

## Stability Analysis of Mooring Lines of a Submersible Fish Cage System Using Numerical Model

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**Abstract:** A numerical model analysis was performed to analyze the stability of the mooring lines of an automatic submersible fish cage system in waves and currents. The fish cage system consisted of a 12-angled rigid frame, net cage, cover net, 12 upper floats, 12 tanks(for fixed and variable ballast), mooring lines, anchors, and a control station. Simulations were performed with the cage at the surface of the water and at a depth of 20 m. A Morison equation type model was used for simulations of the system in two configurations. The force parameters described both regular and random waves, with and without currents, and their values were input to the model. Mooring tension calculations were conducted on the mooring lines, grid lines and lower bridle lines of the cage. The stability of the mooring lines was checked under both static and dynamic conditions.

**Key words:** Numerical analysis, Automatic submersible fish cage, Static tension, Wave and current loadings, Mooring tension

### 1. Introduction

The development of offshore fish cage technology has recently been driven by the limits to expansion being faced by aquaculture production in the near shore and semi-enclosed bays of Korea[1]. However, offshore sites have their own challenges, including increased wave action, which may cause damage to the cages and fish to become stressed; potential conflict with shipping lanes; and the possible lack of access to service the farms during adverse conditions, especially weather.

The submersible fish cage system was developed to reduce the reduction of the wave and current loadings on a fish cage. Several offshore submersible cages, such as Polar Circle, SUB flex, SADCO Shelf and Ocean Spar, which are operated by compressed air, have been developed[2]. In particular, several submersible Ocean Spar fish

cages(from the United States) have been deployed off Jeju and Geomun Islands in Korea. Experience has shown that these systems require two or more divers for their proper maintenance, however, which incurs substantial expense. Similar to traditional Korean surface cages, which allow harvesting, stock inventory and inspection without the need of divers, the development of a new system is needed to save operational costs.

Thus, an automatic submersible fish cage system which can move vertically within the water column via adjustments of the weight and buoyancy of the cage with an automatic control system has been developed. The submerging performances of the variable ballast tank for the cage and the submersible cage system have previously been reported by Kim et al.[3, 4]. In addition, Kim[5] conducted a numerical analysis on the motions of

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the submersible fish cage system.

A numerical model study was conducted to investigate the mooring tension acting on the mooring lines, grid lines and lower bridle lines of an automatic submersible cage system. Especially, the geometry of submerged bridle lines, which are set in the water to maintain the necessary angles and tension or strain on the lines, depends on the depth of the line below the surface(submerged midwater depth). The system was analyzed using a spread mooring configuration with four anchor legs. The numerical model used the Finite Element Analysis approach described in Tsukrov et al.[6, 7].

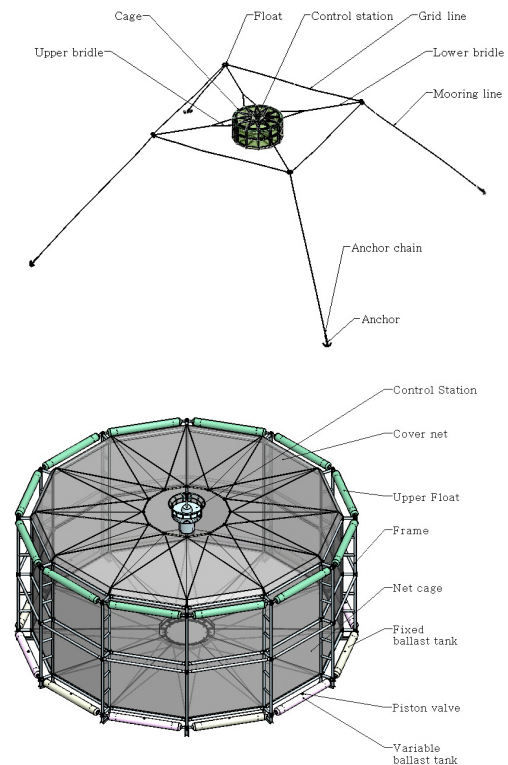
The objectives of this study were to determine the mooring tension response of the cage system at two locations within the water column. A numerical model was constructed, with simulations performed and responses obtained.

