Solid-state reaction kinetics for the formation of aluminium titanate (Al_2TiO_5) from amorphous TiO_2 and α - Al_2O_3

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비정질 TiO_2 와 α - Al_2O_3 부터 Al_2TiO_5 를 합성하기 위한 고체상대 반응속도

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Abstract Reaction kinetics for the solid-state reaction of α -Al₂O₃ with amorphous TiO₂ to produce Al₂TiO₅ (Tialite) was studied in the temperature range of $1200 \sim 1300 \,^{\circ}$ C. Rate of kinetic reaction were determined by using TiO₂-coated Al₂O₃ compact containing 50 mol% TiO₂ and heating the reactant mixtures in MgO at definite temperature for various times. Amount of products and unreacted reactants were determined by X-ray diffractometry. Data from the volume fraction and ratio of peak intensities of β -Al₂TiO₅ indicated that the reaction of α -Al₂O₃ with TiO₂ to form pseudobrookite starts between 1280 and 1300 $^{\circ}$ C. The activation energy for solid-state reaction was determined by using the Arrhenius equation; The activation energy was 622.4 kJ/mol.

요 약 α-Al₂O₃와 비정질 TiO₂부터 Al₂TiO₅를 합성하기 위한 고체상태반응의 반응속도를 1200~1300℃ 온도 범위에서 연구하였다. 한응속도는 Al₂O₃분말을 코팅한 50 mol%의 TiO₂와

일정한 온도에서 여러 시간동안 가열하여 생성된 혼합물에 의하여 결정되었다. MgO안의 반응물과 미반응물의 양은 X-선 회절분석에 의하여 결정되었다. Al_2TiO_5 의 부피율과 peak intensity비의 자료로부터 Al_2O_3 와 TiO_2 의 pseudobrookite(Tialite)형태로의 반응은 1280 $\mathbb C$ 와 1300 $\mathbb C$ 사이에서 시작되었다. 고체상태반응 활성화 에너지는 Arrhenius식에 의하여 결정되었다. 활성화 에너지는 622.4 kJ/mol이다.

1. Introduction

Aluminium titanate (Al₂TiO₅) is well known as a low thermal expansion, a good thermal insulation, and a low Young's modulus thereby has excellent thermal shock resistant material [1,2]. These properties allow for the insert-casting of ceramic portliners into the cylinder head (aluminium or cast iron), where they serve as a thermal insulation of the exhaust gas [3,4]. However, those composites have a low mechanical strength due to the presence of microcracks developed by the large difference in thermal expansion coefficients along crystallographic axes [5,6]. Al₂TiO₅ is a polycrystalline substance that exists in two forms, α and β (Tialite), the first only being stable at temperature higher than 1820℃. Unstabilized aluminium titanate tends to decompose fully into Al₂O₃ and TiO₂ in the range 800~1300℃. The decomposition occurs, it has been theorized, when adjacent aluminium and titanium octahedra collapse because the lattice site occupied by the aluminium is too large. The available thermal energy permits the aluminium to migrate from its position, and results in a structural dissolution to rutile and corundum [7,8]. Following the decomposition, the material exhibits neither a low thermal expansion coefficient nor a favorable thermal shock behavior, that rendered it apparently useless for industrial applications.

Successful application of the materials has depended on the ability to the control the sintering condition and decomposition behavior, together with an ability to understand the microcracking phenomena.

The crystal structure of the β -Al₂TiO₅ is of the pseudobrookite type with a theoretical density of 3.70 g/cm³ [9]. The densities of the starting oxides α -Al₂O₃ and TiO₂-rutile are 3.99 and 4.25 g/cm³, respectively. Therefore reaction (1) is accompanied by an 11 % molar volume increase.

$$\alpha$$
-Al₂O₃+TiO₂-rutile $\rightarrow \beta$ -Al₂TiO₅ (Tialite)
(1)

The quantitative X-ray determination for Al₂TiO₅, corundum and rutile contents is necessary in order to characterize the behavior and properties of such materials.

Quantitative X-ray diffractometric phase analysis assumes that the intensity, I, of the X-ray diffractometric reflection of a crystalline phase α is proportional to the phase's concentration in an aggregate; The following equation is valid:

$$I = C/\mu^* m \tag{2}$$

where I is intensity of the X-ray interference, C is concentration of the crystalline phase α , μ^* m is mass absorption coefficient of the bulk sample.

