# Hidden Part Estimation in the Occluded Objects 겁친 물체에서 가려진 부분의 추정 

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#### Abstract

In this paper a hidden part estimation is proposed for the recognition of occluded objects. The detection process of occluding is made up of counting the number of odd points from the given input image. Also the estimation is performed for hidden parts of the occluded object based on the figure quantity before the feature extraction operation. Firsally the effectiveness of this method is shown by various experiments.


## 요 약





## I . Introduction

Computer vision has been drawing much research and work as its application seems to be limitless. Recently, the focus is on the 3 D computer vision and much effort is extended to overcome the inherent limits of information obtainable from gray level data, thereby to recognize the occluded obj ects. Also there have been various attempts to better utilize the range data so as to distinguish the

[^0]planar objects from the curved ohiectsl 1$]$ [i3].
However in the 3-D computer vision systems, the process of obtaining the range data by the sh ape from $X$ method $[4] \cdot[6]$ or the range finder me thod[7]. [8] is both time-consuming and inaccurate due to various reasons. Also in one of the major application areas of the computer vision systems, the manufacturing line automation, occlusron is quite common because of physical overlapping and contact among objects. To resolve the occlusion problem, a proper method would be to utilize the range data which much account for the situation correctly but it has the problems ment-
roned above. So more practical method may be found in the utilization of the easily obanable gray level data, But the existing methods iry the rec. ognition of the occluded objects without the estimation of hidden parts, which is very prone to false recognition.

In this paper to resolve this difficulty, it is proposed that the estimation on the hidden parts of the occluded object.s based on the human psycho logical terdency atbout rraking objects is to be per. formed before the feature extraction process.

For this, the shape of the hidden parts of the occluded object is estimated using Jough transform[il] and the figure quantity conceptl9]. Ad ditionally, the algorithms for the end point detec: tion, vertex modeling, ocelusion detection and hidden part estimation are presented in making a complete system. Section II describes the existing figure quantity equation and its meaning. and explains the reason for applying in the proposed system,

Section III deals with Hough transform. In section $\bar{V}$. a vertex modeling method to formulate single complete figures. Section $V$ explains the proposed occlusion detection algorithm and the shape estimation method for the hidden parts. Finally, the effectiveness of the proposed system is shown the experimental results.

## I]. Human psychology on the figures| 9 |

Most of the man-made objects are composed of spheres, cylinders, cones and flat surfaces. A report says about $85 \%$ of all artificial objects are made up of these primitives 10 ]. Then the question arises about why human make the object in the way. The one possible answer for the reason may be found in the different figure quantity value of each object established in the human psychology on figures. The psychology says that human feel most comfortable with the objects is their cross section is circle, which accounts for the fact that the cross section of 3 of the above primitive are circle.

In the case of a circle, as shown in Fig.1, the
figure quantity becomes zero and human feel figuratively most comfortable, which is the reason that the cross section of the most man-mad objects is circular. The expression shown below is to compute the figure quantity.
$;(p)=-\int \cdot p(w) \cdot \log p(w) d w$
where $p(w)$ is the power spectrum expression, which contains the information about the curvature and torsion. The above expression is analogous to the entropy expression of the information theory and it repersents the amount of entropy in the image information, s.e., the value of which is the degree of the curvature and torsion of an object. In the information theory, if the degree of irregularity is smaller, then lower the value entropy. Likewise in the figure quantity concept, smaller figure quantity means that the object is of more ordinary, predictable shape. Geometrically, lower the figure quantity value of an object. smaller the degree of curvature and torsion in its shape.

Figure 1 shows a typical example.
As noticed in Fig. I rectangles and squares have different $G(p)$ values. But the line segments of both objects, regardless of their length. have the same $G(p)$ value.


Fig. 1. Figure quantity values for various objects

## III. Detection of line and circle from image data

As mentioned previously, the cross section of the most man-made objects are circle. Furthermore, the tools used in the workshops and factories figuratively composed of line and circle primitives.

Therefore the correct detection of these primit. jves is vital for the recognition of the objects. In this paper we use Hough tranform for the purpose.

### 3.1 Line detection

A line segment in 2 D image of $\mathrm{X} \cdot \mathrm{Y}$ coordinates is defined as one point in a parameter space.

Fig. 2-(a) shows that any line which passes any point ( $X_{i}, \mathrm{l}^{\prime}$ ) on a line segment $L$ is definced as :


Fig. 2. Line segment in parameter space

$$
\begin{align*}
& \therefore \cdot \cos \theta-1 i \sin \theta \cdots R \tag{2}
\end{align*}
$$

Also Figure 2 -(b) shows that all lines passing any point on a line $L$ accumulate to a point ( $0, \mathrm{R}$ ) in parameter space. For example points $A$ and $B$ are represented as one pont as $\theta- \pm 180, \mathrm{R}-\mathrm{ABS}$ (R). If Hough transform is applied to all points in the image, the accumulator array is obtained and after $\theta$-grouping, R-grouping and X-Y grouping processes is performed for the determining of bast line.