## 2. Materials and methods

### 2.1 Structure of submersible fish cage system

The automatic control system of the fish cage monitors environmental parameters, such as the wave height and wind speed, so the cage can be submerged in extreme sea states and then surfaced after the weather has passed[4]. Being able to remotely remove fish cages from the sea surface during extreme storm events will help to prevent damage. The fish cage system consisted of a 12-angled rigid frame, net cage, cover net, 12 upper floats, 12 tanks(for fixed and variable ballast), mooring lines, anchors, and a control station, as shown in **Figure 1**. In particular, the upper part of the frame contained a fixed flotation and the lower part both fixed ballast tanks and variable ballast tanks. The buoyancy of the variable ballast tanks was remotely adjustable. A surface control system operated a switch that enabled compressed air or seawater to enter the tanks to either submerge or surface the fish cage. The

control station was able to regulate both the inflow and outflow of air or seawater to and from the variable ballast tanks in response to the surface environmental conditions. The control station incorporated both wave and wind speed sensors, with a GPS and controller(computer included control program, A/D-D/A board, data acquisition components). The cage was fixed to the bottom using a spread mooring system, and was able to move vertically via the water column through a single grid square connected to the mooring system. The details of the cage and mooring system are provided in **Tables 1 and 2**.



**Figure 1:** General schematic of an automatic submersible fish cage system with a spread mooring system.

### 2.2 Numerical model

Numerical model simulations were performed

using a finite element computer program developed specifically for marine aquaculture applications, Aqua-FE. The program has been described in Tsukrov et al.[6, 7]. Wave and current loadings on the truss and buoy elements were introduced by utilizing the Morison equation[8]. The algorithm employs a nonlinear Lagrangian formulation to account for large displacements in the structural elements. In addition, the unconditionally stable Newmark direct integration scheme was adopted to solve the nonlinear equations of motion. The hydrodynamic forces on the structural elements were calculated using the Morison equation, modified to account for the relative motion between the structural element and the surrounding fluid, as described by Haritos and He[9].

The numerical model requires all of the geometric and material properties of the fish cage and mooring system to be prescribed. The parameters included the mass density, Young's modulus and cross sectional area of each element

**Table 1:** Details of the submersible fish cage system.

Component	Parameter	Value
Upper float	Material	Steel
	Diameter	560 mm
	Overall length	6240 mm
Fixed ballast tank	Material	Steel
	Diameter	560 mm
	Overall length	6240 mm
Variable ballast tank	Material	Steel
	Diameter	560 mm
	Overall length	6240 mm
Frame	Material	Steel
	Diameter	150 mm
Inner frame	Material	Steel
	Diameter	150 mm
Inner ring	Material	Steel
	Overall diameter	150 mm
Net	Material	Nylon
	Twine diameter	2.2 mm
	Bar length	60 mm
Support line	Material	Spectra
	Diameter	22 mm

component. Based on the information provided in **Tables 1 and 2**, the model representation of the components was determined, with the results provided in **Tables 3 and 4**.

**Table 2:** Mooring system design particulars of the submersible fish cage system.

Component	Parameter	Value
Anchor chain	Material	Steel
	Linear mass	70.6 kg/m
	Length	25 m
Mooring line	Material	Spectra
	Diameter	30 mm
	Length	100 m
Grid line	Material	Spectra
	Diameter	30 mm
	Length	76.6 m
Lower bridle line	Material	Spectra
	Diameter	30 mm
	Length	36.5 m
Upper bridle line	Material	Spectra
	Diameter	24 mm
	Length	10 m
Float	Diameter	1.0 m
	Mass	136 kg

Along with the material and geometric properties, the dimensions and configuration of the cage system were then used to build the numerical model. Model schematics are shown in **Figures 2 and 3**. Also shown in **Figure 2** is the orientation of the system to the wave and current environmental loading. Both **Figures 2 and 3** show the major components of the mooring system, including the grid lines, mooring lines, anchor chain and the upper and lower bridle lines.