The intensity of one X-ray reflection of a crystalline phase is compared with a corresponding X-ray reflection of a reference material containing a known percentage of the phase to be determined. The X-ray reflection intensity is also dependent on the mean grain size and on the grain size distribution. The X-ray reflection intensity increase with decreasing grain size and displays a maximum between 20 and 1 μ m. Still smaller mean grain sizes are shown by line broadening and intensity decrease of the X-ray reflections. Crystal disordering and deformation of the crystal structure can also cause intensity decreases. Moreover, grain morphology also influences the reflection intensities: the more the crystallinity deviates from the globular state, the more certain lattice planes show preferred orientation under preparation of powder samples. The resultantly higher intensity may simulate exaggerated phase contents.

In this study, the internal standard method is used for quantitative X-ray phase analysis and reaction kinetics between amorphous TiO_2 and α -Al₂O₃ to

form Al₂TiO₅. A stoichiometric mixture of the reactants in MgO was a high-purity alumina which is coated with a dilute solutions of titanium tetraethoxide Ti(OC₂H₅)₄, and the samples heated between 1250 and 1300°C for various times. The amount of Al₂TiO₅, Al₂O₃, and TiO₂ in the final samples were determined by X-ray diffractometry. The rates for the Al₂TiO₅ formation reaction were determined from these results.

Experimental procedures

Ethyltitanate $Ti(OC_2H_5)_4(Huels AG)$, α -Al₂O₃(A-16 SG; mean particle diameter: $0.3\sim0.5~\mu\,\mathrm{m}$; Alcoa Chem.), and Ethanol (Merck) were used as starting materials. Al₂O₃-TiO₂-amorphous composite powder were prepared by stepwise alkoxide hydrolysis of a molar ratio [H₂O/Ti(OC₂H₅)₄] of 4 in α-Al₂O₃ powder ethanolic colloid solutions. Typical final solution concentrations were 0.05 mol $Ti(OC_2H_5)_4$, 0.2 mol H_2O , and 16.9 mol ethanol. The dispersion of coated powder was next centrifuged to remove the alcoholic solution, then washed with deionized water and redispersed in aqueous NH₄OH solution (pH=10). Power compacts were prepared by centrifugal casting, followed by drying at room temperature for one day. The unagglomerated Al₂O₃-TiO₂-amorphous composite powder (50 mol% TiO2) is shown in Fig. 1. Before firing, compacts were calcined in air at 650°C for 1 h to remove organic material.

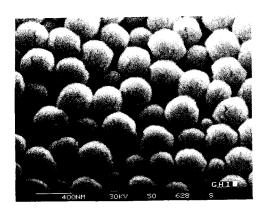


Fig. 1. Scanning electron micrograph of top surface of amorphous TiO₂-coated Al₂O₃ green compact (50 mol% TiO₂) made by centrifugal casting.

After adding KB 2010 (Zschimmer & Schwarz, Lahnstein/Rh) as binder the powders were formed uniaxially into pellets (8×15 mm²) at 400 N/mm². The firing was carried out in air in an electric furnace with molybdenum silicide heating elements. The sample were introduced at a constant rate so that they were exposed within 5min to the indicated temperature. The temperature of the furnace was controlled a Pt-13Rh/Pt thermocouple and at the end of each temperature, they were water quenched.

In this paper, quantitative X-ray measurements (XRD) were performed using Ni-filtered CuK α radiation. The scanning speed was 0.5 2 θ /min. As an internal standard 50 wt% of MgO powder was added to the sample, which has chemical composition of Al₂O₃: TiO₂ in rate of moles 1:4, 1:1, and 4:1, respectively. The mixture was during 5min in a percus-

sion mill. Such a time represents a compromise between particle size reduction which improves reproducibility and crystallite destruction which expecially affected the TiO_2 peak intensity thus changing the peak height ratios. The following peaks were evaluated: MgO(220), Al₂TiO₅(023), α -Al₂O₃(104), and TiO₂-rutile(101). According to the internal standard method, the following equation is used for calculating the phase content of a phase mixture:

$$X_a = I_{ax}/I_e \times \rho_a/\rho_e \times X_e/(1-X_e)$$
 (3)

Where X_a is content of the phase of a in the sample in weight %, X_e is content of the phase of e in the reference material in weight %, I_{ax} is reflection intensity of the phase of a, I_e is reflection intensity of the reference material, ρ_a and ρ_e are density of a and e, respectively.

