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# **Analytical Model of Conduction and Switching Losses of Matrix-***Z***-Source Converter**

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#### **ABSTRACT**

This paper investigates analytical models of Conduction and Switching Losses (CASLs) of a matrix-Z-source converter (MZC). Two analytical models of the CASLs are obtained through the examination of operating principles for a Z-source inverter and ac-dc matrix converter respectively. Based on the two models, the analytical model of CASLs for a MZC is constructed and visualized over a range of exemplified operating- points, each of which is defined by the combination of power factor (pf) and modulation index (M). The model provides a measurable way to approximate the total losses of the MZC.

Keywords: Conduction and Switching Losses, Matrix-Z-Source Converter, Analytical model of loss

#### 1. Introduction

A matrix-Z-source converter (MZC) for bidirectional three-phase ac-dc power conversion was proposed marrying up both the advantages of the matrix converter and the Z-source inverter [1]. For a practical engineering development, MZC needs the investigation of conduction-and-switching-losses (CASLs) caused by its power-switch network. Nevertheless, the CASLs are essential measures in the comparison of merits between the MZC and existing bidirectional three-phase ac-dc power converters. The study of CASLs for MZC, therefore, is desirable and will be presented through analytical modeling in this paper.

The study of CASLs of a given power converter is usually carried out through a specific methodology using

two elements, the operating principle of the converter and the CASLs model of each power-switch <sup>[2]-[9]</sup>. Section 2 briefly describes the operating principles of MZC, and Section 3 introduces the methodology of modeling CASLs and presents the parameters of CASLs for IGBT and Free-Wheeling Diode (FWD) as the base of modeling. Subsequently, sections 4 and 5 investigate the models of CASLs of Z-source inverter and ac-dc matrix converter respectively; section 6 then sets up the complete model of CASLs of MZC by using the two aforesaid models in sections 4 and 5.

# 2. Topology and Modulation Strategies of the Matrix-Z-source Converter

Detail Configuration of MZC may be found in [1] and is not reprinted here for brevity. MZC has two operating modes, the dc-ac inversion mode and the ac-dc rectification mode. Operating principles of each mode are briefly

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described as follows.

### 2.1 Brief description of the operating principle of the MZC in dc-ac inversion mode

MZC has the same configuration as the Z-source inverter when MZC is in dc-ac inversion mode<sup>[1]</sup>. The Z-source inverter has the same structure of a power-switch network as that of VSI but with a different operating principle <sup>[10]</sup>. Fig. 1 shows the basic structure of a Z-source inverter. Its modeling and modulation strategy is given by (1)-(5) derived from Alesina-Venturini optimum PWM (AV-optimum PWM)<sup>[12] and [14]</sup>. In this modeling Maximum Constant Boost Control (MCBC) is employed<sup>[1]</sup>. Details of MCBC may be found in [11]. Fig. 4 in section 4 shows an example of the gate-drive logic and corresponding currents within one switching cycle.

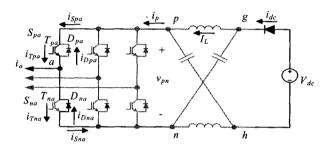


Fig. 1 Basic structure of Z-source inverter used in MZC when MZC is in dc-ac inversion mode

$$\begin{bmatrix} V_{a}(t) \\ V_{b}(t) \\ V_{c}(t) \end{bmatrix} = \begin{bmatrix} d_{pa} & d_{na} \\ d_{pb} & d_{nb} \\ d_{pc} & d_{nc} \end{bmatrix} B \begin{bmatrix} V_{dc}/2 \\ -V_{dc}/2 \end{bmatrix}$$

$$\frac{1}{B} \begin{bmatrix} I_{p} \\ -I_{p} \end{bmatrix} = \begin{bmatrix} d_{pa} & d_{pb} & d_{pc} \\ d_{na} & d_{nb} & d_{nc} \end{bmatrix} \begin{bmatrix} I_{a}(t) \\ I_{b}(t) \\ I_{c}(t) \end{bmatrix}$$
(1)

$$\begin{aligned} d_{pa} &= M[(1/2)\cos(\omega t) - (1/12)\cos(3\omega t)] + 1/2 \\ d_{pb} &= M[(1/2)\cos(\omega t - 2\pi/3) - (1/12)\cos(3\omega t)] + 1/2 \\ d_{pc} &= M[(1/2)\cos(\omega t + 2\pi/3) - (1/12)\cos(3\omega t)] + 1/2 \\ d_{na} &= 1 - d_{pa} \\ d_{nb} &= 1 - d_{pb} \\ d_{nc} &= 1 - d_{pc} \end{aligned} \tag{2}$$

$$B = 1/(\sqrt{3}M - 1) \quad 1/\sqrt{3} < M < 2/\sqrt{3}$$
 (3)

$$D_0 = 1 - \frac{\sqrt{3}}{2}M\tag{4}$$

$$V_{pn} = BV_{dc} = \frac{1}{1 - 2D_0} V_{dc} = \frac{1}{\sqrt{3}M - 1} V_{dc}$$
 (5)

where

$$\begin{bmatrix} V_a(t) \\ V_b(t) \\ V_c(t) \end{bmatrix} = \begin{bmatrix} V_{pk} \cos(\omega t) \\ V_{pk} \cos(\omega t - 2\pi/3) \\ V_{pk} \cos(\omega t + 2\pi/3) \end{bmatrix};$$

$$\begin{bmatrix} I_a(t) \\ I_b(t) \\ I_c(t) \end{bmatrix} = \begin{bmatrix} I_{pk} \cos(\omega t + \Phi) \\ I_{pk} \cos(\omega t - 2\pi/3 + \Phi) \\ I_{pk} \cos(\omega t + 2\pi/3 + \Phi) \end{bmatrix};$$

M is the modulation index;  $d_{ij}$  is the duty-cycle of switch  $S_{ij}$  (i=p,n, j=a,b,c);  $V_{pk}$  and  $I_{pk}$  are peak phase voltage and peak current respectively;  $I_p$  is the average dc-link current;  $V_{dc}$  is the dc source voltage;  $\omega$  is the fundamental electric angular frequency;  $\Phi$  is ac current phase angle; B is the boost factor;  $D_0$  is shoot-through duty-cycle;  $V_{pn}$  is the peak dc-link voltage.

## 2.2 Brief description of the operating principle of the MZC in ac-dc rectification mode

MZC has the came configuration as ac-dc matrix when MZC is in the ac-dc rectification mode <sup>[1]</sup> as shown in Fig. 2. The operating principles using AV-optimum PWM may be described in (6)-(8) <sup>[1] and [13]</sup>. Fig. 5 and Fig. 6 in section 5 show an exemplified procedure of current commutation.

