

# An Adaptive UPFC Based Stabilizer for Damping of Low Frequency Oscillation

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**Abstract** – Unified power flow controller (UPFC) is the most reliable device in the FACTS concept. It has the ability to adjust all three control parameters effective in power flow and voltage stability. In this paper, a linearized model of a power system installed with a UPFC has been presented. UPFC has four control loops that by adding an extra signal to one of them, increases dynamic stability and load angle oscillations are damped. In this paper, after open loop eigenvalue (electro mechanical mode) calculations, state-space equations have been used to design damping controller and it has been considered to influence active and reactive power flow durations as the input of damping controller, in addition to the common speed duration of synchronous generators as input damper signal. To increase stability, further Lead-Lag and LQR controllers, a novel on-line adaptive controller has been used analytically to identify power system parameters. Closed-loop calculations of the electro mechanical mode verify the improvement of system pole placement after controller designing. Suitable operation of adaptive controller to decrease rotor speed oscillations against input mechanical torque disturbances is confirmed by the simulation results.

**Keywords:** UPFC, State-space equations, Dynamic stability improvement, LQR, Adaptive controller

## 1. Introduction

Power transfer in an integrated power system is constrained by transient stability, voltage stability and small signal stability. These constraints limit a full utilization of available transmission corridors. The flexible AC transmission system (FACTS) is the technology that provides the needed corrections of the transmission functionality in order to fully utilize the existing transmission facilities and hence, minimizing the gap between the stability limit and thermal limit [1]. Unified power flow controller (UPFC) is one of the FACTS devices which can control power system parameters such as terminal voltage, line impedance and phase angle [2]. Therefore, it can be used not only for power flow control, but also for power system control.

Recently, researchers have presented dynamic models of UPFC in order to design a suitable controller for power flow, voltage and damping controls [9]-[13]. Wang has presented a modified linearized Heffron-Phillips model of a power system installed with a UPFC [1], [3], [7] and [11]. He has addressed the basic issues pertaining to the design of UPFC damping controllers, i.e., the selection of robust operating conditions for designing damping controllers; and the choice of parameters of the UPFC (such as  $m_E$ ,  $m_B$ ,  $\delta_E$  and  $\delta_B$ ) to be modulated to achieve the desired damping. Wang has not presented a systematic approach to design

the damping controllers. Furthermore, no effort seems to have been made to identify the most suitable UPFC control parameters, in order to arrive at a robust damping controller and has not used the deviation of active and reactive powers,  $\Delta P_e$  and  $\Delta Q_e$  as the input control signals. The  $\Delta P_e$  and  $\Delta Q_e$  signals can be used for oscillation damping as input signals due to their improved convenience over  $\Delta\omega$  specially in states where UPFC is set too far from the generator.

Abido has used the PSO control to design a controller and this manner not only is an off-line procedure, but also depends strongly on the selection of the primary conditions of control systems [4] and [6].

An adaptive controller is able to control a nonlinear system with fast changing dynamics, since the dynamics of a power system are continually identified by a model. Advantages of on-line adaptive controllers over conventional controllers are that they are able to adapt to changes in system operating conditions automatically, unlike conventional controllers whose performance is degraded by such changes and require re-tuning in order to provide the desired performance [9]. In [14], an adaptive based controller for STATCOM has been provided and has been used as a VAR compensator in [15]. In this paper, the dynamic equations of  $\Delta Q_e$  have been calculated and the deviations signals of active and reactive power and their sum, and also rotor speed deviation as input control signals for Lead-Lag controllers have been used and their results have been compared with each other. In addition, it has examined the relative effectiveness of modulating alternative UPFC control parameters  $m_E$ ,  $m_B$ ,  $\delta_E$  and  $\delta_B$  for damping power

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system oscillations via the SVD technique. Additionally, it has designed three kinds of power controllers including Lead-Lag, LQR and on-line adaptive controller with RLS technique for power systems installed with UPFC and their effects has been compared for damping the power system oscillations.

## 2. The Power System Case Study

Fig.1 shows a single-machine-infinite-bus (SMIB) system installed with UPFC. The static excitation system model type IEEE-ST1A has been considered. The UPFC considered here is assumed to be based on pulse width modulation (PWM) converters. The UPFC is a combination of a static synchronous compensator (STATCOM) and a static synchronous series compensator (SSSC) which are coupled via a common dc link, to allow bi-directional flow of real power between the series output terminals of the SSSC and the shunt output terminals of the STATCOM, and are controlled real and reactive series line compensations without an external electric energy source.

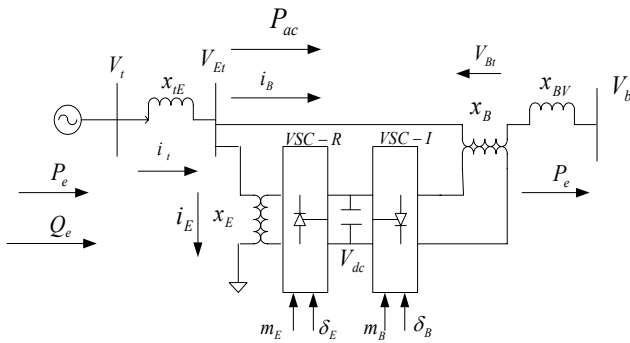


Fig. 1. UPFC installed in a SMIB system.

The UPFC, by means of angularly unconstrained series voltage injection, is able to control, concurrently or selectively, the transmission line voltage, impedance and angle or alternatively, the real and reactive power flow in the line. The UPFC may also provide independently controllable shunt reactive compensation.

Viewing the operation of the UPFC from the stand point of conventional power transmission based on reactive shunt compensation, series compensation and phase shifting, the UPFC can fulfill all these functions and thereby meet multiple control objectives by adding the injected voltage  $V_{Bt}$  with appropriate amplitude and phase angle, to the terminal voltage  $V_{Et}$ .

### 2.1 State Space Equation of Power System

If the general pulse width modulation (PWM) is adopted for GTO-based VSCs, the three-phase dynamic differential equations of the UPFC are [6]:

$$\begin{aligned}\Delta \dot{\delta} &= \omega_b \Delta \omega \\ \Delta \dot{\omega} &= \frac{\Delta P_m - \Delta P_e - D \Delta \omega}{M} \\ \Delta \dot{E}'_q &= \frac{-\Delta E_q + \Delta E_{fd} + (x_d - x'_d) \Delta i_d}{T'_{do}} \\ \Delta \dot{E}_{fd} &= \frac{-\Delta E_{fd} + K_A (\Delta V_{ref} - \Delta v + \Delta u_{pss})}{T_A} \\ \Delta \dot{V}_{dc} &= K_7 \Delta \delta + K_8 \Delta E'_q - K_9 \Delta V_{dc} + \\ &K_{ce} \Delta m_E + K_{c\delta e} \Delta \delta_E + K_{cb} \Delta m_B + K_{c\delta b} \Delta \delta_B\end{aligned}\quad (1)$$

The equations below can be obtained with a line arising from Eq. (1).

$$\Delta P_e = K_1 \Delta \delta + K_2 \Delta E'_q + K_{qd} \Delta V_{dc} + \quad (2)$$

$$\begin{aligned}K_{qe} \Delta m_E + K_{q\delta e} \Delta \delta_E + K_{qb} \Delta m_B + K_{q\delta b} \Delta \delta_B \\ \Delta E'_q = K_4 \Delta \delta + K_3 \Delta E'_q + K_{qd} \Delta V_{dc} +\end{aligned}\quad (3)$$

$$\begin{aligned}K_{qe} \Delta m_E + K_{q\delta e} \Delta \delta_E + K_{qb} \Delta m_B + K_{q\delta b} \Delta \delta_B \\ \Delta V_t = K_5 \Delta \delta + K_6 \Delta E'_q + K_{vd} \Delta V_{dc} +\end{aligned}\quad (4)$$

$$\begin{aligned}K_{ve} \Delta m_E + K_{v\delta e} \Delta \delta_E + K_{vb} \Delta m_B + K_{v\delta b} \Delta \delta_B \\ \Delta V_{dc} = K_7 \Delta \delta + K_8 \Delta E'_q - K_9 \Delta V_{dc} +\end{aligned}\quad (5)$$

$$K_{ce} \Delta m_E + K_{c\delta e} \Delta \delta_E + K_{cb} \Delta m_B + K_{c\delta b} \Delta \delta_B$$

