- [80] Tong, L., Wang, C., and Chen, H.(2004a), "Optimization of Multiple Responses using Principal Component Analysis and Technique for Order Preference by Similarity to Ideal Solution", *International Journal of Advanced Manufacturing Technology*, Vol. 27, pp. 407-414.
- [81] Tong, L., Wang, C., Chen, C., and Chen, J.(2004b), "Dynamic Multiple Responses by Ideal Solution Analysis", *European Journal of Operational Research*, Vol. 156, pp. 433-444.
- [82] Tong, L., Wang, C., Houg, J., and Chen, J.(2001), "Optimizing Dynamic Multiresponse Problems Using the Dual-Response-Surface Method", *Quality Engineering*, Vol. 14, pp. 115-125.
- [83] Tsui, K. L.(1999), "Robust Design Optimization for Multiple Characteristic Problems", *International Journal of Production Research*, Vol. 37, pp. 433-445.
- [84] Vining, G.(1998), "A Compromise Approach to Multiresponse Optimization", *Journal of Quality Technology*, Vol. 30, pp. 309-313.
- [85] Wang, C. and Tong, L.(2005), "Optimization of Dynamic Multi-Response Problems Using Grey Multiple Attribute Decision Making", *Quality Engineering*, Vol. 17, pp. 1-9.
- [86] Wu, F.(2002), "Optimization of Multiple Quality Characteristics Based on Percentage Reduction of Taguchi's Quality Loss", *International Journal of Advanced Manufacturing Technology*, Vol. 20, pp. 749-753.

- [87] Wu, F.(2005), "Optimization of Correlated Multiple Quality Characteristics Using Desirability Function", *Quality Engineering*, Vol. 17, pp. 119-126.
- [88] Wu, F. and Chyu, C.(2004), "Optimization of Robust Design for Multiple Quality Characteristics", *International Journal of Production Research*, Vol. 42, pp. 337-354.
- [89] Xu, K., Lin, D., Tang, L., and Xie, M.(2004), "Multiresponse Systems Optimization Using a Goal Attainment Approach", *IIE Transactions*, Vol. 36, pp. 433-445.
- [90] Yang, T. and Chou, P.(2005), "Solving a Multiresponse Simulation-Optimization Problem with Discrete Variables using a Multiple-Attribute Decision-Making Method", *Mathematics and Computers in Simulation*, Vol. 68, pp. 9-21.
- [91] Zeleny, M.(1982), *Multiple Criteria Decision Making*, McGraw-Hill, New York.

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