## Mathematical Verification of a Nuclear Power Plant Protection System Function with Combined CPN and PVS

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#### Abstract

In this work, an automatic software verification method for Nuclear Power Plant (NPP) protection system is developed. This method utilizes Colored Petri Net (CPN) for system modeling and Prototype Verification System (PVS) for mathematical verification. In order to help flow-through from modeling by CPN to mathematical proof by PVS, an information extractor from CPN models has been developed in this work. In order to convert the extracted information to the PVS specification language, a translator also has been developed. ML that is a higher-order functional language programs the information extractor and translator. This combined method has been applied to a protection system function of Wolsong NPP SDS2(Steam Generator Low Level Trip). As a result of this application, we could prove completeness and consistency of the requirement logically. Through this work, in short, an axiom or lemma based-analysis method for CPN models is newly suggested in order to complement CPN analysis methods and a guideline for the use of formal methods is proposed in order to apply them to NPP Software Verification and Validation.

Key Words: mathematical verification, CPN, PVS, formal method

### 1. Introduction

In safety critical systems, use of computers provides many potential advantages. These advantages include more sophisticated safety algorithms, improved availability, easier maintenance, reduced installation costs, ease of modification, and potential for reuse. However, because of the safety critical nature of the application such as NPP protection system, these advantages have to be weighed against the

problems of ensuring that the computer system can be assured adequately.

The use of digital systems is also on increase in nuclear industry in recent years. Therefore, the importance of system V&V (Verification and Validation) is more emphasized in view of the nuclear safety. Many activities are required for NPP software V&V. IEEE std. 1012-1986 defines software V&V activities. This standard classifies the software V&V activities by tasks: Management of V&V, concept phase V&V, requirements phase

V&V, design phase V&V, implementation phase V&V, test phase V&V, installation and checkout phase V&V and operation and maintenance phase V&V tasks are required [9]. Of these tasks, our work concentrates on the requirements phase V&V task since the requirements phase is the most important of all the software development phases. It is well-known that the most of software faults occur at the requirements phase.

A number of different techniques have been used to verify and validate safety-related systems. Of them, formal methods have many superior properties. Formal methods are approaches, based on the use of mathematical techniques and notations, for describing and analyzing properties of software systems. Examples of formal methods are VDM, Z, CCS, CSP, I/O Automata, and Petri Nets [1]. However, there are few formal methods that support both graphical representation and mathematical proof simultaneously, though visualization and mathematical proof are essential properties of them.

In this work, an automatic software verification method for NPP protection system is developed. This method utilizes CPN for modeling and PVS for mathematical verification. CPN supports visualization and PVS does mathematical proofs. For the safety-critical protection systems, complete analysis of the system is needed since an error in the requirements may result in serious faults of software. CPN has been proved as an adequate tool for requirement analysis [2]. CPN has many advantages such as rapid prototyping and visualization of requirements. However, CPN is not proper for the mathematical verification of the system. That is, CPN has many limitations in analysis methods such as occurrence graphs, place and transition invariants, reduction rules. In order to complement these limitations, an axiom or lemma based-analysis method is suggested in this work. PVS is used for the mathematical verification through the axiom or lemma basedanalysis method.

In this work, first, requirements of Steam Generator Low Level Trip (one of the Wolsung NPP SDS2 parameter) are modeled with Design/CPN. This model enables also the easy communication between users and system developers. Next, PVS specification, which is translated from CPN model, is verified mathematically. The main focus in this work is on the flow-through from CPN model to PVS specification. An information extractor and a translator have been developed for this purpose. We introduce some major aspect of CPN and PVS for this work in section 2. In section 3, the flowthrough from CPN model to PVS specification with the extractor and translator is described. An automatic software verification tool is applied to Wolsung NPP SDS2 function in section 4.