The state-space equations of the system can be calculated by combination of Eqs. (2) to (5) with Eq. (1):

$$\begin{aligned}\dot{x} &= Ax + Bu \\ x &= [\Delta \delta, \Delta \omega, \Delta E'_q, \Delta E_{fd}, \Delta V_{dc}]^T \\ u &= [\Delta u_{pss}, \Delta m_E, \Delta \delta_E, \Delta m_B, \Delta \delta_B]^T\end{aligned}\quad (6)$$

$$\begin{aligned}A &= \begin{bmatrix} 0 & \omega_b & 0 & 0 & 0 \\ -\frac{K_1}{M} & -\frac{D}{M} & -\frac{K_2}{M} & 0 & -\frac{K_{pd}}{M} \\ -\frac{K_4}{M} & 0 & -\frac{K_3}{T'_{do}} & \frac{1}{T'_{do}} & -\frac{K_{qd}}{T'_{do}} \\ -\frac{K_A K_5}{T_A} & 0 & -\frac{K_A K_6}{T_A} & -\frac{1}{T_A} & -\frac{K_A K_{pd}}{T_A} \\ K_7 & 0 & K_8 & 0 & -K_9 \end{bmatrix} \\ B &= \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{K_{pe}}{M} & -\frac{K_{p\delta e}}{M} & -\frac{K_{pb}}{M} & -\frac{K_{p\delta b}}{M} \\ 0 & \frac{K_{qe}}{T'_{do}} & \frac{K_{q\delta e}}{T'_{do}} & \frac{K_{qb}}{T'_{do}} & \frac{K_{q\delta b}}{T'_{do}} \\ \frac{K_A}{T_A} & -\frac{K_A K_{ve}}{T_A} & -\frac{K_A K_{v\delta e}}{T_A} & -\frac{K_A K_{vb}}{T_A} & -\frac{K_A K_{v\delta b}}{T_A} \\ 0 & K_{ce} & K_{c\delta e} & K_{cb} & K_{c\delta b} \end{bmatrix}\end{aligned}\quad (7)$$

That  $\Delta m_E$ ,  $\Delta m_B$ ,  $\Delta \delta_E$  and  $\Delta \delta_B$  are a linearization of the input control signal of the UPFC and the equations related to the K parameters have been presented in Appendix C. The linearized dynamic model of Eqs. (2) to (5) can be seen in Fig.2, where there is only one input control signal for u. Fig. 2 includes the UPFC relating the pertinent vari-

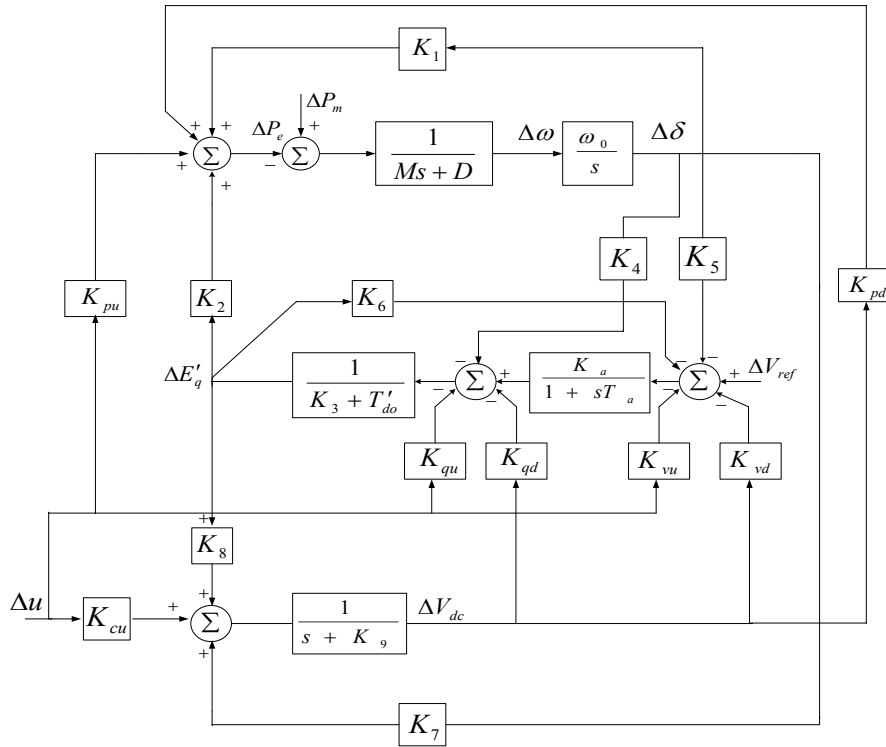


Fig. 2. Modified Heffron-Phillips model of SMIB system with UPFC.

ables of electric torque, speed, angle, terminal voltage, field voltage, flux linkages, UPFC control parameters and dc link voltage.

## 2.2 Operating Points Calculating in Steady Condition

The primary d-q based axis of voltage, current and load angle of the system, necessary for K parameters calculating in Eq. (7), have been obtained for the three conditions shown below:

### CASE A-light operating condition:

$$P_e = 0.2 pu, Q_e = 0.01 pu \quad (8)$$

### CASE B-nominal operating condition:

$$P_e = 0.8 pu, Q_e = 0.167 pu \quad (9)$$

### CASE C-heavy operating condition:

$$P_e = 1.2 pu, Q_e = 0.4 pu \quad (10)$$

**STEP1:** First, by solving the four equations below, we compute the parameters  $V_{td}, V_{tq}, i_{td}$  and  $i_{tq}$  at every operating condition.

$$V_{td}^2 + V_{tq}^2 = 1 \quad (11)$$

$$V_{td}i_{td} + V_{tq}i_{tq} = P_e \quad (12)$$

$$V_{td}i_{tq} - V_{tq}i_{td} = Q_e \quad (13)$$

$$V_{td} = x_q i_{tq} \quad (14)$$

**STEP2:** By solving the 10 equations below, parameters  $V_{Etd}, V_{Eiq}, V_{bd}, V_{bq}, i_{Bd}, i_{Bq}, V_{Btd}, V_{Btq}, i_{Ed}$  and  $i_{Eq}$  will be obtained:

$$\begin{aligned} V_{bd}^2 + V_{bq}^2 &= 1 \\ V_{Etd}i_{Bd} + V_{Eiq}i_{Bq} &= P_{ac} \\ V_{Etd} &= -(x_B + x_{BV})i_{Bq} - V_{Btd} + V_{bd} \\ V_{Eiq} &= (x_B + x_{BV})i_{Bd} - V_{Btq} + V_{bq} \\ V_{Bd}i_{Bd} + V_{Bq}i_{Bq} &= P_{dc} \\ V_{Etd}i_{Ed} + V_{Eiq}i_{Eq} &= P_{dc} \\ V_{Ed} &= V_{Etd} + x_E i_{Eq} \\ V_{Eq} &= V_{Eiq} - x_E i_{Ed} \end{aligned} \quad (15)$$

