

# Analysis of Piled Piers Considering Riverbed Scouring

## 교각세굴을 고려한 말뚝기초의 해석

Jeong, Sang-Seom <sup>*1</sup>	정 상 섭
Suh, Jung-Ju <sup>*2</sup>	서 정 주
Won, Jin-Oh <sup>*3</sup>	원 진 오

### 요 지

본 연구에서는 지반-말뚝, 말뚝-말뚝캡, 그리고 말뚝-유체간의 상호작용 해석을 수행하여 교각세굴을 고려한 말뚝기초의 거동을 해석하였다. 지반-말뚝의 상호작용은 비선형 하중전이곡선(p-y, t-z, 그리고 q-z 곡선)을, 말뚝-말뚝캡의 상호작용에서는 군말뚝의 배열과 말뚝-말뚝캡 사이의 구속조건을 고려하였다. 말뚝-유체의 상호작용은 세굴에 의한 지반의 강성 저하를 고려하여 지반-말뚝의 상호작용에 포함하여 해석하였다. 그 결과 세굴심이 깊어질수록 말뚝에 발생하는 최대 휨모멘트의 값이 증가함을 알 수 있었으며, 이를 바탕으로 세굴에 따른 군말뚝의 안정성 평가에서는 지반-말뚝 및 말뚝-말뚝캡의 상호작용을 고려한 해석을 수행하는 것이 바람직함을 알 수 있었다.

### Abstract

This paper describes a simplified numerical procedure for analyzing the response of bridge pier foundations due to riverbed scouring. A computationally efficient algorithm to analyze the behavior of a pile group is proposed by considering soil-pile, pile-cap, and pile-fluid interactions. The complex phenomenon of the pile-soil interaction is modeled by discrete nonlinear soil springs (p-y, t-z and q-z curves). The pile-cap interaction is considered by geometric configuration of the piles in a group and connectivity conditions between piles and the cap. The pile-fluid interaction is incorporated into the procedure by reducing the stiffness of the soil-pile reactions as a result of nonlinearity and degradation of the soil stiffness with river bridge scouring. Through the numerical study, it is shown that the maximum bending moment increases with increasing scour depth. Thus it is desirable to check the stability of pile groups based on soil-pile and pile-cap interactions by considering scouring depth in the riverbed.

**Keywords** : Pile-cap interaction, Pile group, Pile-soil interaction, Scouring, Soil stiffness

## 1. Introduction

Pile groups are the most common type used for bridge foundations because they can transfer applied axial and lateral loads on superstructure to bearing

ground efficiently and safely. Pile group foundation consists of several single piles and one pile cap. Total bearing capacity of a pile group is the sum of each bearing capacity of single piles and that of a pile cap which is in direct contact with the soil.

\*1 Member, Associate Professor, Dept. of Civil Engrg., Yonsei Univ. (soj9081@yonsei.ac.kr)

\*2 Member, Ph.D. student, Dept. of Civil Engrg., Yonsei Univ.

\*3 Member, Ph.D. student, Dept. of Civil Engrg., Yonsei Univ.

A pile group is not collapsed immediately under sudden attack of flood flows which cause scouring along the pile, because bearing capacity that comes from the interaction between individual pile in a group and a pile cap resists scouring. Therefore, the analysis by considering the scour depth of bridge foundation is required to evaluate the stability of a pile group under applied load.

In this study, a three-dimensional analysis of pile groups is performed by considering soil-pile, pile-cap interactions based on riverbed scouring. The complex phenomenon of the soil-pile interaction is modeled by discrete nonlinear soil springs ( $p$ - $y$ ,  $t$ - $z$ , and  $q$ - $z$  curves) and the effect of riverbed scouring is considered by elimination or degradation of the soil stiffness. The pile-cap interaction is analyzed by stiffness method which can be considered by geometric configuration of the piles in a group and connectivity conditions between piles and a cap. Through the three-dimensional analysis program (YS-GROUP) of pile groups developed in this study, the displacement and rotation of a cap and member forces of individual pile in a group such as bending moment and shear force were estimated with varying scour depth of riverbed.

## 2. Method of Analysis Considering Bridge Scour

If the scour depth affects below the pile cap, pile groups are not failed at once but has some hazardous effects. For example, excessive horizontal displacement of a pile cap resulting from riverbed scouring may lead to structural damage (Fig. 1). Analysis only based on the estimated scour depth is not sufficient to consider the failure mode of pile groups caused by scouring under flood. So, it is a three-dimensional pile group analysis method that is recommended to think over the effect of scouring and the interaction between each pile and a pile cap.