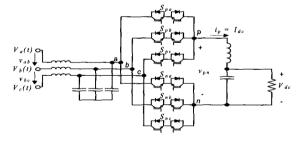


Fig. 2 Basic structure of ac-dc matrix converter used in MZC when MZC is in ac-dc rectification mode

$$\begin{bmatrix} V_{dc}/2 \\ -V_{dc}/2 \end{bmatrix} = \begin{bmatrix} d_{pa} & d_{pb} & d_{pc} \\ d_{na} & d_{nb} & d_{nc} \end{bmatrix} \begin{bmatrix} V_{a}(t) \\ V_{b}(t) \\ V_{c}(t) \end{bmatrix}; \begin{bmatrix} I_{a}(t) \\ I_{b}(t) \\ I_{c}(t) \end{bmatrix} = \begin{bmatrix} d_{pa} & d_{na} \\ d_{pb} & d_{nb} \\ d_{pc} & d_{nc} \end{bmatrix} \begin{bmatrix} I_{dc} \\ -I_{dc} \end{bmatrix}$$

(6)

$$d_{pa} = M \begin{bmatrix} (1/2)\cos(\omega_{in}t) + \\ (7/36)\cos(2\omega_{in}t) - (1/36)\cos(4\omega_{in}t) \end{bmatrix} + 1/3$$

$$d_{pb} = M \begin{bmatrix} (1/2)\cos(\omega_{in}t - 2\pi/3) + \\ (7/36)\cos(2\omega_{in}t + 2\pi/3) - (1/36)\cos(4\omega_{in}t) \end{bmatrix} + 1/3$$

$$d_{pc} = 1 - d_{pa}(t) - d_{pb}(t)$$

$$d_{na} = M \begin{bmatrix} (-1/2)\cos(\omega_{in}t) + \\ (7/36)\cos(2\omega_{in}t) - (1/36)\cos(4\omega_{in}t) \end{bmatrix} + 1/3$$

$$d_{nb} = M \begin{bmatrix} (-1/2)\cos(\omega_{in}t) - (1/36)\cos(4\omega_{in}t) \\ (7/36)\cos(2\omega_{in}t - 2\pi/3) + \\ (7/36)\cos(2\omega_{in}t - 2\pi/3) - (1/36)\cos(4\omega_{in}t) \end{bmatrix} + 1/3$$

$$d_{nc} = 1 - d_{na}(t) - d_{nb}(t)$$

$$0 < M = \frac{4V_{de}}{3\sqrt{3}V_{ce}} < 2/\sqrt{3}$$
 (8)

Where.

$$\begin{bmatrix} V_a(t) \\ V_b(t) \\ V_c(t) \end{bmatrix} = \begin{bmatrix} V_{in} \cos(\omega_{in}t) \\ V_{in} \cos(\omega_{in}t - 2\pi/3) \\ V_{in} \cos(\omega_{in}t + 2\pi/3) \end{bmatrix};$$

$$\begin{bmatrix} I_a(t) \\ I_b(t) \\ I_c(t) \end{bmatrix} = \begin{bmatrix} I_{in} \cos(\omega_{in}t + \Phi) \\ I_{in} \cos(\omega_{in}t - 2\pi/3 + \Phi) \\ I_{in} \cos(\omega_{in}t + 2\pi/3 + \Phi) \end{bmatrix};$$

 $V_{in}$  and  $I_{in}$  are peak phase voltage and peak current respectively;  $\omega_{in}$  is ac angular speed;  $\Phi$  is input ac current phase angle;  $V_{dc}$  and  $I_{dc}$  are the output dc voltage and dc current respectively;  $d_{ij}$  (i = p, n; j = a, b, c) is duty-cycle.

### 3. Method of Modeling CASLs and Experimental Data to be Used

# 3.1 Methodology of modeling CASLs of power converters

The methodology may be grouped into two categories: one for dynamic electro thermal behavior and one for steady-state CASLs. The methodology for dynamic electrothermal behavior focuses on the power-switches in a given power converter; the relevant CASLs model of the power-switch is a physical-based model where the junction temperature is treated as a variable. Due to the complexity of the physical-based models, this methodology relies on simulation tools and has to focus on the study at a single operating-point [2],[3]. In the cases where the quick estimation of the CASLs of a power converter over a range of operating-points is required, this methodology may theoretically be used but will lead to an over complicated procedure. On the other hand, the methodology for steady-

state CASLs focuses on the total CASLs of a power converter; the relevant CASLs model of the power-switch consists of an equivalent conduction-loss model and an equivalent switching-loss model. The junction temperature in this methodology is treated as a given unchangeable condition. Due to its simplicity, this methodology does not rely on simulation tools and is able to analytically express the approximated CASLs of a power converter over a range of operating-points [4], [9]. Within this methodology, on-state voltage/resistance and turn-on/off switching energy at a given junction temperature are critical to approximate the conduction loss and switching loss respectively. A powerful and fairly accurate way is to measure these parameters and then describe the dependency of the conduction loss or the switching loss on the applied voltage and/or current in a simple equation. The equation for the conduction loss is obvious. The equation for the switching loss, however, is obtained through various ways of approximation<sup>[4]-[6], [8]</sup>. A set of the measured on-state voltage/resistance and a quadratic leastsquare approximation of the dependency of the switching energy on the switched voltage/current were reported in [6] and verified through<sup>[7]</sup>. The experimental data will be employed in this paper where the quick estimation of CASLs of MZC over a range of operating-points is required.

### 3.2 Conduction-loss model approximation

Fig.3 shows the model of IGBT or FWD as the combined voltage source and resistor in series. The tested parameters reported in [6] are listed in Table 1.

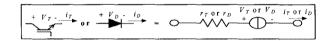


Fig. 3 Equivalent circuit of IGBT or FWD for calculating the conduction loss, where  $V_T$  is voltage drop of IGBT;  $V_D$  is forward voltage drop of FWD;  $r_T$  and  $r_D$  are on-state resistances of IGBT and free-wheel diode respectively

Table 1 Tested On-state parameters of IGBT and FWD at 120 °C of junction temperature

$T_j$	$r_T$	$r_D$	$V_T$	$\overline{V_D}$
120°C	0.0787	0.038	0.768	0.732
Units	V/A	V/A	V	V

The switch devices under discussion are gated on/off by ideal PWM signals. The conduction-loss model within every switching cycle can be approximated as given by (9).

$$p_c = r_{T/D} i_{T/Drms}^2 + v_{T/D} \langle i_{T/D} \rangle$$
 (9)

where  $i_{T/Drms}$  is the R.M.S. current within the switching cycle;  $\langle i_{T/D} \rangle$  is the average current within the switching cycle.

