# Object Tracking in 3-D Space with Passive Acoustic Sensors using Particle Filter 

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#### Abstract

This paper considers the object tracking problem in three dimensional (3-D) space when the azimuth and elevation of the object are available from the passive acoustic sensor. The particle filtering technique can be directly applied to estimate the 3-D object location, but we propose to decompose the 3-D particle filter into the three planes' particle filters, which are individually designed for the 2-D bearings-only tracking problems. 2-D bearing information is derived from the azimuth and elevation of the object to be used for the 2-D particle filter. Two estimates of three planes' particle filters are selected based on the characterization of the acoustic sensor operation in a noisy environment. The Cramer-Rao Lower Bound of the proposed 2-D particle filter-based algorithm is derived and compared against the algorithm that is based on the direct 3-D particle filter.


Keywords: Acoustic sensors, bearings-only tracking, 3-D object tracking, particle filter, data fusion

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## 1. Introduction

Ldocating and tracking an object using passive sensors both indoor and outdoor have been widely used in numerous applications. For tracking an object via passive sensors, several approaches based on the time-delay estimation (TDE) methods and beamforming methods have been proposed. The TDE method estimates location based on the time delay of the arrival of signals at the receivers [1]. The beamforming method uses the frequency-averaged output power of a steered beamformer [2][3]. The TDE method and beamforming method determine the current source location using the data obtained only at the current time. Each method transforms the acoustic data to a spatial data so that the peak represents the source location in a deterministic way.

The estimation accuracy of these methods, however, is sensitive to noise-corrupted signals. In order to overcome the drawback of these methods, a state-space driven approach based on particle filtering has been proposed [4][5]. The particle filtering is an emerging powerful tool for sequential signal processing, especially for nonlinear and non-Gaussian problems [6][7][8][9]. Tracking with particle filters for source localization is formulated in [10], where the TDE and beamforming methods are revised for the new framework. In [10], sensors are positioned at specified locations with constant height to estimate an object's trajectory in two dimensional (2-D) space. The extension to 3-D space from the revised TDE and beamforming methods is difficult, and a large number of microphones are required to generate a new 2-D plane for the 3-D extension. In addition, mobility of the sensors cannot be supported due to their fixed positions. In order to overcome the mobility problem, Direction of Arrival (DOA) based bearings-only tracking has been widely used in many applications [11][12][13]. In [14], acoustic sensors with DOA are incorportated with visual sensors for better accurate estimation in 2-D plane.

In this paper, we analyze the tracking methods based on passive sensors only to achieve flexible and accurate 3-D tracking. Tracking in 3-D has been addressed by directly extending 2-D bearings-only tracking problem to 3-D problem [15][16]. Instead of directly extending traditional particle filtering algorithms for bearings-only tracking in 3-D space, we propose to decompose the 3-D particle filter into several simpler particle filters designed for 2-D bearings-only tracking problems. The decomposition and planes selection are based on the characterization of the acoustic sensor operation under noisy environment. We use the passive acoustic localizer model in [17], where the two angle components (azimuth angle $\theta$ and elevation angle $\phi$ ) between a sensor and an object are detected by the localizer. We compare the proposed approach with the directly extended bearings-only tracking method using Cramer-Rao Lower Bound.

The rest of this paper is organized as follows. Section 2 discusses the background and motivation, where we describe the sensor model and its noise characteristics. The general problem formulation and the dynamic model are also described. In Section 3, we describe the proposed method. Specifically, the Projected Planes Selection (PPS) method and planes combining scheme are discussed. Section 4 derives the Cramer-Rao Lower Bound (CRLB), and the simulation results are presented with CRLB in section 5. Finally, our contribution is summarized in Section 6.

## 2. Background and Problem Description

### 2.1 Problem Formulation for 3-D space Estimation

Consider an object's state vector $\mathbf{X}_{n}$, with discrete time instant $n \in\{1,2, \cdots\}$, evolving according to

$$
\begin{equation*}
\mathbf{X}_{n}=f_{n-1}\left(\mathbf{X}_{n-1}\right)+\mathbf{Q}_{n-1}, \tag{1}
\end{equation*}
$$

where $f_{n-1}$ is a nonlinear dynamic transition function on state vector $\mathbf{X}_{n-1}$ and $\mathbf{Q}_{n-1}$ is a noise process (not-necessarily Gaussian) sampled at time instant $n-1$. The measurements of the object state vector is expressed as

$$
\begin{equation*}
\mathbf{Z}_{n}=h_{n}\left(\mathbf{X}_{n}\right)+\mathbf{E}_{n}, \tag{2}
\end{equation*}
$$

where $h_{n}$ is a nonlinear and time-varying observation function of state vector $\mathbf{X}_{n}$ and $\mathbf{E}_{n}$ is the measurement error referred to as a measurement noise sequence which is an independent identically distributed (IID) noise process. Then, the prediction probability density function (pdf) is obtained as

$$
\begin{equation*}
p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{1: n-1}\right)=\int p\left(\mathbf{X}_{n} \mid \mathbf{X}_{n-1}\right) p\left(\mathbf{X}_{n-1} \mid \mathbf{Z}_{1: n-1}\right) \mathrm{d} \mathbf{X}_{n-1} \tag{3}
\end{equation*}
$$

where $\mathbf{Z}_{1: n}$ represents the sequence of measurements up to time instant $n$, and $p\left(\mathbf{X}_{n} \mid \mathbf{X}_{n-1}\right)$ is the state transition density with Markov process of order one related to $f_{n}(\cdot)$ and $\mathbf{Q}_{n-1}$ in (1) [19]. Note that $p\left(\mathbf{X}_{n-1} \mid \mathbf{Z}_{1: n-1}\right)$ is recursively obtained from previous time instants.