The analytical method considering pile-cap interaction was first suggested by Hrennikoff (1949) using the stiffness method. Reese et al. (1970) developed a 3D analytical method of pile groups, using the modified Hrennikoff's method. This method was extended to incorporate the pile-soil-pile interaction by O'Neill et al. (1977) and Chow (1987). In this study, a similar approach suggested by O'Neill et al. (1977) is used and implemented as follows:

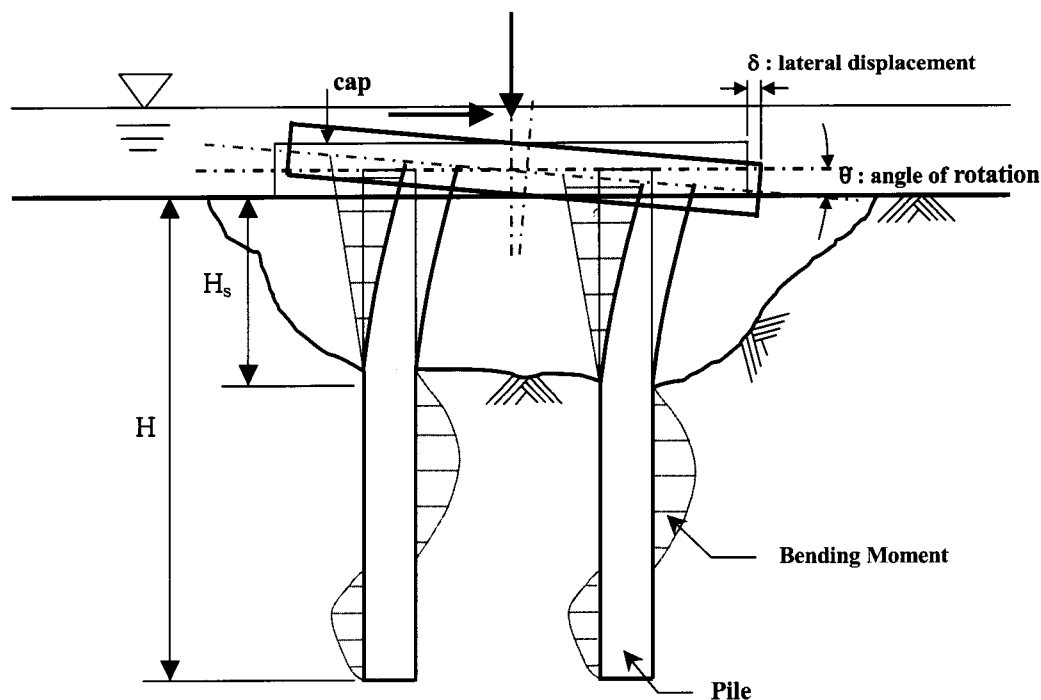


Fig. 1. Pile groups with riverbed scouring

## 2.1 Calculation of a Pile Head Stiffness of Each Pile in a Group

: Calculate a pile head stiffness of an individual pile on each loading step in different cases such as different pile properties (embedded length, diameter, and elastic modulus) and different soil layer properties (scour depth, depths of each soil layer and its properties).

## 2.2 Pile-cap Analysis Considering Individual Pile Head Stiffness ( $k_{ij}$ )

: Using all the individual pile head stiffnesses that are initially estimated in the first loading step, formulate the full stiffness matrix. Calculate pile cap displacement and individual pile head forces ( $P_{ix}$ ,  $P_{iy}$ ,  $P_{iz}$ ) and moments ( $M_{iz}$ ,  $M_{iy}$ , and  $M_{ix}$ ) for all the piles in the group.

## 2.3 Iteration to Convergence

: Compare the computed individual pile head forces and moments with the applied distributed load components used in step (2) for all the individual piles if the difference between them meets the user-specified closure tolerance level. If the convergence criterion is not satisfied, using the new computed pile head forces and moments, calculate a new individual pile head stiffness matrix for each pile again and repeat this iteration process. If it is satisfied, go to next step.

## 2.4 Evaluate Response of All Individual Piles

: Finally, evaluate responses of all the individual piles in a group, using the final individual pile head forces and moments.