## 2. Colored Petri Net and Prototype Verification System

### 2.1. CPN and Design/CPN

Petri Net is a language that has been used in modeling and analyzing the system. Petri Net has expressions of concurrency and formal semantics. In addition, Petri Net can visualize the actual system with ease. However, Petri Net is so basic that the ability of expression is limited and CPN has been developed to overcome this limit. In CPN, color refers to the types of data associated with tokens and is comparable to data types in programming languages. Design/CPN is a powerful tool for the Colored Petri Net. The version of CPN used in Design/CPN incorporates variables (representing the binding of identifiers to specific colored tokens), arc inscriptions (expressions), and the code associated with transitions. In Design/CPN, CPN is a graphical

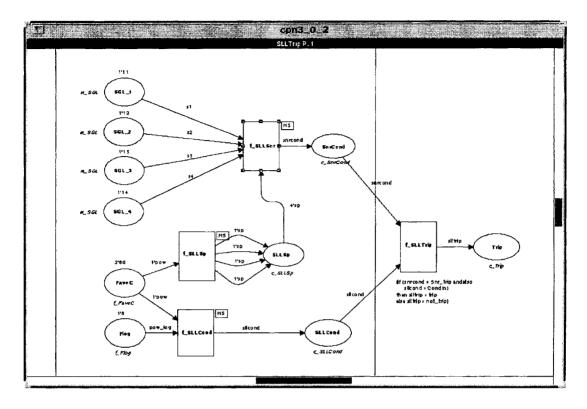


Fig. 2.1. CPN Model of SDS2 Steam Generator Low Level Trip Function

programming language with rich specification and simulation possibilities. The programming language through which CPN specifies desired operations in arc expressions and transition codes is ML.

In CPN, the most straightforward kind of analysis is simulation, which in many respects is similar to the testing and execution of a program. However, it is obvious that, by means of simulation, it is impossible to obtain a complete proof of dynamic properties of CPN. Therefore, there exist a number of formal analysis methods that are based on mathematical proof techniques. The analysis methods are occurrence graphs, place and transition invariants, and reduction rules techniques. The basic idea behind occurrence graphs is to construct a graph containing a node

for each reachable marking and an arc for each occurring binding element. Obviously such a graph may become very large, even for small system. This problem can lead to state explosion. Therefore, we must simplify the CPN by omitting the cycle counters. As reduction methods of occurrence graphs, there exist symmetrical markings, stubborn sets, covering markings and proof rules methods. Place and transition invariants technique is to construct equations which are satisfied for all reachable marking. Analysis by means of place and transition invariants has several attractive properties. First, it is possible to obtain an invariant for a hierarchical CPN by composing invariants of the individual pages. Secondly, we can find invariants without fixing the system parameters, and hence we can

obtain general properties which are independent of the system parameters. Thirdly, we can construct the invariants during the design of a system and this will usually lead to an improved design. However, the main drawback of invariants analysis is the fact that it requires skills which are considerably higher and more mathematical than those required by the other analysis methods. Finally. CPN can also be analyzed by means of reduction, where the basic idea is as follows: First we choose one or more types of properties which we want to investigate. Then we define a set of reduction rules by which we can simplify CPN without changing those properties which we are investigating. A serious problem for many reduction methods is that the absence of a property in the reduced net does not tell much about why the property is absent in the original net [2].

One example Design/CPN model is shown in Fig. 2.1. In this Figure, the CPN model represents the Wolsung NPP SDS2 function (Steam Generator Low Level Trip).

#### 2.2. Prototype Verification System

PVS is a verification system: an interactive environment for writing formal specifications and checking formal proofs. It builds on nearly 20 years experience at SRI in building verification systems, and on substantial experience with other system. The distinguishing feature of PVS is a synergistic integration of an expressive specification language and powerful theoremproving capabilities. PVS has been applied successfully to large and difficult applications in both academic and industrial settings.

PVS provides an expressive specification language that augments classical higher-order logic with a sophisticated type system containing predicate subtypes and dependent types, and with

```
1: sum : THEORY
2: BEGIN
3:
4:
    n: VAR nat
5:
    sum(n): RECURSIVE nat =
6:
           (IF n=0 THEN 0 ELSE n + sum(n-1) ENDIF)
7:
           MEASURE (LAMBDA n: n)
9:
10:
     closed_form: THEOREM sum(n) = (n*(n+1)/2)
11:
12: END sum
```

Fig. 2.2. Specification Language by PVS

parameterized theories and a mechanism for defining abstract data types such as lists and trees. The standard PVS types include numbers (reals, rationals, integers, naturals, and the ordinals to  $\varepsilon_0$ ), records, tuples, arrays, functions, sets, sequences, lists, and trees, etc. The combination of features in the PVS type-system is very convenient for specification, but it makes typechecking undecidable. The PVS typechecker copes with this undecidability by generating proof obligations for the PVS theorem prover. Most such proof obligations can be discharged automatically.

