

# A Performance Analysis of TMN Systems Using Models of Networks of Queues, Jackson's Theorem, and Simulation

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Young Ha Hwang, Sang Wook Chung, Gil-Haeng Lee, and Young Il Kim

**We analyze the performance of a telecommunications management network (TMN) system using models of networks of queues, Jackson's theorem, and simulation. TMN systems for managing public asynchronous transfer mode (ATM) networks generally have a four-level hierarchical structure consisting of a network management system, a few element management systems (EMSs), and several pairs of agents and ATM switches. We construct a Jackson's queuing network and present formulae to calculate its performance measures: distributions of queue lengths and waiting times, mean message response time, and maximum throughput. We perform a numerical analysis and a simulation analysis and compare the results.**

## I. INTRODUCTION

The International Telecommunication Union – Telecommunications (ITU-T) has recommended the telecommunications management network (TMN) system as a management network standard [1]. A TMN, which is based on open system Interconnection (OSI) system management concepts, is organized using object-oriented techniques. The managers in managing systems and the agents in managed systems use a standardized information exchange interface to manage communication networks. The manager sends management operations to agents to obtain information on the managed objects and issues management commands using standard communication protocols, such as the common management information service element/common management information protocol (CMISE/CMIP) [2], [3]. The agents analyze the management commands received from the manager and order appropriate actions for the managed objects or managed resources. The agents also send notifications that may be responses to commands from the manager or events from managed resources such as system faults. CMISE/CMIP is a standard communication protocol for the OSI and TMN system to convey management information between the manager and the agents [4].

The TMN system for public asynchronous transfer mode (ATM) network management generally has a hierarchical structure (Fig. 1). There is an agent system for each ATM switch deployed at each region. The element management system (EMS) is a manager that maintains an ATM sub-network; the network management system (NMS) is a high-level manager that manages several EMSs. Usually, several agents in a TMN system are

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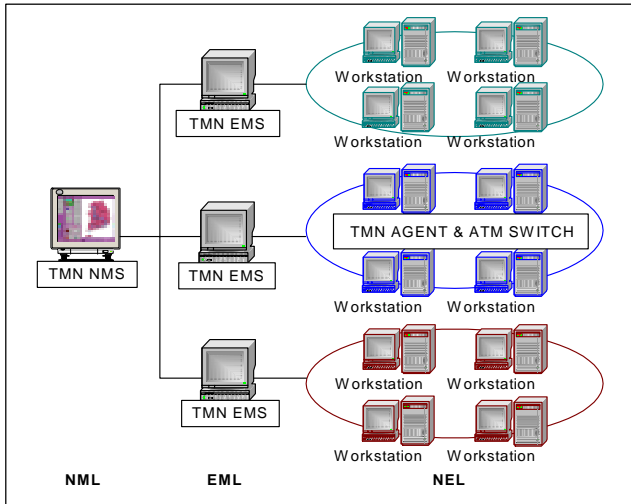


Fig. 1. General structure of a TMN system for public ATM networks.

controlled by a manager [4], [5].

Several authors have studied the problem of analyzing the performance of TMN systems [4], [6]. These previous investigations were concerned only with one EMS, along with several agents and network elements; they did not address the NMS. However, TMN systems consist of many independent sub-systems, and each sub-system plays a key role in the TMN system. Therefore, an analysis of the performance of TMN systems has to contain all sub-systems, such as the NMS, a few EMSs, many agents, and network resources.

Using Jackson's network and simulation models, this paper analyzes the performance of a TMN system that has a four-level hierarchical structure consisting of one NMS, a few EMSs, and several pairs of agents and ATM switches. The feature that makes our investigation different from other studies [4], [6] is that our performance analysis considers all the sub-systems of a TMN system. We construct a queuing network model and present formulae to calculate the performance measures: distributions of queue lengths and waiting times, mean message response time, and maximum throughput. We perform a numerical analysis along with a simulation analysis and compare the results of the numerical analysis with those of the simulation analysis.

## II. QUEUING NETWORK MODEL

### Notation

- $NI$  Queue at which management commands to the NMS arrive
- $NO$  Queue at which notifications from EMSs or the NMS itself arrive
- $EI_i$  Queue at which management commands to  $EMS_i$  arrive ( $i=1, \dots, m$ )
- $EO_i$  Queue at which notifications from agents or  $EMS_i$  itself

arrive ( $i=1, \dots, m$ )

- $AI_{ij}$  Queue at which management commands to agent  $j$  under the control of  $EMS_i$  arrive ( $i=1, \dots, m, j=1, \dots, n_i$ )
- $AO_{ij}$  Queue at which notifications from agent  $j$  itself or switch  $j$  under the control of  $EMS_i$  arrive ( $i=1, \dots, m, j=1, \dots, n_i$ )
- $S_{ij}$  Queue within switch  $j$  under the control of  $EMS_i$  ( $i=1, \dots, m, j=1, \dots, n_i$ )
- $\lambda_k$  Arrival rate of queue  $k$  from internal or external networks
- $\mu_k$  Service rate of queue  $k$

This section presents the queuing network model for the performance analysis of a TMN system implemented for ATM networks. Figure 2 illustrates a TMN system that manages an ATM network. The queuing network model presented in this paper is not original. The basic idea for the model is derived from reference paper [4]. To the basic model we added network elements (NMS, switches), arrival rates ( $\lambda_{HMij}$ ), branching probabilities ( $P_{EXi}, 1-P_{EOi}-P_{EXi}$ ), and the change of locations of arrival rates ( $\lambda_{SRij}, \lambda_{SOSij}$ ) from agents to switches.

### 1. Model of Subordinate Systems

The model is organized in four layers of subordinate systems: an NMS,  $m$  EMSs,  $n$  agents and  $n$  switches.

First, let's look into the NMS model. There are two sources of management commands in the NMS. One is the command from the NMS user ( $\lambda_{NMS}$ ). The other is what the NMS sends to a queue  $NI$  according to notifications from the EMS with probability  $1-P_{NO}$ . The services for some of these commands are completed by the NMS itself with probability  $P_{EIO}$ , and other commands are directed to the  $EMS_i$  system with probability  $P_{Eii}$  ( $i=1, \dots, m$ ). Of course,  $\sum_i P_{Eii}=1$  ( $i=0, \dots, m$ ) must be satisfied. The other queue ( $NO$ ) in the NMS deals with the notifications from the EMS and the NMS itself. After being processed by the NMS, only the messages with probability  $P_{NO}$  exit the network; the messages with probability  $1-P_{NO}$  are sent back into the queue  $NI$  for reprocessing.

