

# 마이크로 프로세서를 이용한 인버터 전압제어와 고조파 제거에 관한 연구

## A Study on Inverter Voltage Control and Harmonics Elimination Using Microprocessor

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### 요 약

전력전자 분야에 대한 마이크로 프로세서의 응용은 제품생산과정, 실현, 정비 및 서비스와 그제어의 융통성에 있어서 이용범위가 확장되고 있는 추세이다.

본 연구는 인버터의 점호각 관계식을 다항식 근사 시킴으로서 마이크로 프로세서로 온-라인 계산을 할 수 있게 한것으로, 인버터 출력의 고조파 제거와 출력전압제어를 위한 스위칭의 이론적 분석을 하고 HP-1000 컴퓨터에 의하여 시뮬레이션을 실행 하였다.

또한 마이크로 프로세서에 의한 인버터 출력전압 및 주파수 제어의 실제적 방법이 제시되고, Z-80 마이크로 컴퓨터에 의한 단상 인버터 출력제어 실험을 하였다.

본고에서 고찰한 단상인버터 경우의 Implementation은 3상으로 확장 할 수 있으며, 얻어진 제 결과들은 실제적으로 인버터 응용에서 단상 및 3상 인버터 출력파형을 얻는 융통성 및 보다 높은 정밀성을 갖는다.

### ABSTRACT

Microprocessor control of power-electronic equipment offers the possibility of improvements in manufacture, realizability, maintenance and servicing, and increased control flexibility. In this paper, simple microprocessor control with a view to approximating the polynomial equations which govern the commutation angles was considered.

The theoretical analysis of this principle which govern the commutation of power switches in order to cancel any predetermined harmonics and vary the fundamental rms voltage of the inverter output is described. Also the spectrum and harmonics were analyzed by HP-1000 computer. Practical aspect of the realization of a voltage controller based on a microprocessor and a suitable system for variable frequency inverter were also presented. The experimental test has been carried out on a Z-80 microcomputer and a single phase transistor inverter. The various results show the feasibility of obtaining practically a single phase and a three phase inverter waveforms, which are highly desirable in most inverter applications.

### I. Introduction

It is always demanded for output voltage of inverter to be controlled in the industrial applications, whether its value has to be varied in a wide range or it must be kept constant despite the variation of the load or of the DC voltage at the inverter. The various methods have been developed for the control of PWM voltage inverters. Such control was initially based on a analog methods, described extensively in references 1)~3) and the corresponding set up was implemented either by analog<sup>4)</sup> or by digital methods.<sup>5)</sup>,<sup>6)</sup> The advent of digital components such as microprocessors and high speed memories opened the way for advanced control devices based on novel algorithm ; elimination of harmonics in the output voltage<sup>7), 8)</sup> and optimization involving different performance index.<sup>9)</sup>

Also the reference (10) has shown the approach to minimize the rms value of the current harmonics in the load by a proper choice of the commutation angles.

Another approach which can be satisfactory utilized for a quasi-continuous control of a PWM inverter output voltage by interpolation method had been described in 1980.<sup>11)</sup>

The general procedure followed by conventional circuitry is to determine the instants at which the power switches should open and close by the intersection of two difference of reference waveforms. By the use of this techniques and analog circuitry, the total harmonic content of the output voltage can be reduced at the complexity of great control, commutation devices.

In this paper, simple microprocessor control with a view to approximating the polynomial equations which govern the commutation angles was studied.

Thus microprocessor on-line control of tran-

sistor inverter is to make possible the implementation of the digital techniques where a predetermined number of unwanted harmonics can be canceled and the inverter frequency, voltage can be control simultaneously. Because the output filter can be used to attenuate the remaining higher harmonics, the use of this method in inverter control presents various advantages, so as to attenuate the harmonics components and, therefore, approximate the sinusoidal waveform.

### II. The Control Technique of the Inverter Output Voltage and Harmonics Elimination

Fig. 1 shows the basic structure of a fixed DC voltage inverter and the output voltage waveform where the switching angles  $\alpha_1$ , are usually modulated so as to minimize the harmonics components in the voltage waveform which are least acceptable, usually the low order harmonics.<sup>2)</sup>

A periodic voltage waveform as shown in Fig. 2 is expected to satisfy the following requirements ;

$$V_{AN}(wt) = V_{AN}(wt + 2\pi) \tag{1}$$

$$V_{AN}(wt) = V_{AN}(\pi - wt) \tag{2}$$

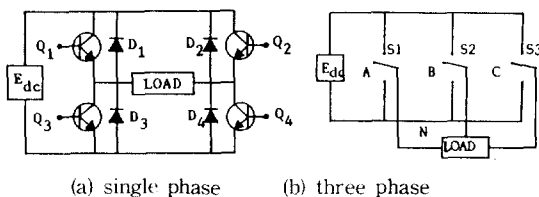


Fig. 1. Basic structure of inverters with constant voltage source  $E_{dc}$ .

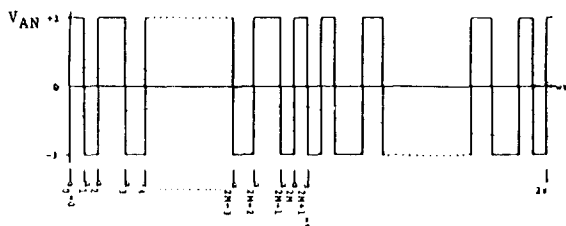


Fig. 2. General waveform of inverter output voltage.