PVS has a powerful interactive theorem prover/proof checker. The basic deductive steps in PVS are large compared with many other systems: there are atomic commands for induction, quantifier reasoning, automatic conditional rewriting, simplification using arithmetic and equality decision procedures and type information, and propositional simplification using binary decision diagrams. The PVS proof checker manages the proof construction process by prompting the user for a suitable command for a given subgoal. The execution of the given command can either generate further subgoals or complete a subgoal and move the control over to the next subgoal in a proof. User-defined proof strategies can be used to enhance the automation in the proof checker. Model-checking capabilities

```
Closed form:
{1} (FORALL (n: nat): sum(n) = (n*(n+1))/2)
Rule? (induct "n")
Inducting on n.
This yields 2 subgoals:
Closed_form.1:
        sum(0) = (0*(0+1))/2
Rule? (postpone)
Postponing closed_form.1.
Closed form.2:
{1}
        (FORALL (j:nat):
         sum(j) - (j*(j+1))/2
                        IMPLIES sum(j+1) = ((j+1) * (j+1) * (j+1+1)) /2
Rule? (assert)
Simplifying, rewriting, and recording with decision procedures,
This completes the proof of closed form.2.
Q.E.D.
```

Fig. 2.3. PVS Proof System

used for automatically verifying temporal properties of finite-state systems have recently been integrated into PVS. PVS's automation suffices to prove many straightforward results automatically: for hard proofs, the automation takes care of the details and frees the user to concentrate on directing the key steps [5].

One example of PVS specification language is shown in Fig. 2.2. Fig. 2.3 shows a part of PVS proof system.

# 3. Verification Technique by Relating CPN with PVS

It is generally well accepted that the complete analysis of requirements is critical for safety and effectiveness of the system. In this work, we have selected CPN as a modeling tool. As mentioned in section 2, in order to analyze requirements of the system based on CPN models, various invariants analysis and reachability analysis techniques have been proposed in many researches [2]. However, these techniques have their own limitations that they can consider only the behavioral aspects of the models, not deal with all the logical aspects, and easily lead to the state explosion problem.

Therefore, we suggest an axiom or lemma based-analysis method in order to supplement the typical CPN analysis methods. For the basis of the axiom or lemma based-analysis, we have shown that CPN models could be translated into axioms or lemmas in a straightforward manner. The translation process is automated through the extractor and the translator developed in this work.

In order to realize the automated analysis for the axioms or lemmas translated from CPN models, an effective theorem prover is required. PVS, which is well known as the verification tool, has been selected in this work. Fig. 3.1 depicts the automatic software verification tool schematically.

### 3.1. CPN Modeling

For modeling systems with CPN, first of all, complete analysis of the system is needed since an error in the requirements may result in serious faults of software. The graphical CPN model may help us to analyze, visualize and simulate system requirements. In CPN, requirements are modeled by objects such as Port, Arc, Place and Transition. Then, CPN model gives users the effects of the rapid prototyping and the visualizing of requirements. Therefore, it is very easy for developers to exchange opinions with users by CPN model.

As shown in Fig. 3.1, CPN model has advantages to analyze the correctness of requirements with type check, syntactic and semantic validation, that is, the simulation with CPN model may prove the completeness of

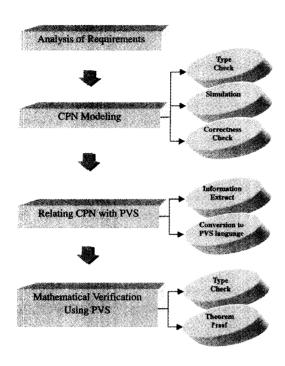


Fig. 3.1. Verification Scheme

requirements and the consistency with requirements. In Design/CPN, type checking is performed by 'Syntax Check' command. Type check supports not only syntactic check of data type but check for properties such as completeness and consistency. 'Enter Simulator' and 'Interactive Run' commands show the feature of simulation process along the each path. Specially, it is shown path by path that tokens of the each page move around. As a result of type check and simulation, correctness check of requirements has been achieved successfully. However, CPN is not proper for the mathematical verification of the system. In this work, therefore, PVS is used for the mathematical verification. Then, PVS help CPN for analysis of the system requirement. PVS also supports the type check function. Data type mismatching is checked by type check function in PVS. In the process of