From the Bayes' rule, the estimation at the next time instant can be done as follow. The posterior pdf is obtained using the prediction pdf as

$$
\begin{equation*}
p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{1: n}\right)=\frac{p\left(\mathbf{Z}_{n} \mid \mathbf{X}_{n}\right) p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{1: n-1}\right)}{\int p\left(\mathbf{Z}_{n} \mid \mathbf{X}_{n}\right) p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{1: n-1}\right) \mathrm{d} \mathbf{X}_{n}} \tag{4}
\end{equation*}
$$

where $p\left(\mathbf{Z}_{n} \mid \mathbf{X}_{n}\right)$ is the likelihood or measurement density in (2) related to the measurement model $h_{n}(\cdot)$ and the noise process $\mathbf{E}_{n}$, and the denominator is the normalizing constant. Note that the measurement $\mathbf{Z}_{n}$ is used to modify the prior density in (3) to obtain the current posterior density in (4) [19].

In this paper, $\theta_{x y, n}$ and $\mathbf{Z}_{n}(x y)$ are interchangeably used as the projected angle measurement in the $x y$-plane. Similarly, $\theta_{y z, n}, \mathbf{Z}_{n}(y z), \theta_{z x, n}, \mathbf{Z}_{n}(z x)$ are for $y z$-plane and $z x$-plane, respectively. The state vectors of an object in 3-D space ( $\mathbf{X}_{n}$ ) and in 2-D planes, $\left(\mathbf{X}_{n}(x y), \mathbf{X}_{n}(y z), \mathbf{X}_{n}(z x)\right)$ are defined as

$$
\mathbf{X}_{n}=\left(\begin{array}{c}
x_{n}  \tag{5}\\
V_{n}^{x} \\
y_{n} \\
V_{n}^{y} \\
z_{n} \\
V_{n}^{z}
\end{array}\right), \mathbf{X}_{n}(x y)=\left(\begin{array}{c}
x_{n}(x y) \\
V_{n}^{x}(x y) \\
y_{n}(x y) \\
V_{n}^{y}(x y)
\end{array}\right), \mathbf{X}_{n}(y z)=\left(\begin{array}{c}
y_{n}(y z) \\
V_{n}^{y}(y z) \\
z_{n}(y z) \\
V_{n}^{z}(y z)
\end{array}\right) \text {, and } \mathbf{X}_{n}(z x)=\left(\begin{array}{c}
z_{n}(z x) \\
V_{n}^{z}(z x) \\
x_{n}(z x) \\
V_{n}^{x}(z x)
\end{array}\right) \text {, }
$$

where $\left\{x_{n}, y_{n}, z_{n}\right\}$ and $\left\{V_{n}^{x}, V_{n}^{y}, V_{n}^{z}\right\}$ are the true source location and the velocity in 3-D Cartesian coordinates at time instant $n .\left\{x_{n}(x y), y_{n}(x y)\right\}$ and $\left\{V_{n}^{x}(x y), V_{n}^{y}(x y)\right\}$ are the projected true source location and velocity on the $x y$-plane at time instant $n$; the same notation is applied for the $y z$ - and $z x$-planes. Note that $x_{n}(x y)$ and $x_{n}(z x)$ are estimated separately and $x_{n}$ is the finally fused value based on $x_{n}(x y)$ and $x_{n}(z x)$; the rest of components are applied in the same way. The three posterior pdf involving prediction probability density functions are given as

$$
\begin{align*}
p\left(\mathbf{X}_{n}(x y) \mid \mathbf{Z}_{1: n}(x y)\right) & =\frac{p\left(\mathbf{Z}_{n}(x y) \mid \mathbf{X}_{n}(x y)\right) p\left(\mathbf{X}_{n}(x y) \mid \mathbf{Z}_{1: n-1}(x y)\right)}{\int p\left(\mathbf{Z}_{n}(x y) \mid \mathbf{X}_{n}(x y)\right) p\left(\mathbf{X}_{n}(x y) \mid \mathbf{Z}_{1: n-1}(x y)\right) \mathrm{d} \mathbf{X}_{n}(x y)},  \tag{6}\\
p\left(\mathbf{X}_{n}(y z) \mid \mathbf{Z}_{1: n}(y z)\right) & =\frac{p\left(\mathbf{Z}_{n}(y z) \mid \mathbf{X}_{n}(y z)\right) p\left(\mathbf{X}_{n}(y z) \mid \mathbf{Z}_{1: n-1}(y z)\right)}{\int p\left(\mathbf{Z}_{n}(y z) \mid \mathbf{X}_{n}(y z)\right) p\left(\mathbf{X}_{n}(y z) \mid \mathbf{Z}_{1: n-1}(y z)\right) \mathrm{d} \mathbf{X}_{n}(y z)},  \tag{7}\\
p\left(\mathbf{X}_{n}(z x) \mid \mathbf{Z}_{1: n}(z x)\right) & =\frac{p\left(\mathbf{Z}_{n}(z x) \mid \mathbf{X}_{n}(z x)\right) p\left(\mathbf{X}_{n}(z x) \mid \mathbf{Z}_{1: n-1}(z x)\right)}{\int p\left(\mathbf{Z}_{n}(z x) \mid \mathbf{X}_{n}(z x)\right) p\left(\mathbf{X}_{n}(z x) \mid \mathbf{Z}_{1: n-1}(z x)\right) \mathrm{d} \mathbf{X}_{n}(z x)} . \tag{8}
\end{align*}
$$

Three 2-D estimates from the posterior pdfs given by equations (6), (7) and (8) can be used to estimate a single object's 3-D state vector. However, equations (6), (7) and (8) are only for the conceptual purpose, and they generally cannot be computed analytically except in special cases such as the linear Gaussian state space model. Instead of using those equations, for a nonlinear system, the particle filter can approximate the posterior pdf using a cloud of particles, and a sequential importance sampling (SIS) can be applied to perform the nonlinear filtering [9]. The particle filtering is further derived to the sequential importance resampling (SIR) algorithm, which chooses the candidates of importance density and performs the resampling at every time instant [20]. In this paper, we use the SIR particle filter that has a generic particle filtering algorithm for object tracking.