## 2.3 $\Delta Q_e$ Calculation

In this section, the dynamic equations relevant to the reactive power deviations will be calculated for use as the input damping control signal. According to Fig. 1, the following equations can be written:

$$Q_e = V_{td}i_{tq} - V_{tq}i_{td} \quad (16)$$

$$V_{tq} = E'_q - x'_d i_{td} \quad (17)$$

$$V_{td} = x_q i_{tq} \quad (18)$$

$$Q_e = (x_q i_{tq}) i_{tq} - (E'_q - x'_d i_{td}) i_{td} \quad (19)$$

Dynamic d-q based equations of currents relevant to the reference system can be obtained as follows:

$$i_{Ed} = \frac{X_{BB} E'_q}{X_{d\Sigma}} - \frac{m_E \sin \delta_E V_{dc} X_{Bd}}{2X_{d\Sigma}} + \frac{X_{dE}}{X_{d\Sigma}} (V_b \cos \delta + \frac{m_B \sin \delta_B V_{dc}}{2}) \quad (20)$$

$$i_{Eq} = \frac{m_E \cos \delta_E V_{dc} X_{Bq}}{2X_{q\Sigma}} - \frac{X_{qE}}{X_{q\Sigma}} (V_b \sin \delta + \frac{m_B \cos \delta_B V_{dc}}{2}) \quad (21)$$

$$i_{Bd} = -\frac{X_{dt}}{X_{d\Sigma}} (V_b \cos \delta + \frac{m_B \sin \delta_B V_{dc}}{2}) - \frac{X_{dE}}{X_{d\Sigma}} \frac{m_E \sin \delta_E V_{dc}}{2} + \frac{X_E}{X_{d\Sigma}} E'_q \quad (22)$$

$$i_{Bq} = -\frac{m_E \cos \delta_E V_{dc} X_{qE}}{2X_{q\Sigma}} - \frac{X_{qt}}{X_{q\Sigma}} (V_b \sin \delta + \frac{m_B \cos \delta_B V_{dc}}{2}) \quad (23)$$

$\Delta Q_e$  Signal can be assumed as Eq. (24):

$$\Delta Q_e = K_{10} \Delta \delta + K_{11} \Delta E'_q + K_{12} \Delta V_{dc} + K_{13} \Delta m_E + K_{14} \Delta \delta_E + K_{15} \Delta m_B + K_{16} \Delta \delta_B \quad (24)$$

From Eqs. (19) to (23) in comparison with Eq. (24) the K-constant values can be calculated as shown below:

$$K_{10} = (-2x_q L)(x_{qE} + x_{qt}) V_b \cos \delta / (x_{q\Sigma}) + E'_q V_b \sin \delta / ((x_{dE} - x_{dt}) / x_{d\Sigma}) (2x'_d S + 1) \quad (25)$$

$$K_{11} = ((x_{BB} - x_E) / x_{d\Sigma}) (2x'_d S - E'_q) - S \quad (26)$$

$$K_{12} = 2X_q L ((x_{Bq} - x_{qE}) \cos \delta_E m_E / 2x_{q\Sigma} + (x_{qt} - x_{qE}) \cos \delta_B m_B / 2x_{q\Sigma}) + (2x'_d L - E'_q) ((x_{dE} - x_{Bd}) \sin \delta_E m_E / 2x_{d\Sigma} + (x_{dE} - x_{dt}) \sin \delta_B m_B / 2x_{d\Sigma}) \quad (27)$$

$$K_{13} = 2x_q L x_{Bq} - x_{qE} \cos \delta_E V_{dc} / 2x_{q\Sigma} + (2x'_d S - E'_q) ((x_{dE} - x_{Bd}) \sin \delta_E V_{dc} / 2x_{d\Sigma}) \quad (28)$$

$$K_{14} = 2x_q L (x_{Bq} + x_{qE}) \sin \delta_E V_{dc} m_E / 2x_{q\Sigma} + (2x'_d S - E'_q) ((x_{dE} - x_{Bd}) \cos \delta_E m_E V_{dc} / 2x_{d\Sigma}) \quad (29)$$

$$K_{15} = 2x_q L (x_{qt} - x_{qE}) \cos \delta_B V_{dc} / 2x_{q\Sigma} + (2x'_d S - E'_q) ((x_{dE} - x_{dt}) \sin \delta_B V_{dc} / 2x_{d\Sigma}) \quad (30)$$

$$K_{16} = 2x_q L (x_{qE} - x_{qt}) \sin \delta_B V_{dc} m_B / 2x_{q\Sigma} + (2x'_d S - E'_q) ((x_{dE} - x_{dt}) \cos \delta_B V_{dc} m_B / 2x_{d\Sigma}) \quad (31)$$

$$L = (m_E \cos \delta_E V_{dc} x_{Bq}) / (2x_{q\Sigma}) - (x_{qE} / x_{q\Sigma}) (0.5 m_B \cos \delta_B V_{dc} + V_b \sin \delta) - (m_E \cos \delta_E V_{dc} x_{qE}) / (2x_{q\Sigma}) + (x_{qt} / x_{q\Sigma}) (0.5 m_B \cos \delta_B V_{dc} + V_b \sin \delta) \quad (32)$$

$$S = (x_{BB} E'_q / x_{d\Sigma}) - (m_E \sin \delta_E V_{dc} x_{Bd}) / (2x_{d\Sigma}) + (x_{dE} / x_{d\Sigma}) (V_b \cos \delta + 0.5 m_B \sin \delta_B V_{dc}) - (x_E E'_q / x_{d\Sigma}) + (x_{dE} m_E \sin \delta_E V_{dc}) / (2x_{d\Sigma}) - (x_{dt} / x_{d\Sigma}) (V_b \cos \delta + 0.5 m_B \sin \delta_B V_{dc}) \quad (33)$$

## 2.4 Singular Value Decomposition

Singular value decomposition (SVD) is employed to measure the controllability of the Electro Mechanical mode (EM mode) from each of the four inputs: ( $m_E$ ,  $m_B$ ,  $\delta_E$  and  $\delta_B$ ) [4] and [6]. The minimum singular value  $\sigma_{\min}$  is estimated over a wide range of operating conditions ( $P_e: [0.05 \rightarrow 1.5]$  and  $Q_e: [-0.4 \rightarrow 0.4]$  pu).

SVD produces a non-negative diatetric matrix (S) with dimensions of  $n \times n$  and it creates unitary U and V matrices as below:

$$x = U * S * V \quad (34)$$

$$[U, S, V] = \text{svd}(x)$$

Fig. 3 shows the  $\sigma_{\min}$  for all four inputs at  $Q_e = 0.4$  pu.

According to Fig. 3, it can be seen that the EM mode controllability with  $\delta_E$  is more than other inputs and is the least affected by loading conditions.

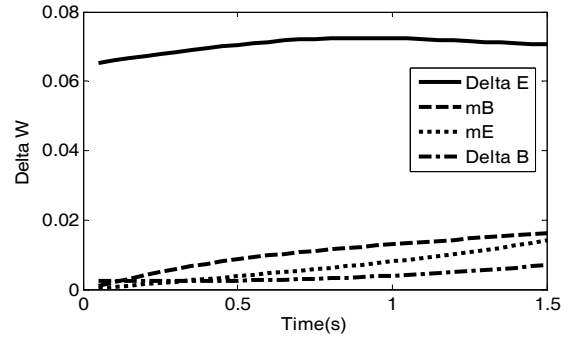


Fig. 3. Minimum singular value with all inputs at  $Q_e = 0.4$  pu.

## 3. Design of Damping Controllers

### 3.1 Lead-Lag Controller

The damping controllers are designed to produce an electrical torque in phase with the speed deviation. The four control parameters of the UPFC (i.e.,  $m_E$ ,  $m_B$ ,  $\delta_E$  and  $\delta_B$ ) can be modulated in order to produce the damping torque. The speed deviation  $\Delta \omega$  is considered as the input to the damping controllers. The structure of the UPFC based damping controller is shown in Fig. 4. It consists of gain, signal washout and phase compensator blocks. The parameters of the damping controller are obtained using the phase compensation technique [12]. According to Fig. 4, the structures of Lead-Lag controllers with  $\Delta \omega$  and

$\Delta P_e$  inputs are very similar. The detailed step-by-step procedure for computing the parameters of the damping controllers using the phase compensation technique is given below.

At first, the natural frequency of oscillations  $\omega_n$  is calculated for the mechanical loop.