Second, in each EMS system there are three sources of management commands. One is the command from the  $EMS_i$  user ( $\lambda_{EMS_i}$ ); another is from the NMS system. The third is what the  $EMS_i$  sends to the queue  $EI_i$  according to notifications from the agent with probability  $1-P_{EOi}-P_{EXi}$ . The services for some of these commands are completed by the  $EMS_i$  itself with probability  $P_{AIO}$  ( $i=1, \dots, m$ ), and other commands are sent to the agent  $j$  system under the control of the  $EMS_i$  with probability  $P_{Aij}$  ( $j=1, \dots, n_i$ ).  $\sum_j P_{Aij}=1$  ( $j=0, \dots, n_i$ ) must be satisfied. The other queue ( $EO_i$ ) in the  $EMS_i$  deals with notifications from an agent and the EMS itself. After being processed by the queue  $EO_i$  in the  $EMS_i$ , the messages with probability  $P_{EXi}$  go out of the network and some messages with probability  $P_{EOi}$  are directed to the queue  $NO$  in the NMS. Also some messages with probability  $1-P_{EOi}-P_{EXi}$  are sent back into the queue  $EI_i$  for reprocessing.

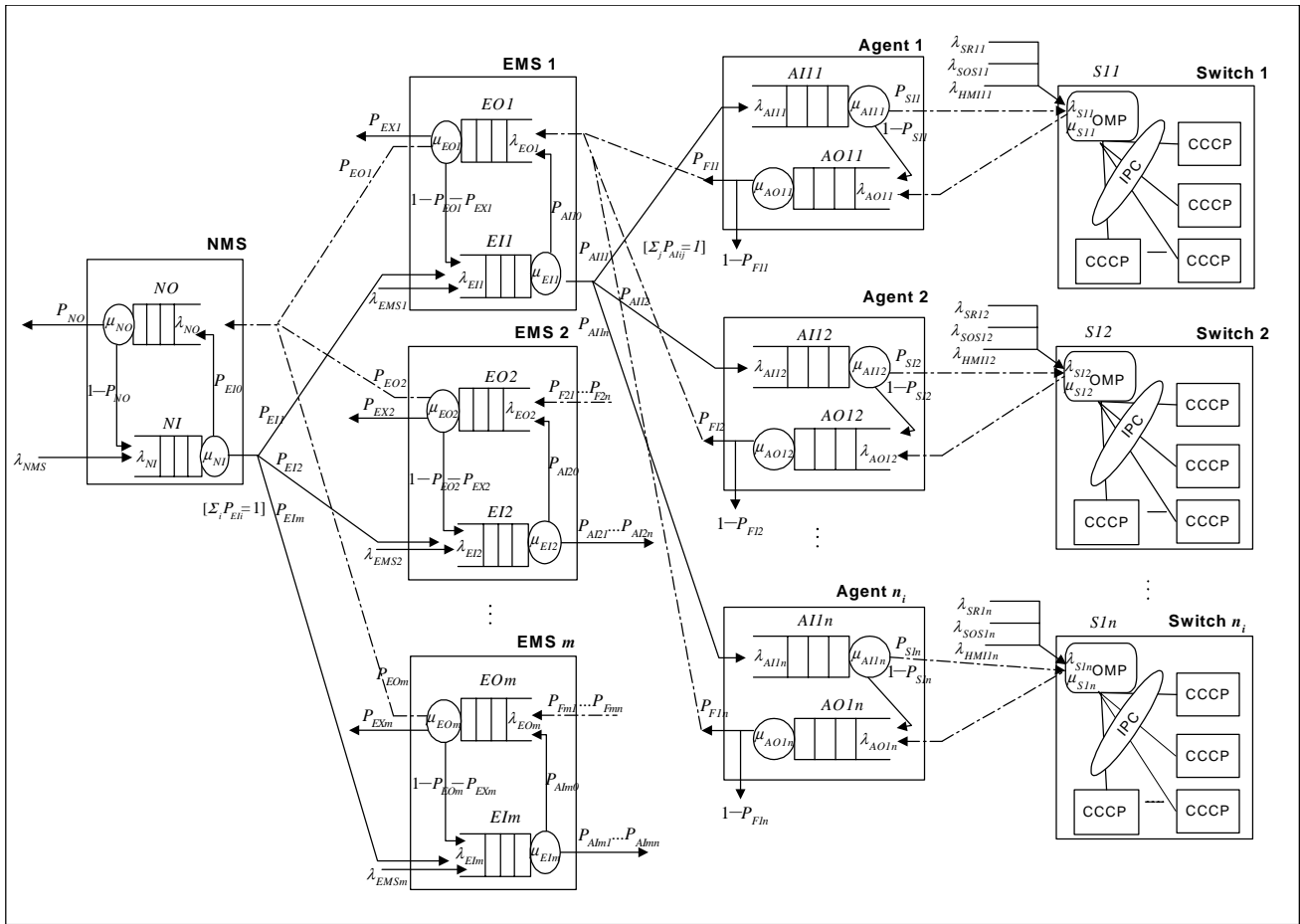


Fig. 2. Queuing network model.

Third, in each agent system the source of management commands is from the EMS system. After being processed by the queue  $AI_{ij}$  in the agent  $j$  system under the control of the  $EMS_i$ , these messages are sent to the switch  $j$  with probability  $P_{Sij}$  and to the queue  $AO_{ij}$  in the agent  $j$  system itself with probability  $1-P_{Sij}$ . There are two kinds of responses the agents ( $AO_{ij}$ ) may receive: The first is from the agent system itself, and the second is the results of the management commands processed by the ATM switch. After being treated by the queue  $AO_{ij}$  in the agent  $j$  system under the control of the  $EMS_i$ , some of these responses are not delivered to the EMS system because of the filtering and scoping action of the agent (with probability  $1-P_{Fij}$ ), and others are sent to the EMS system with probability  $P_{Fij}$ .

Fourth, in each switch system there are four sources of messages that have to be handled by the Operation and Maintenance Processor (OMP,  $S_{ij}$ ) within switch  $j$  under the control of the  $EMS_i$ : The first is from agent  $j$ ; the second from the internal processors within switch  $j$  under the control of the  $EMS_i$  ( $\lambda_{SRij}$ ) by, for example, fault notifications; the third from the operation system that monitors and administers the ATM switch ( $\lambda_{SOSij}$ ); the last from the human-machine interface (HMI) of the ATM switch

system ( $\lambda_{HMIij}$ ). After being handled by the OMP, these notifications are sent to the queue  $AO_{ij}$  in the agent  $j$  system under the control of the  $EMS_i$ .

