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The Electronic Structure and Chemical Bonding between Metal and Oxygen Atoms: T122-Based Copper Oxide Superconductors

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Using tight-binding molecular orbital methods for charged cluster models, we studied the electronic structrue and chemical bonding of thallium-oxygen and copper-oxygen atoms in Tl22-based copper oxide. The interaction between the s orbital of Tl atom and the p_x and p_y orbitals of O3_{ng} atom in the Tl layers results in nonbonding. The interaction between the s orbital of Tl atom and the p_x orbital of O2 and O3_{ax} atoms in Ba and Tl layers results in antibonding. The interaction between the s orbital of Tl atom and the p_x orbital of O2 and O3_{ax} atoms in Ba and Tl layers results in antibonding. The interaction between the d_x^2 orbital of Cu atom and the p_z orbital of O2 atom also results in antibonding. The Tl22-based copper oxide superconductors can be understood in terms of a local electron transfers from Cu layers to Tl layers along c-direction. The resulting electron transfers have the same patterns as those of YBa₂Cu₃O₇ and YBa₂Cu₄O₈ superconductors.

Introduction

At present Tl-based copper oxide superconductors show the highest superconducting transition temperatures T_c^{1-5} . The Tl-based copper oxide superconductors have Cu perovskite-like unit structures. These compounds can be divided into two types according to the space group. Type I that is Tl12-based copper oxide superconductors has space group P4/mmm. Type II that is Tl22-based copper oxide supeconductors has the space group I4/mmm. The ideal superconducting phases of Tl12-based and Tl22-based copper oxide superconductors may be classified into six groups, TlBa₂ CaCu₂O₇(Tl1212 system)⁶, TlBa₂Ca₂Cu₃O₁₀(Tl1223)⁷, TlBa₂Ca₃ Cu₄O₁₁(Tl1234)⁸, Tl₂Ba₂CuO₆(Tl2201)³, Tl₂Ba₂CaCu₂O₈(Tl2212)⁴, and Tl₂Ba₂Ca₂Cu₃O₁₀(Tl2223)⁵.

The structures of these systems are separated by Tl-O monolayer and Tl-O bilayers for Tl12-based and Tl22-based copper oxide superconductors. Figure 1 shows nominal unit cells⁹ for Tl2201, Tl2212, and Tl2223 superconductors. Ca²⁺ cations are between adjacent Cu layers and Ba²⁺ cations between Cu layers and Tl layers. From the comparison of the crystal structures of YBa₂Cu₃O₇ and Tl22-based copper oxide superconductors, copper-oxygen chains are present in a YBa₂Cu₃O₇ superconductor, while these chains are absent in Tl22-based copper oxide superconductors.

Using ASED-MO¹⁰ of the tight-binding molecular orbital method, we studied electronic structures and chemical bonding of the thallium-oxygen and copper-oxygen atoms for Tl 22-based copper oxide superconductors.

The Cluster Size and Calculation Methods

The oxygen atoms in different layers of superconductors are crystallographically ineqivalent. Tl22-based copper oxide



Figure 1. Nominal unit cells for $Tl_2Ba_2CuO_6$, $Tl_2Ba_2CaCu_2O_8$, and $Tl_2Ba_2Ca_2Cu_3O_{10}$ superconductors. (a) $Tl_2Ba_2CuO_2$ superconductors. (b) $Tl_2Ba_2CaCu_2O_8$ superconductor. (c) $Tl_2Ba_2Ca_2Cu_3O_{10}$ superconductors.

superconductors are labeled by O1 (in Cu layers), O2 (in Ba layers), and O3 (in Tl layers). The atoms in the two inequivalent Cu layers are labeled Cu, O1, Cu' and O1'. These labels are shown in Figure 1. We also use atoms $O3_{eq}$ and $O3_{ex}$ which stand for equatorial and axial positions in the Tl double layer for Tl22-based copper oxide superconductors.

Freeman *et al.*¹¹ and Kasowski *et al.*¹² calculated the band structure and electronic structure using the band theory for Tl22-based copper oxide superconductors. Their findings indicate that the Tl and Cu layers affect Fermi energy states. Using the full-potential linearized augmented plane-wave



Figure 2. Models of clusters in calculation for $Tl_2Ba_2CuO_6$, $Tl_2-Ba_2CaCu_2O_6$, and $Tl_2Ba_2Ca_2Cu_3O_{10}$ superconductors. (a) $TlCuO_{11}H_{10}^{7-}$ cluster model for Tl2201 superconductor. (b) $TlCu_2O_{15}H_{16}^{9-}$ cluster model for Tl2212 superconductor. (c) $TlCu_3O_{19}H_{18}^{11-}$ cluster model for Tl2223 superconductor.