The flowchart that shows all the steps described above

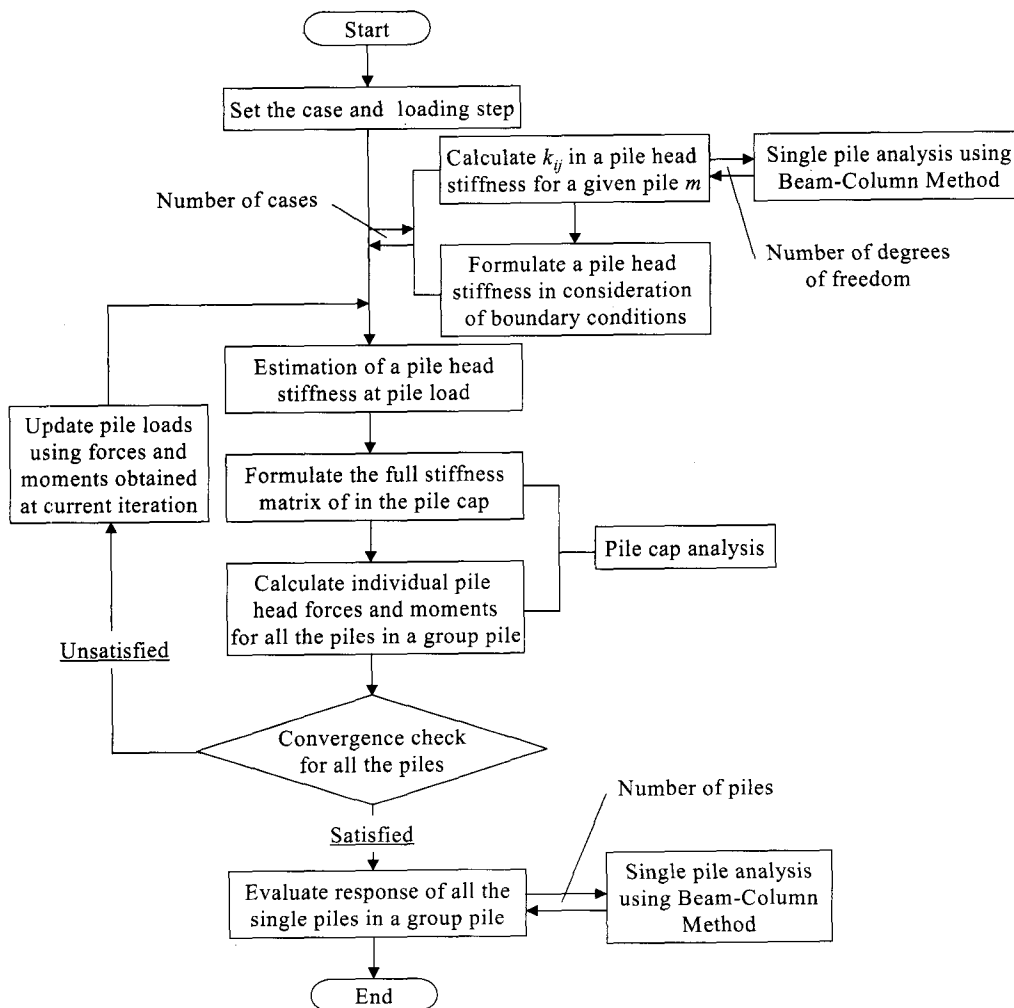


Fig. 2. Algorithm of three-dimensional group pile analysis

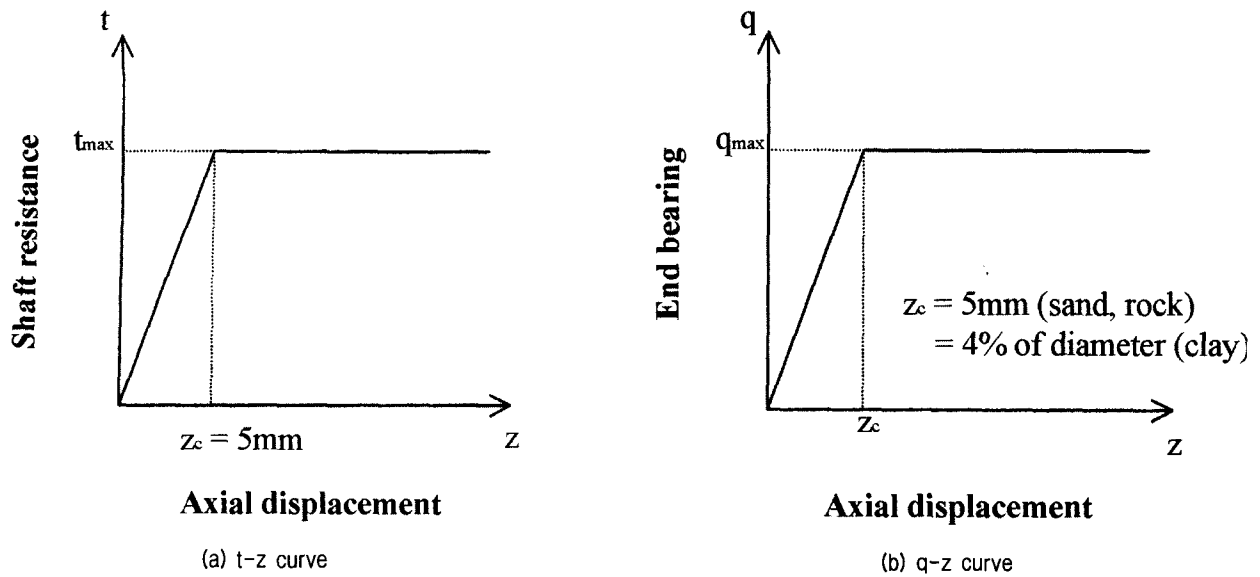


Fig. 3. Load transfer curves of axially loaded pile

is also given in Fig. 2. Based on the proposed algorithm, a new computer program YS-GROUP has been developed to analyze the behavior pile groups by considering both soil-pile and pile-cap interactions. (Jeong et al., 2001)

### 3. Load Transfer Curves

For axially loaded piles, the load-transfer curves were modeled by t-z and q-z curves. The type of t-z and q-z curves supported by the program is a linear elastic-plastic curve as shown in Fig. 3. According to soil types such as soil and rock, a maximum unit skin friction,  $t_{max}$  was estimated as follows:

In the soil,  $t_{max}$  was estimated by  $\beta$  method (Burland, 1973):

$$t_{max} = \beta \sigma'_z \quad (1)$$

where,  $\beta$  is approximately 0.3 and  $t_{max}$  linearly increases to a critical depth ( $15D$ ,  $D$  : diameter), beyond which it remains as a constant to failure.

For the rock,  $t_{max}$  was estimated using the method proposed by Reese and O'Neill (1987):

$$t_{max} = 0.15q_u \quad (2)$$