## 2. Performance Measures

The performance measures to evaluate the performance of the TMN system using the above model are as follows:

- Distribution of queue length (magnitude of waiting messages)
- Distribution of waiting time (waiting time for receiving service)
- Mean message response time (processing time of messages)
- Maximum throughput (maximum magnitude of messages processed per unit time)

The performance measures we use are means to analyze the performance of TMN systems, not ultimate objects. These measures are very important because they are basic measures for analyzing the performance of the systems. Our numerical and simulation analyses are possible by the calculation of these basic measures, and they also make it possible for us to compare the performance of the system for specific cases.

### III. PERFORMANCE ANALYSIS

Using the above queuing network model and Jackson's Theorem, we developed formulae to calculate the following performance measures: distribution of queue length and waiting time, mean message response time, and maximum throughput. We made the following assumptions: that all inter-arrival times of each queue are independently and identically distributed according to an exponential distribution (i.e., the input process is Poisson); that all service times of each queue are independently and identically distributed according to another exponential distribution; that the number of all servers of each queue is one; and that all queues are infinite queues (consequently, the network of  $M/M/1$  queues).

Most mathematical evaluations of the performance of telecommunications systems, such as TMN systems, assume that the traffic characteristics follow Poisson arrival and the service time of an element of the system is exponentially distributed [4], [8]-[10]. It is hard to consider the operations of systems that violate the assumption of the Poisson process. For service system level analysis, the assumption of the Poisson process shows few significant deficiencies. Whenever the Poisson arrival assumption cannot be preserved [11]-[13], other evaluation techniques, such as simulation and measurement, are more appropriate for analyzing the performance of a system.

#### 1. Jackson's Theorem

A Jackson's network is a system of  $m$  service queues where queue  $u$  ( $u=1,2,\dots,m$ ) has

- an infinite queue,
- customers arriving from outside the system according to a Poisson input process with parameter  $a_u$ , and
- $s_u$  servers with an exponential service-time distribution with parameter  $\mu$

The customers visit the queues in different orders or might not visit them all. A customer leaving queue  $u$  is routed next to queue  $v$  ( $v=1,2,\dots,m$ ) with probability  $p_{uv}$  or departs the system with probability

$$q_u = 1 - \sum_{v=1}^m p_{uv}.$$

Under steady-state conditions, each queue  $v$  ( $v=1,2,\dots,m$ ) in a Jackson's network behaves as if it were an independent  $M/M/s$  queuing system with arrival rate

$$\lambda_v = a_v + \sum_{u=1}^m \lambda_u p_{uv}, \text{ where } s_v \mu_v > \lambda_v.$$

In such a Jackson's network, a simple form for the solution, called the product form solution, can be used to obtain measures of

performance for the network [14]-[16].

In this TMN system, there are  $2+2m+m(2n_i+n_i)$  infinite service queues. The parameter  $a_u$  of a Jackson's network corresponds to arrival rates,  $\lambda_{NMS}$ ,  $\lambda_{EMS_i}$ ,  $\lambda_{SRij}$ ,  $\lambda_{HMIij}$ ,  $\lambda_{SOSij}$ . The server  $s_u$  of each queue is one. Probabilities  $p_{uv}$  and  $q_u$  correspond to branching probabilities,  $P_{NO}$ ,  $P_{EIi}$ ,  $P_{EOi}$ ,  $P_{EXi}$ ,  $P_{AIij}$ ,  $P_{Sij}$ ,  $P_{Fij}$ . Parameter  $\mu_u$  corresponds to the service rate  $\mu_k$  of queue  $k$ . Finally, the arrival rate  $\lambda_v$  of queue  $v$  in a Jackson's network corresponds to the arrival rate  $\lambda_k$  of queue  $k$ . Thus, the queuing network of the TMN system that we illustrated in Fig. 2 could be a Jackson's network.

#### 2. Arrival Rate and Utilization Factors

Table 1 shows the arrival rates and utilization factors for each queue. The utilization factor  $\rho_k$  of queue  $k$  is an important parameter called the traffic intensity of the system [17].

Table 1. Arrival rates and utilization factors for each queue.

| Queue     | $\lambda_k$  | $\rho_k$                      |
|-----------|--|-------------------------------|
| $NI$      | $\lambda_{NMS} + (1 - P_{NO})\lambda_{NO}$                                     | $\lambda_{NI} / \mu_{NI}$     |
| $NO$      | $P_{EOi}\lambda_{NI} + \sum_{i=1}^m P_{EOi}\lambda_{EOi}$                      | $\lambda_{NO} / \mu_{NO}$     |
| $EI_i$    | $\lambda_{EMS_i} + P_{EIi}\lambda_{NI} + (1 - P_{EOi} - P_{EXi})\lambda_{EOi}$ | $\lambda_{EIi} / \mu_{EIi}$   |
| $EO_i$    | $P_{AIij}\lambda_{EIi} + \sum_{j=1}^n P_{Fij}\lambda_{AOij}$                   | $\lambda_{EOi} / \mu_{EOi}$   |
| $AI_{ij}$ | $P_{AIij}\lambda_{EIi}$  | $\lambda_{AIij} / \mu_{AIij}$ |
| $AO_{ij}$ | $\lambda_{Sij} + (1 - P_{Sij})\lambda_{AIij}$                                  | $\lambda_{AOij} / \mu_{AOij}$ |
| $S_{ij}$  | $\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIij} + P_{Sij}\lambda_{AIij}$   | $\lambda_{Sij} / \mu_{Sij}$   |

#### 3. Distribution of Queue Length

Let  $P_k(n)$  be the probability of exactly  $n$  messages in queue  $k$ . The probability of exactly  $n$  messages in queue  $k$  is

$$P_k(n) = (1 - \rho_k)\rho_k^n. \quad (1)$$

The expected number of messages (mean queue length) of queue  $k$  is

$$L_k = \rho_k / (1 - \rho_k) = \lambda_k / (\mu_k - \lambda_k). \quad (2)$$

The expected number of messages (mean queue length, excluding messages being served) of queue  $k$  is

$$L_{qk} = \rho_k^2 / (1 - \rho_k) = \lambda_k^2 / [\mu_k(\mu_k - \lambda_k)]. \quad (3)$$

