

Sulfaguanidine Monohydrate 의 結晶 및 分子構造

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The Crystal and Molecular Structure of Sulfaguanidine Monohydrate

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요 약. sulfaguanidine 1 수화물의 결정 및 분자구조를 X-선 회절법으로 규명하였다. 결정은 일사축계에 속하며 단위세포내에는 4 분자가 있으며 공간군은 $P2_1/c$ 이다. 단위세포상수는 $a=7.57 \pm 0.03$, $b=5.44 \pm 0.02$, $c=24.76 \pm 0.06 \text{ \AA}$, $\beta=91.0 \pm 0.2^\circ$ 이다. 결정구조는 패터슨 합수의 해석과 직접법을 병용하여 밝혀냈다. 원자좌표치는 최소자승법으로 정밀화하였으며 1542 개의 독립적인 회절반점에 대한 최종 R 값은 0.14 이었다. sulfaguanidine 분자의 guanidyl 기의 질소원자는 2 개의 다른 물분자를 매개로 하여 수소결합을 하므로써 다른 분자들의 sulfonyl 기의 산소원자에 연결되어 있다. 수소결합 형성에 있어서 물분자는 donor 와 acceptor 의 역할을 겸하고 있으며 수소결합은 사면체의 방향을 하고 있다. 2 차원적인 수소결합에 의하여 연결된 분자들은 (001)면에 평행한 분자층을 형성하고 있다.

Abstract. The crystal and molecular structure of sulfaguanidine monohydrate, $C_7H_{10}N_4O_2S \cdot H_2O$, was determined from visually estimated intensity data from Weissenberg photographs. The crystal data are monoclinic, space group $P2_1/c$ with four molecules in a unit cell of dimensions, $a=7.57 \pm 0.03$, $b=5.44 \pm 0.02$, $c=24.76 \pm 0.06 \text{ \AA}$, $\beta=91.0 \pm 0.2^\circ$. The structure has been solved by an interpretation of a Patterson map and with a help of a direct procedure on a procejection. The parameters were refined isotropically by block-diagonal least-squares methods using 1542 observed independent reflections to give $R=0.14$. By hydrogen bonding a guanidyl nitrogen of a sulfaguanidine molecule is linked to the sulfonyl oxygens of the other molecules indirectly through two different water molecules. The role of water molecule is both a donor and an acceptor in hydrogen-bonding formation and these hydrogen bonds are tetrahedrally oriented. The hydrogen-bonding networks form infinite molecular layers parallel to (001) plane.

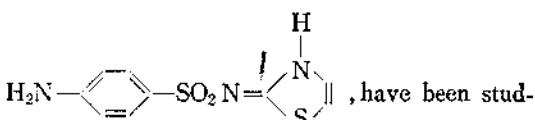
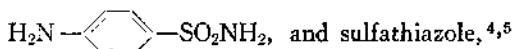
Introduction

As a part of a series of detailed structure

investigation on sulfur-containing compounds which have biologically active groups by X-ray single-crystal diffraction, the crystal and molecular structure of sulfaguanidine monohydrate

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has been determined in this work. Among the sulfa drugs containing sulfanilamido group, the crystal structures of sulfanilamide^{1,2,3},



In this experiment, we have investigated the conformation of the sulfaguanidine molecule, delocalization of π -electron on the guanidyl residue and the role of hydrated water molecule in the crystal-lattice environment.

Experimental

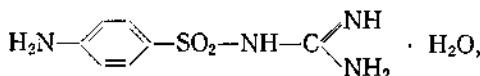
Prismatic crystals of sulfaguanidine monohydrate elongated along the b axis were obtained by slow evaporation from an aqueous acetone solution at room temperature.

Unit cell dimensions were determined by a least-squares refinement of 2θ values for 47 independent reflections measured on the $h0l$ and $0kl$ Weissenberg photographs calibrated with superimposed Al-lines using Cu-K α radiation.

The density of single crystals, measured by flotation method in a mixture of benzene and carbon tetrachloride, was found to be consistent with 4 formula units in a unit cell.

The existence of water molecule in the single crystal was confirmed by the strong O-H stretching peak at 3400 cm^{-1} in IR-spectrum.

The crystal data are as follows; sulfaguanidine monohydrate,



monoclinic, $a=7.57 \pm 0.03$, $b=5.44 \pm 0.02$, $c=$

$24.76 \pm 0.06 \text{ \AA}$, $\beta=91.0 \pm 0.2^\circ$, $V=1019.1 \text{ \AA}^3$, M. W. = 232.26, Z=4, $D_m=1.50$, $D_e=1.51 \text{ g cm}^{-3}$, space group: $P2_1/c$ from systematic absence $h0l$ for l odd, $0k0$ for k odd.

Intensity data were collected from equi-inclination Weissenberg photographs taken with Cu-K α radiation by use of the multiple-film method. The layers from $h0l$ to $h4l$ for the b axis and from $0kl$ to $1kl$ for the a axis were recorded. The approximate dimensions of the crystals used for gathering the intensity data for the a and b axes were $0.2 \times 0.2 \times 1.0$ and $0.2 \times 0.3 \times 0.7 \text{ mm}$ respectively. The relative intensities were measured by visual comparison with a calibrated intensity scale prepared from the same crystals with the X-ray beam under carefully controlled conditions.

The intensities were corrected for spot-shape, Lorentz and polarization effects, but not for extinction or absorption, and converted into the observed structure factors. Interlayer scaling constants were calculated from common equivalent reflections and the structure factors were placed approximately on an absolute scale following the Wilson method⁶. The final number of observed independent reflections was 1542. All calculations were performed on an IBM 1130 computer with a series of programs by Shiono (1968)⁷.

Structure Determination and Refinement

After the structure factors were converted into the normalized structure factors, E , a three-dimensional sharpened Patterson function was computed using 985 normalized structure factors greater than $|E|=0.58$. The sulfur-sulfur Harker peak was easily identified, and trial positional parameters for the six atoms of S, O(1), O(2), C(1), N(1) and N(2) whose numberings are shown in Fig. 1 were obtained

from the inspection of the Patterson map.

Independently a Fourier projection of electron density on $(0kl)$ plane with 78 reflections whose phases were determined manually by an application of the direct method⁸ showed the positions of some of fifteen atoms and these were consistent with those obtained from the Patterson map.

The initial R factor, $R = \sum |F_o| - |F_c| / \sum |F_o|$, based on these six atoms with all assumed $B=3.0 \text{ \AA}^2$ was 0.56 for 1005 reflections. The R factor based on sulfur coordinates alone was 0.70. Two cycles of isotropic block-diagonal least-squares refinement⁹ reduced the R factor to 0.45. A three-dimensional Fourier synthesis, which was computed using the 1005 observed structure factors phased on the contribution of the six atoms, gave the clear picture of the molecule consistent with a chemically reasonable model. The refinement with isotropic temperature

parameters was carried out successively and stopped after several cycles attaining a minimum R value of 0.14 for all the 1542 observed reflections. The function minimized was $w(|F_o| - |F_c|)^2$ and the weighting scheme w proposed by Cruickshank(1965)¹⁰ was used throughout the refinement. The form of the function, w , was $(A+B|F_o|+C|F_o|^2)^{-1}$, where $A=2|F_{\min}|=3.14$, $B=1.00$, $C=2/|F_{\max}|=0.0164$. No allowance was made for the hydrogen atoms. Atomic scattering factor values were taken from the International Table for X-ray Crystallography¹¹. The final positional and thermal parameters for the atoms are given in *Table 1* with their estimated standard deviations as calculated from the least-squares refinement. Observed and calculated structure factors based on the parameters in *Table 1* are listed in *Table 2*. The atoms are numbered according to *Fig. 1*.

Table 1. Final atomic coordinates and isotropic thermal parameters in sulfaguanidine monohydrate.

The estimated standard deviations given in parentheses refer to the last decimal positions

| | <i>x</i> | <i>y</i> | <i>z</i> | <i>B</i> |
|------|-----------|-----------|-----------|----------|
| S | 0.2588(5) | 0.4835(7) | 0.4041(1) | 1.68(6) |
| O(1) | 0.366(2) | 0.301(2) | 0.4306(5) | 2.6(2) |
| O(2) | 0.323(2) | 0.727(2) | 0.4098(5) | 2.9(2) |
| O(3) | 0.349(2) | 0.168(2) | 0.5410(5) | 2.7(2) |
| N(1) | 0.266(3) | 0.273(4) | 0.1671(9) | 5.1(4) |
| N(2) | 0.055(2) | 0.493(2) | 0.4226(5) | 2.7(2) |
| N(3) | 0.022(2) | 0.065(3) | 0.4261(7) | 3.2(3) |
| N(4) | -0.215(2) | 0.324(3) | 0.4386(7) | 3.2(3) |
| C(1) | 0.257(2) | 0.412(3) | 0.3339(6) | 2.4(3) |
| C(2) | 0.338(3) | 0.205(4) | 0.3160(8) | 2.8(3) |
| C(3) | 0.338(3) | 0.157(4) | 0.2603(9) | 3.5(4) |
| C(4) | 0.261(3) | 0.322(4) | 0.2230(8) | 3.3(3) |
| C(5) | 0.175(3) | 0.519(4) | 0.2433(9) | 3.8(4) |
| C(6) | 0.175(3) | 0.573(4) | 0.2983(8) | 3.0(3) |
| C(7) | -0.038(2) | 0.291(3) | 0.4302(6) | 2.2(3) |