The following equations give the concentration of Al₂O₃, TiO₂, and Al₂TiO₅ in mole percent as function of the peak height rations:

$$\begin{split} &C_{Al,O,} = I_{Al,O,(104)} / I_{MgO(220)} \\ &C_{TiO,} = I_{TiO,(101)} / I_{MgO(220)} \\ &C_{Al,TiO,} = I_{Al,TiO,(023)} / I_{MgO(220)} \end{split} \tag{4}$$

If one knows the initial composition of the powder, these eq. (4) allow for the independent determination of the mole percent of Al₂TiO₅. Figure 2 shows the standard sample of Al₂TiO₅ obtained by XRD. The peak height relations have been established experimentally from powder mix-

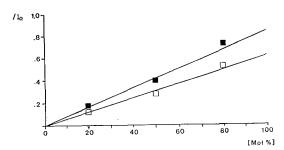


Fig. 2. The standard curve for the formation of Al_2TiO_5

(\blacksquare : α -Al₂O₃, \square : TiO₂-rutile).

tures of known compositions to serve as standards.

The final densities were measured for composite powders. The TiO_2 -coated Al_2O_3 powders consist of spheroidal particles having a narrow size distribution and a large surface area (118.2 m^2/g)

3. Development of chemical kinetic equation

Most ceramic process is carried out by intimately mixing fine powders. In 1929, Jander applied the parabolic rate law, developed for planar interface reactions, to powdered compacts [10].

$$r_0^2 [1 - (1 - X)^{1/3}]^2 = 2kt$$
 (5)

Eq. (5) is the well-known Jander's equation relating X the fraction of reaction completed to time. Where k is the rate constant and r_o is the initial radius of the reacting particles. By plotting $[1-(1-X)^{1/3}]^2$ versus time, reaction-rate constant equiva-

lent to k/r_o² can be obtained, which is characteristic of the reaction conditions. A schematic representation of the geometry that Jander used in developing his solid-state kinetic model is given in Fig. 3.

There are two oversimplifications in eq. (6) which limit its applicability and the range over which it adequately predicts reaction rates. First, eq. (5) is valid only for a small reaction thickness, Y; and second, there was no consideration of a change in molar volume between the reac-

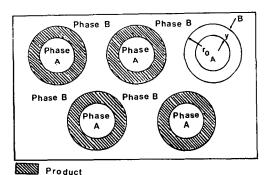


Fig. 3. Jander solid-state reaction geometry (Phase A is completely and constantly covered with particles of component B) [10].

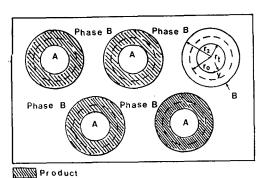


Fig. 4. Carter solid-state reaction geometry (Phase A is completely and constantly covered with particles of component B) [10].

tants and the product layer.

Carter's equation indicated that the time dependence of the fraction reacted corrected for these two constraints is given as:

$$[1+(Z-1)X]^{2/3}+(Z-1)(1-X)^{2/3}$$
=Z+2(1-Z) kt/r_o (6)

Eq. (6) to represent the rate of product formating and entered a Z term to account for the change in volume, where Z represent the volume of the reaction product formed per unit volume of reactants consumed. Figure 4 is a schematic representation of the Carter's mechanism.

