## CATEGORIES DEFINED BY INITIALITY AND FINALITY IN *Top*

## In JAE CHUNG

We consider two subcategories  $\mathcal{A}$  and  $\mathcal{E}$  of Top and define initially defined topological spaces from  $\mathcal{A}$  to  $\mathcal{E}$ , namely a topological space X is said to be initially defined from  $\mathcal{A}$  to  $\mathcal{E}$  if the space  $X^0$  endowed with the initial structure for  $\{f \mid f : X \rightarrow A \text{ continuous and } A \in \mathcal{A}\}$  belongs to  $\mathcal{E}$ .

We define Ini  $(\mathcal{A}:\mathcal{B})$  as the full subcategory formed by initially defined spaces from  $\mathcal{A}$  to  $\mathcal{B}$ .

Firstly, we give internal characterizations and their categorical properties for various categories A and B.

Secondly, we try to get some permanence properities of  $\operatorname{Ini}(\mathcal{A}:\mathcal{E})$ . For a subcategory  $\mathcal{E}$  such that for any  $(X,\overline{\mathcal{E}}) \in \mathcal{E}$ , the space  $(X,\overline{\mathcal{E}}')$  with  $\overline{\mathcal{E}} \subseteq \overline{\mathcal{E}}'$  belongs to  $\mathcal{E}$ , it is shown that if  $\mathcal{E}$  is closed under the formation of products, then so is  $\operatorname{Ini}(\mathcal{A}:\mathcal{E})$ , and that if  $\mathcal{E}$  is hereditary, then so Is  $\operatorname{Ini}(\mathcal{A}:\mathcal{E})$ .

It is also shown that if  $\mathcal{B}$  is closed under the formation of continuous images then Ini  $(\mathcal{A}:\mathcal{B})$  is also closed under the formation of continuous images.

Finally, we try to dualize the above concepts in chapter II and we obtain some corresponding results.

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