### 2.2 Dynamic Model and Observation Likelihood Function

Several dynamic models have been proposed to estimate the time-varying location and velocity. For the bearings-only tracking, three types of models are presented [13]. In the 2-D $x y$-plane, the constant velocity (CV) model, the clockwise coordinated turn (CT) model, and
the anti-clockwise coordinated turn (ACT) model are expressed by state transition matrices $\mathbf{F}_{n}^{(1)}, \mathbf{F}_{n}^{(2)}$ and $\mathbf{F}_{n}^{(3)}$, respectively as

$$
\mathbf{F}_{n}^{(1)}=\left(\begin{array}{cccc}
1 & T_{s} & 0 & 0  \tag{9}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & T_{s} \\
0 & 0 & 0 & 1
\end{array}\right) \text { and } \mathbf{F}_{n}^{(d)}=\left(\begin{array}{cccc}
1 & \sin \left(\mathfrak{R}_{n}^{(d)} T_{s}\right) / \mathfrak{R}_{n}^{(d)} & 0 & -\left(1-\cos \left(\mathfrak{R}_{n}^{(d)} T_{s}\right)\right) / \mathfrak{R}_{n}^{(d)} \\
0 & \left(1-\cos \left(\mathfrak{R}_{n}^{(d)} T_{s}\right)\right) / \mathfrak{R}_{n}^{(d)} & 1 & \sin \left(\mathfrak{R}_{n}^{(d)} T_{s}\right) / \mathfrak{R}_{n}^{(d)} \\
0 & \cos \left(\mathfrak{R}_{n}^{(d)} T_{s}\right) & 0 & -\sin \left(\mathfrak{R}_{n}^{(d)} T_{s}\right) \\
0 & \sin \left(\mathfrak{R}_{n}^{(d)} T_{s}\right) & 0 & \cos \left(\mathfrak{R}_{n}^{(d)} T_{s}\right)
\end{array}\right) \text {, }
$$

where $T_{s}$ is the sampling period, $d=2,3$ and $\mathfrak{R}_{n}^{(d)}$ is the mode-conditioned turning rate expressed as follows;

$$
\begin{equation*}
\mathfrak{R}_{n}^{(2)}=\frac{\alpha}{\sqrt{\left(V_{n}^{x}\right)^{2}+\left(V_{n}^{y}\right)^{2}}} \text { and } \mathfrak{R}_{n}^{(3)}=\frac{-\alpha}{\sqrt{\left(V_{n}^{x}\right)^{2}+\left(V_{n}^{y}\right)^{2}}}, \tag{10}
\end{equation*}
$$

where $\alpha$ is a constant for the rotated angle degree. In addition, the Constant Acceleration (CA) model in $x y$-plane is expressed as follows;

$$
\mathbf{F}_{n}^{(4)}=\left(\begin{array}{cccc}
1 & \left(A_{x} T_{s}^{2} / 2 V_{n-1}^{x}\right)+T_{s} & 0 & 0  \tag{11}\\
0 & \left(A_{x} T_{s} / V_{n-1}^{x}+1\right) & 0 & 0 \\
0 & 0 & 1 & \left(A_{y} T_{s}^{2} / 2 V_{n-1}^{y}\right)+T_{s} \\
0 & 0 & 0 & \left(A_{y} T_{s} / V_{n-1}^{y}\right)+1
\end{array}\right)
$$

where $A_{x}$ and $A_{y}$ denote accelerations in the $x y$-plane for $x$ - and $y$-directions, respectively. For the $y z$ - and $z x$-planes, $V^{x}$ and $V^{y}$ in (10), and $A_{x}$ and $A_{y}$ in (11) are replaced according to the object state directional components. Furthermore, the CA model becomes the CV model when the values of $A_{x}$ and $A_{y}$ are zero.

The SIR particle filter operates as follows [20]. After a dynamic model propagates the sets of $M$ particles for $\mathbf{X}_{n-1}^{(1: M)}(x y), \mathbf{X}_{n-1}^{(1: M)}(y z)$ and $\mathbf{X}_{n-1}^{(1: M)}(z x)$, new sets of particles $\mathbf{X}_{n}^{(1: M)}(x y)$, $\mathbf{X}_{n}^{(1: M)}(y z) \$$, and $\mathbf{X}_{n}^{(1: M)}(z x)$ are generated. Then, the observation likelihood functions

$$
\begin{equation*}
p\left(\mathbf{Z}_{n}(x y) \mid \mathbf{X}_{n}^{(1: M)}(x y)\right), p\left(\mathbf{Z}_{n}(y z) \mid \mathbf{X}_{n}^{(1: M)}(y z)\right), \text { and } p\left(\mathbf{Z}_{n}(z x) \mid \mathbf{X}_{n}^{(1: M)}(z x)\right) \tag{12}
\end{equation*}
$$

calculate the weights of the generated particles and estimate $\mathbf{X}_{n}(x y), \mathbf{X}_{n}(y z)$ and $\mathbf{X}_{n}(z x)$ respectively, through the resampling processes.

### 2.3 Noisy Measurement Characterization on Projected Planes



Fig. 1. Conversion of the original angles $\theta$ and $\phi$ to the projected angles $\theta_{x y}, \theta_{y z}$ and $\theta_{z x}$.