### 3.1.1 Determination of best line



Fig. 3. Best line determmation

If N points as the line edge elements from a line segment, then the normal distance from a point ( $\mathrm{Xi}, \mathrm{Yi}$ ) to the line of expression (2) is as follows:
$d_{i}=R-X_{i} \cos \theta-Y i \sin \theta$

Therefore the total distance from $N$ points to expression (2) is shown as,
$H^{\prime \prime}=\Sigma\left(R-N_{i} \cos \theta-y, \sin \theta\right)^{\prime} . \quad(i=1, \cdots, i)$
Now, the best line is the one which has the murs. immern values of $\boldsymbol{\theta}$ and R for expression (4)

### 3.1.2 Determination of end points

If the projected point from a point (Ni, l's) to the best line is denoted as $(N, f)$, then their val ues are obtained as
$x=\lambda+R \cos \theta-\lambda \cos \theta-\gamma i \sin \theta \cos \theta$
$y_{i}=\lambda_{i}+R \sin \theta \cdots \lambda_{i} \cos \theta \sin \theta-r_{i} \cos ^{2} \theta$

Aso the projection dist ance, $P$ from a given point (Xi, $\mathrm{V}_{i}$ ) in Fig. 3 to a straight line defined by $\theta$ and $R$ is computed as.
$p \quad x_{i} \sin \theta+i \cos \theta$

Smilarly corresponding $P_{1}$ value for 1 he: porec tion point $\left(\mathrm{X}_{1}, \mathrm{Y}_{1}\right)$ is

$$
\begin{equation*}
I_{i} \quad-\dot{\sin \theta} \theta+r \cos \theta \tag{7}
\end{equation*}
$$

Now. after the I', values are sorted, the coordjrates decided by the minimum and maximum va. ]ues become end points.

### 3.2 Circle Detection and Arc End Point Detection

To detect a circle from the image, the center is located by the principle that a line perpendicular to a line connecting two points on a circle must pass the center. Likewise by measuring the distance from the center to each point on the circle, the radius is determined. The same method is applied to an arc in determining its center and radius.

As shown in loig.4, an arc is a part of a cincle which satisfies.

$$
\begin{equation*}
\left.(X-w)^{\prime}+()^{\circ} \cdot\right)^{\prime}=R^{\prime} \tag{8}
\end{equation*}
$$

so. a line connecting any point ( $X$, $Y$ ) and the ati center ( $M, N$ ) is represented as



Fig. 4. Determination of the end point of an arc

If the intersection between expression ( 8 ) and (9) is denoted as

$$
\begin{equation*}
d_{s}=\operatorname{SQR} T\left[\left(\mathrm{~S}_{i}-\mathrm{K}_{\rho}\right)^{\prime}+\left(\mathrm{Y}_{i}-\mathrm{y}_{i}\right)^{\prime}\right] \tag{10}
\end{equation*}
$$

Now the end point of the arc is determined whose di value is minimum.

## N. Vertex modeling

Since the image of every object forms a single closed loop figure, the verlices are selected such that a single closed-loop figure is formed by the relatod lines and arcs which are extracted by Hough tranformation. Therefore, the proposed vertex modeling is to arrange the appropriate vertices of an entire object mage including the occluded parts from the computed end points of lines and arcs through Hough transformation.

The figure shown below gives an example.

(a) Before Vertex Modeling


1, 2, 3, 4, 5, 6. 7 :
Formulated vertex
(b) Results of Vertex Modeling

Fig. 5. Examples of an vertex modeling

## V. Detection of occlusion

If we assume that ant object is composed of a single figure, then the existence of occlusion must be determined.

### 5.1 Distinction between occluding and occluded objects

The decrsion whether there exists an occlusion or not can be made by counting the number of ed ges originating from a chosen vertex and determining if the number is odd or even. We define a vertex from which the odd number edges as an occluding point. Then, if the number of the occluding points is two or more, then it can be judged that the occiusion has actually happened. For example, as shown in Ftgure 6 the vertices, $a, c, d$, f. $g, i, j$ and $\mid$ are non occluding points since the number of edges coming out of them are all even. Meantime, the vertices $b, e, k$ and $h$ are occluding points because the number of edges from them are all odd.

Separation of occluding object from a single figure is done by extracting a whole figure which contains all the occluding points. Fig. 6 shows an example.