where,  $q_u$  is the unconfined shear strength, and limited to  $100\text{kN/m}^2$  (weathered rock),  $150\text{kN/m}^2$  (soft rock), and

$200\text{kN/m}^2$  (hard rock).

In Fig. 3,  $z_c$  is a critical displacement of the pile segment at which  $t_{max}$  is mobilized. Vijayvergiya (1977) recommended 0.2 to 0.3inch for  $z_c$ , so in this study 0.2inch (0.5mm) of  $z_c$  is adopted.

For laterally loaded piles, the load-transfer curves were modeled by p-y curves. A hyperbolic function was used to describe the relationship of the p-y curve (Fig. 4) which has an ultimate resistance ( $p_u$ ) and an initial tangent stiffness ( $E_s$ ). The initial tangent stiffness used in this study was assumed to vary linearly with depth as recommended by Reese et al. (1974).

To analyze the change of group pile behavior, especially

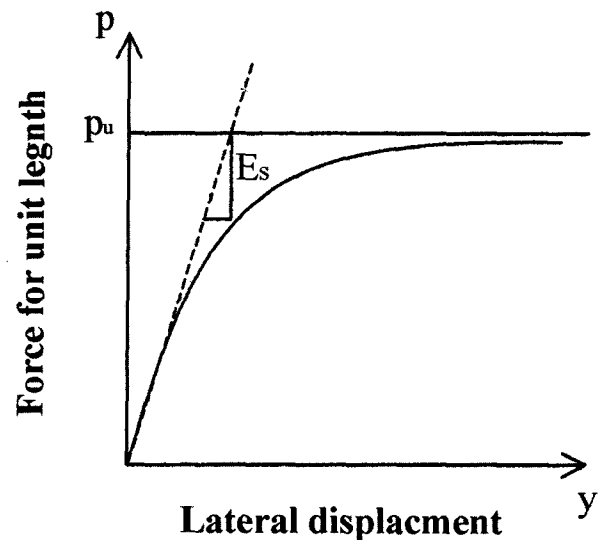


Fig. 4. Load transfer curves of laterally loaded pile (p-y curve)

in the presence of bridge scouring, load transfer curves ( $p$ - $y$ ,  $t$ - $z$ , and  $q$ - $z$  curves) within the scour depth are assumed to be eliminated, beyond which they are reconstructed along the embedded pile length by reducing the ultimate resistance ( $p_u$ ).