Fig. 3.2. A Process of the Extractor in Design/CPN

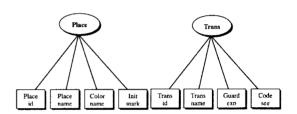


Fig. 3.3. The Example Structure of Extracted Information

Theorem Proofs, semantic check of PVS specification from system requirement is performed and that is checked whether PVS specification is correct logically or not. As a result of this process, software is verified mathematically and may have the enhanced reliability.

# 3.2. Conversion to PVS Specification Language Using Extractor and Translator

It is not meaningless to perform an analysis for each model independently because the analysis of the system is performed in the "divide and conquer" manner. In Design/CPN, it is impossible to access to a data structure of the system directly, but the system information can be extracted by using a ML program. That is, Design/CPN has

```
begin
read the data structure from the output of extractor;
do {
   find a transition t;
   if (t has a guard or arc expression) then
         { check whether clauses can be used for AXIOM or LEMMA;
           if (check = OK) then
                           { find input;
                          if ( there exists input place that is the output place
                              of another transition, and the transition has the
                              OK guard or arc expression)
                           then translate the guard or arc expression into LEMMA;
                           else translate the guard or arc expression into AXIOM;
                           }
           else PASS;
   else PASS;
} until ( there is no more guard or arc expression );
Let the final (i.e., last linked to output place) guard or arc expression
         be THEOREM;
end.
```

Fig. 3.4. The Algorithm of the Translator

internal functions for asking questions to modeled system. Using this ML functions and programs, we can extract the required system information from the CPN models. Therefore, an extractor has been used in this work. The extractor is run on the Design/CPN, as shown in Fig. 3.2. Objects for converting in CPN are Place, Port, Transition,

Sub-Transition, Arc, Color, and variable declaration. When the extractor has met Places in CPN models, that extracts the information such as place id, place name, color name and initial marking. And the extractor can extract transition id, transition name, guard expression and code segment in Transition objects. Fig. 3.3 shows the

example structure of extracted information.

In PVS, it is hard to verify a system with the above results. Therefore, we need a process that the results from CPN model are converted to PVS inputs (PVS specification language). This process is performed with the translator developed in this work. The translator is also constructed with ML language. The translation process is straightforward. Guards of a transition are translated to THEOREM, AXIOM or LEMMA of PVS, if clauses can be used both in guard regions of CPN and for THEOREM, AXIOM or LEMMA expressions. For arc expressions, the same rules are applied. Fig. 3.4 describes the algorithm that the guards and arc expressions of CPN are translated into AXIOMs or LEMMAs of PVS.

When the translation process has finished successfully, PVS input form such as Fig. 2.2 is generated and we can verify with this converted input mathematically.

## 3.3. Verification and Validation Using PVS

In this work, the method of verification is the mathematical verification for the converted PVS specification language. PVS specification language for each page is represented with timed states. Thus, we have considered the signal and the power of the system as functions of time. Then, it is proved mathematically using the PVS proof system.

PVS proof system has interactive form with the real examiner. Therefore, in PVS proof system, prompt is [Rule?]. In this work, PVS proof system analyzes a specification language to be based on conditional sentences of transition, and, we investigate that these conditional sentences are realized in all-time cases. In addition, PVS proof system shows the proof case at constant time(t=0). In PVS proof system, proof commands like skosimp(Skolemize then Flatten), prop

(Propositional Simplification), postpone(Go to Next Remaining Goal), grind(induct and simplify) are used.