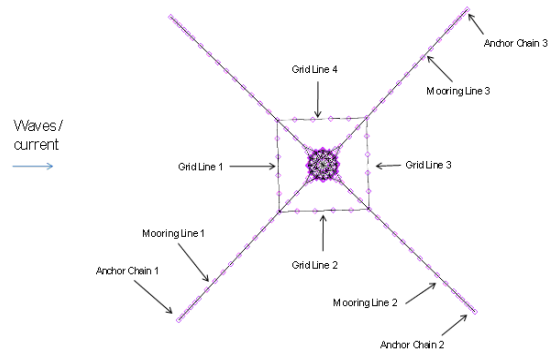
Simulations were performed with the cage at the surface and at a depth of 20 m, as shown in **Figure 4**. In both situations, the depth at the site was 50 m. The CPU model of computer used in the simulation was Dell PowerEdge 4600 configured with Intel 2.2GHz Xeon processor.

**Table 3:** Details of the submersible fish cage component model.

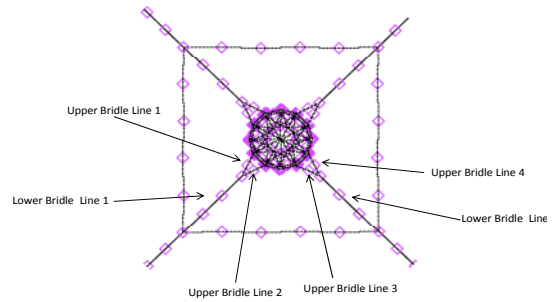
Component	Parameter	Value
Upper float	Density	235.2 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.209 m <sup>2</sup>
Fixed ballast tank	Density	1025 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.209 m <sup>2</sup>
Variable ballast tank	Density(surface)	1481 kg/m <sup>3</sup>
	Density(submerged)	1579 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.209 m <sup>2</sup>
Frame	Density	1638 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.0202 m <sup>2</sup>
Inner frame	Density	1534 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.0209 m <sup>2</sup>
Inner ring	Density	2559 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	0.012 m <sup>2</sup>
Net	Density	994 kg/m <sup>3</sup>
	Modulus of elasticity	1.02×10 <sup>11</sup> Pa
	Cross sectional area	3.801×10 <sup>-6</sup> m <sup>2</sup>
Stiffener	Density	1025 kg/m <sup>3</sup>
	Modulus of elasticity	2.5×10 <sup>11</sup> Pa
	Cross sectional area	5.00×10 <sup>-6</sup> m <sup>2</sup>
Support line	Density	994 kg/m <sup>3</sup>
	Modulus of elasticity	1.02×10 <sup>11</sup> Pa
	Cross sectional area	3.801×10 <sup>-4</sup> m <sup>2</sup>