Table 1. Atomic Parameters Used in the Calculations

Atom	Orbital	H_{ij} (eV)	Exponents		
			ζ1	ζ	
<u>—</u>	- 6s	- 16.20	2.370		
	6¢	- 9.00	1.970		
Cu ^b	4 s	-11.40	2.200		
	4 <i>p</i>	-6.06	2.200		
	3 <i>d</i>	14.00	5.950 (0.5933)	2.300 (0.5744)	
0	2 s	28.48	2.246		
	2 p	-13.62	2.227		
Hď	1 s		2.200		

^aReference 14. ^bReference 15. ^cReference 16. ^dReference 17. ^cEach is followed in parentheses by the coefficients in the double zeta expansion.

method, Markstener et al.13 showed that Ca and Ba atoms in T122-based copper oxide superconductors are highly ionic and contributed little to the valence band density of state. In our calculations, we have selected the TI and Cu atoms, though Ca and Ba atoms were used for Tl22-based copper oxide superconductors. Therefore, we have chosen O3ar-Tl-02-Cu-02, 03ar-TI-02-Cu-Cu-02, 03ar-TI-02-Cu-Cu-Cu-02 sequences along the *c*-direction including the Tl and Cu layers for T12201, T12212, and T12223 superconductors. The results of charged clusters are TlCuO₁₁H₁₀⁷⁻, TlCu₂O₁₅H₁₄⁹⁻, TlCu₃-O₁₉H₁₈¹¹⁻ models for Tl2201, Tl2212, and Tl223 superconductors. These models of charged clusters are shown in Figure 2. We also used point charge techniques with H atoms for the purpose of representing infinite solid to finite cluster. Atomic coordinates were taken from the X-ray crystallographic study of Tl2201 Tl2212, and Tl2223 superconductors by Torardi et al.35 and Subramanian et al.4. Nominal valences per each atoms are 3+, 2+, 2- and 1+ for Tl, Cu, O, and H, respectively. The parameters in tight-binding calculation, valence state ionization energy H_{ii} (eV) and exponent \xi, are shown in Table 1.

Results and Discussion

Table 2. Interatomic Distances (r/Å), bond strength $(s)^{a}$, and atomic valences $(v)^{b}$ for T12201^c, T12212^d, and T12223^c Superconductors

System	, Cu-O	r	5	v	number
TI2201	Cu-O(1)	1.933	0.503		x 4
	-O(2)	2.714	0.061		x 2
				2.012(4)	
				2.134(6)	
Tl2212	Cu(1)-O(1)	1.928	0.511		x 4
	-O(2)	2.699	0.063		x 1
				2.044(4)	
				2.107(5)	
T12223	Cu(1)-O(1)	1.925	0.514		x 4
				2.056(4)	
	Cu(2)-O(2)	1.927	0.512		x 4
	-O(3)	2.480	0.115		x 1
				2.048(4)	
			• ·	2.163(5)	

^{a,b}Reference 23. 'Reference 3. 'Reference 4. 'Reference 5. 'In this paper, the parentheses in atomic valences are coordination number of Cu atom. 'Numbers in sixth column are the number of equivalent O atoms surrounding Cu atom.

One of the common structural features⁴ for copper oxide superconductors is the existence of a Cu atom in a mixedvalence (2+ to 3+). The Tl atom¹⁸ for Tl22-based copper oxide superconductors exists in the mixed-valence. The mixed-valence of T1 atom (1+ to 3+) is made from T1-6s band and conduction band of the Cu layers, as indicated by photoelectron spectroscopy19,20 and band calculations21.22. We calculated the valence and strength of Cu atoms with four-, five-, and six-coordination numbers from the X-ray crystallographic data for Tl22-based copper oxide superconductors by Torardi et al.35 and Subramanian et al.4. The effective mean valence²³ of Cu atom is estimated from the relations of the bond length and bond strength²³. The calculated bond strengths and valences of Cu ion are listed in Table 2. The predicted valence values (and the coordination number) of the Cu ions is 2.012(4), 2.134(6), 2.044(4), 2.107(5), 2.058(4) in the Cu1' atom, 2.048(4), and 2.163(5) in the Cu1 atom for Tl2201, Tl2212, and Tl2223 superconductors. The Cu atoms in the Cu layers have partial oxidation. Therefore, the TI atoms in the TI layers are partially reduced due to the polyhedra coordination of Cu atoms and orbital interactions of the O3ar-Tl-O2-Cu atoms along the c-direction. We find that the valence state of Tl atoms in the Tl layers and of Cu atoms in the Cu layers is <3+ and >2+.

The electron distributions of the Tl and Cu layers with the coordination number of four and $O3_{ax}$ -Tl-O2 atoms along the *c*-direction are shown in Figures 3, 4, and 5. The electron distributions of the Tl and Cu layers with the coordination number of four are very similar to those with the coordination number for five or six for Tl2201, Tl2212, and Tl2223 superconductors. We have not presented the density of states (DOS) of the Tl and Cu layers with the coordination number of five and six. In DOS plots, the highest occupied energy



Figure 3. Total density of states (TDOS) and local density of states (LDOS) in TlCuO₁₁H₁₀⁷⁻ cluster model for Tl2201 superconductor. (a) TDOS in TlCuO₁₁H₁₀⁷⁻ cluster model. (b) LDOS in the Tl layer with the coordination number of four. (c) LDOS in the Cu layer with the coordination number of four. (d) LDOS in O3_{ac}-Tl-O2 atoms along the c-direction.