The 3-D localizer model and its implementation are described in [17], and it is based on the gradient flow to determine the DOA of the acoustic source. Fig. 1 illustrates the simplified angle conversion process. Based on the two measured angles, azimuth $\theta$ and elevation $\phi$, ( $0 \leq \theta<2 \pi, 0 \leq \phi<\pi$ ), three projected angles onto two dimensional (2-D) planes are derived; $\theta_{x y}, \theta_{y z}$ and $\theta_{z x}$. Each of these three angles can be used for 2-D tracking using the particle filter [18]. For example, $\theta_{x y}$ is used in $x y$-plane, $\theta_{y z}$ and $\theta_{z x}$ are used in $y z$-plane and $z x$-plane, respectively. The projected angles are derived and defined as

$$
\begin{equation*}
\theta_{x y}=\theta, \quad \theta_{y z}=\arctan \left(\frac{|\sec \theta|}{\tan \theta \tan \phi}\right)+\beta, \quad \theta_{z x}=\arctan \left(\frac{\tan \phi}{|\sec \theta|}\right)+\gamma, \tag{13}
\end{equation*}
$$

where

$$
\beta=\left\{\begin{array}{cc}
0, & \text { for } y \geq 0, z \geq 0  \tag{14}\\
\pi, & \text { for } y<0, \\
2 \pi, & \text { for } y \geq 0, z<0,
\end{array} \quad \gamma=\left\{\begin{array}{cc}
0, & \text { for } z \geq 0, x \geq 0 \\
\pi, & \text { for } x<0, \\
2 \pi, & \text { for } z \geq 0, x<0,
\end{array} \text { and } \sec \theta=\frac{1}{\cos \theta}\right.\right.
$$

We assume that each of the measurement errors of the original angles of $\theta$ and $\phi$ is and independent and identically distributed random sequence, respectively, and the two random sequences are independent. Also, we assume that the measurement errors are zero-mean with the same variance of $\sigma^{2}$. Then, the noisy measurements of $\theta$ and $\phi$ with the same error
variance of $\sigma^{2}$ are reflected to the projected plane angles $\theta_{x y}, \theta_{y z}$ and $\theta_{z x}$ with their own variances $\sigma_{x y}^{2}, \sigma_{y z}^{2}$, and $\sigma_{z x}^{2}$, respectively. Define the projected plane angles as

$$
\begin{equation*}
\theta_{x y, n}=\bar{\theta}_{x y, n}+e_{n}^{x y}, \quad \theta_{y z, n}=\bar{\theta}_{y z, n}+e_{n}^{y z}, \quad \theta_{z x, n}=\bar{\theta}_{z x, n}+e_{n}^{z x} \tag{15}
\end{equation*}
$$

where $\bar{\theta}_{\mathrm{P}, n}$ is the projected true angle, $e_{n}^{\mathrm{P}}$ is the angle error with the variance $\sigma_{\mathrm{P}}^{2}$ in P -plane at time instant $n$, and $\mathrm{P} \in\{x y, y z, z x\}$. Note that the original measurement error variance, $\sigma^{2}$, is differently projected to $\sigma_{x y}^{2}, \sigma_{y z}^{2}$ and $\sigma_{z x}^{2}$.


Fig. 2. Angle variances $\sigma_{y z}$ in a projected $y z$-plane according to $\theta$ and $\phi$. The originally measured
angle variances are 1. (x-axis: angle $\theta$ (degree), y-axis: variance)


Fig. 3. Angle variances $\sigma_{z x}$ in a projected $z x$-plane according to $\theta$ and $\phi$. The originally measured angle variances are 1 . ( x -axis: angle $\theta$ (degree), y-axis: variance)

The projected angles from the original measurements $\theta$ and $\phi$ are derived in (13), but it is difficult to derive the closed-form expression for their variances from the variances of the original measurement errors - it requires the variance of products and variance of nonlinear functions. The results from the Monte-Carlo simulation in Fig. 2 and Fig. 3 show the projected angles' variances when the original measurements' variances are one. Note that the projected measurement in $x y$-plane, $\theta_{x y}$ is the same as the original $\theta$; thus, $\sigma_{x y}^{2}$ is the same as $\sigma^{2}$. The projected variances in $y z$ - and $z x$-planes are functions of $\theta$ and $\phi$. In $y z$-plane, the elevation angles $\phi$ between $45^{\circ}$ and $135^{\circ}$ are projected with a smaller variance than the
original measurement variance of one. In addition, as the azimuth angle $\theta$ approaches $0^{\circ}$ or $180^{\circ}$, variance further decreases. For $z x$-plane, the other ranges of $\phi$ and $\theta$ are projected with a smaller variance than that of the original measurements.

## 3. Projected Planes Selection for Object Tracking in 3-D Space

### 3.1 Projected Planes Selection (PPS) Method

Planes Selection and Particles Generation: Instead of using the particle filter formulation with the direct 3-D state, the approach in this paper uses two of three possible 2-D particle filter formulations in order to estimate the 3-D state information. In the PPS method, we choose two planes with the smallest variance according to Fig. 2 and Fig. 3. Note that $x y$-plane is always chosen because the projected variance in $x y$-plane is the second best plane with the same variance as the originally measured azimuth angle $\theta$. The other $y z$ - or $z x$-plane is selected based on the measured angle. For example, when $\phi$ is measured between $45^{\circ}$ and $135^{\circ}$, the $y z$-plane is chosen. Otherwise, the $z x$-plane is chosen.

Once the two planes are selected, the two 2-D particle filters estimate the states separately. While the particle filters in the chosen planes estimate the state vectors, the particle filter in the other remained plane awaits for the selection. When the measured angles become close to the range where the projected measurement variance in the remained plane becomes less than the originally measured variance, the selected plane is switched.