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$$V_{AN}(wt) = -V_{AN}(\pi + wt) \tag{3}$$

$$V_{BN}(wt) = V_{AN}(wt - 2\pi/3) \tag{4}$$

$$V_{CN}(wt) = V_{AN}(wt + 2\pi/3) \tag{5}$$

The above three requirements represent the character of the wave periodical, with quarter-cycle symmetry and half cycle antisymmetry ; expansion of  $V_{AN}(\omega t)$  in a Fourier Series exclusively odd sinusoidal wave<sup>12)</sup> The last two requirements represent the symmetric three phase character of the inverter voltage. It constitutes a succession of pulses with normalized amplitude. When the inverter is commutated M times over a quarter cycle subject to the above requirements, the root mean square voltage of its nth harmonic is given by<sup>13)</sup>

$$V_n = \frac{2\sqrt{2}}{n\pi} (1 + 2 \sum_{i=1}^M (-1)^i \cos n \alpha_i) \tag{6}$$

in a Fourier Series, where the angles  $\alpha_i$  with  $i=1, 2, \dots, M$  satisfactory the following condition

$$0 < \alpha_1 < \alpha_2 < \alpha_3 < \dots < \alpha_M < \frac{\pi}{2} \tag{7}$$

$$\alpha_0 = 0, \quad \alpha_{2M+1} = \pi$$

It is possible from (6) that M predetermined harmonics can be canceled by using M commutations when their respective equations are equalized to zero. And it becomes clear the rms that voltage of the fundamental has a fixed value, and is equal to

$$V_1 = \frac{2\sqrt{2}}{\pi} (1 - 2\cos \alpha_1 + 2\cos \alpha_2 - 2\cos \alpha_3 + \dots + (-1)^M 2\cos \alpha_M) \tag{8}$$

In those applications where it is necessary to vary the output voltage, (M-1) harmonics are canceled and the appropriate commutation angles are calculated by the following equations ;

$$\frac{\pi V_1}{2\sqrt{2}} = 1 - 2\cos \alpha_1 + 2\cos \alpha_2 - 2\cos \alpha_3 \dots + (-1)^M 2\cos \alpha_M$$

$$0 = 1 - 2\cos 3\alpha_1 + 2\cos 3\alpha_2 - 2\cos 3\alpha_3 \dots + (-1)^M 2\cos 3\alpha_M$$

$$0 = 1 - 2\cos 5\alpha_1 + 2\cos 5\alpha_2 - 2\cos 5\alpha_3 \dots + (-1)^M 2\cos 5\alpha_M$$

$$\vdots \qquad \qquad \qquad \vdots \qquad \qquad \qquad \vdots$$

$$0 = 1 - 2\cos A\alpha_1 + 2\cos A\alpha_2 - 2\cos A\alpha_3 \dots + (-1)^M 2\cos A\alpha_M \tag{9}$$

where  $V_3, V_5, \dots$  are the (M-1) harmonics to be canceled. As a results, the fundamental voltage is given by

$$V_1 = V(\alpha_1, \alpha_2, \alpha_3, \dots, \alpha_M) \tag{10}$$

Therefore, the rms fundamental voltage can be varied while the chosen M-1 harmonics are canceled. The M commutation angles over a quarter-cycle permit unambiguous definition of the harmonic composition of the output voltage in the ideal inverter. Or, putting it differently, there are M degree of freedom in controlling the amplitudes of the component harmonics M making it possible to eliminate M-1 of the latter and to control the amplitude of the fundamental wave between the limits ;

$$0 \leq V_1 \leq \frac{2\sqrt{2}}{\pi} E_{ac} \tag{11}$$

### III. Polynomial approximation of Laws which Govern the Commutapipn Angles

#### 1. Single Phase Variant

Equation (9) is nonlinear as well as transcendental in nature. There is no general method that can be applied to solve such equations. Thus, the practical method of solving these equations is a trial and error process. Taking all the factors into account, a numerical technique is the best approach in solving the equations. These methods are not practical in real time systems due to the short response times needed. On the other hand, if the microprocessor, which has to work out the correct firing pulse, is to be kept simple, for both economical and practical reasons, the resolution method of such equations must be transformed to suit the microprocessor presently available.

The solution adopted has two possibilities. In both cases the equations must be solved and the data obtained either stored in look-up tables according to the different values of the rms voltage wanted or transformed into linear equations dependent of the rms voltage. For this purpose the M equations are solved canceling M-1 harmonics and obtaining the desired funda-

mental rms voltage. The Damped Newton method for solving nonlinear equations was used with the aid of a computer(HP-1000).<sup>14)</sup>

The simple example of the three pulse bidirectional wave is analyzed by the method presented and its computer algorithm is represented in Fig. 3.

The third and fifth harmonics are canceled

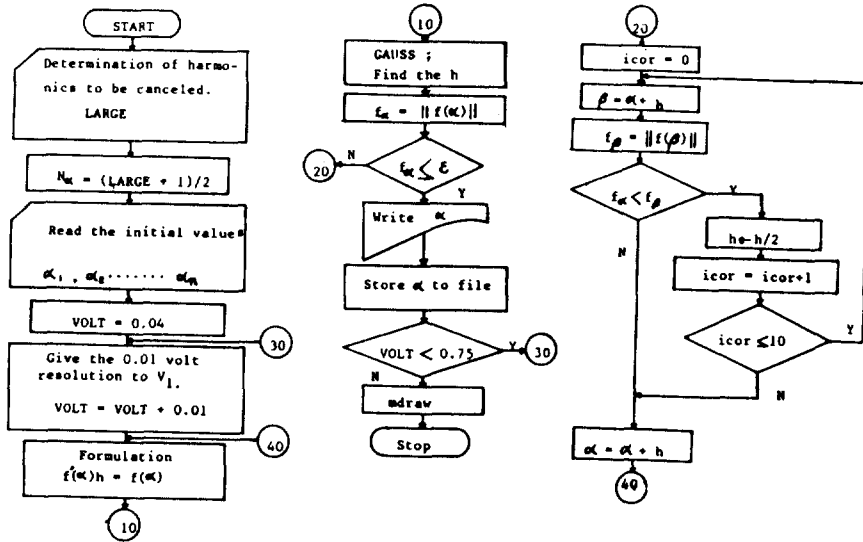


Fig. 3. Program flowchart for solving nonlinear equations(9)