**Table 4:** Details of mooring system components for the submersible fish cage.

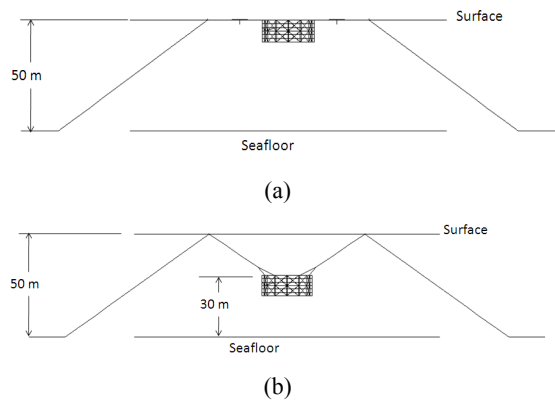
Component	Parameter	Value
Anchor chain	Density	7860 kg/m <sup>3</sup>
	Modulus of elasticity	2.0×10 <sup>11</sup> Pa
	Cross sectional area	8.982×10 <sup>-3</sup> m <sup>2</sup>
Mooring line	Density	1019 kg/m <sup>3</sup>
	Modulus of elasticity	1.11×10 <sup>11</sup> Pa
	Cross sectional area	7.069×10 <sup>-4</sup> m <sup>2</sup>
Grid line	Density	1019 kg/m <sup>3</sup>
	Modulus of elasticity	1.11×10 <sup>11</sup> Pa
	Cross sectional area	7.069×10 <sup>-4</sup> m <sup>2</sup>
Upper bridle line	Density	1019 kg/m <sup>3</sup>
	Modulus of elasticity	1.11×10 <sup>11</sup> Pa
	Cross sectional area	4.524×10 <sup>-4</sup> m <sup>2</sup>
Lower bridle line	Density	1019 kg/m <sup>3</sup>
	Modulus of elasticity	1.11×10 <sup>11</sup> Pa
	Cross sectional area	7.069×10 <sup>-4</sup> m <sup>2</sup>
Mooring float	Density	259.7 kg/m <sup>3</sup>
	Diameter	1.0 m



**Figure 2:** Overview of the numerical model system components for the cage system.



**Figure 3:** Bridle line details of the numerical model system components.



**Figure 4:** Side view of the fish cage at the surface(a) and submerged position(b).

### 2.3 Wave and current input parameters

The numerical model also required environmental forcing parameters. The first set of simulations was conducted with no wave and current load to verify static conditions. Once the static conditions had been verified, the forcing load, consisting of regular and random wave conditions both with and without a superimposed current of 1.0 m/s, was input to the model. Twelve regular wave load cases were prescribed, both with and without current. The details are provided in **Table 5**. In addition to the regular wave, random wave simulations were also performed. The model was forced with a JONSWAP(Joint North Sea Wave Project) type wave profile with a significant wave height of 9.51 m and peak period of 14.01 s, which were chosen according to a design wave condition of the southern sea in Korea over 20-year return periods[10]. For both the surface and submerged configurations, a total of 30 numerical model simulations were performed. The simulations were estimated approximately 6 hours for regular waves and 11 hours for random waves. In addition, the simulations were performed for duration of 500 seconds with time step of 0.005 seconds.

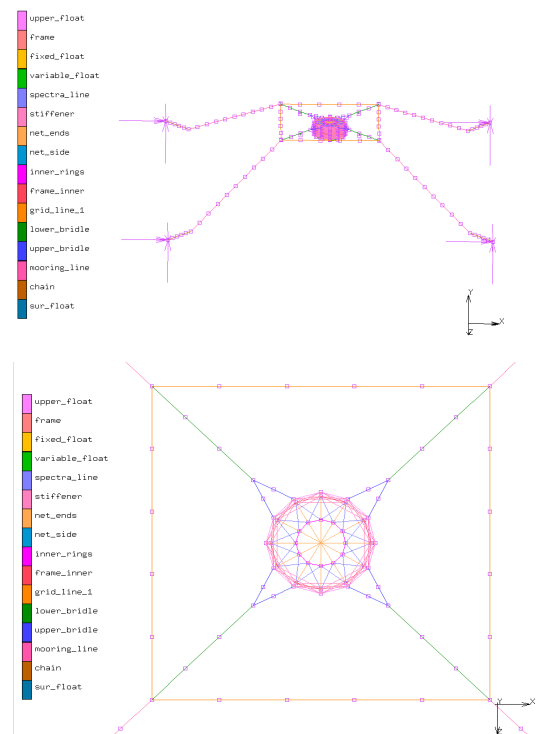
**Table 5:** Wave and current parameters for each regular wave load case.