#### 3.4. Discussion

Requirements phase V&V tasks defined in IEEE std. 1012 are as follows:

- (1) Software Requirements Traceability Analysis.: Trace SRS (Software Requirement Specification) requirements to system requirements in concept documentation. Analyze identified relationships for correctness, consistency, completeness, accuracy.
- (2) Software Requirement Evaluation. : Evaluate SRS requirements for correctness, consistency, completeness, accuracy, readability, and testability. Assess how well SRS satisfies software system objectives. Assess the criticality of requirements to identify key performance or critical areas of software.
- (3) Software Requirements Interface Analysis. :
  Evaluate SRS with hardware, user, operator,
  and software interface requirements
  documentation for correctness, consistency,
  completeness, accuracy, and readability.
- (4a) Test Plan Generation. : Plan system testing to determine if software satisfies system objectives. Criteria for this determination are, at a minimum: (a) compliance with all functional requirements as complete software end item in system environment (b) performance at hardware, software, user, and operator interfaces (c) adequacy of user documentation (d) performance at boundaries (for example, data, interface) and under stress conditions. Plan tracing of system end-item requirements to test design, cases, procedures, and execution results. Plan documentation of test tasks and results.
- (4b) Acceptance Test Plan Generation. : Plan

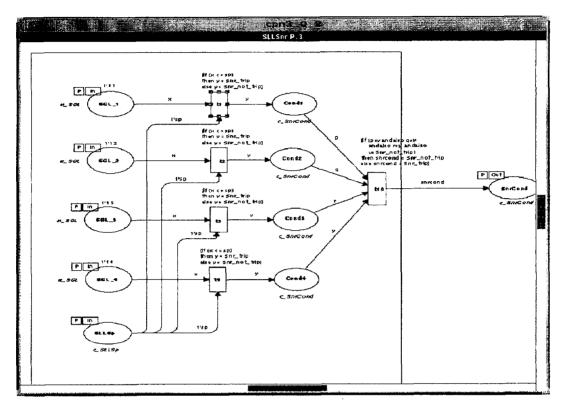


Fig. 4.1. CPN Model of f\_SLLSnr Function

acceptance testing to determine if software correctly implements system and software requirements in an operational environment. Criteria for this determination are, at a minimum: (a) compliance with acceptance requirements in operational environment (b) adequacy of user documentation. Plan tracing of acceptance test requirements to test design, cases, procedures, and execution results. Plan documentation of test tasks and results.

Our work could deal with the issue (2), (3) and (4a) and it is difficult to handle (1) and (4b) through the method proposed in this work. In the CPN modeling process, consistency, accuracy and readability of system requirements could be addressed through the various analysis methods

that Design/CPN has offered basically. The CPN model could be simulated and analyzed in view of occurrence graphs with ease in Design/CPN. This may prove the completeness of requirements and the consistency with requirements. In system test plan generation activity, the information through the simulation of Design/CPN can help to test design, cases, procedures, and execution results. On the other hand, with PVS, we can find the fact that no significant problem can be found logically and we can evaluate completeness and correctness of requirements. In this way, our work can address some issues of requirements V&V phases partially or entirely.

In addition, it is the state of the art of software V&V that the commercial automated-V&V tool

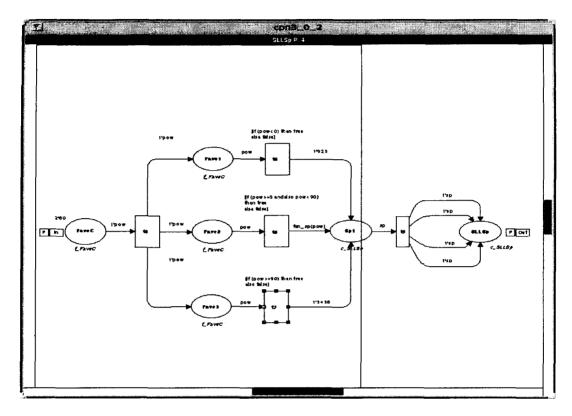


Fig. 4.2. CPN Model of f\_SLLSp Function

does not exist yet. And another modeling tool such as CPN in this work is the Statecharts [1]. Statecharts are very similar to CPN as a point of expressive power and used to specify state transitions in reactive system. However, Statecharts don't have automated formal analysis methods.

## 4. Application

#### 4.1. CPN Modeling

In this work, the target requirement is that for the Wolsung NPP SDS2 function (Steam Generator Low Level Trip). In this requirement, the functional requirements such as f\_SLLCond, f\_SLLCondA, f\_SLLSnr, f\_SLLSp, f\_SLLSpD, and f\_SLLTrip are included. These functional requirements are modeled with Design/CPN.

Fig. 2.1 shows the top-level CPN model of the function, and other sub-models are shown in Fig.  $4.1\ \text{to}\ 4.3$ 

## 4.2. Conversion to PVS Specification Language Using ML Language

This section is for the process to help flowthrough from requirements to PVS specification language using extractor and translator.