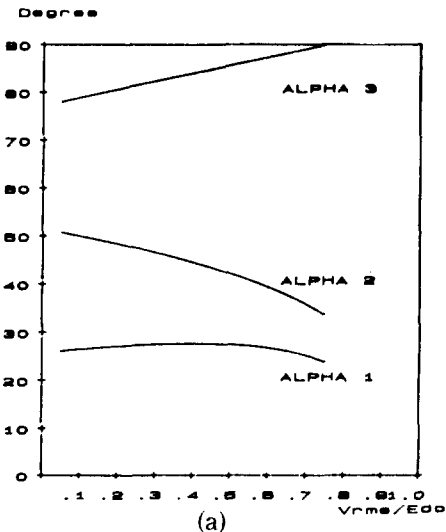


Fig. 4. The switching angles for eliminating the 3rd and 5th harmonics.(single phase inverter)

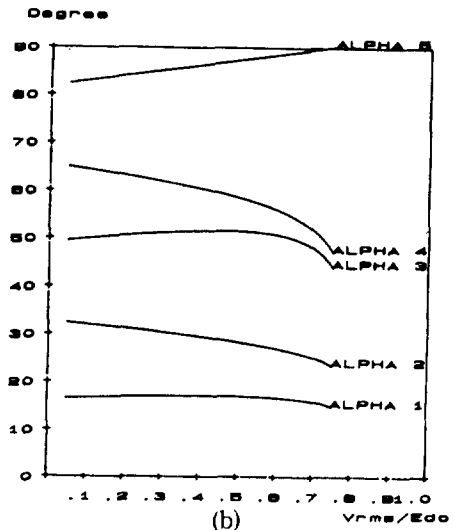


Fig. 5. The switching angles for eliminating the 3rd, 5th, 7th, and 9th harmonics. (single phase inverter)

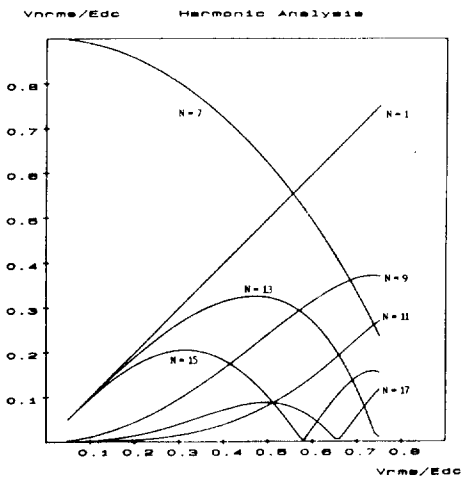


Fig. 6. Harmonic analysis. Relation between fundamental amplitude and 7th, 9th, 11th, 13th, 15th and 17th harmonics.

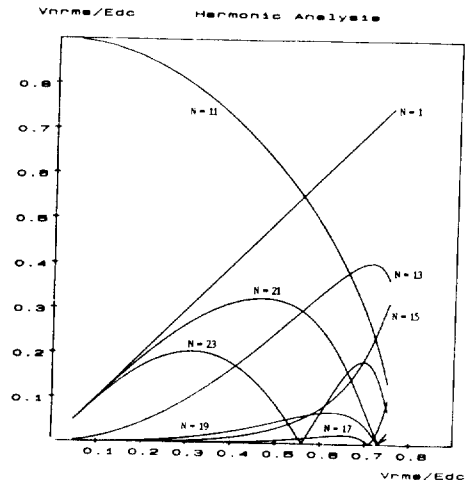


Fig. 7. Harmonic analysis. Relation between fundamental amplitude and 11th, 13th, 15th, 17, 19th, 21th and 23th harmonics.

and the root of equations obtained are plotted in Fig. 4. Also Fig. 5 represents the plotting of the 3rd, 5th, 7th, and 9th harmonics elimination and the root of equations.

The relation between the relative per unit amplitude of the first six harmonics (7th, 9th, 11th, 13th, 15th and 17th) and first seven harmonics (11th, 13th, 15th, 17th, 19th, 21th and 23th) present in the output voltage and the fundamental rms voltage are shown in Fig. 6 and Fig. 7, respectively.

A polynomial approximation dependent on the rms voltage,  $V_1$ , of the laws which govern the commutation angles previously calculated and represented in Fig. 4 and Fig. 5 is possible and the error known by using the least square approach.<sup>14)</sup> In cases  $M = 3$ , and  $M = 5$ , the results of this methods are hereby shown in (12)-(17), where a maximum permissible error of 0.789% can be achieved using the following the third-order equations in case  $M = 3$ .

When these polynomial approximations are used with high order equations, it might be precision to calculate the commutation angles. Thus, the third order equations required to calculate the commutation angles are much ac-

curater. In this paper, the control is implemented by using equations, (14).