The expected total number of messages in the entire system then is

$$L_{total} = \sum_k L_k = \sum_k \frac{\rho_k}{1 - \rho_k}. \quad (4)$$

Using (1) and Jackson's Theorem [14], [15], the joint distribution of the expected number of messages (mean queue length) in a system can be obtained by multiplying the probability of exactly  $n_k$  messages in queue  $k$ . Thus,

$$P(n) = P_{NI}(n_{NI})P_{NO}(n_{NO})P_{EI}(n_{EI})P_{EOI}(n_{EOI})\dots P_{Smi}(n_{Smi}) \quad (5)$$

$$= \prod_k (1 - \rho_k) \rho_k^{n_k},$$

where the state of system  $n$  is the vector  $(n_{NI}, n_{NO}, n_{EI}, n_{EOI}, \dots, n_{Smi})$  that denotes the number of messages at each queue.

#### 4. Distribution of Waiting Time

The expected waiting time (including service time) of messages in queue  $k$ ,  $W_k$ , can be calculated from (2) and Little's formula [16] as

$$W_k = 1 / (\mu_k - \lambda_k). \quad (6)$$

Also, the expected waiting time (excluding service time) of messages in queue  $k$ ,  $W_{qk}$ , is

$$W_{qk} = \lambda_k / [\mu_k(\mu_k - \lambda_k)] = \rho_k / [\mu_k(1 - \rho_k)]. \quad (7)$$

Obtaining  $W_{total}$  (the expected total waiting time including service time in the entire system for a message) is more complicated. The expected waiting times at the respective queues cannot be simply added, because a message does not necessarily visit each queue exactly once. However, Little's formula can still be used, where the system arrival rate  $\lambda_{total}$  is the sum of the arrival rate from outside to the queues [16],

$$\lambda_{total} = \lambda_{NMS} + \sum_{i=1}^m \lambda_{EMSi} + \sum_{i=1}^m \sum_{j=1}^{n_i} (\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj})$$

$$\text{Thus, } W_{total} = L_{total} / \lambda_{total} = \frac{\sum_k \frac{\rho_k}{1 - \rho_k}}{\lambda_{NMS} + \sum_{i=1}^m \lambda_{EMSi} + \sum_{i=1}^m \sum_{j=1}^{n_i} (\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj})}. \quad (8)$$

#### 5. Mean Message Response Time

When the message response time is defined as the time that the response for a management command invoked by an NMS user takes to arrive in the NMS user after being processed by the EMS, Agent, and Switch, its expected value  $W_{NMS}$  can be obtained. The expected message response time of a management command by an NMS user,  $W_{NMS}$ , is

$$W_{NMS} = W_{NI} + P_{EIO} W_{NO} + (1 - P_{EIO})$$

$$\times \left\{ \sum_{i=1}^m \frac{P_{Eli}}{1 - P_{EIO}} [W_{Eli} + P_{AIO} (W_{EOi} + W_{NO}) + (1 - P_{AIO}) a] \right\},$$

where

$$a = \sum_{j=1}^{n_i} \frac{P_{Aij}}{1 - P_{AIO}} (W_{Aij} + W_{AOij} + P_{Sij} W_{Sij} + W_{EOi} + W_{NO}). \quad (9)$$

#### 6. Maximum Throughput

In the above queuing network model, as the arrival rate increases, a queue  $k$  with a larger value of  $\rho_k$  will introduce instability. Hence, the queue with the largest value of  $\rho$  is called the bottleneck of a TMN system [17].

Eq. (7) shows that as the traffic intensity  $\rho_k$  approaches 1, the waiting time for messages approaches infinity. Therefore, the maximum throughput of the system can be predicted by evaluating the traffic intensity of the bottleneck,  $\rho_{bottleneck} = 1$  ( $\mu_{bottleneck} = \lambda_{bottleneck}$ ) [17].

In this system it can be predicted that the bottleneck is the queue  $NO$  in the NMS, because all notifications to management commands from the NMS or EMS user and all notifications from several agents or switch systems are concentrated in the queue  $NO$  through some EMSs, agents, and switches. Therefore, the maximum throughput can be obtained by using [18]

$$\mu_{NO} = \lambda_{NO} = P_{EIO} \lambda_{NI} + \sum_{i=1}^m P_{EOi} \lambda_{EOi}. \quad (10)$$

#### IV. NUMERICAL ANALYSIS

This section presents our numerical analysis for the performance measures of a TMN system composed of one NMS,  $m$  EMSs,  $n$  agents, and  $n$  switches. We assumed that each value of the parameters in all EMSs, agents, and switches is the same. Thus, for example,

$$n_1 = n_2 = \dots = n_m = n, \quad P_{EO1} = P_{EO2} = \dots = P_{EOm},$$

$$P_{EI1} = P_{EI2} = \dots = P_{EIm}, \quad P_{S11} = P_{S12} = \dots = P_{S1m},$$

$$\lambda_{EMSI} = \lambda_{EMSI2} = \dots = \lambda_{EMSI m}, \quad \lambda_{SR11} = \lambda_{SR12} = \dots = \lambda_{SR1 m},$$

$$\mu_{EO1} = \mu_{EO2} = \dots = \mu_{EOi}.$$

In fact, the above assumption is not practical in real TMN systems. However, if we don't make this assumption it is not easy to solve mathematically.