#### 3.3 Switching-loss model approximation

The Switching-loss model is obtained through averaging total energy losses caused by individual turn-on/off actions in a switching cycle. The dependency of the individual energy loss, w, on the switched voltage and switched current is given by (10) (11) (12). The turn-on energy loss of a diode is ignored.

$$w_{Toff} = K_{Toff1}ui + K_{Toff2}ui^2 + K_{Toff3}u^2 + K_{Toff4}u^2i + K_{Toff5}u^2i^2 = w_{Toff}(u, i)$$
(10)

$$w_{Ton} = K_{Ton1}ui + K_{Ton2}ui^2 + K_{Ton3}u^2 + K_{Ton4}u^2i + K_{Ton5}u^2i^2 = w_{Ton}(u,i)$$
(11)

$$w_{Doff} = K_{Don1}ui + K_{Don2}ui^2 + K_{Don3}u^2 + K_{Don4}u^2i + K_{Don5}u^2i^2 = w_{Doff}(u, i)$$
(12)

where u and i are the switched voltage and switched current respectively; T and D denote IGBT and FWD respectively;  $K_i$  (i = 1, 2, ....5) is the coefficient for approximation listed in Table 2 [6].

Table 2 Coefficients of the least-square approximation of the measured IGBT/FWD switching losses at 120 °C junction temperature  $(T_i)^{[6]}$ 

$T_j$		<i>K</i> <sub>1</sub>	<i>K</i> <sub>2</sub>	<b>K</b> <sub>3</sub>	<i>K</i> ₄	<b>K</b> 5
	$T_{off}$	179	- 1.31	0.650	-0.116	0.0034 8
120° C	$T_{on}$	70.0	2.94	0.518	0.102	0.0015 5
	$D_{off}$	97.7	3.73	0.488	0.140	0.0042 7
Units		nWs (VA) <sup>-1</sup>	nWs (VA <sup>2</sup> ) <sup>-1</sup>	nWs(V	nWs(V <sup>2</sup> A) <sup>-1</sup>	nWs(V <sup>2</sup> A <sup>2</sup> ) <sup>-1</sup>

### 4. Average CASLs Model of the Powerswitch Network of Z-source Inverter

The analytical model of power loss for the Z-source inverter is developed in this section. The CASLs of the Z-source inverters is evenly distributed, hence, can be approximated by examining the CASLs of one pair of IGBT and its FWD, i.e. the  $T_{pa}$  and  $D_{na}$  shown in Fig. 1, where current  $i_a$  refers  $I_a(t)$  of (1). Switching frequency is assumed much higher than the line frequency.

# 4.1 Conduction Loss model of Z-source Inverter 4.1.1 Conduction loss Caused by IGBT T<sub>pa</sub> in Z-source Inverter

When the ac load current  $i_a$  is in the positive-half cycle, i.e.  $i_a > 0$ , within every switching cycle, the current crossing the  $T_{pa}$  consists of the shoot-through current and ac load current. Considering Fig. 4, one has (13) and (14) respectively.

$$\left\langle i_{Tpa}\right\rangle = D_0 \frac{2}{3} I_L + d_{pa} i_a \tag{13}$$

$$i_{Tparms}^{2} = D_{0} \left(\frac{2}{3}I_{L} + \frac{i_{a}}{2}\right)^{2} + \left(d_{pa} - \frac{D_{0}}{2}\right)i_{a}^{2}$$
 (14)

where  $\langle i_{Tpa} \rangle$  is the average current over switching cycle;  $i_{Tparms}$  is the R.M.S current over switching cycle;  $D_{\theta}$  is the shoot-through duty-cycle;  $I_{L}$  is the average Z-source inductor current;  $d_{pa}$  is the duty-cycle of  $T_{pa}$ ,  $i_{a}$  is the ac load current.

In the negative-half cycle, i.e.  $i_a < 0$ , only the shoot-through current crosses  $T_{pa}$ , as that of  $i_{Tna}$  in Fig. 4. The average and R.M.S. currents are

$$\left\langle i_{T_{pa}} \right\rangle = D_0(\frac{2}{3}I_L + \frac{i_a}{2}) \tag{15}$$

$$i_{Tparms}^2 = D_0 (\frac{2}{3} I_L + \frac{i_a}{2})^2$$
 (16)

The average conduction loss caused by  $T_{pa}$  over line cycle, therefore, is given by (17)

$$P_{\eta p a c} = \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} (r_{I} i_{\eta p a m s}^{2} + V_{T} \langle i_{\eta p a} \rangle) d\varphi$$

$$= r_{T} \left[ \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} D_{0} (\frac{2}{3} I_{L} + \frac{i_{a}}{2})^{2} d\varphi + \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} (d_{p a} - \frac{D_{0}}{2}) i_{a}^{2} d\varphi \right]$$

$$+ V_{T} \left[ \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} (D_{0} \frac{2}{3} I_{L} + d_{p a} i_{a}) d\varphi + \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} D_{0} (\frac{2}{3} I_{L} + \frac{i_{a}}{2}) d\varphi \right]$$
(17)

where  $\varphi = \omega t$ ;  $i_a$  is  $I_a(t)$  in (1);  $D_0$  was given by (4).

Replacing variables of  $i_a$ ,  $d_{pa}$  and  $D_{\theta}$  in (17). by those in (1), (2) and (4), after some trigonometric operation, the average conduction loss caused by IGBT  $T_{pa}$  may be approximated as given by (18), assuming that the power loss is significantly smaller than the active power flow in a proper designed Z-source converter.

$$P_{\text{go.}c} = \begin{bmatrix} r_{y} \left( I_{x^{2}} \left( \frac{1}{8} + \frac{M \cos \Phi}{3\pi} - \frac{M \cos 3\Phi}{90\pi} \right) + I_{x}^{2} \frac{2(2 - \sqrt{3}M)}{9} \right) + I_{x}^{2} \left( I_{x} \left( \frac{1}{2\pi} + \frac{M \cos \Phi}{8} \right) + I_{x}^{2} \left( \frac{2 - \sqrt{3}M}{2} \right) \right) \end{bmatrix}$$
(18)

where,

$$I_L = \frac{P_o}{V_{dc}} \tag{19}$$

$$I_{pk} = \frac{4}{3} \frac{\sqrt{3}M - 1}{M\cos\Phi} \frac{P_o}{V_{dc}}$$
 (20)

where  $I_L$  is the average Z-source inductor current;  $I_{pk}$  is peak ac load current;  $P_o$  is the active power; M,  $V_{dc}$  and  $\Phi$  were defined in (1), (2) and (3).

# 4.1.2 Conduction loss caused by FWD $D_{na}$ in Z-source Inverter

Only in the positive-half line cycle can the FWD  $D_{na}$  carry load current, as in Fig. 4. The average current and the R.M.S. current of  $i_{Dna}$  over switching cycle is given by (21) and (22).