In Case M - 3. (3rd, 5th harmonics elimination)

1st order equations

$$\begin{aligned} \alpha_1 &= 27.4991 - 1.7795 V_1 & \text{error} &\leq 9.847\% \\ \alpha_2 &= 53.0314 - 23.2248 V_1 & \text{error} &\leq 6.016\% \quad (12) \\ \alpha_3 &= 77.2407 + 16.8670 V_1 & \text{error} &\leq 0.557\% \end{aligned}$$

2nd order equations

$$\begin{aligned} \alpha_1 &= 25.0315 + 14.9498 V_1 - 20.9116 V_1^2 \\ \alpha_2 &= 50.8754 - 8.6007 V_1 - 18.2714 V_1^2 \\ \alpha_3 &= 77.2208 + 16.7580 V_1 + 0.1363 V_1^2 \\ \text{error} &\leq 2.780\% \\ \text{error} &\leq 1.637\% \\ \text{error} &\leq 0.474\% \end{aligned} \quad (13)$$

3rd order equations

$$\begin{aligned} \alpha_1 &= 26.0063 + 3.2747 V_1 + 13.7314 V_1^2 - 28.8695 V_1^3 \\ \alpha_2 &= 51.6810 - 18.2571 V_1 + 10.3609 V_1^2 - 23.8605 V_1^3 \\ \alpha_3 &= 77.1429 + 17.6904 V_1 - 2.6305 V_1^2 + 2.3057 V_1^3 \\ \text{error} &\leq 0.789\% \\ \text{error} &\leq 0.470\% \\ \text{error} &\leq 0.002\% \end{aligned} \quad (14)$$

In case M = 5 (3rd, 5th, 7th, 9th, harmonics elimination)

1st order equations

$$\begin{aligned} \alpha_1 &= 17.1645 - 1.0782 V_1 & \text{error} &\leq 9.925\% \\ \alpha_2 &= 33.6212 - 11.3495 V_1 & \text{error} &\leq 7.171\% \\ \alpha_3 &= 51.4088 - 2.5510 V_1 & \text{error} &\leq 12.338\% \\ \alpha_4 &= 67.5524 - 20.5931 V_1 & \text{error} &\leq 10.461\% \\ \alpha_5 &= 81.8257 + 11.1391 V_1 & \text{error} &\leq 0.087\% \end{aligned} \quad (15)$$

2nd order equations

$$\begin{aligned} \alpha_1 &= 15.9990 + 6.8233 V_1 - 9.8770 V_1^2 \\ \alpha_2 &= 32.3412 - 2.7190 V_1 - 10.7882 V_1^2 \\ \alpha_3 &= 47.4898 + 24.0187 V_1 - 33.2122 V_1^2 \\ \alpha_4 &= 63.9736 + 3.6699 V_1 - 30.3287 V_1^2 \\ \alpha_5 &= 81.8736 + 10.8145 V_1 + 0.4057 V_1^2 \\ \text{error} &\leq 4.582\% \\ \text{error} &\leq 3.464\% \\ \text{error} &\leq 6.317\% \\ \text{error} &\leq 5.285\% \\ \text{error} &\leq 0.051\% \end{aligned} \quad (16)$$

3rd order equations

$$\begin{aligned} \alpha_1 &= 16.6337 - 0.7780 V_1 - 12.6781 V_1^2 - 18.7961 V_1^3 \\ \alpha_2 &= 33.0608 - 11.2535 V_1 + 14.5359 V_1^2 - 21.1037 V_1^3 \\ \alpha_3 &= 50.3446 - 10.1729 V_1 + 63.2433 V_1^2 - 84.5472 V_1^3 \\ \alpha_4 &= 66.5848 - 27.6033 V_1 + 62.4670 V_1^2 - 77.3307 V_1^3 \\ \alpha_5 &= 81.8038 + 11.6507 V_1 - 2.0753 V_1^2 + 2.0676 V_1^3 \\ \text{error} &\leq 2.507\% \\ \text{error} &\leq 1.985\% \\ \text{error} &\leq 3.164\% \\ \text{error} &\leq 2.593\% \\ \text{error} &\leq 0.014\% \end{aligned} \quad (17)$$

### 2. Three Phase Variant

We consider the ideal half bridge three phase inverter shown schematically in Fig. 1. As in the single phase variant, in determining the M angles over a quarter-cycle with a view to eliminating M-1 harmonics, the following nonlinear set of equations-based on equations (6)- has to be solved.

$$\begin{aligned} V_1 &= \text{constant} \\ V_5 = V_7 = V_{11} \dots V_n &= \text{zero} \end{aligned} \quad (18)$$