### 5.2 Estimation of hidden parts

The hidden parts of an occluded can be deter. muned by considering its surrounding the occlud-


Fig. 6. Extraction of an occluding object
ed points and the vertices of the occluded objects and by establishing a relationship among the vertices. the estimation of the hidden parts of the xcluded object is performed. At this time if the estimated line of vertices is formed mside the of uluded object region, then the estumation is very likely to be successful.

Otherwise it is definitely a failure case. Fig. 7 shows the example.

As shown in Figure 7-(a), if the cstimated lines mect each other, the shape estimation for the hid den parts is assumed to be successful fat this time the figure quantily must the the minimum possible value for the chosen configuration). However. if the estimated lines do not meet each other as shoown in Figure 7 -(b). the estunation process is considered to be impossible and regarded as a failure. In this case, even a human can not properly estımate the shape of the hidden parts.

(a) success of estimation

(b) faidure of estimation

Fig. 7. Examples of estimation

The basis for this estimation process is to form an object of the previously mentioned minmurn figure quality vlaue.

## W. Experiment and observation

The edge detection is done with Robert operat or on at $64 \times 64$ image. In the straight line extraction the values projection distance, $P_{j}$ above 7 are selected. For the $P_{j}$ values between 4 and 7 . initi ally a straight line is assumed but after attempt ing to regard it as a circle, an arc or straight line is decided. The end points of each segment are connected to find the true vertices of the figure and a $5 \times 5$ window is used to determine the occluding point.
Fig. 8 shows the original input image. Fig. 9 is the result of the line and arc extraction algorithm of Hough transform, for which the edges are de tected by Robert operator. Further, Fig. 10 is the result of the shape estimatation process for the hidden parts from image in Fig. 9. The reason for the given estimation comes from the minimum figure quantity as shown in Table 1, i.e., the line segments, $\mathrm{h} \cdot \mathrm{i} \cdot \mathrm{s} \cdot \mathrm{r}$ must be regarded as a single line according to the minimum figure quantity value. The same is true for the case of $\mathrm{j} \mathbf{k}-1 \mathrm{~m}$. This result would be the same even for a human since the most of the man-made objects. with the excep-
tion of some very special purpose and use, are of more uniform or constant curvature and of mini mum torsion. Consequently, this article exploits the nature of the man-made objects, the shape of which tend to be of more constand curvature and minimum torsion. We find this nature very strong in estimating the shape of the hidden parts in the occluded objects. Further study and research is expected for the cases in which the estimation lines are not formulated.

Even though the experiment has been performed with $64 \times 64$ images, thereby the resolution is rather coarse, higher resolution images can be easily handled in estimating the hidden parts of the occluded objects by adjusting the ( $\theta, \mathrm{R}$ ) value of Hough transform.

(a)

(b)

(a)

(b)

Fig. 9. The extracted results of the line and arc by Hough transformation

Table I. Result of estimation of the Fig. 10-(a)

| Relations of Estimation | Figure quantity |  |
| :---: | :---: | :---: |
| h i-s-r(same line) | h-i | 2.68 |
|  | s-r | 2.68 |
|  | h-i-s-r |  |
| j $\mathrm{k} \cdot \mathrm{I} \cdot \mathrm{m}$ (same line) | j $k$ | 2.68 |
|  | $1 \cdot \mathrm{~m}$ | 2.68 |
|  | j.k.lm | 2.68 |

Fig. 8. Input image


Fig. 10. Estimated image

Table 2. Result of estimation of the Fig. 10. (b)

| Relatrons of Estimation | Figure quantity |  |
| :---: | :---: | :---: |
| A j i(same line) | 11 | 2. in |
|  | A-j, | 2.68 |
| A-k-lisame lime) | ki | ?180 |
|  | a.k j | 2.188 |
| B $x$-y(same line) | x -y | $\underline{2}$. 88 |
|  | B x.y | 2.68 |
| B $\mathrm{n} \cdot \mathrm{m}$ (same line) | $\mathrm{n} \cdot \mathrm{m}$ | 2.68 |
|  | Bnm | 2.6 кк |
| C v-y(same line) | v-y | 2.68 |
|  | Cvy | 2.1 k |
| Copesame line) | op | 2.68 |
|  | Cop | 2.68 |
| Dstsame line) | st | 2.6\% |
|  | Dst | 2.18 |
| D. quisame line ) | $\mathrm{r}-\mathrm{q}$ | 2.4\% |
|  | D: 4 | ? 68 |

## Vil. Conclusion

A way of estomating the hidden parts of an $o c$. cluded object is proposed. Circles and lines are detected by Hough transform and the concept of the ifgure quantity is utilized in the estumation pro cess. Further research on the cases where the estimated lines do not meet in the estimation pro cess is required.

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