Where r_o is the initial radius, r_t the radius of unreacted material at any time t and r₂ the radius of the sphere which includes reacted and unreacted material at any time t. The values of the rate constant k, as a function of temperature, were analyzed by means of the Arrhenius equation.

$$1_{n}k-1_{n}k_{o}=-E/RT \tag{7}$$

It is assumed that the intensities are proportional to the number of moles the species. The investigated test samples with 50 wt% of original standard by X-ray, was evaluated the rate of moles of unreacted mixture of Al₂O₃ and TiO₂. Because of the stoichiometry of the chemical reaction, i.e.,

$$\alpha$$
-Al₂O₃+TiO₂-amorphous
 $\rightarrow \beta$ -Al₂TiO₅ (8)

Through multiplication with the volumes of the moles was estimated the volume of solid species per mole on the layers on the spheres with following equation.

$$X = \frac{V_{Al,TiO_s}}{V_{Al,O_s} + V_{TiO_s} + V_{Al,TiO_s}}$$
(9)

The volumefraction X of the Al_2TiO_5 can be calculated from Eq. (9). Z can be obtained from the relation of the volume of moles. Because of Al_2O_3 as the starting material was coated from amorphous TiO_2 , obtains one the ratio Z for TiO_2 -coated Al_2O_3 green compact (50 mol% TiO_2) of 1.69. Optical microscopie examination of equimolar sample of Al_2O_3 - TiO_2 composite showed that the particle size was approximately 0.4 μ m in diameter (0.2 μ m in radius), substituted into Eq. (6).

4. Results and discussion

Powder X-ray diffraction intensities of TiO₂ gel without soaking time are shown in Fig. 5. These data were fitted by means of ratio of peak intensities of anatase (101), suboxide (104), (110), (111), and rutile (110). Anatase peaks were detected between 330°C and 920°C. The amorphous TiO₂ began to crystallize at approximately 330°C, and suboxide (TiO₂) peaks were detected between 480°C and 1200°C. Rrutile was first detected at 400°C. The formation of extended defects in Titanium Oxides, with large deviation

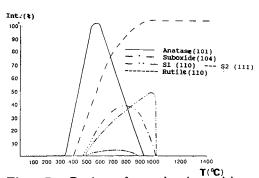


Fig. 5. Ratio of peak intensities of anatase, suboxide, and rutile vs heat-treatment.

from stoichiometry in the direction of a deficit of TiO_{2-x} (Suboxide, $x=1.5\sim2.0$), causes local reconstruction of the crystal lattice.

It has been known that deviation from stoichiometry are caused by the presence of defects in the cation sublattice, whears the anion sublattice is almost perfectly odered. The stoichiometric deviation of TiO_{2-x} increased with decreasing of the partial pressure of oxygen in eq. (10) [11].

$$X = \text{Const. } PO_2^{-1/6}$$
 (10)

The octahedron of TiO_2 are in general jonined by the their edges and form chains, connected by corners of the octahedra. In suboxide $(TiO_2 \rightarrow Ti_2O_3)$ are connected by common faces. The formation of extended defects of TiO_2 by crystallographic shearing are shown schematically in Fig. 6.

The only difference between the crystal structures of higher and lower oxides is

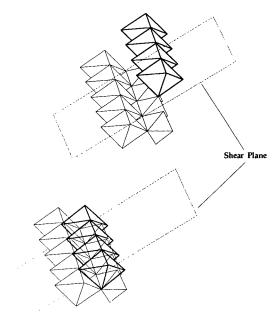


Fig. 6. Formation of $Ti_2O_3(Suboxide)$ and $Ti_3O_5(Anosovit)$.

the coordination number of anions, which changes from 3 to 4 on passing from oxides of the MeO₂ type to Me₂O₃. The above consideration lead to the conclusion that the generation of shear plane in the crystal causes a deviation from stoichiometry in the direction of a deficit in oxygen (or excess of Metal), which is not related to the presence of point defects [12].

The crystalline phase of the amorphous TiO_2 gel powder as function of temperature and soaking time in reported in Table 2. A very small peak of anatase are observed in the pattern of the TiO_2 gel at 200° C, and crystallized at 300° C for 1 hr. Suboxides peaks were detected between 550° C and 900° C. Rutile was detected at 480° C for 1 hr.