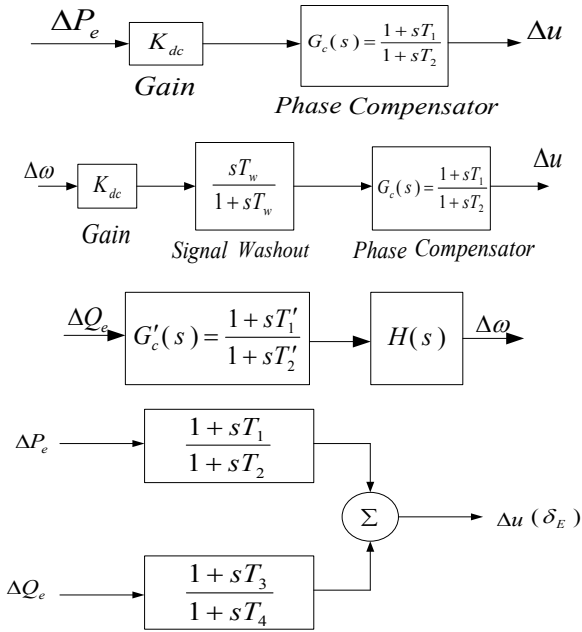


Fig. 4. Structure of UPFC based damping controller.

$$\omega_n = \sqrt{\frac{K_1 \omega_0}{M}} \quad (35)$$

That the amounts of  $\omega_0$ ,  $K_1$  and  $M$  has been presented in Appendix A.

For computing the phase lag between  $\Delta u$  and  $\Delta P_e$  at  $s = j\omega_n$ , we should calculate the transfer function of Fig. 5, which is a simple control model of Fig. 6.

The phase Lead-Lag compensator  $G_C$  is designed to provide the required degree of phase compensation for 100% phase compensation.

$$\angle G_C(j\omega) + \angle \gamma(j\omega) = 0 \quad (36)$$

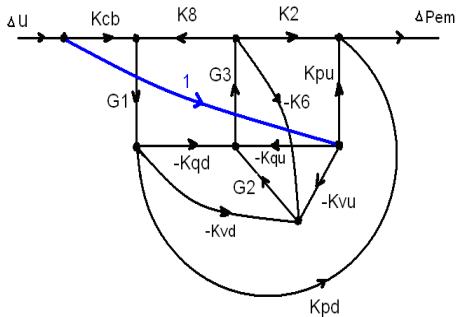


Fig. 5. The graph between  $\Delta P_{EM}$  and  $\Delta u$ .

Assuming one Lead-Lag network,  $T_1 = aT_2$  the transfer function of the phase compensator becomes,

$$G_C(s) = \frac{1 + saT_2}{1 + sT_2} \quad (37)$$

Since the phase angle compensated by the Lead-Lag network is equal to  $-\gamma$ , the parameters  $a$  and  $T_2$  are computed as,

$$a = \frac{1 + \sin \gamma}{1 - \sin \gamma} \quad (38)$$

$$T_2 = \frac{1}{\omega_n \sqrt{a}}$$

The require gain setting  $K_{dc}$  for desired value of damp-ratio  $\xi = 0.5$  is obtained as,

$$K_{dc} = \frac{2\xi\omega_n M}{|G_C(s)| |\gamma(s)|} \quad (39)$$

And  $|G_C(s)|$  and  $|\gamma(s)|$  are computed at  $s = j\omega_n$ .

The signal washout is the high pass filter that prevents steady changes in the speed from modifying the UPFC input parameter. The value of the washout time constant  $T_w$  should be high enough to allow signals associated with oscillations in rotor speed to pass unchanged. From the view point of the washout function, the value of  $T_w$  is not critical and may be in the time range of 1s to 20s.  $T_w$  equal in 10s is chosen in the present studies.

Fig. 6 shows the transfer function of the system relating the electrical component of the power  $\Delta P_{EM}$  produced by the damping controller  $\delta_E$ .

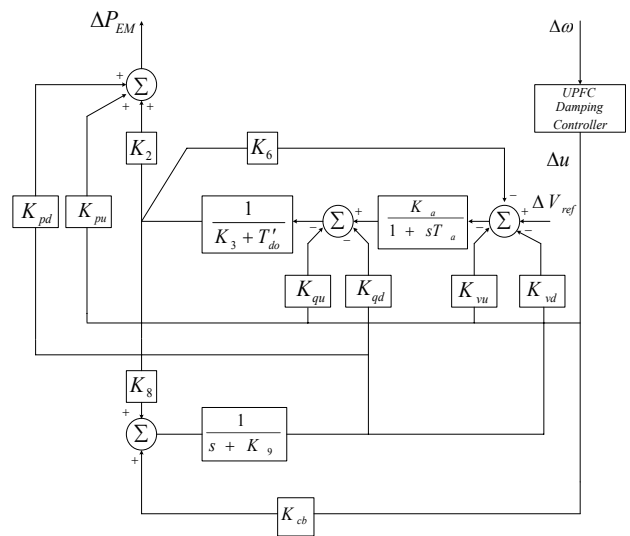


Fig. 6. Transfer function of the system relating component of electrical power  $\Delta P_{EM}$  produced by damping controller  $\delta_E$ .

In order to design a controller with  $\Delta Q_e$  input signal for damping signal  $\delta_E$ , transfer function  $H(s) = \frac{\Delta Q_e}{\Delta \omega}$  must be calculated according to Eq. (24) as shown below:

$$H(s) = \frac{\Delta Q_e}{\Delta \omega} = \frac{K_{10}H_{12} + K_{11}H_{32} + K_{12}H_{52} + K_{14}}{H_{22}} \quad (40)$$

So it can be obtained:

$$\angle \Delta Q_e = \angle H(s) + \angle \Delta \omega \quad (41)$$

Therefore, the Lead-Lag compensator  $G'_c(s)$  must be designed to compensate for the phase shifting between  $\Delta Q_e$  and  $\Delta \omega$ . The transfer function between  $\Delta Q_e$  and  $\Delta \omega$  according to Eq. (24), has been calculated as follows:

$$H(s) = \frac{\Delta Q_e}{\Delta \omega} = \frac{K_{10}H_{12} + K_{11}H_{32} + K_{12}H_{52} + K_{14}}{H_{22}} \quad (42)$$

In order to design the damping controller with input  $\Delta P_e + \Delta Q_e$ , two Lead-Lag compensators must compensate for the phase angle between  $\Delta u$  and  $\Delta P_{EM}$  together.

### 3.2 LQR Controller

The LQR controller for a system described with the state-feedback equation  $\dot{x} = Ax + B$  can calculate the optimal amount of  $K$  so that the state feedback  $u = -Kx$  according to Fig. 7 to minimize the integral of Eq. (43).

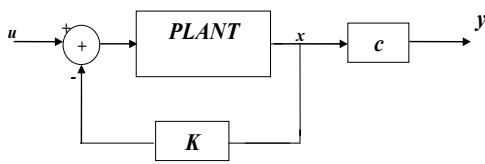


Fig. 7. Block diagram of a state-space based system with negative feedback.

$$J(u) = \int_0^{\infty} (x^T Q x + u^T R u + 2x^T N u) dt \quad (43)$$

In addition to calculating the optimal value of  $K$ , the LQR calculates the solution  $S$  of the associated Riccati equation according to equation (44).

$$A^T s + sA - (sB + N)R^{-1}(B^T s + N^T) + Q = 0 \quad (44)$$

The eigenvalues of closed-loop system  $e = \text{eig}(A - B^* K)$  is calculated, too. Note that the value of  $K$  is calculated using the response of the Riccati equation according to equation (45).

$$K = R^{-1}(B^T s + N^T) \\ [K, s, e] = LQR(A, B, Q, R, N) \quad (45)$$

### 3.3 Adaptive Controller

Fig. 8 shows a block diagram of a process with a self-tuning regulator (STR). The parameters of the power system transfer function are estimated by estimation block with samples taken from input  $\Delta \delta_E$  and output  $\Delta \omega$  with a specified sampling time [15], [16]. It has been shown as the discrete transfer function of the state equation of the power system (7) as follows:

$$H(q) = \frac{\Delta \omega(q)}{\Delta \delta_E} = \frac{B(q)}{A(q)} = \frac{b_0 q^4 + b_1 q^3 + b_2 q^2 + b_3 q + b_4}{q^5 + a_1 q^4 + a_2 q^3 + a_3 q^2 + a_4 q + a_5} \quad (46)$$

The block labeled controller design contains the computation's Diophantine equation required to perform a design of a controller with a specified method and few design parameters that can be chosen externally. The recursive least-square method (RLS) will be used for parameter estimation and the design method is a deterministic pole placement (MDPP). A general linear controller can be described by

$$Ru(t) = Tu_c(t) - Sy(t) \quad (47)$$

Where  $R$ ,  $S$  and  $T$  are polynomials. A block diagram of the closed-loop system is shown in Fig. 9.