The formulae of the numerical analysis for a TMN system under the above conditions are as follows:

- Arrival rates of each queue

$$\lambda_{NO} = (P_{EIO} \lambda_{NMS} + mn P_{EOi} P_{Fij} (\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj})$$

$$+ \{m P_{EOi} (n P_{Fij} + 1) \cdot P_{Aij} \cdot [\lambda_{EMSi} + P_{Eli} \lambda_{NMS}$$

$$+ n P_{Fij} (1 - P_{EOi} - P_{EXi}) (\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj})\})$$

$$/ \{1 - (1 - P_{EOi} - P_{EXi}) P_{Aij} [1 + n P_{Fij} P_{Sij} + n P_{Fij} (1 - P_{Sij})]\})$$

$$/ (1 - P_{EIO} (1 - P_{NO}) - m P_{EOi} (n P_{Fij} + 1) P_{Aij} P_{Eli} (1 - P_{NO})$$

$$/ \{1 - (1 - P_{EOi} - P_{EXi}) P_{Aij}$$

$$\times [1 + n P_{Fij} P_{Sij} + n P_{Fij} (1 - P_{Sij})]\})$$

$$\lambda_{NI} = \lambda_{NMS} + (1 - P_{NO})\lambda_{NO},$$

$$\lambda_{EI} = \{\lambda_{EMSi} + P_{Ei} [\lambda_{NMS} + (1 - P_{NO})\lambda_{NO}] + (1 - P_{EOi} - P_{EXi})nP_{Fij}(\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj})\} / \{[1 - (1 - P_{EOi} - P_{EXi})P_{Aij}][1 + nP_{Fij}P_{Sij} + nP_{Fij}(1 - P_{Sij})]\}$$

$$\lambda_{EOi} = P_{Aij}\lambda_{EI} + nP_{Fij}\lambda_{AOij},$$

$$\lambda_{Aij} = P_{Aij}\lambda_{EI},$$

$$\lambda_{AOij} = \lambda_{Sij}(1 - P_{Sij})P_{Aij}\lambda_{EI},$$

$$\lambda_{Sij} = \lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj} + P_{Sij}\lambda_{Aij},$$

$$\lambda_{total} = \lambda_{NMS} + m\lambda_{EMSi} + mn(\lambda_{SRij} + \lambda_{SOSij} + \lambda_{HMIj}).$$

- Traffic intensity of queue  $k$

$$\rho_k = \lambda_k / \mu_k.$$

- The expected number of messages (mean queue length) of queue  $k$

$$L_k = \rho_k / (1 - \rho_k).$$

- The expected number of messages (mean queue length, excluding messages being served) of queue  $k$

$$L_{qk} = \rho_k^2 / (1 - \rho_k) = \lambda_k^2 / \{\mu_k(\mu_k - \lambda_k)\}.$$

- The expected total number of messages in the entire system

$$L_{total} = L_{NI} + L_{NO} + m(L_{EOi} + L_{EI}) + mn(L_{AOij} + L_{Aij} + L_{Sij}).$$

- The expected waiting time (including service time) of messages in queue  $k$

$$W_k = 1 / (\mu_k - \lambda_k).$$

- The expected waiting time (excluding service time) of messages in queue  $k$

$$W_{qk} = \lambda_k / \{\mu_k(\mu_k - \lambda_k)\} = \rho_k / \{\mu_k(1 - \rho_k)\}.$$

- The expected message response time of a management command by the NMS user

$$W_{NMS} = W_{NI} + P_{EIO}W_{NO} + (1 - P_{EIO})[W_{EI} + P_{AIO}(W_{EOi} + W_{NO}) + (1 - P_{AIO})(W_{Aij} + W_{AOij} + P_{Sij}W_{Sij} + W_{EOi} + W_{NO})].$$

The values of parameters used in this analysis are as follows:

- Arrival rates:  $\lambda_{NMS}, \lambda_{EMSi}, \lambda_{SRij}, \lambda_{HMIj}, \lambda_{SOSij} = 0.07$ .
- Branching Probabilities:  $P_{NO} = 0.99, P_{EIO} = 0.1, P_{Ei} = (1 - P_{EIO})/m, P_{EOi} = 0.5, P_{EXi} = 0.49, P_{AIO} = 0.1, P_{Aij} = (1 - P_{AIO})/n, P_{Sij} = 0.5, P_{Fij} = 0.9$ .
- Service rates:  $\mu_{NI} = 2.9, \mu_{NO} = 2.78, \mu_{EI} = 2.9, \mu_{EOi} = 2.78, \mu_{AOij} = 2.15, \mu_{Aij} = 4.12, \mu_{Sij} = 7.31$  (real data from reference papers [6], [9]).

### 1. Effect of $\lambda_{NMS}$ on $W_{NMS}$

Figure 3 shows the effect of  $\lambda_{NMS}$  on  $W_{NMS}$  under the above conditions. The figure indicates that  $W_{NMS}$  increases drastically as  $\lambda_{NMS}$  increases and that it has the same trend regardless of the increase of  $n$  (the number of agents and switches) and  $m$  (the

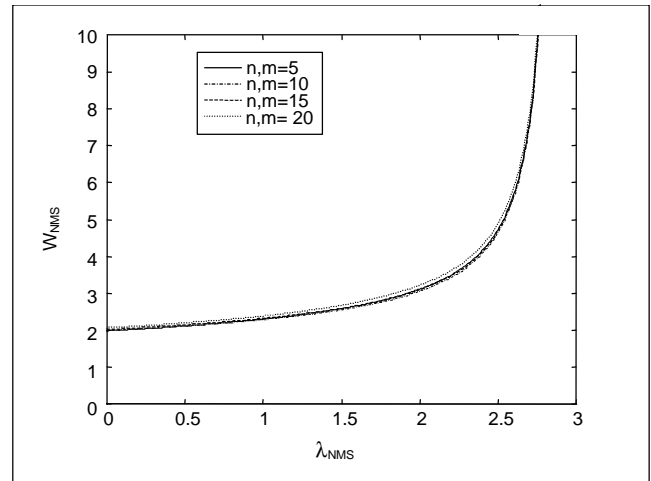


Fig. 3. Effect of  $\lambda_{NMS}$  on  $W_{NMS}$ .

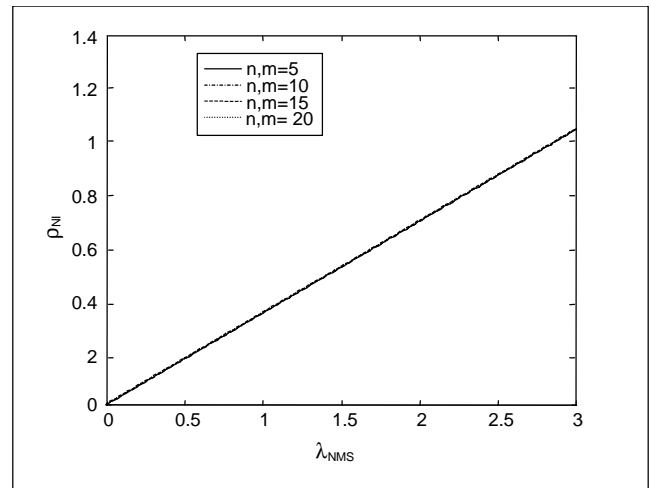


Fig. 4. Effect of  $\lambda_{NMS}$  on  $\rho_{NI}$ .

number of EMSs) ( $n, m = 5, 10, 15, 20$ ). A trend in which the graph increases drastically at the point of about  $\lambda_{NMS} = 2.85$  is revealed. At this point,  $\rho_{NI}$  is 1 (Fig. 4), the bottleneck of the system is queue  $NI$  (the NMS input queue), and the maximum throughput is about  $\lambda_{NI} = 2.90$ , irrespective of the network size (the values of  $n$  and  $m$ ).