where  $n = 6k \pm 1, k = 1, 2, 3, \dots$  Since the load

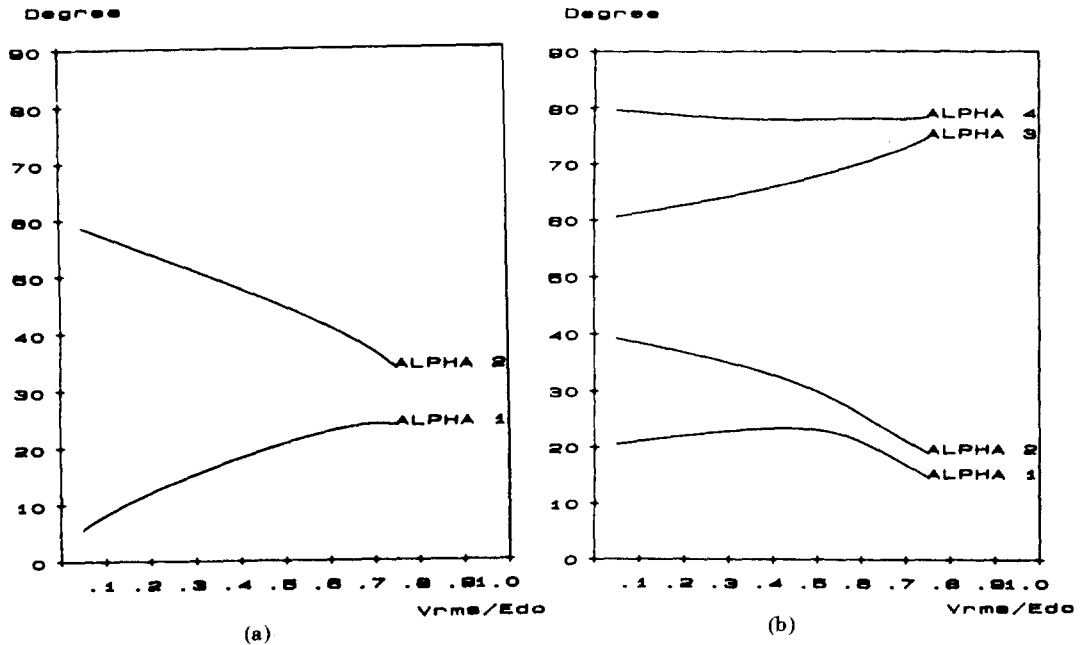


Fig. 8. The switching angles for eliminating in three phase inverter.

(a) 5th only (b) 5th, 7th and 11th

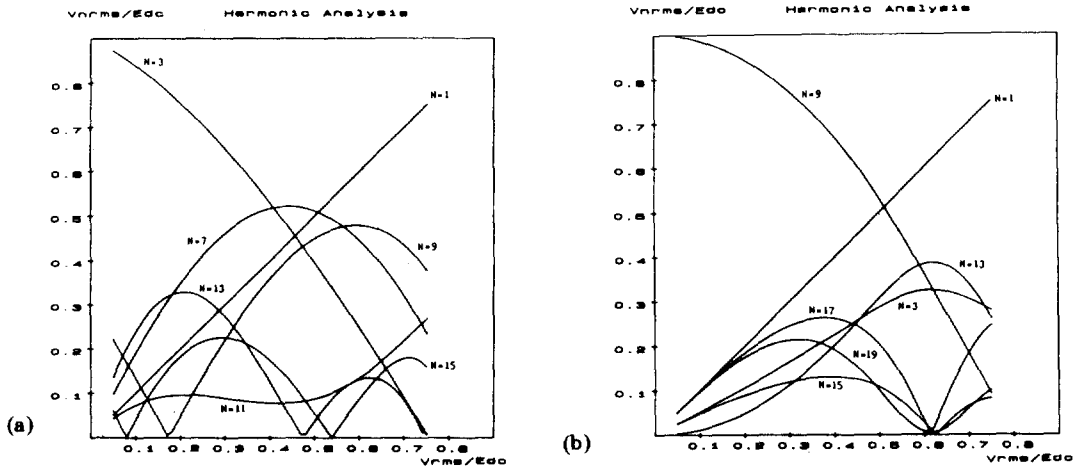


Fig. 9. Harmonics analysis in three phase. Relation between fundamental amplitude and (a) 3rd, 7th, 9th, 11th, 13th and 15th (b) 3rd, 9th, 13th, 15th, 17th and 19th

comprises three conductors, the harmonics  $V_{3k}$  ( $k = 1, 2, \dots$ ) produce current in it and need be eliminated. The amplitude of fundamental wave  $V_1$  was varied from the minimum 0.05 to the maximum 0.75 with 0.01 resolution as in single phase inverter. And for each value  $M$  commutation angles were determined ensuring elimination of  $M-1$  harmonics.

The following two cases of elimination were considered with aid of the above program Fig.3: (a) 5th harmonic only (b) 5th, 7th, and 11th

Results,  $\alpha_1$ , are plotted in Fig. 8 (a)-(b) respectively, with the fundamental amplitude given in normalized values and the angles in degree of arc. On the other hand, the relation between the fundamental rms voltages are shown in Fig. 9 (a)-(b) respectively.

And also, the coefficients and the error of the polynomial approximation equations which govern the commutation angles in the three phase inverter are represented in equations (19)-(24).

In case  $M = 2$  (5th only harmonic elimination)

1st order equations

$$\begin{aligned} \alpha_1 &= 6.6929 + 26.4097 V_1 & \text{error} &\leq 41.612\% \\ \alpha_2 &= 60.7544 - 33.5362 V_1 & \text{error} &\leq 5.635\% \end{aligned} \quad (19)$$

2nd order equations

$$\begin{aligned} \alpha_1 &= 3.6392 + 47.1131 V_1 - 25.8792 V_1^2 \\ \alpha_2 &= 59.3129 - 23.7636 V_1 - 12.2156 V_1^2 \\ \text{error} &\leq 4.796\% \\ \text{error} &\leq 2.718\% \end{aligned} \quad (20)$$

3rd order equations

$$\begin{aligned} \alpha_1 &= 3.9954 + 42.8461 V_1 - 13.2129 V_1^2 - 10.5512 V_1^3 \\ \alpha_2 &= 60.4162 - 36.9529 V_1 + 26.9205 V_1^2 - 32.6138 V_1^3 \\ \text{error} &\leq 7.858\% \\ \text{error} &\leq 1.128\% \end{aligned} \quad (21)$$

In case  $M = 4$  (5th, 7th and 11th harmonics elimination)