Figure 4. Total density of states (TDOS) and local density of states (LDOS) in $TICu_2O_{15}H_{14}^{9-}$ cluster model for TI2212 superconductor. (a) TDOS in $TICu_2O_{15}H_{14}^{9-}$ cluster model. (b) LDOS in the T1 layer with the coordination number of four. (c) LDOS in the Cu layer with the coordination number of four. (d) LDOS in $O3_{ur}$ -T1-O2 atoms along the *c*-direction.

level (HOEL) is -6.9, -7.09, -7.06 eV for Tl2201, Tl2212, and Tl2223 superconductors. We compared Tl layers, Cu layers, and O3_m-Tl-O2 atoms along the *c*-direction to see the result of the total density of states (TDOS) and the local density of states (LDOS). In nearby HOEL, the electron distributions are present in the Tl layers and O2-Tl-O3_m atoms along the *c*-direction, while they are not present in the Cu layers. For Tl2223 superconductors, the electron distributions in the Cu layers are very similar to the Cu' layers. The LDOS patterns in the Cu and Cu' layers for Tl22-based copper oxide superconductors are from the structural characteristics. We know that the Cu layers act as electron donor states, while the Tl layers act as electron acceptor states.

We studied local charge transfers from the Cu layers to the Tl layers. From the decomposition of crystal orbital over-



Figure 5. Total density of states (TDOS) and local density of states (LDOS) in $TlCu_3O_{19}H_{18}^{11-}$ cluster model for Tl2223 superconductor. (a) TDOS in $TlCu_3O_{19}H_{18}^{11-}$ cluster model. (b) LDOS in the Tl layer with the coordination number of four. (c) LDOS in the Cu' layer with the coordination of four. (d) LDOS in the Cu layer with the coordination number of four. (e) LDOS in $O3_{ar}$ -Tl-O2 atoms along the c-direction.

Table 3. Orbital Overlap Populations of Tl, Cu, and O Atoms in the Tl, Cu, and Ba Layers for Tl2201, Tl2212, and Tl2223 Superconductors

Orbital-Orbital	Tl2201	Tl2212	T12223
T1 6s-O3 _{er} pr	-0.078	-0.058	-0.050
TI 6s-O2 p,	0.038	-0.017	-0.064
02 p _r -Cu d ²	0.002	-0.002	-0.005

lap populations for Tl2201, Tl2212, and Tl2223 superconductors, the chemical bonds in p_z orbital of the O3_{ax} atom with s orbital of the Tl atom and the p_z orbital of the O2 atom with the s orbital of the TI atom indicate anticate antibondings. Our calculations agree with those of Freeman et al.¹¹ and Kasowski et al.12 using band calculations. The chemical bonds of the p_z orbital of the O2 atom with d_z^2 orbital of the Cu atom are also antibonding for Tl2201, Tl2212, and Tl2223 superconductors. The calculated orbital overlap populations are shown in Table 3. In the TI layers, the chemical bond of the s orbital of TI atom with p_x or p_y orbital of $O3_{ee}$ atom are weaker than that of the s orbital of Tl atom with the p_{z} orbital of O2 and O3_{ax} atoms. It is because T1-O3_{eq} interatomic distances (2.496, 2.462, 2.48 Å for T12201, Tl2212, and Tl2223 superconductors) are larger than Tl³⁺ and O²⁻ ionic radii (2.25 Å) and TI-O2 (1.995, 1.978, 2.20 Å for T12201, T12212, and T12223 superconductors), $-O_{3ar}$ (2.038, 2.031, 1.92 Å for Tl2201, Tl2212, and Tl2223 superconductors) interatomic distances are smaller. In superconducting state for Tl22-based copper oxide superconductors. the electrons in the Cu layers can move the Tl layers along the *c*-direction. Our calculational results are similar to position distribution contributions by Bharathi et al.24 who have shown electron transfer from the planar O atom to the apical O atom for Tl2223 superconductor. We have published local charge transfers for YBa₂Cu₃O₇(Y123) and YBa₂Cu₄O₈(Y124) superconductors²⁵⁻²⁸. We have found the local charge transfers of Y123 and Y124 superconductors move the Cu layers to the Cu chains. Our charge transfer models for Y123 and



Figure 6. Schematic diagrams of the local charge transfer inferred from the tight-binding MO studies. (a) Y123 superconductor. (b) Tl2223 superconductor.

T12223 superconductors are show in Figure 6. The structural differences between Y123 and T122-based copper oxide superconductors show the Cu-O chains are present in the Y123 and superconductor, while they are not present in the T122-based copper oxide superconductors. If the structures of Cu-O chains are distinguished from those of Y123 and T122-based copper oxide superconductors, the T1 layers for T122-based copper oxide superconductors are the same as the Cu-O chains for Y123 superconductor. Namely, the Cu-O chains and the T1 layers are in electron acceptor states.

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