#### 4. Analysis and Results

To examine the pile group behavior with riverbed scouring, a series of idealized cases were examined based on the major influencing parameters such as cap rigidity and the spacing between piles. Fig. 5 shows a group pile

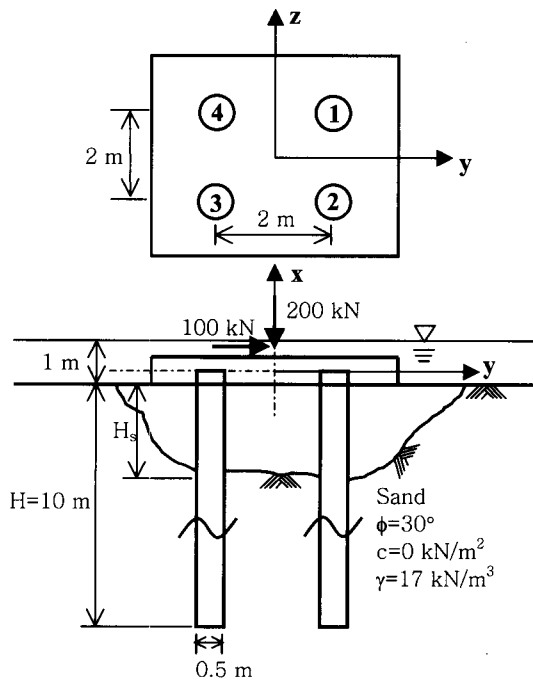


Fig. 5. A group pile configuration with scouring

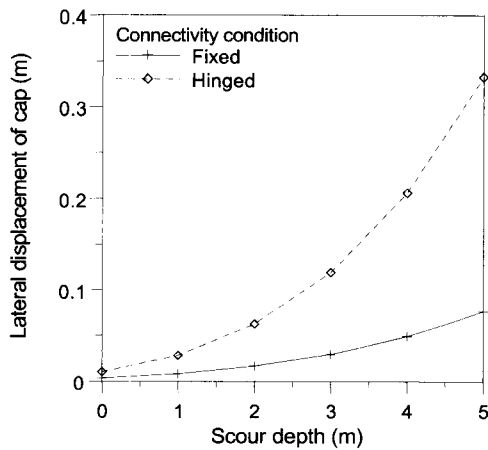


Fig. 6. Lateral cap displacement vs. scour depth

configuration to be analyzed considering scouring. The material properties for pile groups are shown in Table 1. Four piles, arranged by 2 rows and 2 columns and fixed and hinged head conditions are considered between piles and a pile cap. The piles are made of pre-cast concrete and the elastic modulus is  $4,000,000 \text{ kN/m}^2$ . Each pile is 0.5 m in diameter and 10 m in embedded length. The soil is uniform sand and the friction angle, the cohesion, and the unit weight are 30 degree,  $0 \text{ kN/m}^2$ , and  $17.0 \text{ kN/m}^3$ , respectively. The applied axial and lateral loads are 200 kN and 100 kN, respectively. The scour depth ( $H_s$ ) increases from 0 to 5 m by increment of 1 m. In each scour depth a three-dimensional analysis was performed.

##### 4.1 Effect of Cap Rigidity

Figs. 6 and 7 show the displacement and rotation of a cap with varying scour depths in both fixed and hinged

Table 1. Material properties for pile groups

Pile	Diameter	0.5 m
	Length	10 m
Soil	Elastic modulus	$4,000,000 \text{ kN/m}^2$
	Friction angle	30 degree
	Cohesion	$0 \text{ kN/m}^2$
	Unit weight	$17.0 \text{ kN/m}^3$
Connectivity condition	Fixed, Hinged	
Loading	Axial	200 kN
	Lateral	100 kN
Scour depth	0, 1, 2, 3, 4, 5 m	

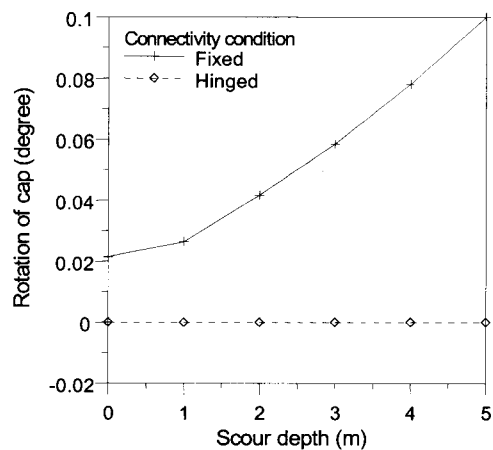


Fig. 7. Rotation of cap vs. scour depth

pile head conditions. As shown in these figures, the displacement of the pile cap increases as the scour depth increases and the magnitude seems to be significantly

larger for the hinged head case than for the fixed head case. The rotation of a pile cap for the fixed head case also increases with increasing the scour, but its absolute