Load case	Currents (m/s)	Wave heights (m)	Periods (s)
1	0	2.55	6.11
2	1.0	2.55	6.11
3	0	3.53	7.08
4	1.0	3.53	7.08
5	0	4.22	8.75
6	1.0	4.22	8.75
7	0	6.85	11.82
8	1.0	6.85	11.82
9	0	8.66	13.26
10	1.0	8.66	13.26
11	0	10.25	15.11
12	1.0	10.25	15.11

### 2.4 Data analysis

Regular wave tests were conducted, using numerical modeling methods, for the load cases provided in **Table 5**. The environmental forcing input into the numerical model also consisted of an irregular wave profile. To obtain an irregular wave profile in the numerical routine, a spectrum was decomposed into multiple frequency components. The spectrum chosen was a form of the JONSWAP spectrum[11]. The data processing was provided in a past study by Kim[12].

### 2.5 Cage motion response locations



**Figure 5:** Numerical model representation of the fish cage system.

It should be noted that these processing techniques work well for the simulations with only waves since the response can be assumed to be linear. In cases with a strong 1.0 m/s current, tensions can be considered a highly nonlinear response; therefore,

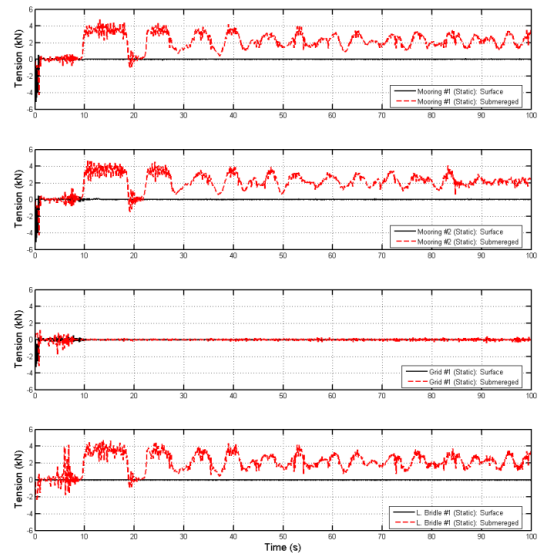
the results of these analysis techniques can be difficult to interpret. For this reason, the RAO(response amplitude operator) calculations were made for the load cases without the 1.0 m/s current.

For each simulation, tension response data sets were acquired to characterize the motion of the cage. Numerical model representations of the fish cage system are shown in **Figure 5**. Referring to **Figures 2** and **3**, the tension values from each of the anchor chain, mooring lines, grid lines and bridle lines were obtained. In this analysis, however, data sets from only mooring lines #1 and #2, grid line #1 and lower bridle line #1 were processed.

### 3. Results and discussion

The first set of numerical model simulations was performed without current and wave loading. In each of the simulations, the buoyancy of the cage created vertical motion as the mooring lines became stretched, pre-tensioning the components. Two static simulations were performed; in the first simulation, the cage was placed at the surface, with the depth of the rim set at 0 m. In the second simulation, the cage was placed at a depth of 20 m. The static tension results are shown in **Figure 6** and **Table 6**. The static tensions acting on the mooring lines of a submersible fish cage system with the submerged configuration were larger than with the surface configuration. Especially, the tension of the lower bridle line in the submerged position was 128.7 times larger than that in the surface position. Conversely, the tension of the grid line under the submerged condition was 2.3 times larger than that under the surface condition. The tension of bridle lines is critical for maintaining the underwater stability of the cage. In particular, in order to obtain more efficient bridle lines, it is necessary to maintain structural tension without compromising flexibility which depends on the geometry of the

lines and the submerging performance of the system. The bridle lines under the surface condition were a static structure, as shown in **Figure 4(a)**. The tension was maintained by the buoyancy of the cage and did not require any particular geometry. The bridle lines under the submerged condition, in comparison, were a dynamic geometric structure, as shown in **Figure 4(b)**. The structural tension of the submerged bridle lines, and their capacity to remain flexible in order to maintain their dynamic geometry, depends on the anchoring system, positive buoyancy of the mooring floats, and the angle of the bridle lines, which were established from the relationship between the length of the bridle lines and the submerged depth.