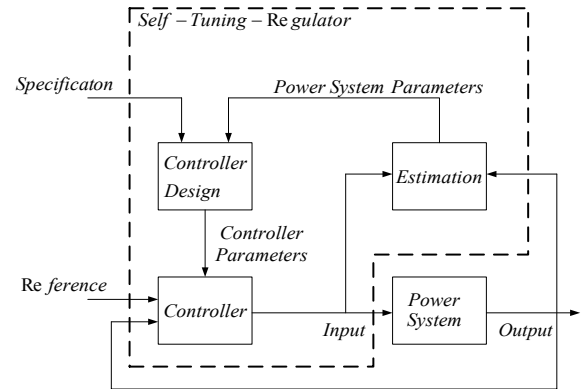


Fig. 8. Block diagram of Self Tuning Regulator.

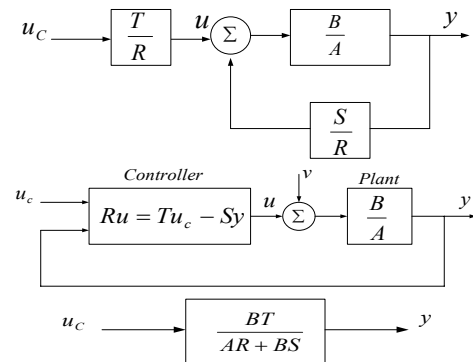


Fig. 9. A general linear controller with 2 degrees of freedom.

General equations of R, S and T are polynomials and have been calculated by MDPP as follows:

$$\begin{aligned} R(q) &= q^4 + r_1q^3 + r_2q^2 + r_3q + r_4 \\ S(q) &= s_0q^4 + s_1q^3 + s_2q^2 + s_3q + s_4 \\ T(q) &= t_0q^4 + t_1q^3 + t_2q^2 + t_3q + t_4 \end{aligned} \quad (48)$$

The closed-loop characteristic polynomial is thus:

$$AR + BS = A_C \quad (49)$$

The key idea of the design method is to specify the desired closed-loop characteristic polynomial  $A_C$ . The polynomial R and S can then be solved from Eq. (49). In the design procedure we consider polynomial  $A_C$  to be a design parameter that is chosen to give desired properties to the closed-loop system. Eq. (49), which plays a fundamental role in algebra, is called the Diophantine equation. The equation always has solutions if polynomials A and B do not have common factors. The solution may be poorly conditioned if the polynomials have factors that are closed. The solution can be obtained by introducing polynomials with unknown coefficients and solving the linear equations obtained. In fact, in an off-line state, the adaptive controller parameters are as according to Fig.10.

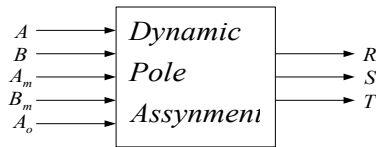


Fig. 10. Block diagram of off-line adaptive controller inputs and outputs.

$\frac{B_m}{A_m}$  is the desired transfer function of power system.  $B_m$  and  $A_m$  polynomials must be chosen in the way that the adaptive controller can omit the perturbation in input mechanical torque with suitable speed. The desired transfer function used in this paper according to Eq. (46) offers as below:

$$\frac{y(q)}{u(q)} = \frac{B_m(q)}{A_m(q)} = \frac{q^4}{q^5 + a_1q^4 + a_2q^3 + a_3q^2 + a_4q + a_5} \quad (50)$$

According to Fig.10, designing an adaptive off-line controller (MDPP technique) consists of the three following steps:

1. Selection polynomials of  $A_m$ ,  $B_m$  and  $A_o$  as below:

$$\deg A_m = \deg A = n \quad (51)$$

$$\deg B_m = \deg B = m \quad (52)$$

$$\deg A_o = \deg A - \deg B^+ - 1 \quad (53)$$

$$B_m = B^+ B^- \quad (54)$$

That  $B^+$  and  $B^-$  are strongly and poorly damped roots polynomials.

2. The Diophantine equation is formed as below and will be solved for finding  $R'$  and  $S$  polynomials:

$$AR' + B^-S = A_o A_m \quad (55)$$

3. Calculating  $R$  and  $T$  control as below:

$$R = R' B^+ \quad (56)$$

$$T = A_o B'_m \quad (57)$$

But the on-line control design consists of the three following steps:

1. Selection polynomials of  $A_m$ ,  $B_m$  and  $A_o$ .
2. Calculation of  $\hat{\theta}$  matrix with RLS as in the equation below:

$$y(q) = \frac{B}{A} u(q) \quad (58)$$

$$A(q)y(q) = B(q)u(q) \quad (59)$$

$$y(q) + a_1y(q-1) + a_2y(q-2) + \dots + a_ny(q-n) = b_1u(q+m-n-1) + \dots + b_mu(q-m) \quad (60)$$

$$y(q) = [-y(q-1) \dots -y(q-n) \quad u(q+m-n-1) \dots u(q-m)] \begin{bmatrix} a_1 \\ \vdots \\ a_n \\ b_1 \\ \vdots \\ b_m \end{bmatrix} \quad (61)$$

$$y(q) = \phi^T(q-1)\theta \quad (62)$$

$$K(q) = P(q)\phi(q) = P(q-1)\phi(q)[I + \phi^T(q)P(q-1)\phi(q)]^{-1} \quad (63)$$

$$P(q) = P(q-1) - P(q-1)\phi(q)[I + \phi^T(q)P(q-1)\phi(q)]^{-1} \times \phi^T(q)P(q-1) = [I - K(q)\phi^T(q)]P(q-1) \quad (64)$$

$$\hat{\theta}(q) = \hat{\theta}(q-1) + K(q)[y(q) - \phi^T(q)\hat{\theta}(q-1)] \quad (65)$$

3. Calculation of  $R$ ,  $S$  and  $T$  polynomials with MDPP.

### 3.4 Simulation Results

Eigen-value (electro mechanical mode) calculations should be done before any controller designing. Table 1 shows the electro mechanical mode of the system without any controller, equipped with Lead-Lag, LQR and an adaptive controller.

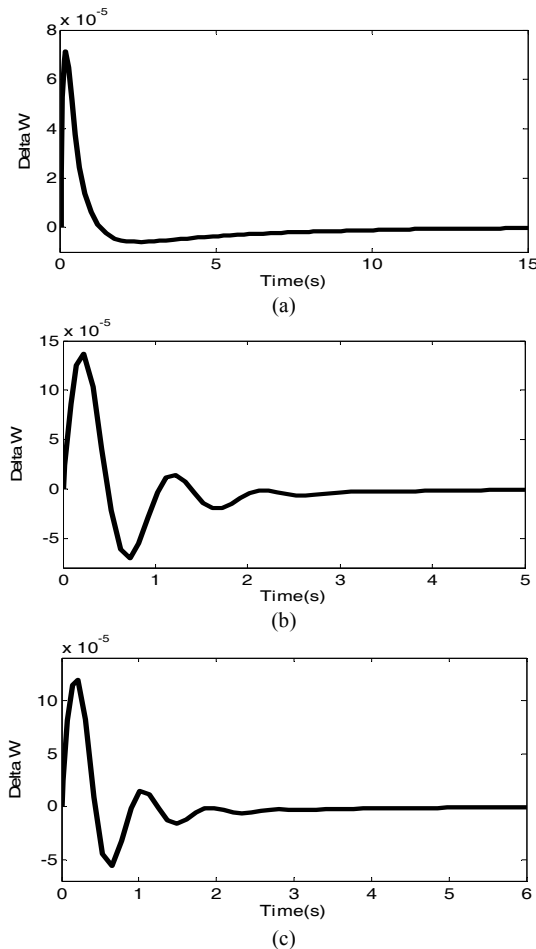
Based on the above table, pole placement of the closed loop system equipped with controllers has improved in comparison with open loop systems and an on-line adaptive controller has the best result among them.