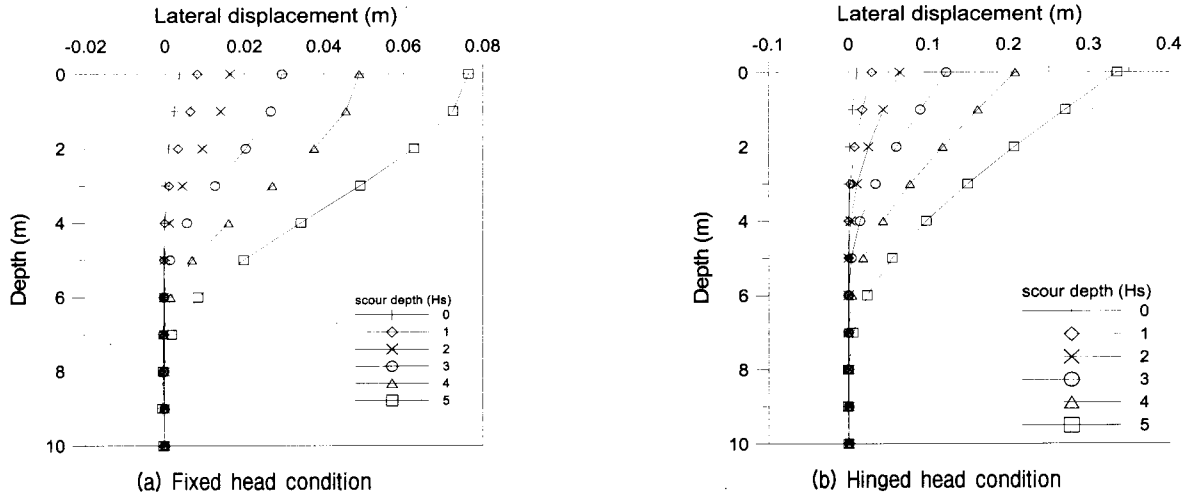


Fig. 8. Displacement profiles for different scour depths (no. ① pile)

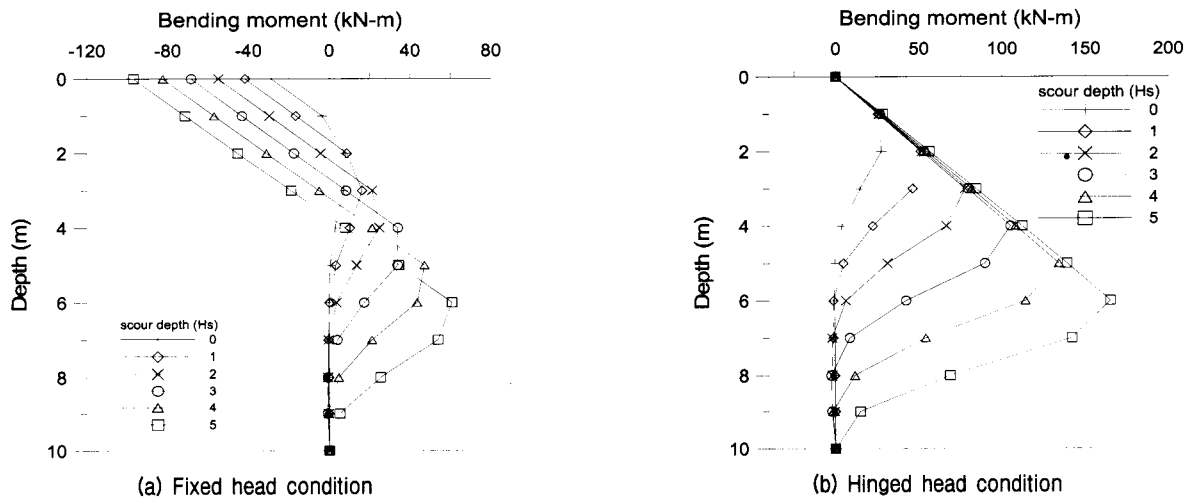


Fig. 9. Bending moment profiles for different scour depths (no. ① pile)