**Figure 6:** Tension of the static simulations. Note that at time = 0 seconds the cage is at its initial prescribed depth(surface: 0 m, submerged: 20 m).

The next set of simulations was performed with regular waves, both with and without a 1.0 m/s current(co-linear), for the surface and submerged models. The wave and current wave parameters are shown in **Figure 3**.

Data sets were obtained for the tension in the

mooring lines #1 and #2, grid line #1 and lower bridle line #1(as shown on **Figures 3** and **4**). The tensions in the selected mooring components were also examined. Processing programs were written to examine the time series tension data sets. The tension response is non-regular; therefore, computing linear RAOs was not practical. Instead, the maximum tension values for each of the data sets were determined. These values are provided in **Table 6**. The results of the tension transfer function for the regular wave simulations without a current are shown in **Figure 7**.

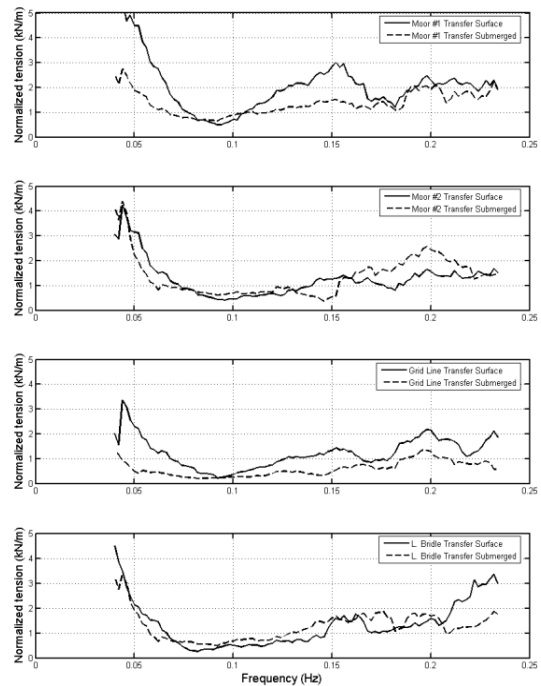
**Table 6:** Maximum mooring tensions of the submersible fish cage under regular waves without current and with a 1.0 m/s current.

(unit: N)

Load case	Position	Mooring line #1	Mooring line #2	Grid line #1	L. Bridle line #1
Static	Surface	493	474	516	37
	Submerged	4762	4732	1172	4762
1	Surface	9645	11490	6855	833
	Submerged	12884	11523	4791	15161
2	Surface	69231	8656	15737	64002
	Submerged	69488	6518	14215	60910
3	Surface	19733	9890	12219	13954
	Submerged	13980	11914	6060	17773
4	Surface	87089	8076	14589	76048
	Submerged	72035	8078	14056	62606
5	Surface	12663	9573	7400	5386
	Submerged	13819	12082	5762	11197
6	Surface	108850	9450	16057	95795
	Submerged	79116	6861	11467	66918
7	Surface	9955	12388	5813	10158
	Submerged	11139	13358	5879	11502
8	Surface	183990	8127	13613	169770
	Submerged	105370	8105	13224	90989
9	Surface	13430	9081	6807	11096
	Submerged	8263	13902	3721	9047
10	Surface	238380	6932	17393	222420
	Submerged	188050	7888	19706	171630
11	Surface	14553	8609	6527	16826
	Submerged	7490	11987	3390	8711
12	Surface	289850	7270	24132	271130
	Submerged	263570	7700	26362	242060