There is always one redundant component that appears in both planes (i.e., $y$-component appears in $x y$-and $y z$-planes). As two particle filters are estimating the states separately, the redundant directional state from two particle filters may differ. For example, as discussed in (5), the intermediate 2-D object state vectors are given as $\left(x_{n}(x y), V_{n}^{x}(x y), y_{n}(x y), V_{n}^{y}(x y)\right)^{T}$ from the $x y$-plane particle filter and $\left(y_{n}(y z), V_{n}^{y}(y z), z_{n}(y z), V_{n}^{z}(y z)\right)^{T}$ from the $y z$-plane particle filter. Both $y_{n}(x y)$ and $y_{n}(y z)$ represent $y$ directional position information, but the two values are different. Therefore, a combining method should be considered in order to get one final 3-D object state vector $\mathbf{X}_{n}$.

Redundancy Consideration in Combining Method: There are two ways to combine the two estimates of the state vectors of the $y$-direction's state vectors when $x y$-and $y z$-planes are selected; the planes weighted combining and the equal weight combining. In the planes weighted combining method, the two estimates are weighted according to the sum of weights of unnormalized particles in each plane's particle filter. This method is derived from the multiple particle filtering method [21], and extended to be combined into a final value with respect to the redundant state. Since a particle represents a point mass of the probability density, the sum of weights of unnormalized particles can be used in evaluating how the expected state is close to the true state [18][21][22]. The final 3-D object state vector $\mathbf{X}_{n}$ with the planes weighted combining method is obtained by

$$
\mathbf{X}_{n}=\left(\begin{array}{cc}
1 & 0  \tag{16}\\
0 & 1 \\
0 & 0 \\
0 & 0 \\
0 & 0 \\
0 & 0
\end{array}\right) \mathbf{X}_{n}(x \mid x y z)+\left(\begin{array}{cc}
0 & 0 \\
0 & 0 \\
1 & 0 \\
0 & 1 \\
0 & 0 \\
0 & 0
\end{array}\right) \mathbf{X}_{n}(y \mid x y z)+\left(\begin{array}{cc}
0 & 0 \\
0 & 0 \\
0 & 0 \\
0 & 0 \\
1 & 0 \\
0 & 1
\end{array}\right) \mathbf{X}_{n}(z \mid x y z)
$$

where $\mathbf{X}_{n}(x \mid x y z), \mathbf{X}_{n}(y \mid x y z)$ and $\mathbf{X}_{n}(z \mid x y z)$ are final 3-D estimated vectors with respect to each directional component representing $\left[x_{n}, V_{n}^{x}\right]^{T},\left[y_{n}, V_{n}^{y}\right]^{T}$ and $\left[z_{n}, V_{n}^{z}\right]^{T}$, respectively. When the $x y$-and $y z$-planes are selected

$$
\begin{array}{r}
\mathbf{X}_{n}(y \mid x y z)=\frac{\mathbf{X}_{n}(y \mid x y) \sum_{i=1}^{M} w_{n}^{(i)}(x y)+\mathbf{X}_{n}(y \mid y z) \sum_{i=1}^{M} w_{n}^{(i)}(y z)}{\sum_{i=1}^{M} w_{n}^{(i)}(x y)+\sum_{i=1}^{M} w_{n}^{(i)}(y z)}, \\
\mathbf{X}_{n}(x \mid x y z)=\mathbf{X}_{n}(x \mid x y), \text { and } \mathbf{X}_{n}(z \mid x y z)=\mathbf{X}_{n}(z \mid y z), \tag{18}
\end{array}
$$

where $\mathbf{X}_{n}(x \mid x y)$ and $\mathbf{X}_{n}(y \mid x y)$ represent the $x$ and $y$ directional 2-D state vectors in $x y$ -plane, respectively. $\mathbf{X}_{n}(y \mid y z)$ and $\mathbf{X}_{n}(z \mid y z)$ represent the $y$ and $z$ directional 2-D state vectors in $y z$-plane. $w_{n}^{(i)}(x y)$ and $w_{n}^{(i)}(y z)$ are the $i$-th particle's weight of the particle filter for $x y$ - and $y z$-plane at time instant $n$, and $M$ represents the number of particles for each particle filter. Thus, the redundant $y$ directional states are combined as in (17), where the weighting factors are $\sum_{i=1}^{M} w_{n}^{(i)}(x y)$ to $x y$-plane and $\sum_{i=1}^{M} w_{n}^{(i)}(y z)$ to $y z$-plane.

For the equal weight combining method, as it simply takes an average value, the redundant component $y$ in (17) is replaced by

$$
\begin{equation*}
\mathbf{X}_{n}(y \mid x y z)=\frac{\mathbf{X}_{n}(y \mid x y)+\mathbf{X}_{n}(y \mid y z)}{2} \tag{19}
\end{equation*}
$$

### 3.2 Discussion

It has been assumed that the nonlinear dynamic transition function $f_{n}$ is known as the state transition matrix $\mathbf{F}_{n}$ - as the particle filter is a model-based approach. If the dynamic model $f_{n}$ changes in the middle of tracking, then the estimation from the particle filter can diverge. Divergence means that a predicted state and a true state continuously become more distant due to the unmatched model of a particle filter. Also, if the state of the unmatched model lasts longer, then the estimation may not recover even after recovering the model. The planes
weighted combining method can discard the estimation from the plane with negligible sum of weights of unnormalized particles based on the likelihood function $p\left(\mathbf{Z}_{n} \mid \mathbf{X}_{n}^{(1: M)}\right)$, and thus prevents estimation deviation. The equal weight combining and the planes weighted combining methods have similar tracking performance if all selected plane-particle filters show good tracking performances. However, when the tracking performance of one of the two particle filters deteriorates, the planes weighted combining method shows better performance.


Fig. 4. Poor tracking in the yz-plane without combining methods. (Number of particles : 1,000).


Fig. 5. Modified tracking performance with combining methods (Number of particles : 1,000) (a) Equal weight combining method (b) Weighted combining method.