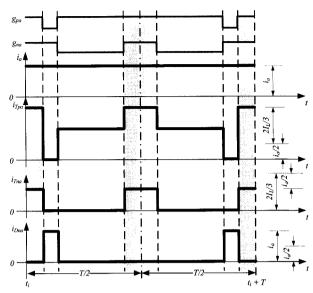


Fig. 4 Waveforms of  $T_{pa}$  and  $D_{na}$  of Fig.1 in one switching cycle when  $i_a > 0$ , where shadowed are shoot-through intervals.  $g_{pa}$  and  $g_{na}$  are gate-drive logic of  $T_{pa}$  and  $T_{na}$  respectively.

$$\langle i_{Dna} \rangle = (1 - d_{pa} - \frac{D_0}{2})i_a = (d_{na} - \frac{D_0}{2})i_a$$
 (21)

$$i^{2}_{Dnarms} = (d_{na} - \frac{D_{0}}{2})i_{a}^{2}$$
 (22)

where  $\langle i_{Dna} \rangle$  is the average current;  $i_{Dnarms}$  is the R.M.S current;  $d_{na}$  is the duty-cycle of  $D_{na}$ ,  $i_a$  is the ac load current. Therefore, the average conduction loss caused by  $D_{na}$  over line cycle is given by (23).

$$P_{Dna,c} = \frac{1}{2\pi} \int_{\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} (r_D i^2_{Dnarms} + V_D \langle i_{Dna} \rangle) d\varphi$$

$$= r_D \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} (d_{na} - \frac{D_0}{2}) i_a^2 d\varphi \right] + V_D \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} (d_{na} - \frac{D_0}{2}) i_a d\varphi \right]$$
(23)

where  $\varphi = \omega t$ ;  $\Phi$  is ac current phase angle;  $i_a = I_a(t)$ . Replacing variables of  $d_{na}$ ,  $i_a$ , in (23) by those in (1) and (2), after some trigonometric operation, the average conduction loss caused by free-wheel diode  $D_{na}$  can be approximated as given by (24).

$$P_{Dna,c} = \begin{bmatrix} r_D I_{pk}^2 \left( \frac{1 - D_0}{8} - \frac{M \cos \Phi}{3\pi} + \frac{M \cos 3\Phi}{90\pi} \right) + \\ V_D I_{pk} \left( \frac{1 - D_0}{2\pi} - \frac{M \cos \Phi}{8} \right) \end{bmatrix}$$
(24)

where  $I_{pk}$  was given by (20).

# 4.1.3 Total average conduction loss in Z-source Inverter

Since the loss is evenly distributed in the power-switch network of the Z-source inverter, the total conduction loss can be approximated through (18) and (24) as given by (25).

$$P_{z,c} = 6 \times (P_{Ipa,c} + P_{Dna,c})$$

$$= 6 \times \begin{bmatrix} r_T I_{pk}^2 \left( \frac{1}{8} + \frac{M\cos\Phi}{3\pi} - \frac{M\cos3\Phi}{90\pi} \right) + r_T \left( \frac{2}{3} I_L \right)^2 D_0 + \\ V_T I_{pk} \left( \frac{1}{2\pi} + \frac{M\cos\Phi}{8} \right) + V_T I_L D_0 + \\ r_D I_{pk}^2 \left( \frac{1 - D_0}{8} - \frac{M\cos\Phi}{3\pi} + \frac{M\cos3\Phi}{90\pi} \right) + \\ V_D I_{pk} \left( \frac{1 - D_0}{2\pi} - \frac{M\cos\Phi}{8} \right) \end{bmatrix}$$
(25)

where  $D_{\theta}$ ,  $I_L$  and  $I_{pk}$  were given by (4), (19) and (20) respectively.

# 4.2 Switching loss model of Z-source Inverter 4.2.1 Switching loss caused by IGBT Tpa in Zsource Inverter

As shown in As shown in, when the ac load current is positive, i.e.  $i_a > 0$ , the  $T_{pa}$  in the Z-source inverter has four switching actions. Two of them, i.e. one turn-on and one turn-off in a non-shoot-through interval, are the same as that in an ordinary VSI, in which the switched voltage is the peak dc-link voltage and the switched current is the ac load current. The other two switching actions, one turn-on and one turn-off during the shoot-through interval, are imposed by the unique shoot-through actions. The switched voltage is still the peak dc-link voltage while the switched current is  $2/3I_L+i_a/2$ . Thus, the energy loss,  $w_I$ , within switching cycle can be approximated using (10) and

(11), as given by (26).

$$w_{l} = w_{Tonoff} \left( V_{pn}, \left( \frac{2}{3} I_{L} + \frac{i_{a}}{2} \right) \right) + w_{Tonoff} \left( V_{pn}, i_{a} \right)$$
 (26)

where  $w_I$  is the energy loss of  $T_{pa}$  in a switching cycle when  $i_a$  is positive.  $w_{Tonoff}$  has the same form of  $w_{off}(u,i)$  or  $w_{on}(u,i)$  where the coefficients  $K_{Toni}$  or  $K_{Toffi}$  becomes  $K_{Tonoffi} = K_{Toni} + K_{Toffi}$ , i = 1, 2, ...5;  $V_{pn}$  is the peak dc-link voltage of Z-source inverter;  $I_L$  is in (19);  $i_a$  is the load current.

When ac load current is negative, i.e.  $i_a < 0$ , the  $T_{pa}$  carries the current in the same way as that of  $T_{na}$  with  $i_a > 0$  in. Thus, switching actions of  $T_{pa}$  can be illustrated by  $i_{Tna}$  of  $T_{na}$  in Fig. 4. The waveform of  $i_{na}$  shows that the most left-hand turn-off is zero-voltage switching actions because the terminal voltage of  $T_{na}$  is clamped to almost zero voltage by the anti-parallel diode  $D_{na}$ , which matches the most right-hand turn-on. Hence, the relevant switching losses may be ignored. Only turn-on/off occurring in the middle position is taken into account. From the approximation model in (10) and (11), one has

$$w_2 = w_{Tonoff} \left( V_{pn}, \left( \frac{2}{3} I_L + \frac{i_a}{2} \right) \right) \tag{27}$$

where  $w_2$  is the switching energy loss of  $T_{pa}$  per PWM cycle in the negative-half cycle;  $w_{Tonoff}$  was defined in (26). Thus

$$P_{Tpa,sw} = f_{sw} \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} (w_1 + w_2) d\varphi \right]$$

$$= f_{sw} \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} w_{Tonoff} (V_{pn}, \left(\frac{2}{3}I_L + \frac{i_a}{2}\right)) d\varphi \right]$$

$$+ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} w_{Tonoff} (V_{pn}, i_a) d\varphi$$

$$(28)$$

where  $P_{Tpa,sw}$  is the average switching loss in one line cycle. Replacing  $i_a$  by that in (1) and (2) with some trigonometric operation,

$$P_{Tpa,sw} = f_{sw} \left[ \frac{3}{2} K_{T3} V_{pn}^{2} + (K_{T1} V_{pn} + K_{T4} V_{pn}^{2}) (\frac{3}{2\pi} I_{pk} + \frac{2}{3} I_{L}) + (K_{T2} V_{pn} + K_{T5} V_{pn}^{2}) (\frac{1}{\pi} I_{pk} I_{L} + \frac{5}{16} I_{pk}^{2} + \frac{4}{9} I_{L}^{2}) \right]$$

(29)

where  $K_{Ti}=K_{Ton,i}+K_{Toff,b}$  i=1,2,..5;  $f_{sw}$  is the switching frequency;  $V_{pn}$ ,  $I_L$  and  $I_{pk}$  were given by (5), (19) and (20) respectively.