Once the static and regular wave tests had been completed, the random wave tests were conducted, with and without the 1.0 m/s superimposed current, for both the surface and submerged configurations. Simulations were performed using the JONSWAP wave spectrum, with and without the superimposed, co-linear current. Examples of the time series results for the simulations, with and without current, are shown in **Figure 8**. Next, using the time series results, the spectral representation of the wave input, the tension responses were calculated. The tension spectral results of the random wave simulations, without a current, are provided in **Figure 9**. The tension response in the mooring system was also investigated for both the surface and submerged configurations, both with and without a current. The significant tension response of the submersible fish cage system is shown in

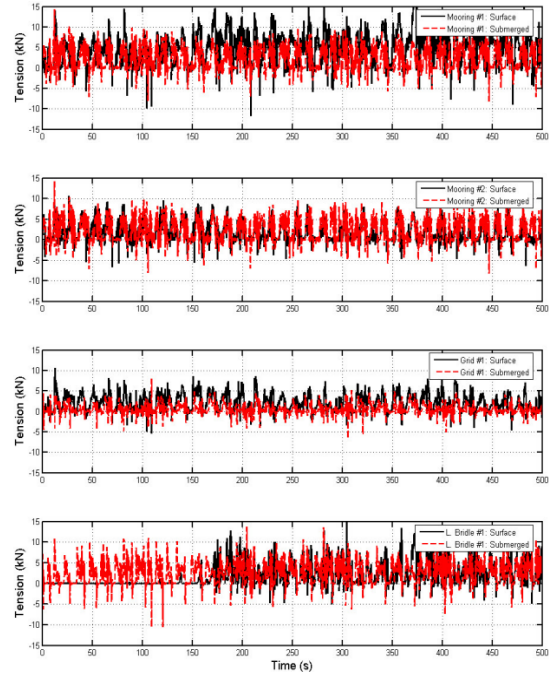
**Table 7.**



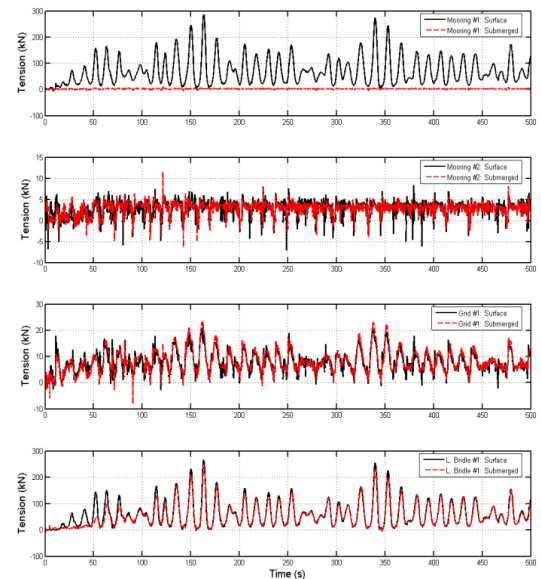
**Figure 7:** Tension transfer function results of the regular wave simulations without current.

The maximum values from the time series were identified, and provided in **Table 8**. The maximum mooring tensions of the cage system in irregular wave and a 1.0 m/s current were 286,450 N in mooring line #1 and 267,230 N in lower bridle line #1. In addition, the safety of the mooring lines listed in **Table 3** was checked on the basis of the tensile strength of the Spectra rope[13]. Assuming a safety factor of 1.25[14], the maximum tensions in **Table 8** were recalculated, and found to be 358,063 N in mooring line #1, 29,179 N in grid line #1 and 334,038 N in lower bridle line #1. The Spectra rope, with a diameter of 22mm, was confirmed to remain safe enough to withstand the hydrodynamic loadings to the cage under random wave and a 1.0 m/s current. The mooring tensions under the submerged condition were somewhat smaller than those under the surface condition with waves and currents.