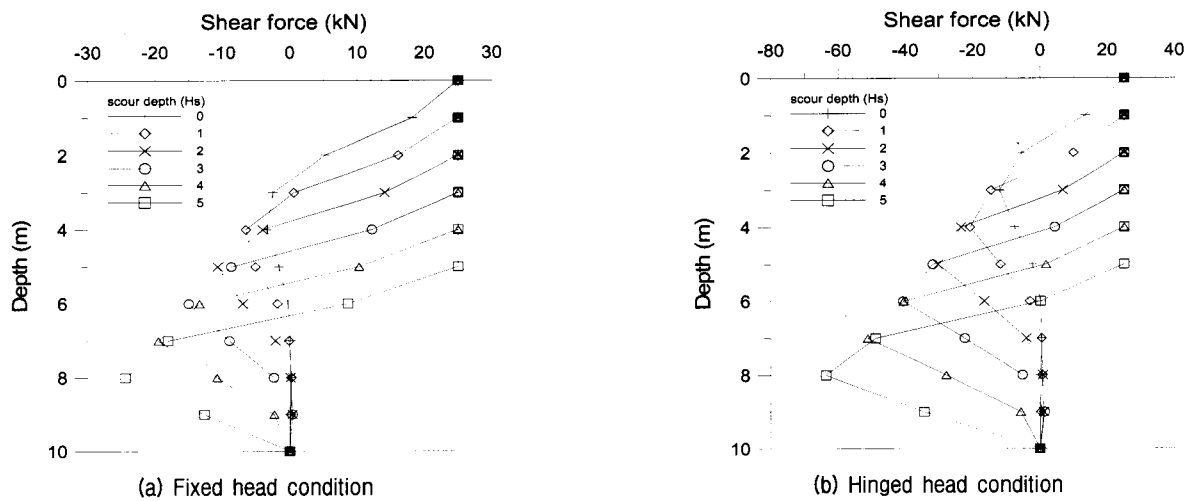


Fig. 10. Shear force profiles for different scour depths (no. ① pile)

value is not significant. For the hinged head case the rotation of a pile cap always seems to be zero.

Figs. 8, 9, and 10 show lateral pile displacement, bending moment, and shear force profiles along the embedded pile length of no. ① pile as shown in Fig. 5. Fig. 8 shows that the lateral displacement of pile increases as the scour depth increases. The distribution of bending moment along the pile and its change with scouring are represented in Fig. 9. For the fixed head case, the maximum bending moment occurs at the pile head. When scour depth increases from 0 to 5m, the maximum bending moment at the pile head increases approximately up to 340%. For the hinged head, the position where the maximum bending moment occurs moves down and its magnitude increases approximately up to 600% as the scour depth increases. Fig. 10 is the distribution of shear forces along the pile. For the fixed head case the shear force has a maximum value at the scoured bed level, but for the hinged head case it has a maximum value below the scoured bed level and the magnitude also increases as the scour depth increases.

#### 4.2 Effect of Spacing (s/d)

In the analysis, the pile groups with different pile center-to-center spacing were assumed to have the same initial scour depth. Pile spacings (s/d) selected in this study were 2.0, 4.0, and 8.0. Scour depth used changes from 0 to 5m. Figs. 11 and 12 show the effect of pile spacing with varying scour depths on the lateral displacement and rotation of pile cap. The lateral displacement and rotation of pile cap increase as scour depth increases. On the other hand, the effect of s/d was more sensitive to the rotation than to the lateral displacement.

Fig. 13 shows the magnitude of maximum bending moment as a function of the pile spacing and scour depth. The maximum bending moment developed at the pile head and varied linearly as scour depth increased. However, for the three spacings studied, there is little difference in maximum bending moment.

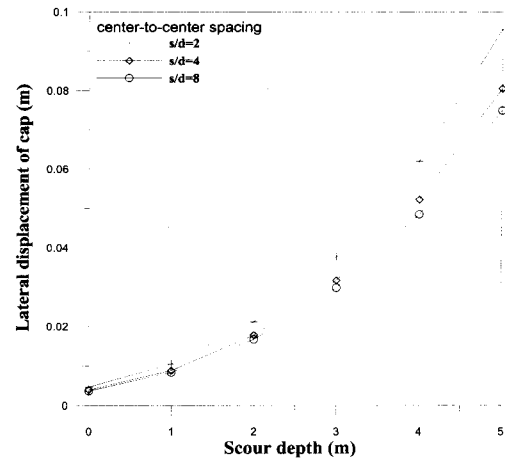


Fig. 11. Effect of pile spacing on lateral deflection of cap (fixed head condition)