### 4.2.2 Switching loss cause by Diode Dna in Zsource Inverter

 $D_{na}$  carries current only in the positive half cycle of load current. The turn-on switching loss of a diode is ignored. The waveform of  $i_{Dna}$  in Fig. 4 shows that the most right-hand turn-off of the diode is a zero-voltage turn-off due to the switched voltage clamped by  $T_{na}$ , hence, the relevant switching loss is ignored. Thus, only the turn-off at the left-hand contributes to switching loss energy

$$W_{Doff} = W_{Doff}(V_{pn}, i_a) \tag{30}$$

where  $V_{pn}$  was given in (5);  $i_a$  is the load current.

The average switching power loss of  $D_{na}$  in one line-cycle is

$$P_{Dna,iw} = f_{iw} \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{3\pi}{2} + \Phi} w_{Doff} d\varphi \right] = f_{iw} \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} w_{Doff} d\varphi \right]$$

$$= f_{iw} \left[ \frac{1}{2\pi} \int_{-\frac{\pi}{2} + \Phi}^{\frac{\pi}{2} + \Phi} w_{Doff} (V_{pn}, i_a) d\varphi \right]$$
(31)

Replacing  $i_a$  by the  $I_a(t)$  in (1), the average switching power loss of the FWD can be approximated by (32).

$$P_{Dna,sw} = f_{sw} \begin{bmatrix} K_{D3}V_{pn}^{2} + (K_{D1}V_{pn} + K_{D4}V_{pn}^{2})\frac{1}{\pi}I_{pk} \\ + (K_{D2}V_{pn} + K_{D5}V_{pn}^{2})\frac{1}{4}I_{pk}^{2} \end{bmatrix}$$
(32)

where  $K_{Di}=K_{Doff,b}$  i=1,2,...5;  $f_{sw}$  is the switching frequency;  $V_{pn}$  and  $I_{pk}$  were given by (5) and (20) respectively.

### 4.2.3 Total average switching loss in Z-source Inverter

Since the switching power loss is evenly distributed, the total average switching loss can be approximated by

$$P_{z,sw} = 6 \times (P_{Tpa,sw} + P_{Dna,sw})$$

$$= 6 \times f_{sw} \begin{bmatrix} \frac{3}{2} K_{T3} V_{pn}^{2} + (K_{T1} V_{pn} + K_{T4} V_{pn}^{2}) (\frac{3}{2\pi} I_{pk} + \frac{2}{3} I_{L}) + \\ (K_{T2} V_{pn} + K_{T5} V_{pn}^{2}) (\frac{1}{\pi} I_{pk} I_{L} + \frac{5}{16} I_{pk}^{2} + \frac{4}{9} I_{L}^{2}) + \\ K_{D3} V_{pn}^{2} + (K_{D1} V_{pn} + K_{D4} V_{pn}^{2}) \frac{1}{\pi} I_{pk} + \\ (K_{D2} V_{pn} + K_{D3} V_{pn}^{2}) \frac{1}{4} I_{pk}^{2} \end{bmatrix}$$
(33)

where parameters have been defined in (29) And (32).

### 5. Average CASLs Model of the Threephase ac-dc Matrix Converter

## 5.1 Average conduction-loss model of ac-dc matrix converter

It is well known that ac load current dominates the average conduction loss of an ac-ac matrix converter. For the case of ac-dc matrix, dc load current dominates

$$P_{mc,c} = 2[(V_T + V_D)I_{dc} + (r_T + r_D)I_{dc}^2]$$
(34)

where  $P_{mc,c}$  is the average conduction loss; the square bracketed item is the conduction loss per output phase.

### 5.2 Average switching loss model of ac-dc matrix converter

The model of switching loss of ac-dc matrix converter is not as obvious as that of the conduction loss. For the convenience of discussion, Fig. 5 presents the timing diagram of a switching cycle in an arbitrary  $60^{\circ}$ -sector of line-cycle; Fig. 6 illustrates the detail switching actions within the commutation period  $T_{CM}$  immediately after the instant  $t_{CMp1}$  in Fig. 5. The basic condition for the discussion is that the sequence of current commutation is in the way of " $a \rightarrow b \rightarrow cc \rightarrow b \rightarrow a$ " all the time as shown in Fig. 5, and that the four-step method in Fig. 6 is used for every commutation. The ac source is assumed three-phase balanced. Gate-drives for individual switches are assumed

ideal and lossless. Switched voltage that is equal to the forward voltage drop of IGBT or FWD does not contribute to switching loss.

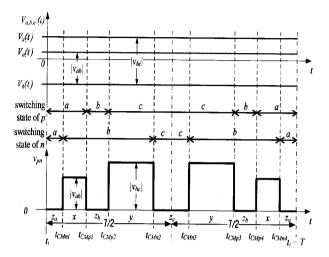


Fig. 5 One instance of switching states of the circuit in Fig.2 in one switching cycle T, where x and y are the intervals of active states;  $z_{av}$   $z_b$ , and  $z_c$  are the ones of zero-states;  $t_{CMpi}$  and  $t_{CMni}$  (i = 1, 2, 3, 4) are the instants of current commutation of phase p and n respectively

At instant  $t_{CMp1}$  in the left-hand half switching cycle of Fig. 5, when  $i_p$  commutates from phase a to b, the switching actions are the turn-off of the switch-cell  $S_{na}$  and the turn-on of  $S_{pb}$ ; no switching action occurs in the switchcell  $S_{pc}$ ; the switched voltage is  $v_{ab}$ . Examining Fig. 6. shows that, when  $i_p$  is positive, i.e. the forward current, the turn-off of the backward switch  $S_{paB}$  at  $t_1$  is a zero-current turn-off (ZC-off) not producing switching loss due to the absence of backward current; the turn-on of the forward switch  $S_{pbF}$  at  $t_2$  is a zero-current turn-on (ZC-on) not producing switching loss because its reversed terminal voltage under the condition of line voltages  $(V_a(t)>V_b(t))$ blocks the forward current during the turn-on; the turn-off of the forward switch  $S_{paF}$  at  $t_3$  is a non-zero-current turnoff (NZC-off) certainly producing switching loss due to the existence of switched current; the turn-on of the backward switch  $S_{pbB}$  at  $t_4$  is a ZC-on not producing switching loss due to the absence of backward current. At instant  $t_{CMp4}$ with the same switched voltage of  $v_{ab}$ , by symmetry of the switching states as shown in Fig. 5, switch-cell  $S_{pa}$ produces the switching loss through a non-zero-current

turn-on (NZC-on) of forward switch  $S_{paF}$  when the forward current  $i_p$  commutates from phase b back to a. Similar examination applied to the two instants at  $t_{CMp2}$  and  $t_{CMp3}$  shows that the NZC-on and NZC-off occur in the switch-cell  $S_{pc}$ , and produce switching loss at the two instants respectively when forward current commutates between phase b and c with the switched voltage of  $v_{bc}$ . Details of the examination are ignored for abbreviation. Thus, with the common switched current, two combinations of NZC-on and NZC-off produce switching loss with two switched voltages  $v_{ab}$  and  $v_{bc}$  respectively.