When the cage is in a submerged state; however, compensation will be made for the slack in the mooring lines. Using only the variable ballast system, without the presence of taut mooring lines, could result in oscillations around the cage, potentially leading to an unstable system, which may be detrimental to the caged fish stock[4]. The presence of taut mooring lines could reduce cage oscillations. Therefore, the mooring lines containing the bridle connections to the cage always should be taut and relatively tensioned. In the presence of a relatively large tension from the bridle lines to the cage, a slightly negatively or positively buoyant state should be established as required and maintained using the variable ballast system to confer stability on the submersible cage system at the desired depth. Another approach would consist of collecting the slack portion of the mooring line, with cage based or anchor based mechanisms, to make the mooring lines taut when the cage reaches the desired depth, and to then bestow and maintain a slightly positive buoyant state.



(a)



(b)

**Figure 8:** Tension time series results acting on mooring lines of the cage in both the surface and submerged positions under random wave without current(a) and with a 1.0 m/s current(b).

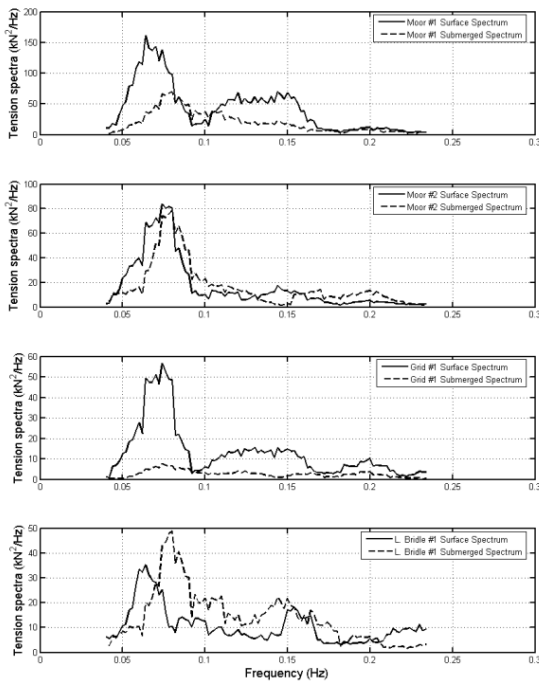


**Table 7:** Significant tension response of the submersible fish cage system under random wave without current. (unit: N)

Configuration	Mooring line #1	Mooring line #2	Grid line #1	L. Bridle line #1
Surface	11423.5	7238.5	6399.6	5741.2
Submerged	7775.3	7204.1	2862.1	6619.1

**Table 8:** Maximum tensions of submersible fish cage system under random wave without current and with a 1.0 m/s current. (unit: N)

Load case	Position	Mooring line #1	Mooring line #2	Grid line #1	L. Bridle line #1
Without current	Surface	19779	10586	10629	15020
	Submerged	14599	14227	8017	13634
1.0 m/s current	Surface	286450	8297	21110	267230
	Submerged	258640	11509	23343	237640



**Figure 9:** Tension spectral results of the random wave simulations without current.

#### 4. Conclusion

The results of the mooring tension response for

an automatic submersible fish cage system were obtained using the results from a numerical model. Simulations of the system were conducted using a Morison equation type model. The first set of tests was conducted with the fish cage system, with no force, to verify the static characteristics of the system. The next set of tests was performed with the numerical model in regular and irregular waves(JONSWAP spectrum), both with and without the 1.0 m/s current. The calculations for the tension on the mooring line, grid line and bridle line were then conducted. The static tensions acting on the mooring lines of the cage with the submerged configuration were larger than with the surface configuration. In addition, the static and dynamic tensions were very large in mooring line #1 and lower bridle line #1 compared with those in mooring line #2 and grid line #1. It was confirmed that the mooring lines provided in this study remained safe enough to withstand the hydrodynamic loadings to cage under waves and currents. The tension of bridle lines is critical for maintaining the underwater stability of the cage. Further verifications, using physical model tests, in-situ measurements and structural analysis, will be needed to more accurately analyze the hydrodynamic characteristics of the cage system so that the results of the study could be practically useful.

#### Acknowledgements

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