1st order equations

$$\begin{aligned} \alpha_1 &= 23.5361 - 5.4094 V_1 & \text{error} &\leq 32.917\% \\ \alpha_2 &= 42.6442 - 28.1912 V_1 & \text{error} &\leq 12.901\% \\ \alpha_3 &= 58.7078 + 19.2771 V_1 & \text{error} &\leq 2.105\% \\ \alpha_4 &= 79.0112 - 1.7398 V_1 & \text{error} &\leq 0.874\% \end{aligned} \quad (22)$$

2nd order equations

$$\begin{aligned} \alpha_1 &= 17.8236 + 33.3192 V_1 - 48.4109 V_1^2 \\ \alpha_2 &= 38.8980 - 2.7930 V_1 - 31.7477 V_1^2 \\ \alpha_3 &= 60.4057 + 7.7658 V_1 + 14.3891 V_1^2 \\ \alpha_4 &= 79.9522 - 8.1196 V_1 + 7.9748 V_1^2 \end{aligned}$$

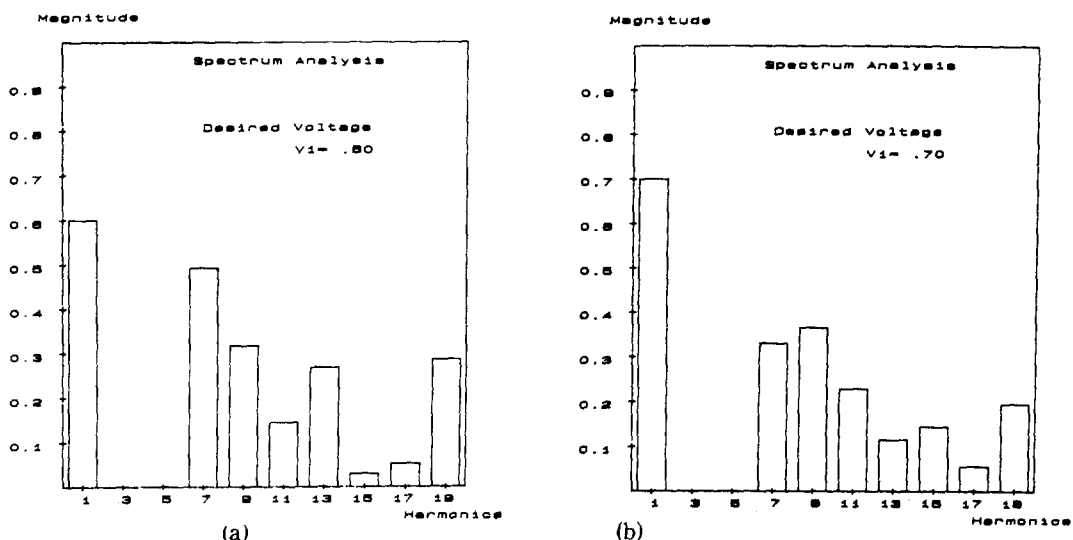


Fig. 10. Normalized voltage spectrum in single phase, 3rd and 5th harmonics elimination.  
 (a)  $V_1=0.60(7V)$ , 30Hz (b)  $V_1=0.70(8.5V)$ , 400Hz

error  $\leq 6.325\%$   
 error  $\leq 1.410\%$   
 error  $\leq 0.555\%$   
 error  $\leq 0.213\%$  (23)

3rd order equations

$$\begin{aligned} \alpha_1 &= 20.5375 + 0.8158 V_1 + 48.0355 V_1^2 - 80.3729 V_1^3 \\ \alpha_2 &= 39.7785 - 13.3382 V_1 - 0.4574 V_1^2 - 26.0756 V_1^3 \\ \alpha_3 &= 59.9274 + 13.4939 V_1 - 2.6076 V_1^2 - 2.6076 V_1^3 \\ \alpha_4 &= 80.2475 - 11.6561 V_1 + 18.4684 V_1^2 - 8.7447 V_1^3 \end{aligned}$$

error  $\leq 2.682\%$   
 error  $\leq 2.768\%$   
 error  $\leq 0.244\%$   
 error  $\leq 0.185\%$  (24)

#### IV. Microprocessor Methods for Processing and Implementation

The method used to process the laws which govern the commutation angles with a microprocessor depends largely on the complexity of the expressions chosen for this purpose. Where very high order linear equations are necessary, the microprocessor will take a very long time to calculate the commutation angles and, therefore the best procedure will be to store the discrete

values of the commutation angles for each value of the fundamental rms voltage. When these approximations are low order equations, it might be useful to use the microprocessor to calculate them. Here the memory requirements are greatly reduced at the expense of a more complex software. In this paper, the example previously studied, where the 3rd and the 5th harmonics are canceled, is considered. In this case the microprocessor calculates  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$  from the three 3rd order linear approximation equation(14), for

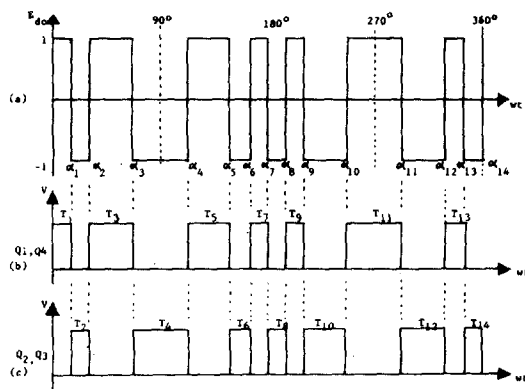


Fig. 11. Base driving time duration of the inverter.



every desired output condition.