Note that the switching cycle and 60°-sector of linecycle are arbitrarily selected in the aforementioned examination, and that the line-to-line voltage  $v_{ca}$  has no chance to be the switched voltage due to the definite absence of the current commutation between phase a and c for the given commutation sequence of " $a \rightarrow b \rightarrow cc \rightarrow b \rightarrow a$ " all the time. The examination may be applied to the other 60°-sectors, revealing that the difference in the switching actions between different sectors is merely the way how the two combinations of the NZC-on and NZC-off are allocated, as shown in Table 3. Considering the IGBTs and FWDs used in the switch-cells are identical, the common facts from the examination about the switching loss of output phase p with forward current is that the switching loss is caused by two and only two combinations of NZCon and NZC-off at switched voltages  $v_{ab}$  and  $v_{bc}$ respectively.

Therefore, using (10), (11), and (12), switching energy within one switching cycle in the output phase p may be approximated as given by (35).

$$\begin{split} w_{sw} &= \begin{bmatrix} w_{Ton}(v_{ab}, I_{dc}) + w_{Toff}(v_{ab}, I_{dc}) + w_{Doff}(v_{ab}, I_{dc}) + \\ w_{Tom}(v_{bc}, I_{dc}) + w_{Toff}(v_{bc}, I_{dc}) + w_{Doff}(v_{bc}, I_{dc}) + \end{bmatrix} \\ &= w_{TonoffDoff}(v_{ab}, I_{dc}) + w_{TonoffDoff}(v_{bc}, I_{dc}) \\ &= w_{sw}(K_{i}, v_{ab}, I_{dc}) + w_{sw}(K_{i}, v_{bc}, I_{dc}) \end{split}$$

$$(35)$$

where  $K_i = K_{iTon} + K_{iToff} + K_{iDoff}$ ;  $K_{iTon}$ ,  $K_{iToff}$ , and  $K_{iDoff}$  are in Table 2(i = 1, 2, ...5);  $w_{sw}(K_b, v_{ab}, I_{dc})$  and  $w_{sw}(K_b, v_{bc}, I_{dc})$  are the switching energy loss when switched voltage are  $v_{ab}$ , and  $\underline{v_{bc}}$  respectively;  $I_{dc}$  is the forward current equal to the output dc current. From the model (6),  $v_{ab}$  and  $v_{bc}$  are

$$v_{ab} = \sqrt{3}V_{in}\cos(\varphi_{in} + \pi/6); \quad v_{bc} = \sqrt{3}V_{in}\cos(\varphi_{in} - \pi/2)$$
(36)

where  $\varphi_{in} = \omega_{in}t$ ;  $\omega_{in}$  and  $V_{in}$  were defined in (6).

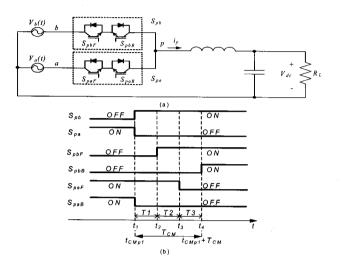


Fig. 6 Illustration of four-step commutation at the instant  $t_{CMp1}$  in Fig. 5 when the forward current of output phase p commutates from phase a to b (a) the simplified circuit, where each physical switch is comprised of a combination of one IGBT and one FWD in series; F and B denote forward and backward respectively. (b) the timing diagram of four-step commutation, where  $S_{pa}$  and  $S_{pb}$  are logic signals for switch-cells;  $S_{pjk}$  (j = a, b; k = F, B) are on/off states of the physical switches;  $T_{CM}$  is the commutation period.

Table 3 Feature of switching actions of the switch-cells connected to the output phase p in each  $60^{\circ}$ -sector of line-cycle according to the given sequence of current commutation and the four-step commutation method

	Sectors	Switch- cells	a → b	b → c	c → b	b → a
		$S_{pa}$	NZC- off			NZC- on
1	$v_a > v_b > v_c$	$S_{pb}$	ZC-on	NZC- off	NZC- on	ZC-off
		$S_{pc}$		ZC-on	ZC-off	
		$S_{pa}$	ZC -off			ZC -on
2	$v_b > v_c > v_a$	$S_{pb}$	NZC -	NZC- off	NZC- on	NZC - off
		$S_{pc}$		ZC-on	ZC-off	

	Sectors	Switch- cells	a → b	b → c	c <b>→</b> b	b → a
		$S_{pa}$	NZC - off			NZC - on
3	$v_c > v_a > v_b$	$S_{pb}$		ZC-off	ZC-on	ZC -off
		$S_{pc}$		NZC-	NZC-	
il				on	off	
П		$S_{pa}$	ZC -off			ZC -on
4	$v_c > v_b > v_a$	$S_{pb}$	NZC -	ZC-off	ZC-on	NZC - off
		$S_{pc}$		NZC-	NZC-	
		pc		on	off	
		$S_{pa}$	ZC -off			ZC -on
5	$v_b > v_a > v_c$	$S_{pb}$	NZC -		NZC-	
	1		on	off	on	off
		$S_{pc}$		ZC-on	ZC-off	
		$S_{pa}$	NZC -			NZC -
			off			on
6	$v_a > v_c > v_b$	$S_{pb}$	ZC -on	ZC-off	ZC-on	ZC -off
		$S_{pc}$		NZC-	NZC-	
L				on	off	

From (35) and(36), by some trigonometric operation, the average switching loss in the output phase p in one switching cycle,  $p_{swsw}$ , can be approximated as given by (37).

$$P_{swsw} = f_{sw} W_{sw}$$

$$= f_{sw} (W_{sw} (K_i, v_{ab}, I_{dc}) + W_{sw} (K_i, v_{bc}, I_{dc}))$$

$$= A \sqrt{3} V_{in} \cos(\varphi_{in} - \pi/6) + 3B V_{in}^{2} (1 - 0.5 \cos 2(\varphi_{in} - \pi/6))$$
(37)

where  $f_{sw}$  is the switching frequency;  $A = K_1 I_{dc} + K_2 I_{dc}^2$  and  $B = K_3 + K_4 I_{dc} + K_5 I_{dc}^2$ ;  $K_i$  (i = 1, 2, ...5) were defined in (35);  $\varphi_{in} = \omega_{in}t$ ;  $\omega_{in}$  and  $V_{in}$  were defined in (6).