Table 2. Observed and calculated structure factors. Columns are Index, $10|F_{obs}|$ and $10|F_{cal}|$

| $h=0 k=0$ | 16 | 366 | 208 | 9 | 65 | 72 | 15 | 166 | 152 | 8 | 195 | 202 | 5 | 62 | 55 | 8 | 556 | 505 | |
|-------------|-----------|-----|-----|-----------|-----|-----|-----------|-----------|-----|-----------|-----------|-----|-----------|-----|-----|-----------|-----|-----|--|
| 4 324 319 | 18 | 285 | 219 | 10 | 451 | 490 | 16 | 271 | 268 | 9 | 268 | 225 | 6 | 53 | 54 | 9 | 56 | 12 | |
| 6 1058 1548 | 20 | 72 | 56 | 11 | 397 | 612 | 17 | 336 | 303 | 10 | 330 | 285 | 8 | 58 | 43 | 10 | 623 | 599 | |
| 8 1157 1098 | 22 | 191 | 130 | 12 | 357 | 326 | 19 | 292 | 215 | 11 | 62 | 52 | 9 | 85 | 79 | 11 | 198 | 211 | |
| 10 114 36 | 26 | 163 | 148 | 13 | 47 | 65 | 21 | 107 | 112 | 12 | 199 | 170 | 10 | 95 | 124 | 12 | 119 | 100 | |
| 12 835 815 | 28 | 111 | 99 | 14 | 234 | 168 | 22 | 190 | 170 | 13 | 220 | 231 | 2 | 57 | 61 | 13 | 86 | 93 | |
| 16 158 154 | $h=5 k=0$ | 15 | 79 | 67 | 23 | 87 | 81 | 15 | 249 | 206 | 3 | 444 | 499 | 14 | 177 | 192 | | | |
| 18 77 100 | 2 | 200 | 188 | 16 | 191 | 121 | 25 | 136 | 141 | 16 | 238 | 224 | 15 | 160 | 172 | | | | |
| 22 64 62 | 4 | 444 | 406 | 17 | 347 | 267 | 27 | 216 | 193 | 17 | 189 | 132 | 4 | 212 | 192 | 16 | 403 | 365 | |
| 26 107 107 | 6 | 332 | 273 | 18 | 415 | 417 | 28 | 108 | 123 | 21 | 79 | 68 | 5 | 197 | 167 | 17 | 153 | 130 | |
| 30 180 173 | 8 | 158 | 169 | 19 | 209 | 186 | 30 | 53 | 57 | 22 | 80 | 58 | 6 | 354 | 295 | 18 | 177 | 172 | |
| $h=1 k=0$ | 10 | 132 | 135 | 20 | 128 | 135 | $h=3 k=1$ | 23 | 133 | 113 | 7 | 310 | 279 | 20 | 225 | 230 | | | |
| 0 159 148 | 12 | 181 | 148 | 21 | 63 | 89 | 0 | 40 | 62 | 24 | 52 | 48 | 8 | 360 | 342 | 21 | 77 | 98 | |
| 2 676 1037 | 14 | 417 | 350 | 22 | 107 | 110 | 1 | 428 | 412 | 25 | 87 | 97 | 9 | 65 | 43 | 22 | 81 | 91 | |
| 4 94 115 | 16 | 107 | 107 | 23 | 59 | 42 | 2 | 310 | 287 | 26 | 45 | 34 | 10 | 356 | 377 | 23 | 79 | 88 | |
| 6 747 800 | 18 | 381 | 282 | 24 | 139 | 127 | 3 | 120 | 124 | $h=6 k=1$ | 11 | 143 | 146 | 25 | 56 | 59 | | | |
| 8 1047 1076 | 20 | 196 | 169 | 25 | 133 | 138 | 4 | 272 | 236 | 1 | 341 | 307 | 12 | 163 | 152 | 26 | 82 | 123 | |
| 10 558 496 | 22 | 119 | 131 | 26 | 115 | 127 | 5 | 91 | 109 | 2 | 90 | 90 | 13 | 106 | 98 | 28 | 43 | 58 | |
| 12 746 699 | 24 | 98 | 96 | 27 | 154 | 175 | 6 | 328 | 291 | 4 | 162 | 143 | 14 | 104 | 119 | 29 | 49 | 57 | |
| 14 774 710 | 26 | 123 | 119 | 28 | 70 | 78 | 7 | 367 | 328 | 5 | 307 | 259 | 16 | 275 | 228 | $h=3 k=2$ | | | |
| 16 419 324 | $h=6 k=0$ | 29 | 204 | 31 | 9 | 258 | 254 | 7 | 210 | 162 | 17 | 245 | 212 | 0 | 439 | 423 | | | |
| 18 325 255 | 2 | 77 | 86 | 31 | 121 | 150 | 10 | 130 | 120 | 11 | 181 | 179 | 18 | 198 | 140 | 1 | 53 | 41 | |
| 20 286 289 | 4 | 184 | 152 | $h=1 k=1$ | 13 | 266 | 221 | 12 | 67 | 69 | 19 | 163 | 120 | 2 | 236 | 212 | | | |
| 24 130 143 | 6 | 74 | 50 | 0 | 567 | 659 | 14 | 158 | 117 | 13 | 151 | 118 | 20 | 303 | 227 | 4 | 71 | 87 | |
| 26 98 107 | 8 | 75 | 75 | 1 | 645 | 676 | 15 | 192 | 167 | 15 | 261 | 197 | 26 | 122 | 130 | 6 | 219 | 166 | |
| 28 182 131 | 10 | 239 | 208 | 2 | 520 | 624 | 17 | 288 | 241 | 17 | 127 | 108 | 28 | 74 | 69 | 7 | 289 | 253 | |
| 30 108 77 | 12 | 258 | 188 | 3 | 369 | 380 | 18 | 360 | 322 | 18 | 244 | 190 | 29 | 31 | 34 | 3 | 282 | 242 | |
| $h=2 k=0$ | 16 | 405 | 324 | 4 | 298 | 239 | 19 | 143 | 142 | 21 | 170 | 142 | 30 | 51 | 67 | 10 | 58 | 87 | |
| 0 960 1364 | 22 | 154 | 144 | 5 | 297 | 268 | 22 | 76 | 53 | 23 | 95 | 94 | $h=1 k=2$ | 11 | 241 | 198 | | | |
| 2 191 186 | $h=7 k=0$ | 6 | 336 | 278 | 23 | 171 | 150 | $h=7 k=1$ | 1 | 183 | 171 | 12 | 303 | 219 | | | | | |
| 6 210 168 | 0 | 103 | 83 | 7 | 339 | 357 | 24 | 88 | 86 | 0 | 149 | 139 | 2 | 506 | 534 | 13 | 109 | 120 | |
| 8 352 299 | 2 | 275 | 190 | 8 | 76 | 93 | 25 | 166 | 157 | 1 | 85 | 96 | 3 | 122 | 129 | 14 | 134 | 119 | |
| 10 104 80 | 4 | 297 | 247 | 9 | 367 | 340 | 26 | 107 | 92 | 3 | 270 | 236 | 4 | 124 | 103 | 15 | 110 | 103 | |
| 12 98 87 | 6 | 199 | 156 | 10 | 297 | 204 | 29 | 162 | 148 | 4 | 59 | 54 | 5 | 117 | 133 | 16 | 113 | 102 | |
| 14 325 271 | 8 | 180 | 151 | 11 | 93 | 59 | $h=4 k=1$ | 6 | 131 | 121 | 6 | 348 | 263 | 17 | 88 | 114 | | | |
| 16 438 400 | 10 | 209 | 163 | 12 | 191 | 104 | 0 | 287 | 243 | 7 | 194 | 160 | 7 | 418 | 379 | 18 | 302 | 268 | |
| 18 433 359 | 14 | 205 | 135 | 13 | 383 | 314 | 1 | 264 | 208 | 9 | 237 | 189 | 8 | 389 | 281 | 21 | 41 | 40 | |
| 20 298 275 | 18 | 156 | 130 | 14 | 242 | 211 | 2 | 147 | 156 | 10 | 132 | 114 | 9 | 52 | 36 | 22 | 79 | 124 | |
| 22 419 357 | 20 | 73 | 46 | 15 | 236 | 167 | 3 | 298 | 255 | 12 | 184 | 131 | 10 | 51 | 45 | 23 | 35 | 26 | |
| 26 373 313 | $h=8 k=0$ | 16 | 59 | 54 | 4 | 92 | 90 | 13 | 276 | 231 | 11 | 252 | 222 | 24 | 196 | 199 | | | |
| 28 267 231 | 0 | 177 | 140 | 17 | 374 | 281 | 5 | 237 | 224 | 14 | 60 | 72 | 12 | 315 | 297 | 25 | 33 | 31 | |
| 30 111 72 | 2 | 138 | 120 | 18 | 267 | 179 | 6 | 139 | 113 | 15 | 217 | 175 | 14 | 262 | 196 | 27 | 35 | 30 | |
| $h=3 k=0$ | 6 | 69 | 66 | 19 | 292 | 260 | 8 | 191 | 154 | 16 | 53 | 74 | 16 | 87 | 80 | 23 | 101 | 128 | |
| 0 854 959 | 10 | 114 | 71 | 20 | 132 | 103 | 10 | 166 | 138 | 17 | 123 | 80 | 18 | 526 | 406 | $h=4 k=2$ | | | |
| 2 456 345 | 12 | 149 | 114 | 22 | 88 | 89 | 11 | 207 | 196 | 18 | 85 | 70 | 19 | 31 | 16 | 0 | 394 | 391 | |
| 4 382 339 | 14 | 80 | 63 | 23 | 99 | 109 | 12 | 191 | 137 | 19 | 90 | 85 | 21 | 73 | 66 | 1 | 249 | 251 | |
| 6 56 87 | 16 | 171 | 134 | 25 | 184 | 187 | 15 | 260 | 226 | 20 | 83 | 54 | 24 | 231 | 203 | 2 | 282 | 294 | |
| 8 270 254 | $h=9 k=0$ | 29 | 149 | 147 | 17 | 212 | 195 | $h=8 k=1$ | 25 | 36 | 29 | | 3 | 81 | 115 | | | | |
