A Study on the Number of Sample Units for Yield Components (I)

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收量構成要素를 爲한 標本數에 對한 研究 (第1報)

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要 約

1967 年 및 1968 年度에 얻은 成績을 利用하여 株當 數穗調査에 必要한 標本數를 計算한 바 他道에 比하여 標本誤差가 큰 江原道와 全羅南道에서 더 많은 標本을 取하여야 하는것으로 생각된다.

收量構成要素를 爲한 標本數는 緯度에 따라 다른 것이 아니라 道內에서의 이들 收量構成要素의 變異性에 따라 左右된다고 보며 5%의 標本을 取함으로서 約 75% 乃至 85%의 相對的 情報를 얻을수 있다고 생각된다.

1. Introduction

In field experiments it is frequently required to estimate the number of samples which should be taken in order to determine some the values of certain population parameters with a specified precision based on appropriate agronomic characters.

Abraham (1966) indicated with a sample size of 5% when the plot size is 28 m² about 60 to 70 percent of the relative information could be obtained. Frey and Rodgers (1961) worked on the optimum

number of heads for spikelet counts in oats, taking the cost into account, and prescribed that the optimum number of samples will vary with year and location, cost ratio and experimental precision desired. In these two studies the sampling units were small units of area taken from experimental plots or the number of panicles of oats from a certain length of sowing bed.

It is common to transplant paddy in hills of 3-5 seedlings each, so that the ultimate sampling unit for measuring average number of panicles per hill would naturally be the hills in a plot. From this agronomic point of view, an attempt has been made, in this paper, to determine, with a specified precision, the number of hills for tiller or panicle count in a plot at different stages of paddy growth.

2. Materials and statistical analysis

a. Materials

Recently a large number of experiments have been carried out in farmers' fields adopting 3×3×3 confounded factorial design in representative soils

in each province. The size of a plot was $27 \,\mathrm{m}^2$ and the spacing $15 \,\mathrm{cm} \times 30 \,\mathrm{cm}$ of between hills and between rows accomodating 416 hills per plot. The agricultural practices remained same as the farmers'. From these experiments four replications have been taken from a soil group for this study at harvsting stage in Kangwon Do, Chungchong Nam Do, Kyongsang Nam Do and Chulla Nam Do in 1967, at maximum tillering stage in Kyonggi Do and Kangwon Do and at ear formation stage in Kyonggi Do, Kangwon Do and Chungchong Nam Do in 1963. From these experiments 12 hills composed of three hills at the end of each of the predetermined rows were taken in 1967 and 4 hills at radonm in 1968 after having discarded the border rows.

b. Statistical analysis

Experience has shown that the distribution of the number of panicles or tillers follows normal distribution, so that the following model may be consid-

a p propriate to express the number of tillers or anicles. Let there be r replicates with t treatments and s samples from each plot. Then, the linear model for the number of tillers or panicles, yijht, may be written as

y_{ijkl} =
$$\mu + \gamma_i + b_{ij} + t_k + e_{ijk} + \eta_{ijkl}$$
Where $\mu = \text{Over all mean}$
 $\gamma_i = \text{The effect of the } i^{th} \text{ replicate}$

$$b_{ij} = \text{Contribution of the } j^{th} \text{ block within}$$
the i^{th} replicate
$$t_k = \text{Effect of the } k^{th} \text{ treatment}$$

$$e_{ijk} = \text{Experimental error}$$

$$\eta_{ijkl} = \text{Sampling error}$$

$$E(e_{ijk}) = 0, E(\eta_{ijkl}) = 0$$

Assuming that the experimental error, e_{ijk} and sampling error, η_{ijkl} are normally and independently distributed with variances σ_{σ}^2 and σ_{s}^2 , respectively, the analysis of variance will be as follows.