The linearized model of the case study system in Fig. 1 with parameters shown in Appendix. A and K parameters shown in Appendix. C, has been simulated with MATLAB/

SIMULINK. In order to examine the robustness of the damping controllers to a step load perturbation, it has been applied a step duration in mechanical power (i.e.,  $\Delta P_m = 0.01 pu$ ) to the system seen in Fig. 2. Consequently, the reference system has four inputs; the damping input signal in Fig. 3 has been added to the most effective input  $\delta_E$  calculated by the SVD technique. Fig. 11 shows the dynamic responses of  $\Delta\omega$  with different operating conditions by Lead-Lag controller for  $\delta_E$  input control signal.

**Table 1.** Electromechanical mode of the individual terms at Nominal loading condition

Without controller	0.1052 ± j2.8455			
Lead-Lag	$\delta_E$	$m_E$	$\delta_B$	$m_B$
	-1.780 ± j2.7446	-0.46 ± j2.9	-1.4187 ± j7276	3.3661 ± j1.3204
LQR	-0.417 ± j2.9290			
On-line Adaptive controller	-1.394 ± j0.3304			

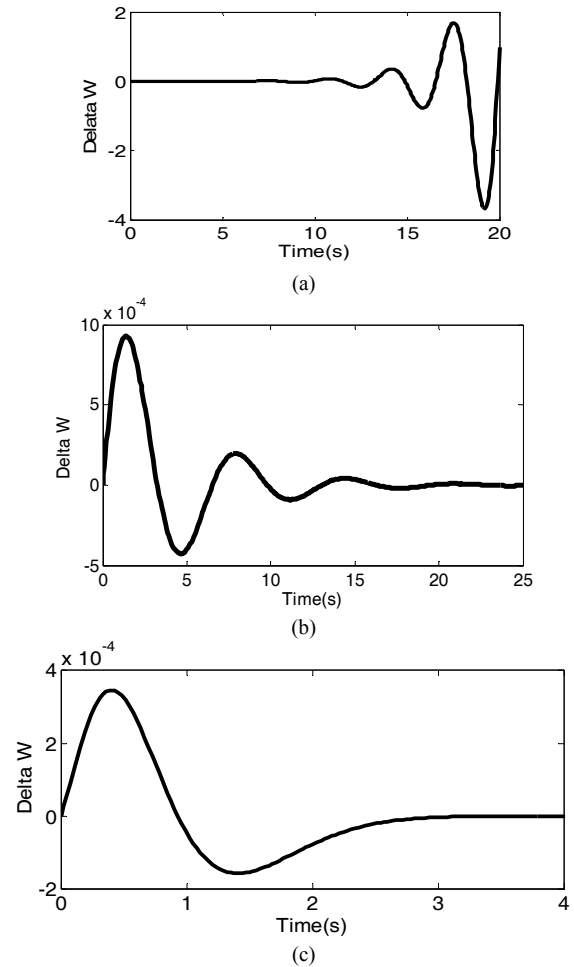


**Fig. 11.** Dynamic responses of  $\Delta\omega$  with input control signal  $\delta_E$  for different operating conditions (a): Light load (b): Nominal load (c): Heavy load.

It is clearly seen that the dynamic performance at a heavy condition is better significantly compared to that obtained at light and nominal loadings because the speed deviation has been damped with minimum settling time at a heavy condition. The response of the nominal condition has the second rank after the heavy condition because its settling time is less than five seconds and its peak amplitude value is even greater than the heavy condition.

According to the above, it can be calculated by dynamic responses to the  $\Delta P_m = 0.01 pu$  perturbation for other input control signals that by comprising all of the responses, we can see that adding the damping control signal to  $\delta_E$  is better than other control inputs because of its speed oscillation damp with a shorter time than five seconds and minimum amplitude. Fig. 12 shows the dynamic responses of  $\Delta\omega$  for nominal operating conditions by Lead-Lag controller with  $\Delta Q_e$ ,  $\Delta P_e$  and  $\Delta P_e + \Delta Q_e$  input control signal.

By comparing the above figures with those obtained by the controller with  $\Delta\omega$  input in Fig. 11.b, it can be seen that the response quality of  $\Delta Q_e$ ,  $\Delta P_e$ ,  $\Delta P_e + \Delta Q_e$  based



**Fig. 12.** Dynamic responses of  $\Delta\omega$  at nominal operating conditions for different input control signal (a):  $\Delta Q_e$  (b):  $\Delta P_e$  (c):  $\Delta P_e + \Delta Q_e$ .



controller is less than  $\Delta\omega$  based controller in terms of peak amplitude. Therefore it has been used from  $\Delta\omega$  input signal for LQR and adaptive controller designing.

It can be seen by the dynamic responses to the  $\Delta P_m = 0.01 pu$  perturbation of input mechanical power for systems equipped with an LQR controller in the following.

Fig. 13 shows the dynamic responses of  $\Delta\omega$  at nominal condition with LQR damping controller.

Dynamic response has nearly the same quality in comparison with the Lead-Lag controller at Fig. 11 (b) in terms of settling time and peak amplitude. Fig. 14 is related to an estimation of the control reference system in the on-line adaptive controller at nominal condition calculated by RLS technique. Some of the coefficients of the transfer function

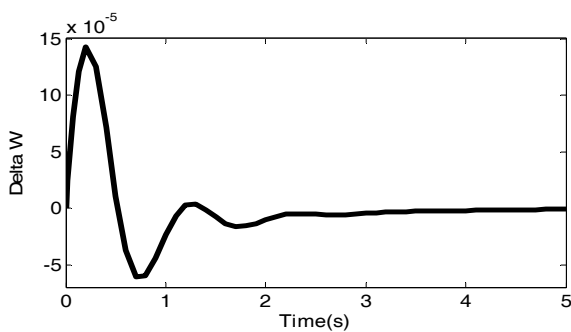


Fig. 13. The dynamic responses of  $\Delta\omega$  at nominal condition with LQR damping controller.

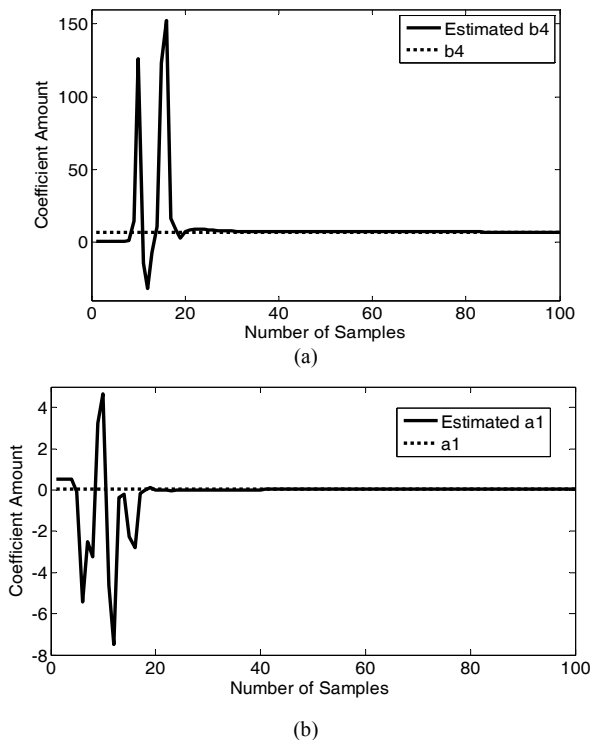


Fig. 14. Adaptive controller polynomial coefficients of RLS estimated plant at nominal operating condition:(a) :  $b_4$  (b) :  $a_1$ .

of the power system in Eq. (45) and their estimation by RLS technique have been shown in Fig. 14. It can be seen that the estimation of transfer function coefficients have been converged to the polynomials of the reference power system model at less than 20 iterations.

After estimation of the transfer function of the reference control model, in order to calculate the on-line adaptive controller polynomial coefficients, the Diophantine equation must be solved. In the following, it has been shown some of the parameters R and S in Fig. 15 at a nominal condition. It can be considered that the coefficients have been converged at less than 20 iterations.