Powder X-ray diffraction intensities of

Table 1
Physical properties of amorphous TiO₂-coated Al₂O₃ powders

Precursor	Corundum	Ti(OC ₂ H ₅) ₄ +corundum
Crystal form	α-corundum	amorphous+corundum
Average particle size range (μ m)	$0.2 \sim 0.3$	0.4
Green density (g/m³)	2.15	1.9
Density (g/m³)	3.91	$3.1 \sim 3.4$
Surface area (m²/g)	10~15	118.2

Table 2 Phase composition of the amorphous TiO_2 gel (high temperature X-ray diffraction)

Temp./Soaking time	Phase composition of the amorphous TiO ₂ -gel (hkl)							
(℃/hr.)								
	A(101)	S(104)	S(110)	S(012)	R(110)			
200	vs							
300	vs							
300/1	m							
400/1	S							
480/1	S				vw			
550	vs	w		vw	m			
550/1	vs	w	w	vw	S			
800	S	m	w	vw	S			
800/2	m	s	m	vw	S			
900	w	m	vw		vs			
900/2	vw				vs			
1000	vw				VS			
1000/2					vs			

Phase: A=Anatase, S=Suboxide, R=Rutile

Intensity: vs=very strong, s=strong, m=middle, w=weak, vw=very weak.

the amorphous TiO_2 -coated α - Al_2O_3 gel powder at 200 to $1400\,^{\circ}\mathrm{C}$ without soaking time are shown in Fig. 7. These data were fitted to Fig. 6 by means of ratio of peak intensities of β - Al_2TiO_5 , anatase, rutile and corundum vs heat-treatment, which relative peak intensities with of β -

Al₂TiO₅ (023), anatase (101), rutile (110) and α -Al₂O₃ (104) were measured on the X-ray powder diffraction. The crystallization of amorphous TiO₂ occurred and peaks were observed in the pattern of the samples heated at > 450°C, broad peaks of anatase between 450 and 1100°C and rutile

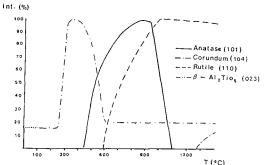


Fig. 7. Ratio of peak intensities of anatase, rutile, corundum, and β -Al₂TiO₅ vs heat-treatment.

at > 600°C. β -Al₂TiO₅ was first detected in the heat-treated samples at 1280°C. No evidence of aluminium titanate formation can be found, which is consistent with the fact that the specimen had been heat-treated below the eutectoid temperature of 1280°C [13].

The crystalline phase of the amorphous TiO_2 -coated α - Al_2O_3 gel powder as a funtion of temperature and soaking time is reported in Table 3. No β - Al_2TiO_5 was

Table 3 Phase composition of the amorphous TiO_2 -coated α - Al_2O_3 (high temperature X-ray diffraction)

Temp./Soaking time	Phase composition of the amorphous TiO ₂ + α -Al ₂ O ₃								
(°C/hr)	(hkl)								
	С	С	A	С	A	R	R	AT	AT
	(104)	(012)	(101)	(110)	(004)	(101)	(110)	(110)	(023)
100	w	W							
200	s	m							
300	vs	S		w					
400	vs	S		m					`
500	s	s	s	m	m				
600	w	vs	S	m	m	w	w		
900	w	vs	vs	W	w	m	s		
900/1	w	m	m	w		m	vs		
1000	w	m	m	w		s	vs		
1000/1	w	w		vw		s	vs		
1200	w	w		vw		s	vs		
1200/2	w	vw		vw		s	vs		
1300	w	vw				s	vs	w	vw
1300/2	vvw	vvw				m	s	m	m
1300/3	vvw	vvw				vw	m	S	s
1400	vw	vvw				w	m	vs	s

Phase : A=Anatase, R=Rutile, C=Corundum, $AT = \beta - Al_2TiO_5$

Intensity: vs=very strong, s=strong, m=middle, w=weak, vw=very weak, vvw=very very weak.

detected in the heat-treated samples at 1200° C, even after soaking for 2 hrs. This AT-gel powder heat-treated at 1300° C/3 hrs show β -Al₂TiO₅ as the major phase with a small amount of α -Al₂O₃ and TiO₂. The presence of this starting materials could arise either due to slow reaction rate because of the generation of large diffusion paths with the progressive formation of aluminium titanate. These results indicate that aluminium titanate formation occurs above 1300° C.

 a given temperature for a specified period of time. The experimental data are: (1) heating time, (2) temperature, (3) the mol % and volume of reacted and unreacted material at any time and (4) the volume fraction of Al₂TiO₅. These data are presented in Table 4.