| 10 131 63 | 0 | 97 | 71 | $h=2 k=1$ | 18 | 181 | 161 | 1 | 173 | 176 | 26 | 68 | 65 | 4 | 159 | 114 | | | |
| 12 181 155 | 2 | 226 | 134 | 0 | 589 | 735 | 19 | 119 | 106 | 4 | 117 | 102 | 27 | 38 | 30 | 5 | 132 | 105 | |
| 14 195 182 | 4 | 153 | 130 | 1 | 251 | 260 | 20 | 49 | 26 | 5 | 147 | 125 | 28 | 76 | 101 | 6 | 313 | 316 | |
| 18 389 279 | 8 | 121 | 101 | 2 | 265 | 254 | 21 | 129 | 141 | 7 | 81 | 71 | 29 | 32 | 32 | 7 | 85 | 83 | |
| 24 196 165 | 10 | 184 | 147 | 3 | 302 | 249 | 23 | 96 | 100 | 8 | 71 | 69 | 30 | 86 | 102 | 8 | 68 | 75 | |
| 28 215 214 | $h=0 k=1$ | 4 | 309 | 309 | 25 | 54 | 71 | 10 | 127 | 87 | $h=2 k=2$ | 9 | 38 | 39 | | | | | |
| $h=4 k=0$ | 1 | 478 | 683 | 5 | 435 | 425 | 27 | 138 | 141 | 11 | 140 | 129 | 0 | 100 | 64 | 10 | 250 | 208 | |
| 0 391 388 | 2 | 154 | 217 | 6 | 61 | 36 | $h=5 k=1$ | 13 | 83 | 76 | 1 | 180 | 165 | 11 | 37 | 41 | | | |
| 2 414 345 | 3 | 328 | 298 | 8 | 540 | 481 | 0 | 94 | 93 | 15 | 190 | 146 | 2 | 463 | 378 | 12 | 76 | 93 | |
| 4 107 102 | 4 | 427 | 421 | 10 | 359 | 320 | 1 | 106 | 100 | 16 | 93 | 82 | 3 | 336 | 266 | 13 | 125 | 133 | |
| 6 307 248 | 5 | 572 | 662 | 11 | 476 | 410 | 2 | 379 | 340 | $h=9 k=1$ | 4 | 458 | 356 | 14 | 33 | 38 | | | |
| 8 272 338 | 6 | 141 | 136 | 12 | 106 | 111 | 3 | 265 | 189 | 0 | 159 | 113 | 5 | 193 | 182 | 15 | 39 | 70 | |
| 12 286 268 | 7 | 307 | 324 | 13 | 92 | 73 | 4 | 373 | 328 | 3 | 202 | 149 | 6 | 259 | 261 | 16 | 197 | 172 | |
| 14 232 215 | 127 | 105 | 14 | 138 | 110 | 7 | 255 | 213 | 4 | 82 | 72 | 7 | 218 | 202 | 17 | 47 | 45 | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----|-----|-----|---------------|-----|-----|---------------|-----|---------------|---------------|-----|---------------|---------------|-----|---------------|---------------|-----|---------------|---------------|-----|---------------|-----|-----|--|--|--|--|--|
| 18 | 43 | 62 | 16 | 116 | 112 | 15 | 51 | 49 | 24 | 26 | 16 | 5 | 42 | 45 | 17 | 90 | 102 | 2 | 212 | 196 | | | | | | | |
| 19 | 58 | 52 | 17 | 44 | 36 | 16 | 193 | 173 | 25 | 42 | 63 | 6 | 123 | 89 | 18 | 22 | 210 | 3 | 158 | 184 | | | | | | | |
| 20 | 133 | 130 | 18 | 135 | 135 | 17 | 46 | 49 | 26 | 25 | 8 | 7 | 50 | 57 | 20 | 162 | 147 | 5 | 63 | 60 | | | | | | | |
| 21 | 43 | 55 | $\hbar=8 k=2$ | | 18 | 54 | 68 | $\hbar=4 k=3$ | | 9 | 122 | 112 | 21 | 113 | 111 | 6 | 161 | 156 | | | | | | | | | |
| 22 | 76 | 81 | 0 | 115 | 99 | 19 | 221 | 177 | 0 | 187 | 177 | 10 | 35 | 14 | 22 | 25 | 38 | 7 | 49 | 45 | | | | | | | |
| 23 | 57 | 75 | 2 | 253 | 208 | 20 | 47 | 44 | 1 | 179 | 145 | 11 | 70 | 56 | 23 | 49 | 61 | 8 | 63 | 75 | | | | | | | |
| 24 | 70 | 67 | 4 | 101 | 94 | 21 | 17 | 41 | 2 | 180 | 183 | 12 | 27 | 28 | 24 | 193 | 176 | 9 | 37 | 36 | | | | | | | |
| 25 | 57 | 67 | 6 | 95 | 95 | 22 | 88 | 92 | 3 | 80 | 93 | 13 | 111 | 82 | 25 | 38 | 67 | 10 | 87 | 101 | | | | | | | |
| 26 | 83 | 104 | 8 | 105 | 90 | 23 | 203 | 174 | 4 | 45 | 10 | 14 | 50 | 57 | $\hbar=2 k=4$ | | 11 | 30 | 6 | | | | | | | | |
| 27 | 30 | 18 | 10 | 36 | 43 | 24 | 27 | 38 | 5 | 358 | 310 | 15 | 32 | 38 | 0 | 151 | 169 | 12 | 121 | 123 | | | | | | | |
| | | | $\hbar=5 k=2$ | | 12 | 124 | 114 | 25 | 61 | 81 | 6 | 203 | 184 | 16 | 31 | 32 | 1 | 33 | 14 | 13 | 114 | 109 | | | | | |
| 0 | 42 | 39 | 13 | 61 | 71 | 27 | 68 | 87 | 7 | 220 | 181 | 17 | 117 | 117 | 2 | 104 | 124 | 14 | 39 | 33 | | | | | | | |
| 1 | 79 | 75 | $\hbar=9 k=2$ | | 28 | 77 | 74 | 9 | 85 | 116 | $\hbar=8 k=3$ | | 3 | 189 | 264 | 15 | 32 | 46 | | | | | | | | | |
| 2 | 391 | 380 | 0 | 192 | 135 | $\hbar=2 k=3$ | | 10 | 206 | 204 | 0 | 56 | 43 | 4 | 99 | 116 | 16 | 108 | 113 | | | | | | | | |
| 3 | 111 | 128 | 1 | 53 | 45 | 0 | 14 | 5 | 11 | 202 | 210 | 1 | 125 | 95 | 5 | 149 | 162 | 17 | 28 | 34 | | | | | | | |
| 4 | 373 | 324 | 2 | 106 | 120 | 1 | 101 | 105 | 12 | 46 | 30 | 3 | 76 | 82 | 6 | 162 | 116 | 18 | 72 | 81 | | | | | | | |
| 7 | 61 | 62 | 4 | 145 | 125 | 2 | 291 | 276 | 13 | 153 | 166 | 5 | 57 | 51 | 7 | 105 | 116 | 19 | 56 | 70 | | | | | | | |
| 8 | 338 | 318 | 6 | 36 | 37 | 3 | 462 | 457 | 14 | 34 | 32 | 6 | 30 | 29 | 7 | 105 | 116 | 20 | 36 | 43 | | | | | | | |
| 10 | 323 | 288 | $\hbar=0 k=3$ | | 4 | 20 | 42 | 15 | 99 | 107 | 7 | 90 | 77 | 8 | 59 | 46 | 22 | 86 | 81 | $\hbar=5 k=4$ | | | | | | | |
| 11 | 91 | 99 | 1 | 172 | 212 | 5 | 429 | 394 | 17 | 56 | 77 | 8 | 52 | 39 | 9 | 200 | 187 | | | | | | | | | | |
| 12 | 57 | 60 | 2 | 240 | 248 | 6 | 102 | 80 | 18 | 50 | 47 | 9 | 76 | 62 | 10 | 223 | 208 | 0 | 92 | 66 | | | | | | | |
| 13 | 69 | 98 | 3 | 154 | 197 | 7 | 202 | 188 | 19 | 86 | 72 | 10 | 97 | 19 | 11 | 89 | 70 | 1 | 198 | 190 | | | | | | | |
| 14 | 259 | 243 | 4 | 83 | 77 | 8 | 161 | 119 | 21 | 68 | 64 | $\hbar=0 k=4$ | | 12 | 186 | 169 | 2 | 52 | 48 | | | | | | | | |
| 15 | 117 | 119 | 5 | 17 | 19 | 9 | 276 | 252 | 23 | 44 | 52 | 0 | 337 | 388 | 13 | 274 | 283 | 3 | 50 | 40 | | | | | | | |
| 17 | 79 | 79 | 6 | 177 | 194 | 10 | 163 | 166 | 25 | 137 | 134 | 2 | 133 | 134 | 14 | 151 | 156 | 4 | 192 | 183 | | | | | | | |
| 18 | 29 | 51 | 7 | 41 | 44 | 11 | 314 | 287 | $\hbar=5 k=3$ | | 3 | 88 | 104 | 15 | 151 | 159 | 5 | 25 | 11 | | | | | | | | |
| 20 | 55 | 69 | 8 | 93 | 69 | 12 | 84 | 80 | 0 | 192 | 201 | 4 | 236 | 285 | 16 | 179 | 186 | 6 | 25 | 43 | | | | | | | |
| 21 | 101 | 95 | 9 | 297 | 279 | 13 | 85 | 85 | 1 | 73 | 77 | 5 | 283 | 314 | 17 | 59 | 67 | 7 | 86 | 93 | | | | | | | |
| 22 | 48 | 55 | 10 | 88 | 95 | 14 | 283 | 258 | 2 | 133 | 118 | 6 | 333 | 346 | 18 | 70 | 82 | 8 | 187 | 182 | | | | | | | |
| 24 | 107 | 120 | 11 | 145 | 153 | 15 | 288 | 285 | 3 | 495 | 605 | 7 | 157 | 174 | 19 | 31 | 42 | 9 | 91 | 83 | | | | | | | |