Samples have been taken from the input and output of the transfer function of the case study with sampling time  $T_s = 0.01s$  for adaptive control designing. The desired transfer function of Eq. (50) has been presented in Appendix B. Fig. 16 shows the dynamic responses of  $\Delta\omega$  with adaptive controller at nominal operating loads due to  $\Delta P_m = 0.01 pu$  perturbation.

It is clearly seen that the dynamic performance at different loading conditions have an almost similar quality in terms of settling time and peak amplitude. From comparisons between the results of the adaptive controller with Lead-Lag, LQR controllers and without controller, it can be seen that the dynamic response of the system equipped with an adaptive controller (Fig. 16) in comparison with the system equipped with an LQR controller (Fig. 13) has greater quality because the adaptive controller could decrease the settling time for more than 0.1 seconds. Also, the dynamic response of the system equipped with the adaptive controller (Fig. 16) in comparison with a system equipped with Lead-Lag controller (Fig. 11 (b)) has less settling time and the peak amplitude amount of the adaptive control is

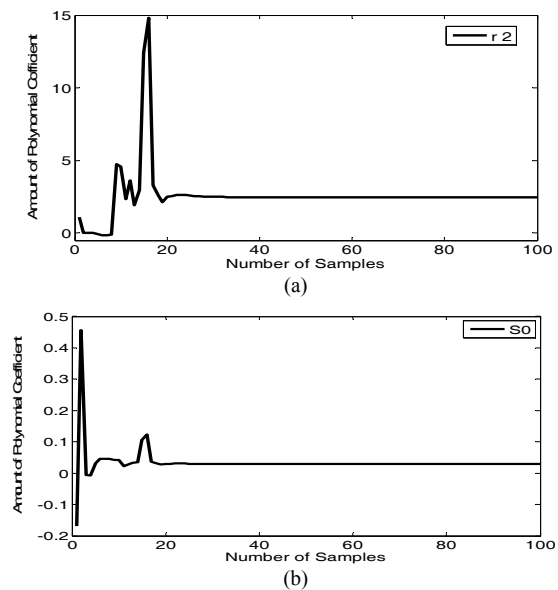
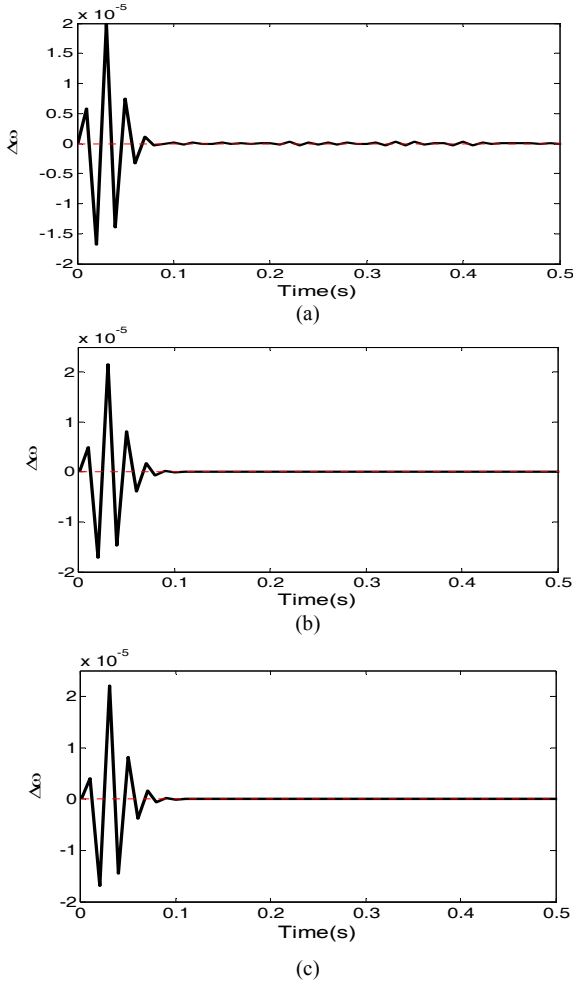


Fig. 15. Adaptive controller parameters calculated with Diophantine equation at nominal operating condition:(a):  $r_2$  (b) :  $s_0$ .



**Fig. 16.** Dynamic responses of  $\Delta\omega$  with adaptive controller at different operating conditions due to  $\Delta P_m = 0.01 pu$  (a): Light (b): Nominal (c): Heavy.

less than Lead-Lag controller, too. Moreover, the proposed adaptive controller stabilizes the power system, while the power system without a controller is unstable according to Table 1. So, the adaptive controller gives the best results according to Table 1.

#### 4. Conclusion

In this paper, a UPFC has been used for dynamic stability improvement and state-space equations have been applied for the design of damping controllers. Simulation results operated by MATLAB/SIMULINK show that using input speed deviation signal is better than inputs of power deviations, and also adding control signals to the active power control loop of the shunt inverter decreases speed oscillations effectively. According to the simulation results, the designed adaptive controller for the system has the perfect effect in oscillation damping and dynamic stability improvement in comparison with other controllers.

#### Acknowledgements

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#### Appendix

##### A: The test system parameters are:

Generator:

$$M = 2H = 8.0MJ / MVA$$

$$D = 0.0$$

$$T'_{do} = 5.044s$$

$$X_d = 1.0 pu$$

$$X_q = 0.6 pu$$

$$X'_d = 0.3 pu$$

Excitation System:

$$K_a = 100$$

$$T_a = 0.01s$$

Transformer :

$$X_{tE} = 0.1 pu$$

$$X_E = X_B = 0.1 pu$$

$$X_E = X_B = 0.1 pu$$

Transmission Line:

$$X_{BV} = 0.3 pu$$

$$X_e = X_{BV} + X_B + X_{tE} = 0.5 pu$$

Operating Condition:

$$V_t = 1.0 pu$$

$$P_e = 0.8 pu$$

$$V_b = 1.0 pu$$

$$f = 60Hz$$

Parameters of DC Link:

$$V_{dc} = 2 pu$$

$$C_{dc} = 1 pu$$

##### B: Adaptive controller parameters:

$$A_m = (q - 0.01)(q - 0.03)(q - 0.02)(q - 0.1)(q + 0.1)$$

$$B_m = q^4$$

$$A_o = 1$$

$$\deg B_m = \deg B = m = 4$$

$$\deg A_m = \deg A = n = 5$$

##### C: K parameters

$$K_1 = \frac{(V_{td} - I_{tq}x'_d)(x_{dE} - x_{dt})V_b \sin \delta}{x_{d\Sigma}} + \frac{(x_q I_{td} + V_{tq})(x_{qt} - x_{qE})V_b \cos \delta}{x_{q\Sigma}}$$

$$K_2 = \frac{-(x_{BB} + x_E)V_{td} + (x_{BB} + x_E)x'_d I_{tq}}{x_{d\Sigma}x_d} + \frac{(x_{BB} + x_E)x'_d I_{tq}}{x_{d\Sigma}}$$

$$K_3 = 1 + \frac{(x'_d - x_d)(x_{BB} + x_E)}{x_{d\Sigma}}$$

$$K_4 = \frac{(x'_d - x_d)(x_{dE} - x_{dt})V_b \sin \delta}{x_{d\Sigma}}$$

$$K_5 = \frac{V_{td}x_q(x_{qt} - x_{qE})V_b \cos \delta}{V_t x_{q\Sigma}} - \frac{V_{tq}x'_d(x_{dE} - x_{dt})V_b \sin \delta}{V_t x_{d\Sigma}}$$