The average switching loss in the output phase p in one line-cycle,  $p_{swph}$ , is

$$p_{swph} = \frac{1}{2\pi} \int_{0}^{2\pi} p_{swsw} d\varphi_{in} = \frac{3}{\pi} \int_{-\pi/6}^{\pi/6} p_{swsw} d\varphi_{in} = f_{sw} (1.43 \, A \, V_{in} + 2.38 \, B \, V_{in}^{2})$$
(38)

where A and B were defined in (37);  $V_{in}$  was defined in (6).

The average switching loss in output phase n is the same as that in output phase p because of the balanced input voltages and the identical switch-cells. Therefore, the average switching power loss of the whole ac-dc matrix converter is

$$P_{mc,sw} = 2 \times p_{swph} = f_{sw} \begin{bmatrix} 4.76K_3V_{in}^2 + (2.86K_1V_{in} + 4.76K_4V_{in}^2)I_{dc} \\ +(2.86K_2V_{in} + 4.76K_5V_{in}^2)I_{dc}^2 \end{bmatrix}$$
(39)

where  $K_i$  (i = 1, 2, ....5) were defined in (35);  $f_{sw}$  is the switching frequency;  $I_{dc}$  and  $V_{in}$  were defined in (6). Thus, the average switching power loss,  $P_{mc,sw}$ , of the whole acdc matrix converter has dependency on output dc load current and input ac peak phase voltage. Considering the relation in (8), one has

$$V_{in} = 4V_{dc} / (3\sqrt{3}M) \tag{40}$$

Replacing  $V_{in}$  in (39) with that in (40), the  $P_{mc,sw}$  becomes

$$P_{mc,sw} = f_{sw} \begin{bmatrix} \frac{2.12K_3V_{dc}^2}{3/4M^2} + I_{dc}(\frac{1.91K_1V_{dc}}{\sqrt{3}/2M} + \frac{2.12K_4V_{dc}^2}{3/4M^2}) \\ + I_{dc}^2(\frac{1.91K_2V_{dc}}{\sqrt{3}/2M} + \frac{2.12K_5V_{dc}^2}{3/4M^2}) \end{bmatrix}$$
(41)

where  $f_{sw}$  is the switching frequency;  $I_{dc}$  and  $V_{dc}$  were defined in (6), and M in (8).

It can be seen from (34) and (41) that the conduction and switching losses in an ac-dc matrix converter has no dependency on  $\cos(\Phi)$ , i.e. the power factor (pf).

### 6. Average CASLs Model of the Proposed MZC

Thus far, the power loss approximation has been investigated for power-switch network in a Z-source inverter or ac-dc matrix converter. MZC marries up both structures of Z-source inverter and ac-dc matrix converter. Therefore, its power loss approximation for the power-switch network can be examined now. Table 4 shows the conditions for the calculation. The calculated results will be converted into the form of "mWatts per Watt" as given by (42) for the convenience of visualization.

$$P'_{loss} = \frac{P_{loss}}{P_o} \times 1000 \tag{42}$$

where  $P'_{loss}$  is the result to be visualized;  $P_{loss}$  is the calculated loss at certain operating point indicated by a pair of modulation index (M) and power factor (pf) in Table;  $P_o$  is defined in Table 4.

Table 4 Conditions for the calculation of power loss using the analytical model of conduction and switching losses of MZC

Symbo		Values		
1	Description	For dc-ac inversion	For ac-dc rectification	
pf	cos(Φ)	0.7 < pf < 1.0	0.7 < pf < 0.9	
М	Modulation index	0.866 < M < 1.155	0.5 < M < 1.155	
$V_{dc}$	dc voltage	36 V	42 V	
Po	Active power	2000 W	2000 W	
f <sub>sw</sub>	Switching frequency	10 kHz	10 Hz	

## 6.1 Average CASLs Model of the proposed MZC in dc-ac inversion mode

# 6.1.1 Average conduction loss of the proposed MZC in dc-ac inversion mode

In dc-ac operation mode, the MZC operates as a *Z*-source inverter in which each switch consists of two commonemitter connected IGBTs with respective anti-paralleled FWDs. One of the two IGBTs is set at on-state all the time, and the other one serves as an active IGBT as shown in Fig. 7(a) <sup>[1]</sup>. Fig. 7(b) presents the equivalent configuration. Fig. 7 (c) shows the equivalent model during the on-state of the active IGBT. For this reason, the  $V_T$ ,  $V_D$ ,  $r_T$ , and  $r_D$ , used in (18)–(25) for the approximation of average conduction loss are replaced by  $V_{T+D}$ ,  $V_{D+T}$ ,  $r_{T+D}$ , and  $r_{D+T}$  respectively.  $V_{T+D}$ ,  $V_{D+T}$ ,  $r_{T+D}$ , and  $r_{D+T}$  are given by (43) and (44).

$$V_{T+D} = V_{D+T} = V_T + V_D (43)$$

$$r_{T+D} = r_{D+T} = r_T + r_D (44)$$

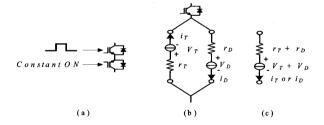


Fig. 7 Equivalent model of IGBT and FWD in MZC when MZC is in dc-ac inversion mode, (a) illustrative gatedrive signals and common-emitter IGBT-pair, (b) active switching IGBT and the model of constant-on IGBT, (c) model of whole common-emitter IGBT-pair

Equations (18) and (24) share the same parameters,

hence the average conduction loss of Z-source inverter given by (25) can be arranged in (45)

$$P_{mzc-dcac,c} = 6 \times \begin{bmatrix} r_{T+D} I_{pk}^{2} \left( \frac{2 - D_{0}}{8} \right) + r_{T+D} \left( \frac{2}{3} I_{L} \right)^{2} D_{0} + V_{T+D} I_{pk} \left( \frac{2 - D_{0}}{2\pi} \right) + V_{T+D} I_{L} D_{0} \end{bmatrix}$$

$$(45)$$

Where

$$I_L = \frac{P_o}{V_{dc}}; \quad I_{pk} = \frac{4(\sqrt{3}M - 1)P_o}{3MV_{dc}\cos\Phi}; \quad D_0 = 1 - \frac{\sqrt{3}M}{2}$$

The calculated result using the given values for dc-ac inversion in Table 4 is visualized in Fig. 8(a1).