| 25 | 71 | 54 | 12 | 57 | 65 | 17 | 156 | 144 | 4 | 51 | 93 | 8 | 56 | 52 | 20 | 102 | 123 | 10 | 82 | 68 | | | | | | | |
| | | | $\hbar=6 k=2$ | | 13 | 128 | 139 | 18 | 34 | 40 | 5 | 197 | 207 | 9 | 19 | 4 | 21 | 101 | 110 | 11 | 25 | 1 | | | | | |
| 0 | 336 | 270 | 14 | 338 | 333 | 19 | 59 | 55 | 8 | 193 | 170 | 10 | 279 | 271 | 22 | 131 | 147 | 12 | 57 | 54 | | | | | | | |
| 1 | 80 | 108 | 15 | 394 | 402 | 20 | 100 | 94 | 9 | 210 | 196 | 11 | 120 | 128 | 23 | 34 | 42 | 13 | 99 | 84 | | | | | | | |
| 2 | 195 | 158 | 16 | 125 | 113 | 21 | 138 | 162 | 12 | 96 | 84 | 12 | 274 | 284 | 24 | 21 | 15 | 14 | 141 | 127 | | | | | | | |
| 4 | 371 | 312 | 17 | 188 | 195 | 22 | 35 | 32 | 13 | 54 | 36 | 13 | 306 | 321 | 25 | 10 | 12 | 16 | 51 | 55 | | | | | | | |
| 6 | 283 | 260 | 18 | 100 | 115 | 23 | 144 | 143 | 14 | 54 | 49 | 14 | 40 | 47 | $\hbar=3 k=4$ | | 17 | 41 | 35 | | | | | | | | |
| 8 | 74 | 59 | 19 | 53 | 49 | 25 | 96 | 92 | 15 | 116 | 104 | 16 | 119 | 143 | 0 | 108 | 101 | 18 | 67 | 77 | | | | | | | |
| 9 | 61 | 34 | 20 | 36 | 55 | 26 | 68 | 69 | 16 | 40 | 40 | 17 | 95 | 109 | 1 | 237 | 239 | 19 | 58 | 57 | | | | | | | |
| 10 | 259 | 245 | 21 | 254 | 251 | 27 | 43 | 62 | 17 | 119 | 119 | 18 | 103 | 103 | 2 | 42 | 28 | 20 | 84 | 97 | | | | | | | |
| 12 | 229 | 317 | 22 | 29 | 42 | $\hbar=3 k=3$ | | 18 | 58 | 51 | 19 | 161 | 137 | 3 | 222 | 249 | $\hbar=6 k=4$ | | | | | | | | | | |
| 13 | 83 | 98 | 23 | 168 | 156 | 0 | 54 | 65 | 19 | 101 | 107 | 20 | 60 | 82 | 4 | 280 | 309 | 0 | 121 | 118 | | | | | | | |
| 14 | 53 | 64 | 24 | 93 | 86 | 2 | 189 | 159 | 21 | 26 | 11 | 21 | 35 | 39 | 5 | 161 | 168 | 1 | 28 | 24 | | | | | | | |
| 15 | 43 | 24 | 25 | 43 | 55 | 3 | 309 | 330 | 22 | 57 | 32 | 22 | 121 | 98 | 6 | 46 | 34 | 2 | 79 | 87 | | | | | | | |
| 16 | 260 | 233 | 26 | 85 | 82 | 4 | 63 | 51 | 23 | 87 | 86 | 23 | 141 | 120 | 7 | 135 | 152 | 3 | 151 | 154 | | | | | | | |
| 18 | 86 | 103 | 27 | 42 | 57 | 5 | 42 | 37 | $\hbar=6 k=3$ | | 24 | 26 | 38 | 8 | 99 | 108 | 4 | 71 | 68 | | | | | | | | |
| 20 | 83 | 83 | 28 | 38 | 40 | 6 | 23 | 41 | 1 | 141 | 123 | 25 | 81 | 105 | 9 | 28 | 20 | 5 | 53 | 49 | | | | | | | |
| 22 | 187 | 180 | $\hbar=1 k=3$ | | 7 | 171 | 136 | 2 | 118 | 108 | 26 | 72 | 103 | 10 | 127 | 116 | 6 | 174 | 151 | | | | | | | | |
| | | | $\hbar=7 k=2$ | | 0 | 107 | 54 | 8 | 100 | 102 | 4 | 85 | 91 | $\hbar=1 k=4$ | | 11 | 131 | 144 | 7 | 28 | 11 | | | | | | |
| 0 | 166 | 156 | 1 | 170 | 183 | 9 | 142 | 130 | 5 | 316 | 254 | 0 | 23 | 67 | 12 | 72 | 69 | 8 | 43 | 52 | | | | | | | |
| 1 | 161 | 136 | 2 | 164 | 178 | 10 | 63 | 39 | 7 | 166 | 140 | 1 | 301 | 342 | 13 | 166 | 179 | 9 | 76 | 78 | | | | | | | |
| 2 | 97 | 94 | 3 | 107 | 125 | 11 | 179 | 162 | 9 | 168 | 149 | 2 | 291 | 289 | 14 | 36 | 33 | 19 | 144 | 120 | | | | | | | |
| 3 | 163 | 149 | 4 | 274 | 248 | 12 | 102 | 100 | 10 | 94 | 80 | 4 | 350 | 394 | 15 | 129 | 124 | 11 | 45 | 46 | | | | | | | |
| 4 | 39 | 35 | 5 | 89 | 63 | 13 | 275 | 237 | 13 | 174 | 150 | 7 | 114 | 128 | 19 | 28 | 26 | 14 | 23 | 17 | | | | | | | |
| 5 | 142 | 120 | 6 | 219 | 215 | 15 | 138 | 137 | 14 | 42 | 45 | 8 | 283 | 296 | 20 | 44 | 53 | 15 | 120 | 38 | | | | | | | |
| 6 | 39 | 18 | 7 | 387 | 357 | 16 | 56 | 26 | 15 | 121 | 107 | 9 | 113 | 111 | 21 | 40 | 39 | $\hbar=7 k=4$ | | | | | | | | | |
| 7 | 140 | 123 | 8 | 44 | 52 | 17 | 157 | 164 | 15 | 121 | 107 | 12 | 217 | 210 | 23 | 56 | 76 | 2 | 76 | 59 | | | | | | | |
| 8 | 109 | 91 | 9 | 199 | 173 | 18 | 88 | 80 | 17 | 156 | 164 | 10 | 178 | 158 | 22 | 100 | 97 | 0 | 34 | 38 | | | | | | | |
| 9 | 41 | 31 | 10 | 131 | 135 | 19 | 144 | 154 | 19 | 27 | 21 | 12 | 217 | 210 | 23 | 56 | 76 | 2 | 76 | 59 | | | | | | | |
| 11 | 105 | 101 | 11 | 92 | 88 | 20 | 35 | 36 | $\hbar=7 k=3$ | | 13 | 55 | 54 | 24 | 113 | 141 | 4 | 67 | 83 | | | | | | | | |
| 12 | 151 | 140 | 12 | 188 | 195 | 21 | 61 | 46 | 1 | 63 | 54 | 14 | 150 | 143 | $\hbar=4 k=4$ | | 5 | 46 | 43 | | | | | | | | |
| 13 | 85 | 85 | 13 | 376 | 350 | 22 | 30 | 28 | 3 | 219 | 198 | 15 | 196 | 211 | 0 | 156 | 178 | 8 | 158 | 153 | | | | | | | |
| 14 | 269 | 218 | 14 | 22 | 39 | 23 | 121 | 123 | 4 | 37 | 21 | 16 | 74 | 55 | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | |
|----------------|-----|-----|----------------|-----|-----|----------------|-----|-----|----------------|----------------|-----|----------------|----------------|-----|----------------|----------------|-----|-----|
| 10 | 21 | 0 | -2 | 602 | 584 | -8 | 147 | 98 | -16 | 223 | 245 | <i>h=7 k=1</i> | -9 | 103 | 93 | -4 | 190 | 204 |
| 11 | 77 | 14 | -4 | 206 | 160 | <i>h=1 k=1</i> | -17 | 242 | 237 | -1 | 109 | 121 | -10 | 100 | 88 | -5 | 121 | 125 |
| <i>h=0 k=5</i> | -6 | 755 | 807 | -1 | 590 | 702 | -18 | 136 | 166 | -3 | 189 | 167 | -11 | 33 | 26 | -6 | 68 | 70 |
| 1 | 237 | 270 | -8 | 579 | 547 | -2 | 226 | 213 | -19 | 140 | 165 | -4 | 64 | 81 | -12 | 51 | 33 | |
| 2 | 95 | 97 | -10 | 73 | 50 | -3 | 431 | 430 | -20 | 97 | 104 | -7 | 66 | 78 | -13 | 104 | 106 | |
| 3 | 82 | 110 | -12 | 790 | 778 | -4 | 524 | 641 | -23 | 117 | 170 | -8 | 103 | 97 | -14 | 188 | 206 | |
| 4 | 109 | 120 | -14 | 214 | 205 | -6 | 418 | 390 | -24 | 98 | 139 | -13 | 80 | 89 | -15 | 263 | 275 | |
| 5 | 361 | 438 | -16 | 189 | 196 | -7 | 255 | 235 | -25 | 76 | 85 | -14 | 60 | 54 | -16 | 41 | 21 | |
| 7 | 214 | 240 | -18 | 500 | 461 | -8 | 89 | 93 | -27 | 72 | 107 | -15 | 83 | 53 | -17 | 136 | 143 | |
| 11 | 159 | 199 | -20 | 372 | 288 | -9 | 276 | 291 | -29 | 133 | 156 | -17 | 165 | 166 | -18 | 87 | 110 | |
| 13 | 121 | 138 | -22 | 319 | 233 | -10 | 316 | 315 | <i>h=4 k=1</i> | -18 | 123 | 116 | -19 | 124 | 128 | -18 | 45 | 38 |
| 17 | 120 | 110 | -24 | 230 | 185 | -11 | 118 | 121 | -1 | 358 | 355 | -21 | 63 | 80 | -20 | 247 | 268 | |