These figures also indicate that  $\lambda_{NMS}$  has little effect on the determination of the optimal number of EMSs and Agents ( $n, m$ , network size).

### 2. Effect of $\lambda_{SRij}$ on $W_{NMS}$

Figure 5 shows the effect of  $\lambda_{SRij}$  (messages from internal processors within switch  $j$  under the control of the EMS $i$  may relate to fault event reports) on  $W_{NMS}$ . The figure indicates that  $W_{NMS}$  increases drastically as  $\lambda_{SRij}$  increases and that it also has a much quicker rising trend according to the increase of  $n$  and  $m$  ( $n, m = 5, 10, 15, 20$ ). The figure also reveals a trend wherein the

graph increases drastically at about  $\lambda_{SRij}=0.24, 0.06, 0.025, 0.015$ . At this point,  $\rho_{NO}$  is 1 (Fig. 6), the bottleneck of the system is queue *NO*, and the maximum throughput is about  $\lambda_{NO}=2.78$ , irrespective of the network size (the values of  $n$  and  $m$ ). That is, the bottleneck is the NMS output queue and waiting time increases with the fault event rate, which increases with the network size.

These figures also indicate that if  $\lambda_{SRij}=0.215, 0.055, 0.022, 0.013$  and  $\rho_{NO}$  (the utilization factor of the bottleneck of systems) = 0.9, the optimal number of EMSs and Agents is  $n, m=5, 10, 15, 20$ .

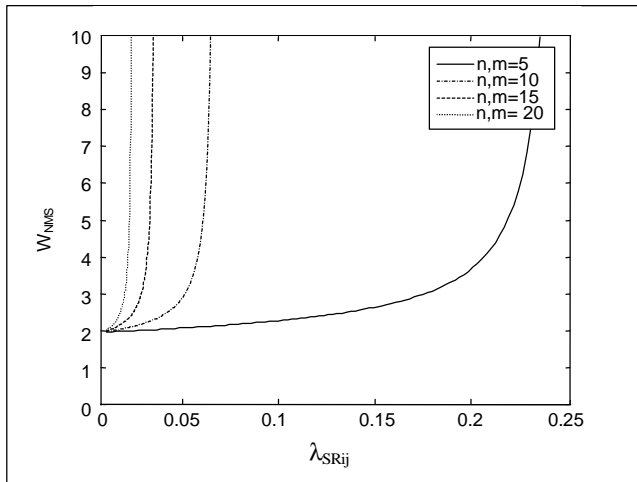


Fig. 5. Effect of  $\lambda_{SRij}$  on  $W_{NMS}$ .

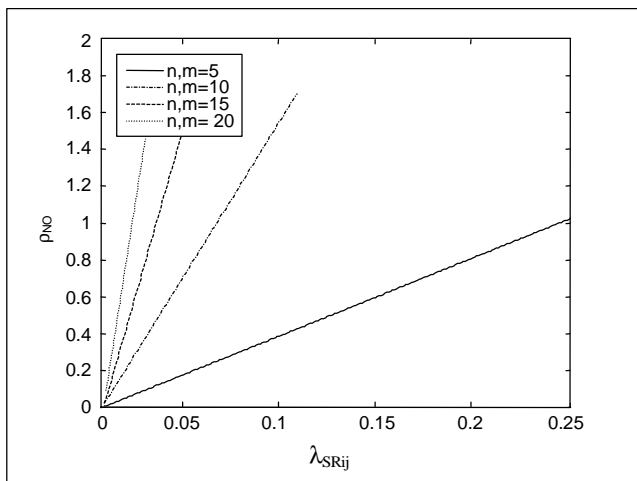


Fig. 6. Effect of  $\lambda_{SRij}$  on  $\rho_{NO}$ .

### 3. Effect of $n$ on $W_{NMS}$

Figure 7 shows the effect of  $n$  on  $W_{NMS}$ . The figure indicates that  $W_{NMS}$  increases drastically as  $n$  increases, and that it has a much quicker rising trend due to the increase of  $\lambda_{SRij}$  ( $\lambda_{SRij}=0.10, 0.15, 0.20, 0.25$ ). A trend wherein the graph increases drastically at about  $n=5, 6, 8, 12$  is displayed. At these points,  $\rho_{NO}$  is 1 (Fig. 8),

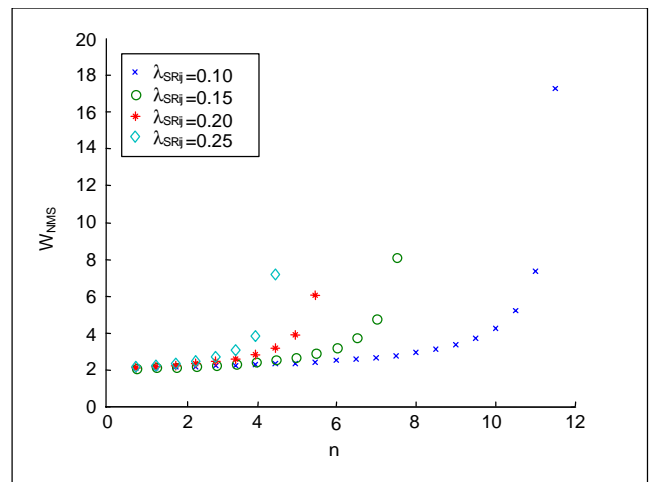


Fig. 7. Effect of  $n$  on  $W_{NMS}$ .