Tracking performance is shown in Fig. 4 and Fig. 5, where the particle filter in $y z$-plane results in a deviated estimation. Since the $x y$ - and $y z$-planes are selected, the $y$ direction's state estimates are combined. Fig. 4 shows an example of tracking deviation in the $y z$-plane due to the unmatched model or a particle filter's performance degradation. Fig. 5 shows a final estimation after applying two combining methods. Especially in Fig. 5(b), it is shown that the planes weighted combining method maintains the object tracking by considering the contribution of the sum of weights of unnormalized particles from different planes. PPS Versus Direct 2-D Method: The 3-D object state model directly uses two original measurements and a cone shape likelihood function for assigning 3-D distributed particle
weights [23]. The direct 3-D Method uses the two original measurements with $\sigma^{2}$, while the PPS method uses two projected measurements with $\sigma_{x y}^{2}$ and $\min \left(\sigma_{y z}^{2}, \sigma_{z x}^{2}\right)$. Fig. 6 shows the sum of weights of unnormalized particles corresponding to the selected $y z$-plane and the direct 3-D model. It is shown that the selected plane is less sensitive to measurement noise than the direct 3-D model; thus, the unnormalized particles weight-sums of PPS method is larger than those of the direct 3-D Method. In addition, the direct 3-D Method cannot achieve redundancy, and thus there is no opportunity to avoid performance degradation when a particle filter has poor performance. The performances are compared according to the Cramer-Rao Lower bound (CRLB) in Section 4.


Fig. 6. Comparison between the selected $y z$ - planes and 3-D space: unnormalized particles weight-sums according to the variances of original measurements (The number of particles: 100).

## 4. Cramer-Rao Lower Bound Derivation and Performance Analysis

The Cramer-Rao Lower Bound (CRLB) has been widely used as a reference in evaluating an estimator by representing the minimum covariance of the estimated states that an unbiased estimator can achieve. For the object tracking problem with bearings-only measurements, the CRLB is investigated in [24], and similar approaches are taken in this paper. As in [24], we assume that the process noise $\mathbf{Q}_{n}$ is zero and the dynamic models are fixed and known; otherwise, the derivation is intractable. The covariance matrix of the state estimate $\hat{\mathbf{X}}_{n}$ is given as follows

$$
\begin{equation*}
\mathbf{C}_{n}=E\left[\left(\hat{\mathbf{X}}_{n}-\mathbf{X}_{n}\right)\left(\hat{\mathbf{X}}_{n}-\mathbf{X}_{n}\right)^{T}\right] \geq \mathbf{J}_{n}^{-1} \tag{20}
\end{equation*}
$$

where $\mathbf{J}_{n}$ is the information matrix, and it is defined as

$$
\begin{equation*}
\mathbf{J}_{n}=E\left\{\left[\nabla_{\mathbf{x}_{n}} \log p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{n}\right)\right]\left[\nabla_{\mathbf{X}_{n}} \log p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{n}\right)\right]^{T}\right\} \tag{21}
\end{equation*}
$$

where $\nabla_{\mathbf{X}_{n}}$ denotes the gradient operator with respect to the state vector $\mathbf{X}_{n}$, and $p\left(\mathbf{X}_{n} \mid \mathbf{Z}_{n}\right)$ is the conditional pdf of state $\mathbf{X}_{n}$ given the observation $\mathbf{Z}_{n}$. Note that the inequality of the square matrix in (20) means that matrix $\mathbf{C}_{n}-\mathbf{J}_{n}^{-1}$ is positive definite. The CRLB's of the components in the state vector $\mathbf{X}_{n}$ is the lower bound of its variance, and it is the diagonal elements of the inverse matrix of $\mathbf{J}_{n}$ [25].

We do not directly obtain the information matrix as in (21), but it is derived recursively as follows. In the absence of process noise, the evolution of state vector is deterministic, and it is given as [19][26]

$$
\begin{equation*}
\mathbf{J}_{n+1}=\left[\mathbf{F}_{n}^{-1}\right]^{T} \mathbf{J}_{n} \mathbf{F}_{n}^{-1}+\mathbf{H}_{n+1}^{T} \mathbf{R}_{n+1}^{-1} \mathbf{H}_{n+1}, \tag{22}
\end{equation*}
$$

where $\mathbf{F}_{n}$ is the state transition matrix that represents CV or CA as shown in (10) and (11), respectively, $\mathbf{R}_{n+1}$ is the covariance matrix of the bearing measurements and $\mathbf{H}_{n}$ is the gradient component of a measurement function $h_{n} . \mathbf{H}_{n}$ is referred to as the Jacobian of $h_{n}$, and it is given as follows

$$
\begin{equation*}
\mathbf{H}_{n}=\left(\nabla_{\mathbf{X}_{n}} h_{n}^{T}\left(\mathbf{X}_{n}\right)\right)^{T} . \tag{23}
\end{equation*}
$$

In the following subsections, the CRLB's of the PPS method are compared against the direct 3-D Method. The dynamic model of interest is assumed to be CV in the $x$-axis, CA with $A_{y}$ and $A_{z}$ in the $y$ and $z$-axis.

### 4.1 CRLB Derivation based on the PPS Method

In the PPS method, two information matrices in (22) are generated for each selected plane. For clear notation, we put the plane type P as $\mathbf{J}_{n}^{\mathrm{P}}$, which represents $\mathbf{J}_{n}^{x y}, \mathbf{J}_{n}^{y z}$ or $\mathbf{J}_{n}^{z x}$. Similarly, the transition matrix, measurement variance and Jacobian of $h_{n}$ are also denoted as $\mathbf{F}_{n}^{\mathrm{P}}, \mathbf{R}_{n}^{\mathrm{P}}$ and $\mathbf{H}_{n}^{\mathrm{P}}$, respectively for $\mathrm{P} \in\{x y, y z, z x\}$. From (9) and (11), transition matrices $\mathbf{F}_{n}^{\mathrm{P}}$ 's are derived as