$$\begin{aligned}
K_6 &= \frac{V_{iq}(x_{d\Sigma} + x'_d(x_{BB} + x_E))}{V_i x_{d\Sigma}} \\
K_7 &= 0.25C_{dc}(V_b \sin \delta(m_E \cos \delta_E x_{dE} - m_B \cos \delta_B x_{dt})) - \\
&\frac{m_B \cos \delta_B x_{dt}}{x_{d\Sigma}} + \\
&V_b \cos \delta(m_B \sin \delta_B x_{qt} - m_E \sin \delta_E x_{qe}) \\
K_8 &= -0.25 \frac{m_B \cos \delta_B x_E + m_E \cos \delta_E x_{BB}}{x_{d\Sigma}} \\
K_9 &= 0.25C_{dc} \left( \frac{m_B \sin \delta_B (m_B \cos \delta_B x_{dt} - m_E \cos \delta_E x_{dE})}{2x_{d\Sigma}} + \right. \\
&\frac{m_E \sin \delta_E (m_E \cos \delta_E x_{Bd} - m_B \cos \delta_B x_{dt})}{2x_{d\Sigma}} \\
&\left. \frac{m_B \cos \delta_B (m_B \sin \delta_B x_{qt} - m_E \sin \delta_E x_{qe})}{2x_{q\Sigma}} + \right. \\
&\left. \frac{m_E \cos \delta_E (-m_B \sin \delta_B x_{qe} + m_E \sin \delta_E x_{Bq})}{2x_{q\Sigma}} \right) \\
K_{pe} &= \frac{(V_{td} - I_{iq} x'_d)(x_{Bd} - x_{dE}) V_{dc} \sin \delta_E}{2x_{d\Sigma}} + \\
&\frac{(x_q I_{td} + V_{iq})(x_{Bq} - x_{qE}) V_{dc} \cos \delta_E}{2x_{q\Sigma}} \\
K_{poe} &= \frac{(V_{td} - I_{iq} x'_d)(x_{Bd} - x_{dE}) V_{dc} m_E \cos \delta_E}{2x_{d\Sigma}} + \\
&\frac{(x_q I_{td} + V_{iq})(-x_{Bq} + x_{qE}) V_{dc} m_E \sin \delta_E}{2x_{q\Sigma}} \\
K_{pb} &= \frac{(V_{td} - I_{iq} x'_d)(x_{dt} - x_{dE}) x_{dc} \sin \delta_B}{2x_{d\Sigma}} + \\
&\frac{(x_q I_{td} + V_{iq})(x_{qt} - x_{qE}) V_{dc} \cos \delta_B}{2x_{q\Sigma}} \\
K_{pob} &= \frac{(V_{td} - I_{iq} x'_d)(x_{dE} + x_{dt}) V_{dc} m_B \cos \delta_B}{2x_{d\Sigma}} + \\
&\frac{(x_q I_{td} + V_{iq})(-x_{qt} + x_{qE}) V_{dc} m_B \sin \delta_B}{2x_{q\Sigma}} \\
K_{pd} &= (V_{td} - I_{iq} x'_d) \left( \frac{(x_{dt} - x_{dE}) m_B \sin \delta_B}{2x_{d\Sigma}} + \right. \\
&\left. \frac{(x_{Bd} - x_{dE}) m_E \sin \delta_E}{2x_{d\Sigma}} \right) + \\
&(x_q I_{td} + V_{iq}) \left( \frac{(x_{qt} - x_{qE}) m_B \cos \delta_B}{2x_{q\Sigma}} + \right. \\
&\left. \frac{(x_{Bq} - x_{qE}) m_E \cos \delta_E}{2x_{q\Sigma}} \right) \\
K_{qe} &= - \frac{(x'_d - x_d)(x_{Bd} - x_{dE}) V_{dc} \sin \delta_E}{2x_{d\Sigma}} \\
K_{qoe} &= - \frac{(x'_d - x_d)(x_{Bd} - x_{dE}) m_E V_{dc} \cos \delta_E}{2x_{d\Sigma}} \\
K_{qb} &= - \frac{(x'_d - x_d)(x_{dt} - x_{dE}) V_{dc} \sin \delta_B}{2x_{d\Sigma}} \\
K_{qob} &= - \frac{(x'_d - x_d)(x_{dE} - x_{dt}) m_B V_{dc} \cos \delta_B}{2x_{d\Sigma}} \\
K_{qe} &= -(x'_d - x_d) \left( \frac{(x_{Bd} - x_{dE}) m_E \sin \delta_E}{2x_{d\Sigma}} + \frac{(x_{dt} - x_{dE}) m_B \sin \delta_B}{2x_{d\Sigma}} \right) \\
K_{ve} &= \frac{V_{td}(x_{Bq} - x_{qE}) V_{dc} \cos \delta_E}{2V_i x_{q\Sigma}} - \frac{V_{iq}(x_{Bd} - x_{dE}) V_{dc} \sin \delta_E}{2V_i x_{d\Sigma}}
\end{aligned}$$

$$\begin{aligned}
K_{v\delta E} &= \frac{V_{td} x_q (x_{qe} - x_{Bq}) m_E V_{dc} \sin \delta_E}{2V_i x_{q\Sigma}} - \frac{V_{iq} x'_d (x_{Bd} - x_{dE}) m_E V_{dc} \cos \delta_E}{2V_i x_{q\Sigma}} \\
K_{vb} &= \frac{V_{td} x_q (x_{qt} - x_{qE}) V_{dc} \cos \delta_E}{2V_i x_{q\Sigma}} - \frac{V_{iq} x'_d (x_{dt} - x_{dE}) V_{dc} \sin \delta_E}{2V_i x_{d\Sigma}} \\
K_{v\delta B} &= \frac{V_{td} x_q (x_{qe} - x_{qE}) m_B V_{dc} \sin \delta_E}{2V_i x_{q\Sigma}} + \frac{V_{iq} m_B x'_d (x_{dE} + x_{dt}) V_{dc} \cos \delta_E}{2V_i x_{d\Sigma}} \\
K_{vd} &= \frac{V_{td} x_q (x_{Bq} - x_{qE}) m_E \cos \delta_E}{2V_i x_{q\Sigma}} + \frac{(x_{qt} - x_{qE}) m_B \cos \delta_B}{2x_{q\Sigma}} - \\
&\frac{V_{iq} m_E x'_d (x_{Bd} - x_{dE}) \sin \delta_E}{2V_i x_{d\Sigma}} + \frac{m_B (x_{dt} - x_{qE}) \sin \delta_E}{2x_{d\Sigma}} \\
K_{ce} &= 0.25C_{dc} \frac{V_{dc} \sin \delta_E (m_E \cos \delta_E x_{Bd} - m_B \cos \delta_B x_{dE})}{2x_{d\Sigma}} + \\
&\frac{V_{dc} \cos \delta_E (m_E \sin \delta_E x_{Bq} - m_B \sin \delta_B x_{qE})}{2x_{q\Sigma}} \\
K_{c\delta E} &= \frac{0.25m_E}{C_{dc}} (\cos \delta_E I_{Eq} - \sin \delta_E I_{Ed}) + \\
&\frac{0.25}{C_{dc}} (m_E V_{dc} \cos \delta_E \frac{(m_E \cos \delta_E x_{Bd} - m_B \cos \delta_B x_{dE})}{2x_{d\Sigma}} + \\
&m_E V_{dc} \sin \delta_E \frac{(m_B \sin \delta_B x_{qE} + m_E \sin \delta_E x_{Bq})}{2x_{q\Sigma}}) \\
K_{cb} &= 0.25C_{dc} \frac{V_{dc} \sin \delta_B (-m_E \cos \delta_E x_{dE} + m_B \cos \delta_B x_{dt})}{2x_{d\Sigma}} + \\
&\frac{V_{dc} \cos \delta_B (m_B \sin \delta_E x_{qt} - m_E \sin \delta_E x_{qE})}{2x_{q\Sigma}} \\
K_{c\delta B} &= \frac{0.25m_B}{C_{dc}} (\cos \delta_B I_{Bq} - \sin \delta_B I_{Bd}) + \\
&\frac{0.25}{C_{dc}} (m_B V_{dc} \cos \delta_B \frac{(m_E \cos \delta_E x_{dE} + m_B \cos \delta_B x_{dt})}{2x_{d\Sigma}} + \\
&m_B V_{dc} \sin \delta_B \frac{(-m_B \sin \delta_E x_{qt} + m_E \sin \delta_E x_{qE})}{2x_{q\Sigma}})
\end{aligned}$$

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