As mentioned in section 2.1, PVS specification language is composed of simple THEORYs. Therefore, the main page is translated to SLLTrip

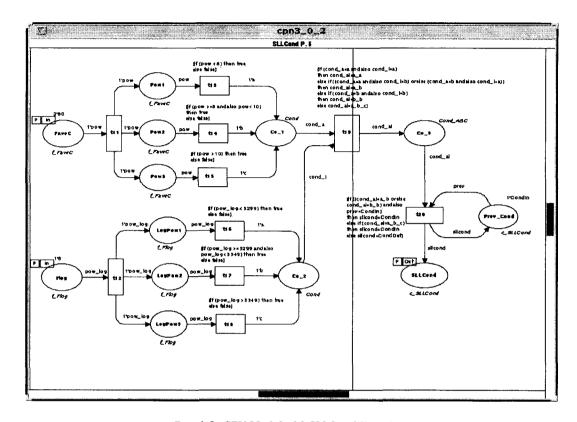


Fig. 4.3. CPN Model of f\_SLLCond Function

function THEORY and sub-pages to SLLSnr, SLLSp and SLLCond function THEORYs, respectively. Each THEORY is described in the next section.

#### 4.3. Verification and Validation Using PVS

This section describes PVS specification converted from SDS2 system models by the translator. The PVS specification language is composed of SLLTrip.pvs (Fig. 4.7), SLLSnr.pvs (Fig. 4.8), SLLSp.pvs (Fig. 4.9), and SLLCond.pvs (Fig. 4.10) files, named after CPN model pages. The declaration part is translated to dictionary.pvs (Fig. 4.5) and variables.pvs (Fig. 4.6) files which are imported to the

THEORYs using IMPORTING command.

Fig. 4.11 describes the partial of proof in SLLSnr specification language.

#### 4.4. Discussion

In this application for Wolsung NPP SDS2, system requirements were modeled by CPN. Therefore, rapid prototyping and visualization could be achieved and it was very easy to simulate the system. In Design/CPN, the correctness and consistency of requirements could be analyzed through various analysis methods. As a result of this application, we could found that any logical problems do not exist in the specification. We also found that

dictionary % [ parameters ]	variables % [ parameters ]	SLLTrip % [ parameters ]
: THEORY	: THEORY	: THEORY
BEGIN	BEGIN	BEGIN
% ASSUMING	% ASSUMING	% ASSUMING
% assuming declarations	% assuming declarations	% assuming declarations
% ENDASSUMING	% ENDASSUMING	% ENDASSUMING
time : TYPE = nat	IMPORTING dictionary	
m_SGL: TYPE = int	% variable declare	IMPORTING dictionary
f_FaveC : TYPE = int		IMPORTING variables
f_Flog : TYPE = int	t : time	IMPORTING SLLSnr
c_SLLSp : TYPE = int	s1:m_SGL	IMPORTING SLLCond
c_SnrCond : TYPE = Snr_trip,	s2:m_SGL	IMPORTING SLLSp
Snr_not_trip	s3:m_SGL	
c_SLLCond : TYPE = CondIn,	s4 : m_SGL	f_SLLTrip : THEOREM (IF
CondOut	pow : POWT	snrcond=Snr_trip AND sllcond=CondIn
c_Trip : TYPE = trip, not_trip	pow_log : POWLOGT	THEN slltrip=trip ELSE slltrip=not_trip
Cond_ABC: TYPE = a_a, a_b,	sp : c_SLLSp	ENDIF)
b_b, a_b_c	snrcond : c_SnrCond	
Co: TYPE = a, b, c	sllcond : c_SLLCond	END SLLTrip
	prev : c_SLLCond	
XT : TYPE = [time -> m_SGL]	slltrip : c_Trip	
YT : TYPE = [time -> c_SnrCond]	x1 : XT	
POWT : TYPE = [time -> f_FaveC]	x2 : XT	
POWLOGT : TYPE = [time ->	x3:XT	
f_Flog]	x4 : XT	
	yl:YT	
END dictionary	y2 : YT	
	y3 : YT	
	y4 : YT	
	cond_a : Co	
	cond_1 : Co	
	cond_al : Cond_ABC	
	END variables	

of Dictionary.pvs

Fig. 4.5. Specification Language Fig. 4.6. Specification Language of Variables.pvs

Fig. 4.7. Specification Language of SLLTrip.pvs

CPN has insufficient expressive power to specify time-related properties. Therefore we can suggest improving the CPN.