The subsequent nearly horizontal lines for $T=1250\,^{\circ}\!\!\mathrm{C}$ correspond to the lower temperature initial reaction stage operating without any significant overall volume fraction variation. A constant sample volume while the fraction is in progress means that the porosity reduction or densification closely matches the volume expansion due to aluminium titanate formation.

A demonstration that eq. (6) is to 8.6 % volume fraction in Fig. 8 for the reaction

Table 4

The data of quantitative X-ray measurements

1250℃	Mol%	Mol%			/ol.(cm³/mc	AT	
Soaking time	R	С	AT	R	С	AT	Volfraction X
0 hr.	50	50	0	9.3	14.7	0.0	0.0
3 hrs.	49	49	2	9.2	14.5	1.0	0.4
6 hrs.	48	49	3	9.0	14.5	1.5	0.68
12 hrs.	48	48.5	3.5	9.0	14.3	1.75	0.7
24 hrs.	47	48.5	4.5	8.8	14.3	2.25	0.9
1300℃	<u>-</u>						
0 hr.*							
3 hrs.	40	41	19	7.5	12.1	9.5	3.3
6 hrs.	29.5	33	37.5	4.3	6.2	18.8	6.4
12 hrs.	18	19	63	2.6	3.5	31.5	8.4
24 hrs.	15.5	17.5	67	2.2	3.2	33.6	8.6

^{*} see Fig. 6 and Table 3.

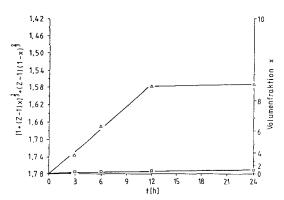


Fig. 8. Reaction between amorphous TiO₂ and Al₂O₃ to form Al₂TiO₅ by Cater's equation.

 $Al_2O_3+amorphous$ $TiO_2\rightarrow\beta$ - Al_2TiO_5 . The volume fraction of Al_2TiO_5 at $1300^{\circ}C$ increased with the soaking time. During the curve for $T1=1250^{\circ}C$ proceeded continuously with very low slope. The curve of $T_2=1300^{\circ}C$ in the first stage to 12 hrs can be observed the higher gradient. This phenomena can be agreed the results of report [14].

Despite of longer soaking time, the Al_2 TiO_5 growth velocities in the second stage of the kinetic reaction turn out to be significantly smaller than those observed initially. Therefore an average growth velocity for product layer was estimated for comparison with fast growth regime; $T = 1250 \,^{\circ}\text{C}$ ($k = 4.025 \times 10^{21} \text{m}^2/\text{s}$), $T = 1300 \,^{\circ}\text{C}$ ($k = 1.34 \times 10^{-19} \text{m}^2/\text{s}$), and after 12 hrs at $1300 \,^{\circ}\text{C}$ ($k = 5.03 \times 10^{-21} \text{m}^2/\text{s}$). After consideration of differential product thickness, yielded the same results of literature [15] ($k = 1.6 \times 10^{-18} \text{m}^2/\text{s}$ at $1300 \,^{\circ}\text{C}$).

An Arrhenius plot of the powder rate constants yields an apparent activation energy of 622.4 kJ/mol. This high activation energy for nucleation was related to the grain boundary stresses interfering with the nucleation process. The same activation energy reported in the literature[11] is 700 kJ/mol. The only other activation energy for solid-state reaction for the formation of Al₂TiO₅ from oxygen-deficient TiO₂ and α-Al₂O₃ was 299.45 kJ/mol [16]. But it was measured at low unspecified oxygen pressure, i.e., under condition that many not be directly comparable to ours.

5. Conclusions

The formation of Al₂TiO₅ has been studied in an unagglomerated, monosized, equimolar TiO₂-coated Al₂O₃ powder mixture of 0.4 μm small particle sizes and moderate purity (99.8 wt%) at temperature around 1250° °C, where the volume fraction for the formation of Al₂TiO₅ is very small. Crystallizations lead to TiO₂ (1000°C/1 h) which must be then lost the potential advantages of coating process. The transformation of Al₂O₃ and TiO₂ into β-Al₂TiO₅ appears between 1280 and 1300℃. The activation energy for the chemical kinetics for the solid-state reaction of amorphous TiO_2 with α -Al₂O₃ to produce β -Al₂TiO₅ was 622.4 kJ/mol.

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