| <i>h=1 k=5</i> | -26 | 198 | 139 | -13 | 418 | 454 | -2 | 73 | 94 | <i>h=8 k=1</i> | -21 | 128 | 141 | -20 | 44 | 49 | | |
| 1 | 143 | 173 | -28 | 87 | 92 | -14 | 132 | 132 | -3 | 184 | 432 | -3 | 71 | 50 | -23 | 40 | 53 | |
| 3 | 218 | 237 | <i>h=4 k=0</i> | -15 | 148 | 147 | -4 | 430 | 439 | -5 | 90 | 119 | -24 | 91 | 102 | -23 | 60 | 74 |
| 4 | 188 | 200 | -2 | 310 | 296 | -17 | 195 | 219 | -5 | 254 | 235 | -7 | 80 | 70 | -26 | 161 | 211 | |
| 5 | 101 | 118 | -4 | 745 | 689 | -18 | 67 | 39 | -6 | 80 | 98 | -9 | 117 | 116 | <i>h=3 k=2</i> | <i>h=6 k=2</i> | | |
| 7 | 273 | 287 | -6 | 132 | 98 | -19 | 226 | 244 | -7 | 41 | 44 | -11 | 99 | 97 | -1 | 79 | 36 | |
| 9 | 153 | 169 | -8 | 327 | 270 | -20 | 120 | 125 | -8 | 42 | 40 | -12 | 62 | 47 | -2 | 200 | 176 | |
| 10 | 109 | 122 | -10 | 516 | 501 | -23 | 55 | 72 | -9 | 190 | 197 | -13 | 90 | 78 | -3 | 88 | 92 | |
| 12 | 107 | 125 | -12 | 381 | 314 | -25 | 83 | 113 | -10 | 160 | 153 | -15 | 169 | 164 | -4 | 189 | 149 | |
| 13 | 145 | 176 | -14 | 254 | 213 | -26 | 56 | 60 | -11 | 250 | 225 | <i>h=9 k=1</i> | -5 | 102 | 105 | -7 | 127 | 103 |
| 15 | 142 | 136 | -16 | 365 | 292 | -27 | 81 | 74 | -13 | 67 | 74 | -1 | 215 | 165 | -6 | 34 | 12 | |
| 17 | 67 | 81 | -20 | 202 | 171 | -28 | 55 | 69 | -14 | 125 | 118 | -3 | 113 | 90 | -7 | 38 | 53 | |
| 19 | 214 | 170 | -24 | 76 | 84 | -29 | 140 | 134 | -15 | 365 | 404 | -4 | 93 | 82 | -8 | 97 | 90 | |
| 21 | 70 | 61 | -26 | 262 | 182 | <i>h=2 k=1</i> | -16 | 106 | 95 | -5 | 93 | 64 | -9 | 89 | 67 | -11 | 47 | 46 |
| <i>h=1 k=6</i> | -28 | 47 | 41 | -1 | 619 | 712 | -18 | 67 | 76 | -7 | 164 | 131 | -12 | 139 | 133 | -12 | 64 | 75 |
| 5 | 96 | 101 | <i>h=5 k=0</i> | -2 | 251 | 226 | -19 | 76 | 100 | <i>h=1 k=2</i> | -13 | 39 | 54 | -13 | 59 | 66 | | |
| 6 | 93 | 125 | -2 | 72 | 42 | -3 | 560 | 643 | -21 | 228 | 273 | -1 | 227 | 244 | -14 | 260 | 284 | |
| 8 | 102 | 113 | -4 | 164 | 161 | -4 | 318 | 240 | -25 | 59 | 111 | -2 | 316 | 420 | -15 | 111 | 117 | |
| 9 | 73 | 86 | -6 | 188 | 132 | -5 | 391 | 436 | -27 | 93 | 148 | -3 | 242 | 193 | -16 | 226 | 212 | |
| 12 | 138 | 128 | -8 | 109 | 90 | -6 | 193 | 149 | <i>h=5 k=1</i> | -4 | 174 | 120 | -18 | 124 | 122 | -20 | 98 | 109 |
| 14 | 99 | 102 | -10 | 224 | 174 | -7 | 326 | 319 | -1 | 269 | 242 | -5 | 403 | 368 | -19 | 41 | 48 | |
| 15 | 62 | 50 | -12 | 385 | 310 | -8 | 243 | 212 | -3 | 204 | 196 | -6 | 352 | 276 | -22 | 86 | 121 | |
| <i>h=1 k=0</i> | -16 | 349 | 295 | -9 | 66 | 87 | -4 | 104 | 96 | -7 | 165 | 163 | -23 | 75 | 84 | -1 | 109 | 106 |
| -2 | 537 | 722 | -18 | 379 | 288 | -10 | 278 | 279 | -5 | 254 | 247 | -8 | 141 | 99 | -24 | 151 | 168 | |
| -4 | 309 | 312 | -20 | 101 | 80 | -11 | 342 | 398 | -6 | 144 | 134 | -9 | 29 | 21 | -28 | 132 | 165 | |
| -6 | 117 | 80 | -22 | 227 | 167 | -13 | 41 | 45 | -7 | 237 | 249 | -10 | 74 | 67 | <i>h=4 k=2</i> | -4 | 42 | 31 |
| -8 | 727 | 672 | -24 | 176 | 134 | -14 | 139 | 134 | -8 | 59 | 68 | -11 | 200 | 209 | -1 | 165 | 130 | |
| -10 | 668 | 553 | -26 | 56 | 33 | -15 | 172 | 204 | -9 | 153 | 152 | -12 | 34 | 16 | -2 | 205 | 191 | |
| -12 | 509 | 390 | <i>h=6 k=0</i> | -16 | 128 | 129 | -10 | 50 | 42 | -13 | 139 | 156 | -3 | 178 | 168 | -8 | 210 | 201 |
| -16 | 126 | 59 | -4 | 426 | 351 | -17 | 45 | 54 | -11 | 121 | 127 | -14 | 129 | 119 | -4 | 385 | 390 | |
| -18 | 132 | 126 | -10 | 174 | 124 | -18 | 56 | 70 | -12 | 48 | 29 | -15 | 42 | 59 | -5 | 113 | 99 | |
| -20 | 78 | 81 | -16 | 235 | 150 | -19 | 141 | 144 | -13 | 332 | 358 | -16 | 131 | 123 | -6 | 303 | 313 | |
| -22 | 416 | 300 | -18 | 339 | 239 | -20 | 48 | 41 | -16 | 150 | 157 | -18 | 173 | 180 | -7 | 48 | 40 | |
| -24 | 131 | 118 | -24 | 130 | 117 | -21 | 156 | 180 | -17 | 179 | 212 | -19 | 53 | 51 | -8 | 69 | 73 | |
| -28 | 253 | 213 | <i>h=7 k=0</i> | -25 | 122 | 133 | -18 | 91 | 73 | -20 | 81 | 90 | -9 | 47 | 40 | -18 | 126 | 153 |
| -30 | 110 | 97 | -4 | 85 | 88 | -26 | 78 | 60 | -19 | 95 | 113 | -21 | 70 | 45 | -10 | 242 | 261 | |
| <i>h=2 k=0</i> | -6 | 80 | 77 | -27 | 120 | 152 | -23 | 122 | 169 | -23 | 46 | 55 | -12 | 255 | 270 | -1 | 145 | 121 |
| -2 | 683 | 812 | -8 | 133 | 81 | <i>h=3 k=1</i> | -25 | 58 | 82 | -24 | 97 | 98 | -13 | 82 | 78 | -2 | 67 | 79 |
| -4 | 310 | 304 | -10 | 118 | 97 | -1 | 281 | 279 | -26 | 73 | 81 | -25 | 42 | 20 | -14 | 196 | 203 | |
| -6 | 89 | 19 | -12 | 156 | 124 | -2 | 382 | 337 | <i>h=6 k=1</i> | -27 | 41 | 52 | -15 | 92 | 104 | -6 | 61 | 83 |
| -8 | 429 | 401 | -16 | 324 | 209 | -3 | 109 | 161 | -1 | 242 | 231 | -28 | 103 | 139 | -16 | 136 | 139 | |
| -10 | 509 | 515 | -18 | 115 | 94 | -4 | 172 | 142 | -3 | 104 | 109 | -30 | 42 | 55 | -17 | 90 | 99 | |
| -12 | 420 | 313 | -20 | 55 | 53 | -5 | 358 | 342 | -4 | 140 | 144 | <i>h=2 k=2</i> | -18 | 106 | 112 | -12 | 24 | 40 |
| -14 | 732 | 616 | <i>h=8 k=0</i> | -6 | 149 | 132 | -5 | 208 | 224 | -1 | 199 | 177 | -19 | 96 | 103 | -14 | 159 | 164 |
| -16 | 465 | 368 | -4 | 317 | 231 | -7 | 214 | 190 | -7 | 78 | 55 | -2 | 432 | 361 | -20 | 118 | 114 | |
| -18 | 91 | 100 | -10 | 118 | 74 | -8 | 212 | 207 | -9 | 87 | 97 | -3 | 286 | 218 | -22 | 144 | 175 | |
| -20 | 368 | 319 | -14 | 68 | 57 | -9 | 56 | 100 | -11 | 181 | 178 | -4 | 129 | 91 | <i>h=9 k=2</i> | -2 | 184 | 146 |
| -22 | 110 | 97 | -16 | 195 | 136 | -10 | 248 | 213 | -12 | 93 | 81 | -5 | 101 | 60 | -27 | 35 | 59 | |
| -26 | 267 | 210 | <i>h=9 k=0</i> | -11 | 199 | 212 | -15 | 204 | 238 | -6 | 22 | 19 | <i>h=5 k=2</i> | -4 | 26 | 41 | | |
| -30 | 204 | 155 | -2 | 176 | 118 | -12 | 190 | 188 | -18 | 86 | 84 | -7 | 24 | 10 | -1 | 42 | 31 | |
| <i>h=3 k=0</i> | -6 | 182 | 130 | -13 | 440 | 466 | -21 | 75 | 115 | -8 | 44 | 18 | -2 | 616 | 646 | -8 | 34 | 46 |