Furthermore, with PVS, the mathematical

verification for CPN models was performed in order to achieve the improved software reliability. In order to enhance the mathematical verification with PVS, more proof strategies of

SLLSnr % [ parameters ]	SLLSp % [ parameters ]	SLLCond % [ parameters ]
: THEORY	: THEORY	: THEORY
BEGIN	BEGIN	BEGIN
% ASSUMING	% ASSUMING	% ASSUMING
% assuming declarations	% assuming declarations	% assuming declarations
% ENDASSUMING	% ENDASSUMING	% ENDASSUMING
IMPORTING dictionary	IMPORTING dictionary	IMPORTING dictionary
IMPORTING variables	IMPORTING variables	IMPORTING variables
t1: AXIOM (IF x1(t) <= sp THEN	t8: THEOREM	T11:THEOREM
y1(t)=Snr_trip ELSE y1(t)=Snr_not_trip	(FORALL(t:time):( IF pow(t) < 0 THEN	(FORALL(t:time):(IF pow(t)<8 THEN
ENDIF)	sp=923 ELSE (IF pow(t)>=0 AND	cond_a=a ELSE (IF pow(t)>=8 AND
$t2 : AXIOM (IF x2(t) \le sp THEN$	pow(t)<90 THEN sp=(28*pow(t)+923)	pow(t)<10 THEN cond_a=b ELSE
y2(t)=Snr_trip ELSE y2(t)=Snr_not_trip	ELSE sp=3438 ENDIF) ENDIF))	cond_a=c ENDIF) ENDIF))
ENDIF)		
t3: AXIOM (IF x3(t) <= sp THEN	END SLLSp	T12 : THEOREM
y3(t)=Snr_trip ELSE y3(t)=Snr_not_trip		(FORALL(t:time):(IF pow_log(t)<3299
ENDIF)		THEN cond_l=a ELSE (IF
t4 : AXIOM (IF x4(t) <= sp THEN		pow_log(t)>=3299 AND
y4(t)=Snr_trip ELSE y4(t)=Snr_not_trip		pow_log(t)<3349 THEN cond_l=b
ENDIF)		ELSE cond_l=c ENDIF) ENDIF))
t10 : THEOREM		
(FORALL(t:time):(IF		T19: THEOREM (IF cond_a=a AND
y1(t)=y2(t) AND $y2(t)=y3(t)$		cond_l=a THEN cond_al=a_a ELSE (IF
AND y3(t)=y4(t) AND		(cond_a=a AND cond_l=b) OR
y4(t)=Snr_not_trip THEN		(cond_a=b AND cond_l=a) THEN
snrcond=Snr_not_trip ELSE		cond_al=a_b ELSE (IF cond_a=b AND
snrcond = Snr_trip ENDIF))	· ·	cond_l=b THEN cond_al=b_b ELSE
		cond_al=a_b_c ENDIF) ENDIF)
END SLLSnr		ENDIF)
		T20: THEOREM (IF (cond_al=a_b
		OR cond_al=b_b) AND prev=CondIn
		THEN sllcond=Condin ELSE (IF
		cond_al=a_b_c THEN sllcond=CondIn
		ELSE slicond=CondOut ENDIF)
		ENDIF)
		END SLLCond

Fig. 4.8. Specification Language Fig. 4.9. Specification Language Fig. 4.10. Specification Language of SLLSnr.pvs