$$
\mathbf{F}_{n}^{x y}=\left(\begin{array}{cccc}
1 & T_{s} & 0 & 0  \tag{24}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & A_{y} T_{s}^{2} / 2 V_{n-1}^{y}+T_{s} \\
0 & 0 & 0 & A_{y} T_{s} / V_{n-1}^{y}+1
\end{array}\right), \quad \mathbf{F}_{n}^{z x}=\left(\begin{array}{cccc}
1 & A_{z} T_{s}^{2} / 2 V_{n-1}^{z}+T_{s} & 0 & 0 \\
0 & A_{z} T_{s} / V_{n-1}^{z}+1 & 0 & 0 \\
0 & 0 & 1 & T_{s} \\
0 & 0 & 0 & 1
\end{array}\right),
$$

and

$$
\mathbf{F}_{n}^{y z}=\left(\begin{array}{cccc}
1 & A_{y} T_{s}^{2} / 2 V_{n-1}^{y}+T_{s} & 0 & 0  \tag{25}\\
0 & A_{y} T_{s} / V_{n-1}^{y}+1 & 0 & 0 \\
0 & 0 & 1 & A_{z} T_{s}^{2} / 2 V_{n-1}^{z}+T_{s} \\
0 & 0 & 0 & A_{z} T_{s} / V_{n-1}^{z}+1
\end{array}\right)
$$

In the PPS method, the covariance matrix of measurement, $\mathbf{R}_{n}^{\mathrm{P}}$ becomes $\sigma_{x y}^{2}, \sigma_{y z}^{2}$ or $\sigma_{z x}^{2}$, which is the variance of a single (projected) bearing measurement in the projected plane $x y$, $y x$ or $z x$-plane, respectively. The performance of the PPS method is mainly enhanced by taking only the measurement with smaller variance. According to Fig. 2 and Fig. 3, the raw bearings, $\theta$ and $\phi$, are projected onto the three planes with the different angle variances according to the object's position.

For Jacobians in the $x y$-plane, $\mathbf{H}_{n+1}^{x y}$ is derived from

$$
\begin{equation*}
h_{n+1}^{T}\left(\mathbf{X}_{n+1}(x y)\right)=\theta_{x y}\left(\mathbf{X}_{n+1}(x y)\right)=\arctan \left(\frac{y_{n+1}}{x_{n+1}}\right) \tag{26}
\end{equation*}
$$

and

$$
\begin{gather*}
\frac{\partial}{\partial x_{n+1}} \arctan \left(\frac{y_{n+1}}{x_{n+1}}\right)=\frac{-y_{n+1}}{x_{n+1}^{2}+y_{n+1}^{2}}, \frac{\partial}{\partial y_{n+1}} \arctan \left(\frac{y_{n+1}}{x_{n+1}}\right)=\frac{x_{n+1}}{x_{n+1}^{2}+y_{n+1}^{2},} \\
\frac{\partial}{\partial V_{n+1}^{x}} \arctan \left(\frac{y_{n+1}}{x_{n+1}}\right)=\frac{\partial}{\partial V_{n+1}^{y}} \arctan \left(\frac{y_{n+1}}{x_{n+1}}\right)=0 . \tag{27}
\end{gather*}
$$

Then,

$$
\begin{equation*}
\mathbf{H}_{n+1}^{x y}=\left(\nabla_{\mathbf{x}_{n+1}(x y)} h_{n+1}^{T}\left(\mathbf{X}_{n+1}(x y)\right)\right)^{T}=\left(\frac{-y_{n+1}}{x_{n+1}^{2}+y_{n+1}^{2}}, 0, \frac{x_{n+1}}{x_{n+1}^{2}+y_{n+1}^{2}}, 0\right), \tag{28}
\end{equation*}
$$

and by the same way, the Jacobians for $y z$ - and $z x$-planes are derived as follows

$$
\begin{equation*}
\mathbf{H}_{n+1}^{y z}=\left(\frac{-z_{n+1}}{y_{n+1}^{2}+z_{n+1}^{2}}, 0, \frac{y_{n+1}}{y_{n+1}^{2}+z_{n+1}^{2}}, 0\right) \text { and } \mathbf{H}_{n+1}^{z x}=\left(\frac{-x_{n+1}}{x_{n+1}^{2}+z_{n+1}^{2}}, 0, \frac{z_{n+1}}{x_{n+1}^{2}+z_{n+1}^{2}}, 0\right) \tag{29}
\end{equation*}
$$

For the PPS method with a single sensor, the information matrix $\mathbf{J}_{n}$ given in (22) can be recursively obtained using equations from (24) to (38) except the initial condition. We can assume that $\mathbf{J}_{0}$ is a zero matrix -- no information at all at the beginning of the estimation.

### 4.2 CRLB Derivation based on the Direct 3-D Method

In the direct 3-D method, the information matrix $\mathbf{J}_{n}$ is expressed as a $6 \times 6$ matrix, and the lower bound is directly obtained from (22) with the extension of 2-D state vector based matrices. The state transition matrix is expressed as

$$
\mathbf{F}_{n}=\left(\begin{array}{cccccc}
1 & T_{s} & 0 & 0 & 0 & 0  \tag{30}\\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & A_{y} T_{s}^{2} / 2 V_{n-1}^{y}+T_{s} & 0 & 0 \\
0 & 0 & 0 & A_{y} T_{s} / V_{n-1}^{y}+1 & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & A_{z} T_{s}^{2} / 2 V_{n-1}^{z}+T_{s} \\
0 & 0 & 0 & 0 & 0 & A_{z} T_{s} / V_{n-1}^{z}+1
\end{array}\right) .
$$

## 5. Analysis and Simulation

In this section, the PPS and direct 3D methods are compared in terms of their simulation results and CRLB's. As the proposed method selects the smallest measurement variance, the covariance $\mathbf{R}_{n}$ plays an important role for the lower bound. The minimum covariances obtained via the PPS method minimize the lower bound - the PPS method flexibly chooses planes with the smallest variances. Several scenarios are considered for performance comparison. Scenario 1 and 2 show the single sensor based plane selection according to $\phi$. Scenario 3 shows the changes of the plane selection from $x y$ - and $y z$-planes to $x y$ - and $z x$ -planes according to $\phi$. In all scenarios, the sensor is measuring $\theta$ and $\phi$ with the interval of 0.1 second and the variances of the measurements are both 3 .