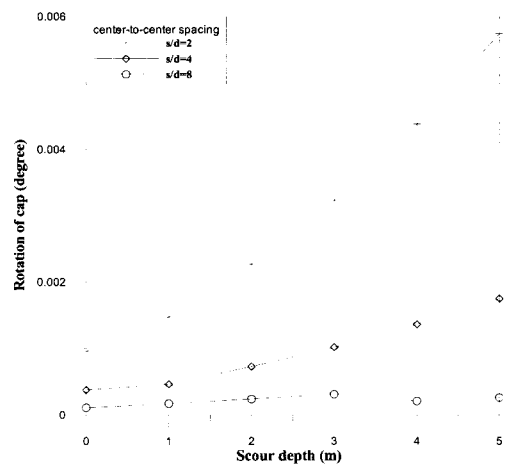


Fig. 12. Effect of pile spacing on cap rotation (fixed head condition)

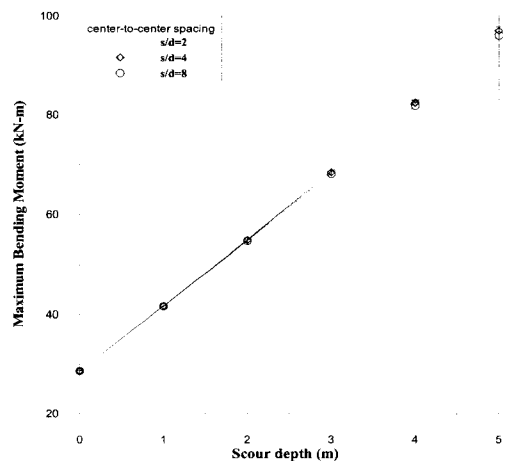


Fig. 13. Effect of pile spacing on maximum bending moment (fixed head)

## 5. Conclusions

In this study, a computationally efficient algorithm to analyze a group pile behavior is proposed in consideration

of soil-pile, pile-cap, and pile-fluid interactions. A limited parametric study of the response of pile groups was performed to examine the scouring effect. The following conclusions are drawn from the present study:

- (1) Under the same loading applied before and after scouring, the displacement along the pile length increases with increasing scour depth.
- (2) The maximum bending moment along the pile increases as the scour depth increases. This is particularly more significant for hinged head condition than for fixed head condition.
- (3) The pile spacing effect is significant for the rotation of pile. However, the lateral pile cap deflection and maximum bending moment are more influenced by scour depth than pile spacing.
- (4) To check the stability of bridge piers in the riverbed, it is recommended to perform a group pile analysis considering soil-pile and pile-cap interactions based on scouring effect.

### Acknowledgements

This paper was supported by grant No. 1999-1-311-02-3 from the Interdisciplinary Research Program of the KOSEF in Korea.

### References

1. Burland, J. B. (1973), "Shaft Friction Piles in Clay - A Simple Fundamental Approach." *Ground Engineering*, Vol.6, No.3, pp. 30-42.
2. Chow, Y. K. (1987), "Three-dimensional analysis of pile groups." *Journal of Geotechnical Engineering*, ASCE, Vol.113, No.6, pp. 637-651.
3. Hrennikoff, A. (1949), "Analysis of pile foundation with batter piles." *Trans., ASCE*, Vol.79, pp.351-374.
4. Jeong, S. S., Chung, S. H., and Won, J. O. (2001), "Analysis of group pile-cap interaction by load transfer approach." *Journal of the Korean Geotechnical Society*, Vol.17, No.3, pp.95-102, Korea.
5. O'Neill, M. W., Ghazzaly, O. I., and Ha, H. B. (1977), "Analysis of three-dimensional pile groups with nonlinear soil response and pile-soil-pile interaction." *Proc. 9th Offshore Technology Conf. 2*, pp.245-256.
6. Reese, L. C., and O'Neill, M. W. (1987), "Drilled shafts: construction procedures and design methods" *Design manual*, U.S. Department of Transportation, Federal Highway Administration, McLean, Va.
7. Reese, L. C., Cox, W. R., and Koop, F. D. (1974), "Analysis of laterally loaded piles in sand." *Proc. 6th Annu. Offshore Technol. Conf., Offshore Technol. Conf., Richardson, Tex.*, pp.473-483.
8. Reese, L. C., O'Neill, M. W., and Smith, R. E. (1970), "Generalized analysis of pile foundation." *Journal of Soil Mech. Found. Div., ASCE*, Vol.96, No.1, pp.235-250.
9. Vijayvergiya, V. N. (1977), "Load-movement characteristics of piles," *4<sup>th</sup> Annual Symposium of the Waterway, Port, Coastal and Ocean Division of ASCE*, Long Beach.

(received on Apr. 15, 2002, accepted on Jun. 3, 2002)