# 6.1.2 Average switching loss of the proposed MZC in dc-ac inversion mode

MZC in dc-ac inversion mode operates as the Z-source inverter. The average switching loss then can be approximated by (29), (32), and (33). One has Switching loss caused by IGBT  $T_{pa}$ 

$$P_{mac-descTpa,sw} = f_{sw} \left[ \frac{3}{2} K_{T3} V_{pn}^{2} + (K_{T1} V_{pn} + K_{T4} V_{pn}^{2}) (\frac{3}{2\pi} I_{pk} + \frac{2}{3} I_{L}) + (K_{T2} V_{pn} + K_{T5} V_{pn}^{2}) (\frac{1}{\pi} I_{pk} I_{L} + \frac{5}{16} I_{pk}^{2} + \frac{4}{9} I_{L}^{2}) \right]$$

(46)

where  $K_{Ti}$  (i=1,2,...) is no longer the same one in (29) the one in the following expression because of the extra diode in series with  $T_{pa}$ , shown in Fig.7.

$$K_{Ti} = K_{Ton,i} + K_{Toff,i} + K_{Doff,i}$$
 (47)

Switching loss caused by FWD  $D_{na}$  is

$$P_{mzc-dcacDna,sw} = f_{sw} \begin{bmatrix} K_{D3}V_{pn}^{2} + (K_{D1}V_{pn} + K_{D4}V_{pn}^{2})\frac{1}{\pi}I_{pk} \\ + (K_{D2}V_{pn} + K_{D5}V_{pn}^{2})\frac{1}{4}I_{pk}^{2} \end{bmatrix}$$
(48)

where  $K_{Di}=K_{Doff,j}$  (i=1,2,...) is the same as defined (32),

since the constant on-state IGBT in series with the diode is merely offering a conduction path without active switching actions. The model for the approximation of the average switching loss of MZC in dc-ac inversion is

$$P_{mc-drac,sw} = 6 \times (P_{mc-drac} I_{pa,sw} + P_{mc-drac} I_{pa,sw})$$

$$= 6 \times f_{sw} \left\{ \begin{bmatrix} \frac{3}{2} K_{I3} V_{pn}^{2} + (K_{I1} V_{pn} + K_{I4} V_{pn}^{2}) (\frac{3}{2\pi} I_{pk} + \frac{2}{3} I_{L}) \\ + (K_{I2} V_{pn} + K_{I5} V_{pn}^{2}) (\frac{1}{\pi} I_{pk} I_{L} + \frac{5}{16} I_{pk}^{2} + \frac{4}{9} I_{L}^{2}) \end{bmatrix} \right\}$$

$$+ \left[ K_{D3} V_{pn}^{2} + (K_{D1} V_{pn} + K_{D4} V_{pn}^{2}) \frac{1}{\pi} I_{pk} \\ + (K_{D2} V_{pn} + K_{D5} V_{pn}^{2}) \frac{1}{4} I_{pk}^{2} \right]$$

$$(49)$$

where

$$I_L = \frac{P_o}{V_{ck}}; \quad I_{pk} = \frac{4}{3} \frac{\sqrt{3}M - 1}{M\cos\Phi} P_o; \quad V_{pm} = \frac{1}{\sqrt{3}M - 1} V_{ck}$$

The calculated result using the given values for dc-ac inversion in Table 4 is visualized in Fig. 8(a2).

#### 6.1.3 Average CASLs of MZC in dc-ac mode

By the results in the previous two sub-sections, the total average loss caused by power semiconductors in dc-ac mode of MZC can be approximated as given by (50).

$$P_{mx-dxx} = P_{mx-dxx,c} + P_{mx-dxx,sw}$$
 (50)

where  $P_{mzc-dcac,c}$  and  $P_{mzc-dcac,sw}$  are given in (45) and (49) respectively. The calculated result using the given values for dc-ac inversion in Table 4 is visualized in Fig. 8(a3).

## 6.2 Average CASLs Model of the proposed MZC in ac-dc rectification mode

In ac-dc rectification, the MZC is operated as ac-dc matrix converter shown in Fig. 2. The conduction loss and switching loss models of ac-dc matrix converter in (34) and (41) of section 5 can be used straightaway. The conduction loss  $P_{mzc\text{-}acdc,c}$ , switching loss  $P_{mzc\text{-}acdc,sw}$ , and CASLs  $P_{mzc\text{-}acdc}$  of MZC in ac-dc rectification mode are given by(51), (52), and (53) respectively.

$$P_{mzc-acdc,c} = P_{mc,c}$$

$$= 2[(V_T + V_D)I_{dc} + (r_T + r_D)I_{dc}^2]$$
(51)

$$P_{mzc-acdc,sw} = P_{mc,sw}$$

$$= f_{sw} \begin{bmatrix} \frac{2.12K_3V_{dc}^2}{3/4M^2} + I_{dc} \left( \frac{1.91K_1V_{dc}}{\sqrt{3}/2M} + \frac{2.12K_4V_{dc}^2}{3/4M^2} \right) \\ + I_{dc}^2 \left( \frac{1.91K_2V_{dc}}{\sqrt{3}/2M} + \frac{2.12K_5V_{dc}^2}{3/4M^2} \right) \end{bmatrix}$$
(52)

$$P_{mzc-acdc} = P_{mzc-acdc,c} + P_{mzc-acdc,sw}$$
 (53)

where  $V_{dc}$  and  $I_{dc}$  are dc voltage and dc current respectively; M is modulation index,  $0 < M < 2/\sqrt{3}$ ;  $K_i = K_{Ton,i} + K_{Toff,i} + K_{Doff,i}$  is the switching loss parameters given by Table 2;  $r_T$ ,  $r_D$ ,  $v_T$ , and  $v_D$  are On-state parameters given by Table 1.

Fig. 8(b1 - b3) are the visualized results of conduction loss, switching loss, and CASLs of MZC in the condition of ac-dc rectification mode in Table 4, in which dc voltage is 42 V.

#### 7. Conclusion

The analytical models for the approximation of the conduction and switching losses of the power-switch network in the MZC have been achieved.

When the MZC is in dc-ac inversion mode, the

analytical model for MZC is the same as that for the Z-source inverter except that the parameters of on-state resistance and forward voltage drop used in the approximation of conduction loss for MZC are higher than those for the Z-source inverter.

When the MZC is in ac-dc rectification mode, both the analytical models and the parameters in calculation are the same as that for the ac-dc matrix converter.

For the practice of engineering design work, the models developed in this paper are ready for use in the estimation of CASLs of Z-source inverters, ac-dc matrix converters, or MZC, after the acquisition of the experimental data of the on-state and switching energy of employed power-switches.

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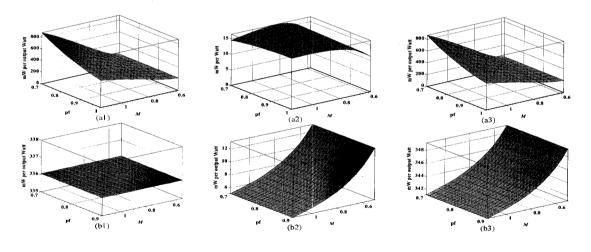


Fig. 8 Visualized losses of MZC. (a1), (a2), and (a3) are conduction loss, switching loss, and CASLs of MZC respectively when  $V_{dc} = 36 \text{ V}$  in dc-ac inversion mode; (b1), (b2), and (b3) are conduction loss, switching loss, and CASLs of MZC respectively when  $V_{dc} = 42 \text{ V}$  in ac-dc rectification mode.

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