| $h=1 k=3$ | -20 | 91 | 108 | -18 | 56 | 73 | -20 | 69 | 66 | -22 | 76 | 100 | -21 | 24 | 26 | $h=6 k=4$ | | |
|-------------|-----------|-----|-----|-----------|-----|-----|-----------|-----|-----|-----------|-----|-----|-----------|-----|-----------|------------|--|--|
| -1 254 256 | -21 | 128 | 140 | -19 | 68 | 65 | -21 | 23 | 67 | -23 | 66 | 73 | -22 | 96 | 134 | -1 52 42 | | |
| -2 196 208 | -23 | 27 | 24 | -20 | 49 | 51 | $h=7 k=3$ | | | -24 | 114 | 131 | -23 | 25 | 44 | -2 38 51 | | |
| -3 122 149 | -24 | 99 | 121 | -21 | 93 | 119 | -1 | 53 | 28 | -25 | 23 | 38 | -24 | 70 | 102 | -3 72 69 | | |
| -4 154 126 | -25 | 96 | 130 | -22 | 45 | 43 | -2 | 186 | 145 | -26 | 55 | 67 | $h=4 k=4$ | | | -4 84 96 | | |
| -5 140 179 | -27 | 38 | 57 | -23 | 24 | 25 | -3 | 188 | 165 | $h=2 k=4$ | | | -1 | 81 | 82 | -6 79 78 | | |
| -6 137 167 | $h=3 k=3$ | | | -24 | 37 | 42 | -5 | 131 | 117 | -1 | 93 | 79 | -2 | 39 | 27 | -10 77 89 | | |
| -7 312 331 | -1 | 191 | 155 | -25 | 56 | 98 | -6 | 61 | 58 | -2 | 22 | 56 | -3 | 26 | 41 | -11 30 51 | | |
| -8 73 87 | -2 | 109 | 87 | $h=5 k=3$ | | | -7 | 162 | 194 | -3 | 107 | 107 | -4 | 191 | 199 | -13 26 54 | | |
| -9 256 222 | -3 | 334 | 313 | -1 | 221 | 195 | -8 | 42 | 31 | -4 | 213 | 238 | -5 | 21 | 33 | -14 66 88 | | |
| -11 104 122 | -4 | 167 | 113 | -2 | 73 | 62 | -9 | 51 | 64 | -5 | 72 | 80 | -6 | 145 | 157 | -16 64 91 | | |
| -12 112 98 | -5 | 189 | 203 | -3 | 489 | 498 | -10 | 91 | 102 | -6 | 178 | 186 | -7 | 35 | 62 | $h=7 k=4$ | | |
| -13 212 196 | -7 | 180 | 168 | -4 | 68 | 62 | -11 | 135 | 151 | -7 | 91 | 89 | -8 | 129 | 132 | -2 72 81 | | |
| -14 54 60 | -8 | 154 | 132 | -5 | 71 | 89 | -13 | 149 | 162 | -8 | 106 | 118 | -9 | 31 | 13 | -3 157 147 | | |
| -15 90 107 | -9 | 135 | 123 | -6 | 71 | 75 | -14 | 91 | 92 | -9 | 64 | 80 | -10 | 183 | 184 | -4 74 63 | | |
| -16 143 145 | -10 | 71 | 79 | -7 | 216 | 223 | -15 | 40 | 51 | -10 | 218 | 241 | -11 | 85 | 89 | $h=8 k=3$ | | |
| -17 72 70 | -13 | 88 | 83 | -8 | 53 | 76 | -16 | 21 | 28 | -11 | 29 | 37 | -13 | 23 | 41 | -5 49 50 | | |
| -18 69 79 | -14 | 136 | 140 | -9 | 244 | 249 | -17 | 80 | 131 | -12 | 37 | 69 | -14 | 131 | 153 | -6 58 63 | | |
| -19 166 168 | -15 | 147 | 172 | -10 | 39 | 62 | $h=9 k=3$ | | | -13 | 52 | 47 | -15 | 37 | 41 | -2 74 94 | | |
| -20 32 43 | -16 | 95 | 125 | -12 | 39 | 43 | -1 | 51 | 66 | -14 | 144 | 165 | -16 | 141 | 167 | -9 47 52 | | |
| -21 143 163 | -17 | 53 | 73 | -13 | 141 | 151 | -2 | 70 | 89 | -15 | 43 | 59 | -17 | 119 | 122 | -10 28 32 | | |
| -22 39 52 | -18 | 99 | 115 | -15 | 93 | 96 | -3 | 146 | 144 | -16 | 147 | 169 | -19 | 73 | 99 | -11 43 53 | | |
| -23 110 150 | -19 | 179 | 200 | -16 | 31 | 28 | -4 | 82 | 69 | -17 | 39 | 53 | -20 | 126 | 184 | -12 19 48 | | |
| -25 64 71 | -20 | 68 | 81 | -17 | 25 | 31 | -5 | 123 | 130 | -18 | 22 | 5 | -21 | 46 | 57 | $h=1 k=5$ | | |
| -26 69 94 | -21 | 174 | 195 | -18 | 32 | 35 | -6 | 41 | 44 | -19 | 26 | 42 | -22 | 70 | 90 | -2 101 106 | | |
| -27 73 96 | -22 | 33 | 54 | -19 | 98 | 134 | -9 | 132 | 140 | -20 | 165 | 200 | $h=5 k=4$ | | | -3 184 210 | | |
| $h=2 k=3$ | | | -23 | 134 | 173 | -22 | 40 | 48 | -11 | 22 | 50 | -21 | 71 | 76 | $h=6 k=3$ | | | |
| -1 300 303 | -25 | 96 | 99 | $h=6 k=3$ | | | $h=1 k=4$ | | | -22 | 105 | 119 | -1 | 38 | 11 | -4 73 112 | | |
| -2 77 94 | -26 | 98 | 128 | -1 | 182 | 169 | -1 | 123 | 137 | -23 | 63 | 76 | -2 | 157 | 141 | -5 116 139 | | |
| -3 207 157 | $h=4 k=3$ | | | -2 | 50 | 71 | -2 | 238 | 252 | -24 | 57 | 67 | -3 | 162 | 163 | -7 149 193 | | |
| -4 14 7 | -1 | 141 | 124 | -3 | 73 | 102 | -3 | 93 | 89 | -25 | 34 | 49 | -4 | 38 | 27 | -25 34 49 | | |
| -5 207 188 | -2 | 241 | 245 | -4 | 120 | 113 | -4 | 249 | 286 | $h=3 k=4$ | | | -5 | 157 | 161 | -12 60 42 | | |
| -6 131 130 | -3 | 115 | 135 | -5 | 214 | 214 | -5 | 78 | 59 | -1 | 44 | 65 | -6 | 134 | 114 | -13 71 121 | | |
| -7 34 34 | -4 | 44 | 53 | -6 | 35 | 30 | -6 | 20 | 2 | -2 | 191 | 211 | -7 | 55 | 78 | -15 60 75 | | |
| -8 123 119 | -5 | 206 | 182 | -7 | 95 | 105 | -7 | 27 | 37 | -3 | 76 | 85 | -8 | 219 | 250 | -17 79 119 | | |
| -9 159 172 | -6 | 131 | 137 | -8 | 43 | 38 | -8 | 224 | 285 | -6 | 195 | 157 | -9 | 104 | 107 | -18 74 95 | | |
| -10 39 32 | -7 | 32 | 46 | -9 | 136 | 143 | -9 | 99 | 90 | -8 | 285 | 358 | -10 | 65 | 99 | -19 53 83 | | |
| -11 24 31 | -8 | 62 | 58 | -11 | 88 | 104 | -10 | 32 | 7 | -9 | 33 | 35 | -11 | 110 | 125 | $h=1 k=6$ | | |
| -12 35 34 | -9 | 286 | 323 | -12 | 55 | 53 | -11 | 100 | 91 | -10 | 144 | 157 | -12 | 86 | 108 | $h=1 k=6$ | | |
| -13 146 132 | -10 | 52 | 64 | -13 | 38 | 50 | -12 | 171 | 161 | -12 | 191 | 212 | -13 | 85 | 93 | -4 79 104 | | |
| -14 137 144 | -11 | 213 | 228 | -14 | 37 | 29 | -14 | 82 | 93 | -14 | 137 | 163 | -14 | 97 | 100 | -5 82 124 | | |
| -15 201 219 | -12 | 90 | 89 | -15 | 89 | 104 | -15 | 228 | 245 | -15 | 31 | 42 | -16 | 44 | 59 | -6 68 115 | | |
| -16 230 222 | -14 | 118 | 132 | -16 | 52 | 65 | -17 | 56 | 49 | -16 | 39 | 57 | -17 | 56 | 67 | -8 109 134 | | |
| -17 83 92 | -15 | 182 | 200 | -17 | 29 | 42 | -18 | 138 | 167 | -18 | 132 | 170 | -18 | 77 | 102 | -12 51 64 | | |
| -18 96 126 | -16 | 63 | 58 | -18 | 27 | 41 | -20 | 59 | 81 | -19 | 104 | 124 | -19 | 37 | 61 | -14 46 76 | | |
| -19 84 89 | -17 | 177 | 178 | -19 | 90 | 111 | -21 | 69 | 79 | -20 | 56 | 89 | -20 | 21 | 39 | -15 43 52 | | |