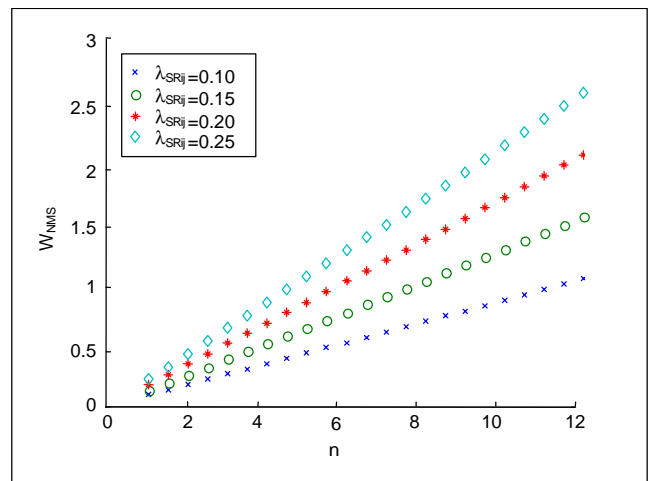


Fig. 8. Effect of  $n$  on  $\rho_{NO}$ .

the bottleneck of the system is queue *NO* (the NMS output queue), and the maximum throughput is about  $\lambda_{NO}=2.78$  (regardless of the value of  $\lambda_{SRij}$ ).

These figures also indicate that if  $\lambda_{SRij}=0.10, 0.15, 0.20, 0.25$  and  $\rho_{NO}$  (the utilization factor of the bottleneck of systems) = 0.9, the optimal number of Agents is  $n=4, 5, 7, 10$ .

## V. SIMULATION ANALYSIS

This section describes our simulation analysis of the performance of a TMN system composed of one NMS,  $m$  ( $m=5$ ) EMSs,  $n$  ( $n=5$ ) agents, and  $n$  ( $n=5$ ) switches. AweSim (Visual SLAM [19]) is used as a simulation tool. The basic assumptions, the values of the parameters, and the formulae used in this analysis are the same as those used in the numerical analysis in section IV. The distribution of the inter-arrival time and the service time of the

commands or messages in queue  $k$  are  $\text{Exp}(1/\lambda_k)$  and  $\text{Exp}(1/\mu_k)$ , respectively. To obtain the results in a steady-state, we used one million times and two million times as run-times.

In the first simulation (Simulation I), the above conditions were used with the model in Fig. 2. However, in the second simulation (Simulation II), we used a different queuing network model (Fig. 9). For Simulation I, it was impossible to measure the mean message response time ( $W_{NMS}$ ) because of the continuous circulation of messages by the branching probabilities ( $1-P_{NO}$ ,  $1-P_{EOI}-P_{EXI}$ ) within the gray circle in Fig. 9. In Simulation II those branching probabilities were changed as follows:

- Branching Probabilities:  $1-P_{NO}=0$ ,  $P_{NO}=1$ ,  $1-P_{EOI}-P_{EXI}=0$ ,  $P_{EOI}=0.5$ ,  $P_{EXI}=0.5$ .

We expected differences in the results of Simulations I and II. For the comparison of the results of the mean message response time ( $W_{NMS}$ ) in section V.2, the results of Simulation II were used.

Table 2 shows the results of the two simulations: the results for the two run-times are nearly the same. Thus, the system is in a steady-state. The results of the two million run-time were used for the comparison with the analytic method proposed in this paper. However, there was a slight difference between the results of Simulation I and Simulation II because we used different queuing network models (Figs. 2 and 9).

Table 3 shows the results of the comparison of the analytic

method and simulation method; the results are almost the same. For the comparison, we used the results of Simulation I except for the mean message response time, for which we used the result of Simulation II. Thus, there was a little difference between the results of the mean message response time ( $W_{NMS}$ ).

In accordance with the compared results of the analytic and the simulation method, there was no significant difference between the results of the two methods. Hence, we can conclude that the analytic method of the performance analysis proposed in this paper is suitable.

## VI. CONCLUSION

We devised a queuing network model and an analytic model for performance analysis using Jackson's Theorem and then performed numerical and simulation analyses for specific cases.

The numerical analysis clearly showed that the number of subordinate subsystems and the quantity of traffic within the system had substantial effects on the performance of the system. In addition, by determining the optimal number of subordinate subsystems in specific cases we showed how to design an appropriate TMN system and to evaluate its performance efficiently.