On the other hand, Fig. 11. represents the pulses of the base driving time duration for switching in the single phase inverter(Fig.1). In order to realize pulses of Fig. 11-(a) the signals with time duration such as Fig. 11-(b), (c) have to be yielded from the computer. In this case the relationship between the switching angles,  $\alpha_n$  and base driving time duration  $T_n$ , ( $n=1, 2, 3, \dots$ ) and desired frequency  $f$ , in the inverter output from Fig. 11 follows as ;

$$T_n = \left[ (\alpha_n - \alpha_{n-1}) \frac{10^4}{3 \cdot 6f} - d \right] f_c \tag{25}$$

where  $f_c$  denotes the system clock frequency and  $d$  is the dead time for protecting the power transistor in switching. In implementation the time  $d$  is considered with 10 micro seconds but this time is very small compare with switching time  $T_n$ .

Consequently, in such as inverter voltage 8.5V, desirous frequency 400Hz, unwanted harmonics are 3rd, 5th order, the error rate of switching angles  $\alpha_n$  is 1.71772% maximum, or 0.334584% minium. Thus, the error that is produced by dead time could be ignored and the goal of the harmonics elimination and the voltage control is accomplished.

On the other hand, Fig. 12. is the flowchart for generating the time duration of Fig. 11.-(b), (c). In flowchart Fig. 12, the calculation process of

the swiching time  $T_n$ , was programed with the aid of the aid of a FORTRAN language and the processing which transmit the consequent data  $T_n$  to inverter circuit was programmed by Z-80 assembly language in order to the real time processing.

The notation  $V_p$  denotes the DC power source and  $V_d$  is the desired rms voltage value of the inverter output.

In addition, the control circuit and harsware developed in based on Zilog's Z-80 microcomputer is represented in Fig. 13. The clock of the microcomputer was adjusted to 2.5 Mhz.

The practical scheme used in the experimental test is shown in Fig. 13.-(b). It is based on the circuit, as shown in Fig. 1. and employs the 7 watt lamp as resistor load and DC 12 V as  $V_{cc}$ .

Photo 1-(a), (b) show the voltage waveforms at inverter output. These waveforms represents the desired voltages 7 volt (30 Hz) and 8.5 volt (400 Hz) while the 3rd and the 5th harmonics are canceled in single phase inverter output, respectively.

As a practical result of calculation, the photo 1-(a), (b) rms voltage are 6.957644491 V and 8.520 089438 V respectively. Thus they take 0.6 percent and 0.236 percent in error rate.

As assumming, previously studied in section II, they have the three commutations within the each quadrant and show they are odd-quarter