of SLLSp.pvs

of SLLTCond.pvs

```
110:
                                                                                  Rule? (grind)
                                                                                  stty:: 303770706510 00167466
    (FORALL (t: time):
                                                                                  stty:: 303770706510 00167466
       (IF y1(t) = y2(t) AND y2(t) = y3(t) AND y3(t) = y4(t) AND y4(t) = Snr_not_tp
                                                                                  Trying repeated skolemization, instantiation, and if-lifting,
        THEN sarcond = Snr_not_trip ELSE snrcond = Snr_trip ENDIF))
                                                                                  this simplifies to:
Rule? (skosimo)
                                                                                 t10.1.1:
Skolemizing and flattening,
                                                                                 [-1]
                                                                                           t!1 = 0
this simplifies to:
                                                                                 -2
                                                                                         y1(0) = y4(0)
t10:
                                                                                  -3
                                                                                         y2(0) = y4(0)
                                                                                  -4
                                                                                         y3(0) = y4(0)
1 (IF y1(t!1) \approx y2(t!1) AND y2(t!1) = y3(t!1) AND y3(t!1) = y4(t!1)
                                                                                 -5
                                                                                         Snr_not_trip?(y4(0))
     AND y4(t!1) = Snr_not_trip THEN snrcond = Snr_not_trip
     ELSE surcond = Snr_trip
                                                                                        Snr_not_trip?(snrcond)
                                                                                 1
     ENDIF)
                                                                                 Rule? (postpone)
Rule? (prop)
                                                                                 Postponing t10.1.1.
Applying propositional simplification,
                                                                                 t10.1.2:
this yields 5 subgoals:
                                                                                 [-1]
                                                                                           y1(t!1) = y2(t!1)
t10.1:
                                                                                           y2(t!1) = y3(t!1)
                                                                                 [-2]
-1
    y1(t!1) = y2(t!1)
                                                                                 [-3]
                                                                                           y3(t!1) = y4(t!1)
-2 y2(t!1) = y3(t!1)
                                                                                 [-4]
                                                                                           y4(t!1) = Snr_not_trip
-3 y3(t!1) = y4(t!1)
-4 y4(t!1) = Snr_not_trip
                                                                                        t!1 = 0
                                                                                 1
1 snrcond = Snr_not_trip
                                                                                 [2]
                                                                                          snrcond = Snr_not_trip
Rule? (case "t!1=0")
                                                                                 Rule? (assert)
Case splitting on
                                                                                 Simplifying, rewriting, and recording with decision procedures,
   t!1=0,
                                                                                 this simplifies to:
this yields 2 subgoals:
                                                                                 t10.1.2:
t10.1.1:
                                                                                 [-1]
                                                                                           y1(t!1) = y2(t!1)
-1 t!1 = 0
                                                                                 [-2]
                                                                                           y2(t!1) = y3(t!1)
[-2] y1(t!1) = y2(t!1)
                                                                                 [-3]
                                                                                           y3(t!1) = y4(t!1)
      y2(t!1) = y3(t!1)
[-3]
                                                                                 [-4]
                                                                                           y4(t!1) = Snr_not_trip
[-4]
      y3(t!1) = y4(t!1)
[-5] y4(t!1) = Snr_not_trip
                                                                                 [1]
                                                                                          t!1 = 0
                                                                                 [2]
                                                                                          snrcond = Snr_not_trip
[1] snrcond = Snr_not_trip
```

Fig. 4.11. The Partial of Proof in SLLSnr Specification

PVS proof checker should be also developed.

## 5. Conclusions and Further Study

In this work, an axiom or lemma basedanalysis method for CPN models is newly suggested in order to complement CPN analysis

Fig. 4.11. The Partial of Proof in SLLSnr Specification (Cont'd)

methods. Since an existing analysis techniques have their own limitations that they can consider only the behavioral aspects of the models, not deal with all the logical aspects, and easily lead to the state explosion problem. In addition, a guideline for the use of formal methods in order to apply them to NPP software V&V is

proposed in this work.

We could visualize the system requirements easily by using CPN model and verify the system mathematically by using PVS. The integration of CPN and PVS, which realizes rapid prototyping and mathematical verification, can enhance the software reliability by logical analysis using PVS. CPN and PVS can cover disadvantage of each other. In order to help flow-through from modeling by CPN to mathematical proof by PVS, an information extractor from CPN models has been developed. And a translator also has been developed and used in this work. Our software verification method is demonstrated to be useful with a simple example application and the completeness and consistency of system requirements is proved successfully.

In the future, we are planning to use this software verification method for safety critical system in other areas. As a result of this work, this software verification method may be a foundation of enhancement for Design/CPN and PVS. And, in order to improve the CPN, timing issue must be addressed and this can be based on an advancing state based modeling tool. In addition, we are going to develop the more adequate prover. Then we can realize the integrated software V&V tool.

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