### 5.1 Scenario 1

In this scenario, an object is moving in the range of $\phi$ being between $45.36^{\circ}$ and $76.74^{\circ}$ as well as in the range of $\theta$ being between $45.00^{\circ}$ and $49.04^{\circ}$. More specifically, a single sensor is placed in the origin ( $0 m, 0 m, 0 m$ ), and the initial position of the object is ( $3 m, 3 m, 1 m$ ) with an initial velocity of $(1 \mathrm{~m} / \mathrm{s}, 1 \mathrm{~m} / \mathrm{s}, 1 \mathrm{~m} / \mathrm{s})$. The observed object is moving in CV in the $x$ -direction, in CA in the $y$ and $z$ directions, with $0.1 \mathrm{~m} / \mathrm{s}^{2}$ and $0.5 \mathrm{~m} / \mathrm{s}^{2}$, respectively. Since the $\phi$ is measured in the range between $45.36^{\circ}$ and $76.74^{\circ}$, the $x y$ - and $y z$-planes are selected. In addition, the initial object state is given.

### 5.2 Scenario 2

In this scenario, an object is moving in the range of $\phi$ being between $25.24^{\circ}$ and $36.26^{\circ}$ as well as in the range of $\theta$ being between $45.00^{\circ}$ and $50.28^{\circ}$. Similar to scenario 1 , a single sensor is placed at the origin $(0 m, 0 m, 0 m)$ with the same initial object velocity and movement. The initial object position is ( $1 \mathrm{~m}, 1 \mathrm{~m}, 3 \mathrm{~m}$ ). Since $\phi$ is in the range between $25.24^{\circ}$ and $36.26^{\circ}$, the $x y$-and $z x$-planes are selected. Also, the initial object state is given.

### 5.3 Scenario 3

In this scenario, an object moves in the range of $\phi$ being between $28.07^{\circ}$ and $48.24^{\circ}$ crossing $45^{\circ}$. The sensor is placed at the origin $(0 m, 0 m, 0 m)$, and the initial position of the object is $(2 m, 1 m, 2 m)$ with an initial velocity of $(0.3 m / s, 0.3 m / s, 0.3 m / s)$. Similar to previous scenarios, the observed object is moving in CV in the $x$-direction, in CA in the $y$ - and $z$ -directions, with $0.1 \mathrm{~m} / s^{2}$ and $0.5 \mathrm{~m} / s^{2}$, respectively. Since $\phi$ of the first 13 time instants is measured between $48.24^{\circ}$ and $45.42^{\circ}$, the $x y$ - and $y z$-planes are selected. In the last 37 time instants, $x y$ - and $z x$-planes are selected since $\phi$ is measured between $28.07^{\circ}$ and $44.96^{\circ}$.


Fig. 7. Scenario 1: Selected $x y$ - and $y z$-planes based on PPS show better performance.


Fig. 8. Scenario 2: Selected $x y$ - and $z x$-planes based on PPS show better performance.

### 5.4 Results

Fig. 7, Fig. 8 and Fig. 9 represent the lower bound and RMSE in each direction based on scenario 1, 2 and 3, respectively. In Fig. 7, selecting the $y z$-plane with $x y$-plane and in Fig. 8,
selecting the $z x$-plane with $x y$-plane show good performance, which proves that the PPS method is a good estimator. Note that all boundaries are presented for comparing the selection of other planes. In addition, a dynamic plane selection is shown in simulated in Fig. 9. Also, note that PF we use is known as the best estimator in nonlinear and non-Gaussian tracking problem. Under the condition with linear and Gaussian tracking problem, Kalman filter with PPS method will provide the optimum estimation in 3-D space.


Fig. 9. Scenario 3: The first 13 time instants $x y$ - and $y z$-planes are selected, and the last 37 time instants, the $x y$ - and $z x$-planes are selected. For the performance comparison between PPS and direct 3D method, the certain section in CRLB is enlarged (A and B).

### 5.5 Computational Complexity Comparison

Fig. 10 shows the simplified overall flows of PPS and direct method, where PPS performs multiple 2-D particle filters, and direct method performs single 3-D particle filter. In the case of sphere density with radius $r$, direct method ideally requires $\pi r^{3}$ particles wile PPS method requires $\pi r^{2}$ particles. It means that direct method requires $r^{\frac{3}{2}}$ time particles and its corresponding computational resources. Thus, under dual processors available, PPS method has $r^{\frac{3}{2}}$ time less complexity.


Fig. 10 Simplified algorithmic flows of PPS and direct method.

## 6. Conclusions

We have proposed an object tracking algorithm in 3-D space with a passive acoustic sensor. The particle filtering technique used in the 2-D bearings-only tracking problem has been applied to the 3-D space. 3-D space is decomposed into 2-D planes, and by exploiting the fact that the noisy measurements of the acoustic sensor differ on the projected planes, we have proved the effectiveness of the plane selection based on the characteristics. We have shown that the particle filtering with the proposed plane selection is more flexible than the direct 3-D method where the proposed method can be easily extended to multiple sensor particle filtering. We have also analyzed the performance of the proposed method using the Cramer-Rao Lower Bound (CRLB) and the theoretical lower bound, and the simulation results are compared to those of the direct 3-D method. We have shown that the proposed method outperforms the direct 3-D method.

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