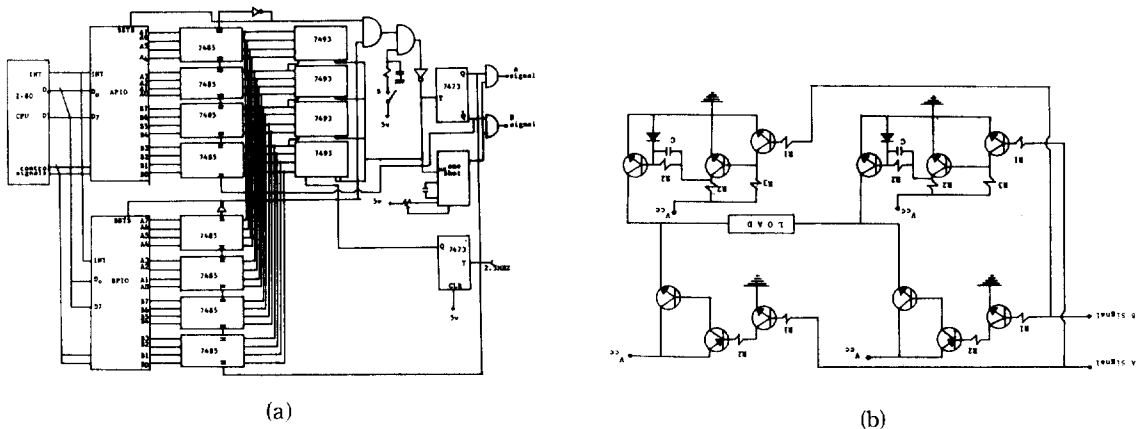


Fig. 13. (a) Microcomputer hardware (b) Inverter power circuit

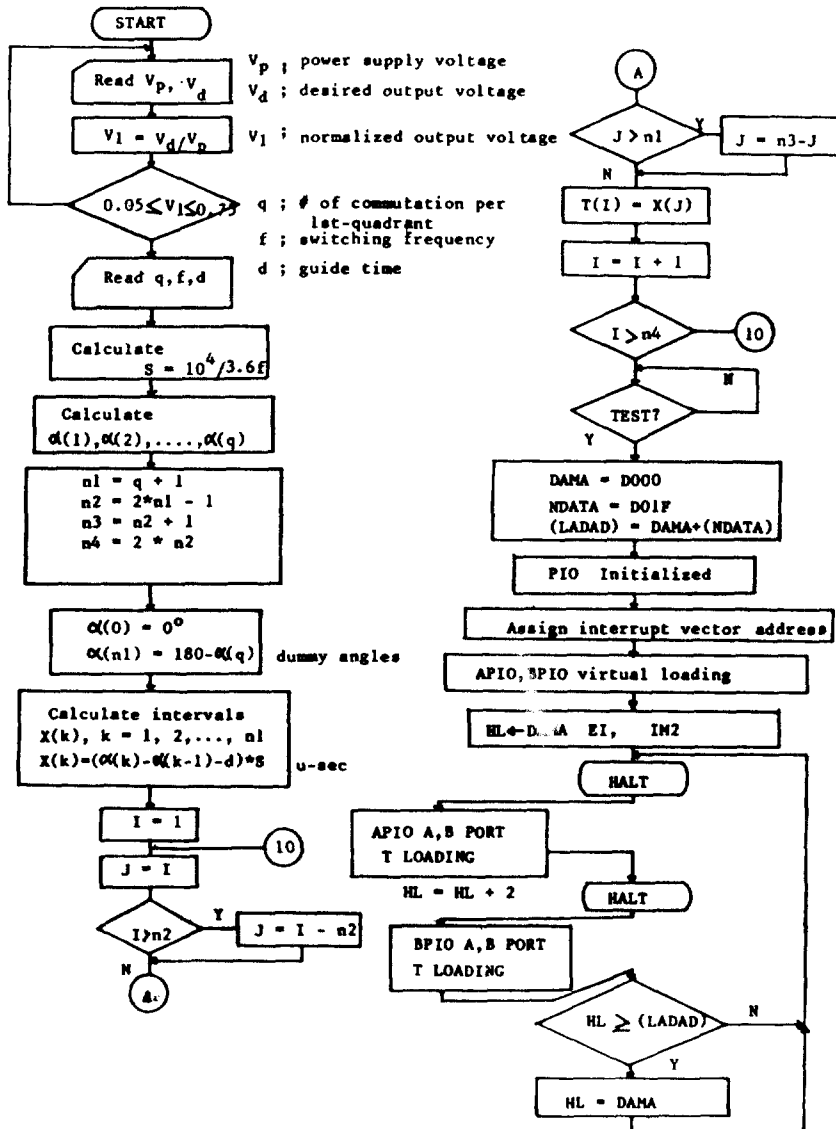
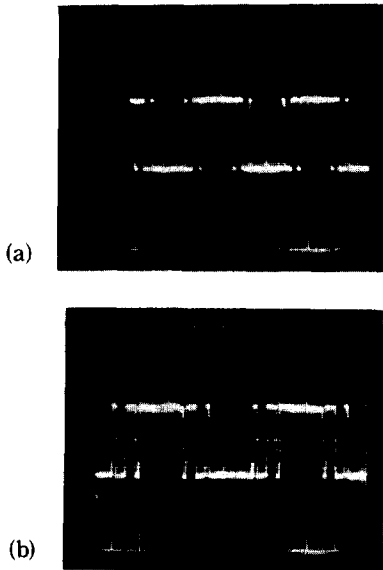


Fig. 12. Flowchart for generating the time durations of Fig. 11-(b) and (c).

symmetry waveforms.

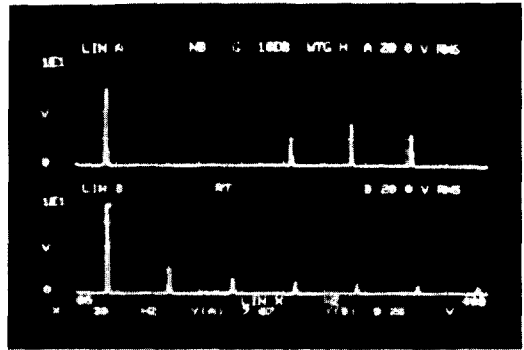
On the other hand, Photo 2-(a)~(d) show the spectrum analyses of photo 1-(a), 1-(b), respectively. As can be seen, we find that the predetermined 3rd and 5th harmonics are eliminated through the load.

On the other hand, the usable frequency of inverter is depended upon the number of necessary clock cycle to process the machine language of the whole program. Furthermore, the critical limit of inverter frequency is not depended upon the number of unwanted harmonics but also the computer system clock frequency. Thus, we can not determine the relationship to regulate the

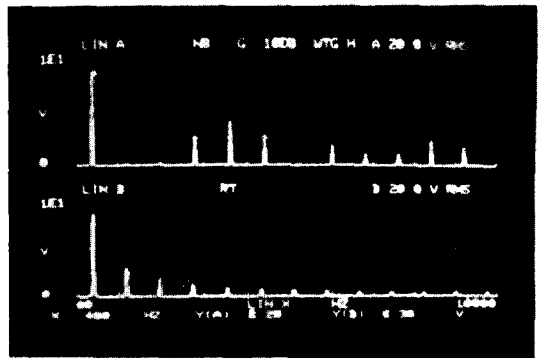


**Photo. 1.** Inver output waveforms versus desired voltage and frequency in single phase.  
 (a) 7V, 30Hz Hori : 10ms/div, vert ;  
 (b) 8.5V, 400 Hz Hori : 0.5 ms/div, vert : 10V/div

usable limit of inverter frequency. However, in any case, we can fix the desirous higher limit of inverter frequency by of the short program calculated. Here the inverter frequency on this experiment is higher than 100 Hz.



(a)



(b)

**Photo. 2.** Experimental PWM spectra results in  
 Upper ; eliminated inverter frequency,  
 (a) 30Hz, (b) 400Hz.  
 Lower : non-eliminated.

### V. Conclusion

In this paper, the analysis of the equations which govern the more accurate commutation of power switches in order to cancel any predetermined harmonics and very the fundamental rms voltage was presented and the realization of constructing such a control circuit were discussed.

The experimental test has been carried out on a Z-80 microcomputer with a view to controlling in the single phase inverter. As can be seen, the effective elimination of any order harmonics and the frequency control were able to be accomplished by using polynomial approximation equations. In addition, throughout the experimental investigations, it can be summarized that the inverter output control has the various features as follows to the conventional ones ;

- (1) effective elimination of low order harmonics
- (2) generation of the ignoble error be due to consideration of the dead time(guide time), d.
- (3) adjustment of inverter output frequency that is based on the necessary clock frequency of machine language program and computer system.

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