This paper presented a general model for performance analysis

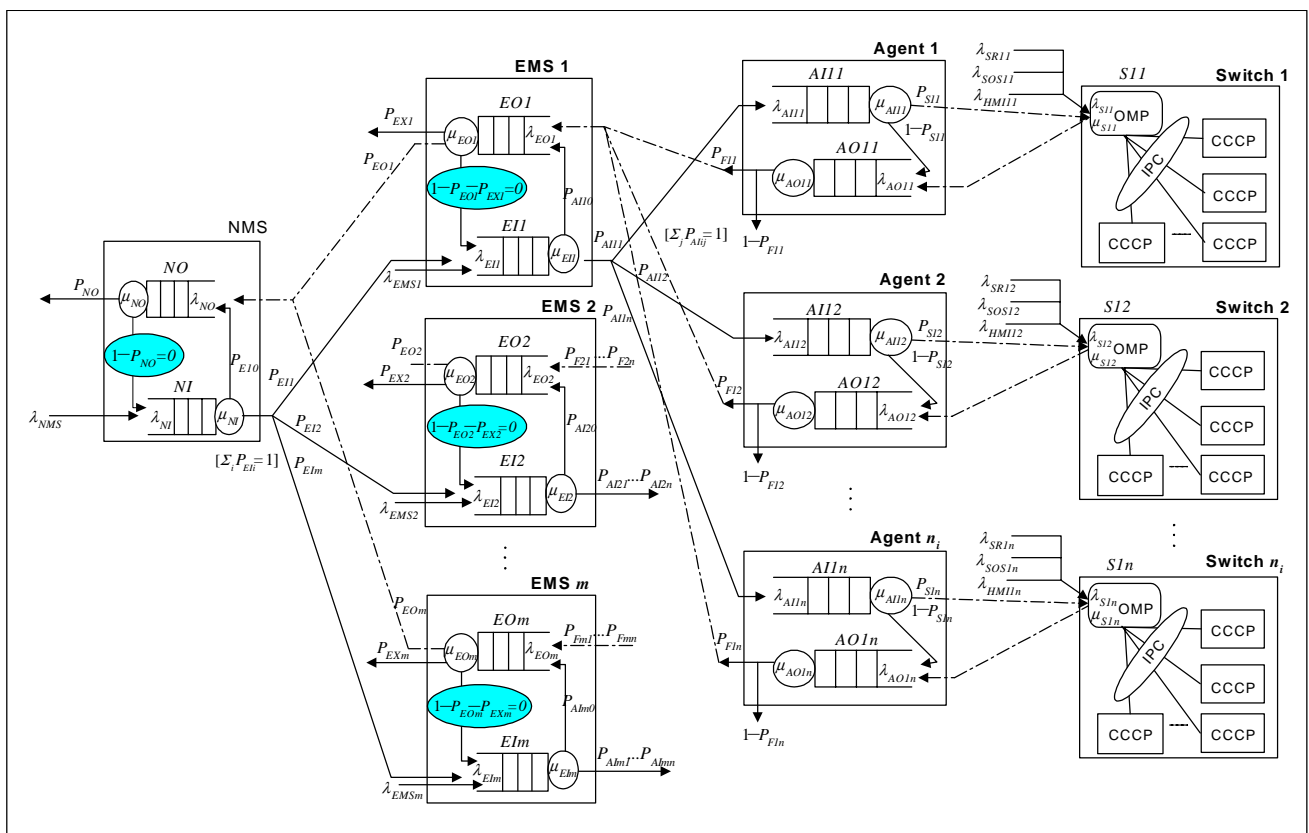


Fig. 9. Queuing network model used in simulation II.



Table 2. Results of the simulation.

| Measures   | Measures for each queue | Simulation I   |                | Simulation II  |                |
|--|-------------------------|----------------|----------------|----------------|----------------|
|  |                         | Run-time       |                | Run-time       |                |
|  |                         | 1 million time | 2 million time | 1 million time | 2 million time |
| Utilization Factors<br>( $\rho_k$ )                                | $\rho_{NI}$             | 0.033          | 0.033          | 0.024          | 0.024          |
|  | $\rho_{NO}$             | 0.932          | 0.933          | 0.920          | 0.919          |
|  | $\rho_{Ei}$             | 0.034          | 0.034          | 0.028          | 0.028          |
|  | $\rho_{EOi}$            | 0.372          | 0.372          | 0.368          | 0.367          |
|  | $\rho_{AOij}$           | 0.106          | 0.106          | 0.105          | 0.105          |
|  | $\rho_{Aij}$            | 0.004          | 0.004          | 0.004          | 0.004          |
|  | $\rho_{Sij}$            | 0.030          | 0.030          | 0.030          | 0.030          |
| Queue Lengths<br>(excluding messages being served)<br>( $L_{qk}$ ) | $L_{qNI}$               | 0.001          | 0.001          | 0.001          | 0.001          |
|  | $L_{qNO}$               | 12.798         | 12.846         | 10.411         | 10.348         |
|  | $L_{qEi}$               | 0.001          | 0.001          | 0.001          | 0.001          |
|  | $L_{qEOi}$              | 0.221          | 0.220          | 0.214          | 0.212          |
|  | $L_{qAOij}$             | 0.012          | 0.012          | 0.012          | 0.012          |
|  | $L_{qAij}$              | 0.000          | 0.000          | 0.000          | 0.000          |
|  | $L_{qSij}$              | 0.001          | 0.001          | 0.001          | 0.001          |
| Waiting Times<br>(excluding service time)<br>( $W_{qk}$ )          | $W_{qNI}$               | 0.011          | 0.011          | 0.008          | 0.008          |
|  | $W_{qNO}$               | 4.937          | 4.955          | 4.070          | 4.048          |
|  | $W_{qEi}$               | 0.012          | 0.012          | 0.010          | 0.010          |
|  | $W_{qEOi}$              | 0.214          | 0.213          | 0.209          | 0.208          |
|  | $W_{qAij}$              | 0.001          | 0.001          | 0.001          | 0.001          |
|  | $W_{qAOij}$             | 0.054          | 0.054          | 0.055          | 0.055          |
|  | $W_{qSij}$              | 0.004          | 0.004          | 0.004          | 0.004          |
| Mean Message Response Time   | $W_{NMS}$               | -              | -              | 6.124          | 6.123          |

Table 3. Results of analytic and simulation methods.

| Measures   | Measures of each queue | Results         |                   |
|--|------------------------|-----------------|-------------------|
|  |                        | Analytic method | Simulation method |
| Utilization Factors<br>( $\rho_k$ )                                | $\rho_{NI}$            | 0.0332          | 0.033             |
|  | $\rho_{NO}$            | 0.9403          | 0.933             |
|  | $\rho_{Ei}$            | 0.0337          | 0.034             |
|  | $\rho_{EOi}$           | 0.3747          | 0.372             |
|  | $\rho_{AOij}$          | 0.1059          | 0.106             |
|  | $\rho_{Aij}$           | 0.0043          | 0.004             |
|  | $\rho_{Sij}$           | 0.0299          | 0.030             |
| Queue Lengths<br>(excluding messages being served)<br>( $L_{qk}$ ) | $L_{qNI}$              | 0.0011          | 0.001             |
|  | $L_{qNO}$              | 14.8044         | 12.846            |
|  | $L_{qEi}$              | 0.0012          | 0.001             |
|  | $L_{qEOi}$             | 0.2246          | 0.220             |
|  | $L_{qAOij}$            | 0.0125          | 0.012             |
|  | $L_{qAij}$             | 0.000018306     | 0.000             |
|  | $L_{qSij}$             | 0.0009221       | 0.001             |
| Waiting Times<br>(excluding service time)<br>( $W_{qk}$ )          | $W_{qNI}$              | 0.0118          | 0.011             |
|  | $W_{qNO}$              | 5.6636          | 4.955             |
|  | $W_{qEi}$              | 0.0120          | 0.012             |
|  | $W_{qEOi}$             | 0.2156          | 0.213             |
|  | $W_{qAij}$             | 0.0010          | 0.001             |
|  | $W_{qAOij}$            | 0.0551          | 0.054             |
|  | $W_{qSij}$             | 0.0042          | 0.004             |
| Mean Message Response Time   | $W_{NMS}$              | 7.8947          | 6.123             |

of TMN systems. With the values of any parameter for a specific system design (for example,  $n, m, \lambda, \mu$ ), a performance analysis for the specific design is possible, and the results are useful in designing an appropriate system.

As a further study, with an analysis of the structure of the communication protocol stack of a real TMN system, we will be able to consider many kinds of operational processes and management messages (e.g., an extra ordinal fault situation and burst type event reports) occurring within systems. In addition, by measuring actual traffic and obtaining empirical data (including the number of Network Elements and the speed of lines), an analysis of the performance of TMN systems considering real user demand and non-Poisson traffic could be the focus of significant research.

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