Description and Discussion of the Structure

Bond lengths and angles. The intramolecular bond lengths and angles are given in Table 3 and Fig. 1.

The benzene ring is slightly distorted from regular hexagon. Ring C-C bond lengths vary from 1.35 to 1.41 Å with the average 1.39 Å which is in agreement with the C-C bond length in crystalline benzene of 1.392±0.010 Å (Cox, Cruickshank & Smith, 1958)¹². It has

been pointed out by many authors, namely, Klug (1970)¹³, Arona & Sundaralingam (1917)¹⁴, Kruger & Gafner (1971)⁴ etc., that there is a tendency of stabilization of p-substituted benzene ring with the distortion from regular hexagonal form. It was found that the internal valence angles (range 117~122°) at the substituted benzene ring show significant deviations from the ideal hexagonal value of 120°.

The C(4)-N(1) bond length is 1.41 Å which

Table 3. Bond lengths and angles in sulfaguanidine monohydrate.

The estimated standard deviations given in parentheses refer to the last decimal positions of respective values

| <i>i</i> | <i>j</i> | $D_{ij}(\text{\AA})$ | <i>i</i> | <i>j</i> | <i>k</i> | $\angle_{ijk}(\text{°})$ |
|----------|----------|----------------------|----------|----------|----------|--------------------------|
| S | C(1) | 1.78(2) | O(1) | S | O(2) | 114.3(7) |
| S | O(1) | 1.43(1) | O(1) | S | C(1) | 106.8(7) |
| S | O(2) | 1.42(1) | O(1) | S | N(2) | 115.2(7) |
| S | N(2) | 1.62(1) | O(2) | S | C(1) | 107.4(8) |
| C(1) | C(2) | 1.36(3) | O(2) | S | N(2) | 105.8(7) |
| C(2) | C(3) | 1.40(3) | C(1) | S | N(2) | 107.0(7) |
| C(3) | C(4) | 1.41(3) | C(2) | C(1) | S | 120(1) |
| C(4) | C(5) | 1.35(3) | C(6) | C(1) | S | 119(1) |
| C(5) | C(6) | 1.39(3) | C(1) | C(2) | C(3) | 119(2) |
| C(6) | C(1) | 1.38(3) | C(2) | C(3) | C(4) | 121(2) |
| C(4) | N(1) | 1.41(3) | C(3) | C(4) | C(5) | 117(2) |
| N(2) | C(7) | 1.32(2) | C(4) | C(5) | C(6) | 122(2) |
| C(7) | N(3) | 1.32(2) | C(5) | C(6) | C(1) | 119(2) |
| C(7) | N(4) | 1.37(2) | C(6) | C(1) | C(2) | 121(2) |
| | | | N(1) | C(4) | C(3) | 120(2) |
| | | | N(1) | C(4) | C(5) | 122(2) |
| | | | S | N(2) | C(7) | 122(1) |
| | | | N(2) | C(7) | N(3) | 125(2) |
| | | | N(2) | C(7) | N(4) | 116(1) |
| | | | N(3) | C(7) | N(4) | 118(2) |

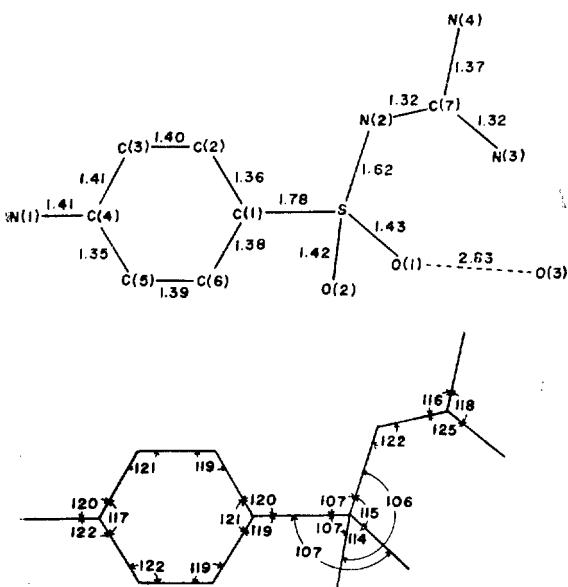


Fig. 1. Bond lengths (\AA) and angles ($^{\circ}$) in sulfaguanidine monohydrate

is shorter than the C—N single bond of 1.47 \AA

(Pauling, 1950)¹⁵.

Bonding around the sulfur atom is distorted from the ideal tetrahedral. The maximum and minimum values for O—S—N are 115° and 106° respectively as in sulfathiazole II⁴. Distortion from the tetrahedral symmetry is the general property of the derivatives of sulfanilamide. Reference to Table 4 shows a comparison of bond lengths and angles around the tetrahedral sulfur atom obtained from the compounds containing sulfonyl group with their average values. The S—C(1) bond length 1.78 \AA is longer than the theoretical S—C(sp^2) value 1.75 \AA calculated from the atomic radii and electronegativities given by Truter (1962)¹⁹. The S—O(1) and S—N(2) bond lengths are in good agreement with the results of the other related compounds. The S—O(2) bond length 1.42 \AA is insignificantly shorter than the S—O

Table 4. A comparison of bond lengths and angles around sulfur atom in sulfaguanidine monohydrate and related compounds.

| Compound | Bond length (Å) | | | Range of angle(°) | |
|--|-----------------|----------|-----------|-------------------|-------------|
| | S—O | S—N(2) | S—C(1) | | |
| Sulfaguanidine monohydrate | 1.42(1) | 1.43(1) | 1.62(1) | 1.78(2) | 105.8~115.2 |
| α -Sulfanilamide ¹ | 1.41 | 1.47 | 1.61 | 1.74 | 105.7~119.0 |
| β -Sulfanilamide ² | 1.448(2) | 1.454(2) | 1.620(2) | 1.750(2) | 105.5~118.2 |
| γ -Sulfanilamide ³ | 1.44(2) | 1.45(1) | 1.67(2) | 1.74(1) | 106.4~117.3 |
| Sulfanilamide monohydrate ¹⁴ | 1.448(9) | 1.463(9) | 1.620(11) | 1.748(12) | 106.0~118.3 |
| Sulfathiazole II ⁴ | 1.435(2) | 1.444(2) | 1.589(3) | 1.759(3) | 104.7~116.6 |
| Sulfathiazole I & III ⁵ | 1.434(10) | 1.440(6) | 1.606(9) | 1.754(9) | 104.8~117.1 |
| Methanesulfonanilide ¹⁷ | 1.425(2) | 1.443(2) | 1.633(2) | 1.746(2) | 105.3~118.6 |
| 2'-Hydroxymethanesulfonanilide ¹³ | 1.435(6) | 1.447(6) | 1.617(6) | 1.736(6) | 106.5~119.2 |
| S,S-Diphenyl-N-p-tolylsulfonyl guanilimine ¹⁸ | 1.430(8) | 1.435(8) | 1.598(8) | 1.756(8) | 104.8~118.1 |
| Average | 1.44 | 1.62 | 1.75 | 109.5 | |

average value 1.44 Å (see Table 4).

In the guanidyl residue the C—N bond lengths range from 1.32 Å in C(7)—N(2) to 1.37 Å in C(7)—N(4), angles from 116° in N(2)—C(7)—N(4) to 125° in N(2)—C(7)—N(3). There is a considerable deviation from the dimensions of free guanidium ion, $[\text{C}(\text{NH}_2)_3]^+$ (Haas, Harris & Mills, 1965)²⁰ of the average values 1.323 Å and 120°. This fact indicates that there is a flexibility in the geometry of guanidyl residue, subjecting to the crystal lattice environment.

By Wheatley's order/length curve for C—N bonds²¹, the C—N bond length of 1.319 Å corresponds to 50 % double bond character. Thus the bond lengths and the good planarity of guanidyl residue (see Table 5) suggest that the guanidyl residue has a delocalized π -electron system.

Planarity and molecular conformation The least-squares planes are listed in Table 5. The benzene ring is planar within the errors of the structure determination. The sulfur atom and the nitrogen atom N(1) are displaced 0.07 and 0.05 Å respectively from the ring plane. The

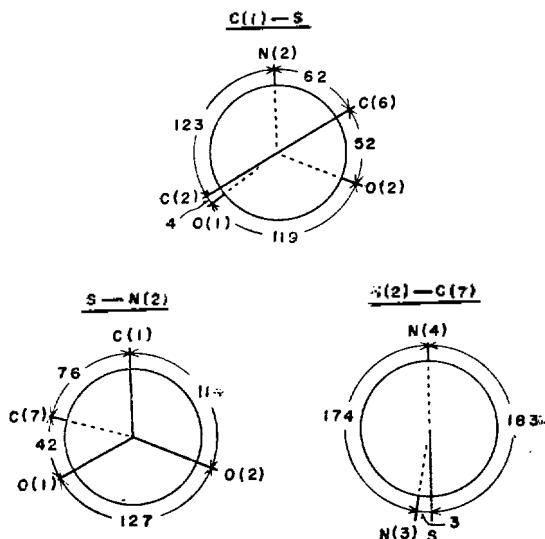


Fig. 2. Newman projection down the C(1)—S, S—N(2) and N(2)—C(7) bonds in sulfaguanidine monohydrate showing the conformation angles in degrees.

small distortion may result from the crystal packing forces. The guanidyl residue is planar within the experimental error and the sulfur atom is displaced -0.18 Å from the guanidyl plane which makes an angle of 96° with the benzene ring plane.

Table 5. Least-squares planes in sulfaguanidine monohydrate.

Equation for plane: $Ax + By + Cz = D$, where x, y, z are in Å

| Atoms in plane | Atoms out of plane | Distance in Å from best plane | Constant |
|----------------------------|--------------------|----------------------------------|------------|
| <i>A. Benzene ring</i> | | | |
| C (1) | | 0.01 | $A=0.857$ |
| C (2) | | 0.00 | $B=0.511$ |
| C (3) | | -0.01 | $C=-0.073$ |
| C (4) | | 0.03 | $D=2.072$ |
| C (5) | | -0.02 | |
| C (6) | | 0.00 | |
| S | | 0.07 | |
| N (1) | | 0.05 | |
| O (1) | | 0.19 | |
| <i>B. Guanidyl residue</i> | | | |
| N (2) | | -0.01 | $A=0.182$ |
| N (3) | | -0.01 | $B=0.018$ |
| N (4) | | -0.01 | $C=0.983$ |
| C (7) | | 0.03 | $D=10.383$ |
| S | | -0.18 | |
| O (1) | | 0.60 | |
| O (2) | | 0.07 | |

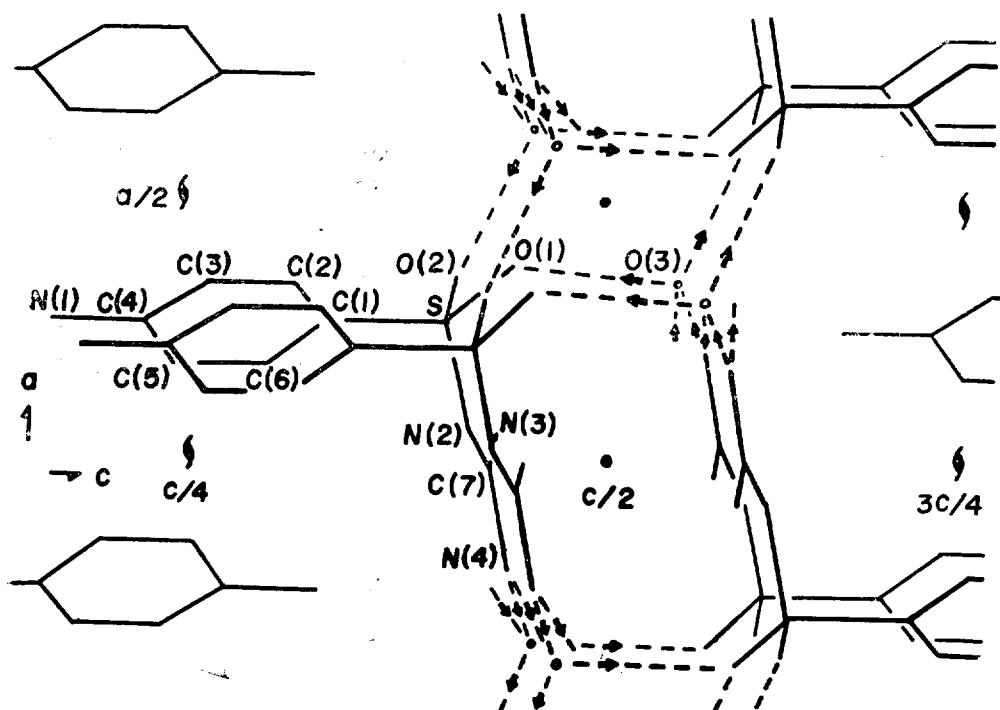


Fig. 3. Projection of the crystal structure of sulfaguanidine monohydrate along the b axis. Dashed lines are hydrogen bonds; arrows indicate donor direction

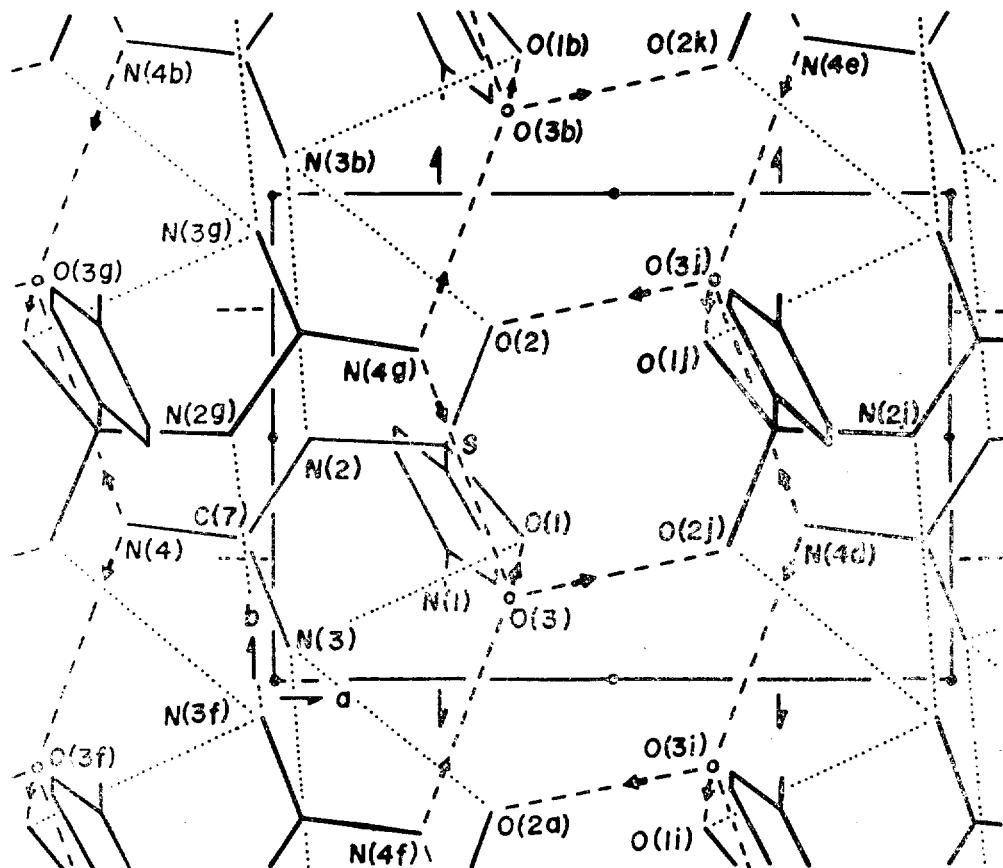


Fig. 4. Projection of the crystal structure of sulfaguanidine monohydrate along the *c* axis. Dashed lines are hydrogen bonds; arrows indicate donor direction. Dotted lines are probable hydrogen bonds.

The conformation angles about the C(1)–S, S–N(2) and N(2)–C(7) bonds are given in Fig. 2. The molecule does not take a symmetrical form. The benzene ring makes a torsional angle of 62° rather than 90° to the S–N(2) bond while in the case of sulfanilamide monohydrate¹⁶ it is 88°.

Hydrogen bonding and crystal packing. The structure of sulfaguanidine monohydrate projected along the *b* and *c* axis is shown in Fig. 3 and Fig. 4. The molecules related by the symmetry centers are joined indirectly by two N–H(guanidyl)…O–H(water)…O(sulfon-

yl) hydrogen bonds. As shown in Fig. 5, the water molecule plays an important role in the hydrogen-bonding scheme by forming a distorted tetrahedral configuration and water oxygen O(3) is involved in two donor O(3)–H…O hydrogen bonds to sulfonyl oxygen O(1) and O(2j) and two acceptor N–H…O(3) hydrogen bonds from N(4f) and N(4g). The close inter- and intramolecular approaches less than 3.5 Å are listed in Table 6. Though the positions of the hydrogen atoms can not be located under the present accuracy it may be possible to suppose the hydrogen location and then consider the possi-

Table 6. Intermolecular distances and angles in sulfaguanidine monohydrate

| <i>i</i> | <i>j</i> | $D_{ij}(\text{\AA})$ | <i>i</i> | <i>j</i> | <i>k</i> | $\angle_{ijk}(\text{^\circ})$ |
|-----------------|----------|----------------------|----------|----------|----------|-------------------------------|
| O(3) | O(2j) | 2.80(2)* | O(1) | O(3) | N(4f) | 115(1) |
| O(3) | O(1) | 2.83(2)* | O(1) | O(3) | N(4g) | 87(1) |
| O(3) | N(4f) | 2.91(2)* | O(1) | O(3) | O(2j) | 108(1) |
| O(3) | N(4g) | 3.00(2)* | O(2j) | O(3) | N(4f) | 115(1) |
| N(3) | O(1) | 2.90** | O(2j) | O(3) | N(4g) | 92(1) |
| N(3) | O(2a) | 2.97** | N(4f) | O(3) | N(4g) | 134(1) |
| N(3) | N(2a) | 3.13** | | | | |
| Symmetry code : | | | | | | |
| O(1) | O(2a) | 3.18 | <i>x</i> | <i>y</i> | <i>z</i> | |
| N(4) | O(1c) | 3.18 | <i>a</i> | <i>x</i> | $-1+y$ | <i>z</i> |
| O(3) | N(3f) | 3.20 | <i>b</i> | <i>x</i> | $1+y$ | <i>z</i> |
| O(3) | N(1h) | 3.21 | <i>c</i> | $-1+x$ | <i>y</i> | <i>z</i> |
| O(1) | O(3i) | 3.40 | <i>d</i> | $1+x$ | <i>y</i> | <i>z</i> |
| O(2) | C(2b) | 3.49 | <i>e</i> | $1+x$ | $1+y$ | <i>z</i> |
| | | | <i>f</i> | $-x$ | $-y$ | $1-z$ |
| | | | <i>g</i> | $-x$ | $1-y$ | $1-z$ |
| | | | <i>h</i> | <i>x</i> | $1/2-y$ | $1/2+z$ |
| | | | <i>i</i> | $1-x$ | $-y$ | $1-z$ |
| | | | <i>j</i> | $1-x$ | $1-y$ | $1-z$ |
| | | | <i>k</i> | $1-x$ | $2-y$ | $1-z$ |

*hydrogen bonds, **probable hydrogen bonds

bilities of forming the hydrogen bonds. Analogy in this way may lead to the conclusion that N(3) can be involved in the three hydrogen bonds, one acceptor N(3)…H—N(2a) (intermolecular), two donor N(3)—H…O(1) (intramolecular) and N(3)—H…O(2a) (intermolecular). These are shown as the dotted lines in Fig. 4. But as there is only one hydrogen atom available to N(3), the latter two donor hydrogen bonds may exist as bifurcated hydrogen bond

in the form of $\text{N}(3)-\text{H}\begin{cases} \text{O}(1) \\ \text{(2a)} \end{cases}$

These hydrogen-bonding networks form infinite molecular layers parallel to (001) plane and the interlayer force appears to be van der Waals in character.

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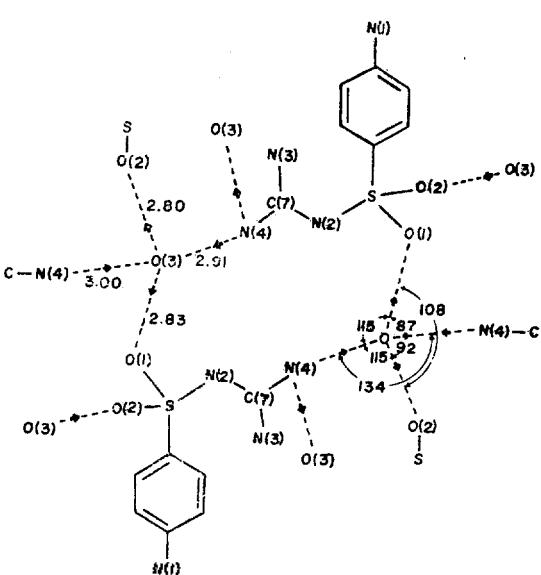


Fig. 5. Environment around water oxygen atom O(3) in sulfaguanidine monohydrate

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