Analysis of Variance

source of variation	D.F.	M.S.	Expected M.S.
Replications	r-1		
Blocks within replication	r(b-1)		
Treatments	t-b		
Replications X Treatments	(r-1)(t-b)) Ee	$\sigma_s^2 + s\sigma_e^2$
Sampling Error	rt(s-1) or by subt	Es raction	σs^2
Total	(rts-1)		

Obviously the estimated sampling error term will be Es and true plot error will be (Ee-Es)/s and the variance of a treatment mean when s samples are taken is given by

$$\frac{\sigma e^2}{r} + \frac{\sigma s^2}{rs}$$

and the percentage of plot error will be

$$\frac{\sqrt{\frac{\sigma e^2}{r} + \frac{\sigma s^2}{rs}}}{\sqrt[n]{r}} \times 100$$

Letting P be the specified percentage of error with which the average is to be estimated, the minimum number of samples to be taken are given by

$$S = \frac{\sigma s^2}{\frac{rp^2\bar{y}^2}{100^2} - \sigma_{\theta}} = \frac{\text{(Percentage sampling error)}^2}{\text{rp}^2 - \text{(Percentage true plot error)}^2}$$

Further, the efficiency of s sampling is given in terms of ratio of two variances: Variance for treatment means with s samples and that when the whole plot is taken as sample.

$$E = \frac{\frac{\sigma e^2}{r} + \frac{\sigma s^2}{rN}}{\frac{\sigma e^2}{r} + \frac{\sigma s^2}{rs}}$$

Where $\frac{\sigma_{e^2}}{r} + \frac{\sigma_{s^2}}{rN}$ is the variance

when the whole plot is taken as a sample.

3. Results and discussion

Table 3. Average number of tillers of panicles per plot and percentage of errors obtained from the results.

At maximum tillering stage									
8.6	16.1		-	_					
9.5	20.6	ing.	-	-					
	maximun 8.6 9.5	8.6 16.1	8.6 16.1 —	8.6 16.1					

Percentage of true plot error	9.2	9.3		_							
Efficiency	48.8	47.0	_	—	-						
At ear formation stage											
Mean per sampling unit	17.8	14.0	17.3	-	-						
Percentage of sampling error	18.7	19.8	26.5								
Percentage of true plot error	7.8	9.6	8.2	-							
Efficiency	42.4	46.7	30.4		_						
At harvesting stage											
Mean per sampling unit	-	12.7	15.8	16.7	18.4						
Percentage of sampling error	-	29.4	24.3	23.2	25.2						
Percentage of true plot error		5.7	4.8	3.1	6.4						
Efficiency		54.8	68.0	46.0	63.0						

As given in Table 3, average number of tillers at maximum tillering stage have appeared to be more or less same in Kyonggi Do and Kangwon Do, northern part. At ear formation stage there is no difference between Kyonggi Do and Chungchong-

Nam-Do but much lower number of tillers were observed in Kangwon Do, as compared to the other two provinces and it is decreasing with the stages of growth.

Table 4. Minimum number of hills

Provinces		r = 2			r = 3			r = 4			r =5		
	p=3	p=5	p=10	p=3	p=5	p=10	p=3	p=5	p=10	p=3	p=5	p=10	
			1. 4	At maxi	mum t	illering	stage						
Kyonggi	_	-	4	_	_	2	-	24	2		10	1	
Kangwon	_	_	4	-	_	2		31	2	-	11	2	
			2	. At ea	ır form	ation st	age						
Kyonggi		_	3		22	2	_	9	2	-	6	1	
Kangwon	_		4		-	2	-	19	2	-	9	1	
Chung nam	-		6	-	90	4	-	22	3	_	13	2	
				3.	At ha	rvesting	stage						
Kyonggi		-	_	_	_	-	_	-		_	_	_	
Kangwon	-	49	6	-	21	4	227	13	3	68	10	2	
Chungnam	-	-	5	-	26	3	_	13	2		9	2	
Kyongnam	61	14	3	31	9	2	21	6	2	16	6	2	
Chunnam	-	69	6	-	19	3		11	2	149	8	2	

r: replication

p: percentage of error.

Difference in percentage of sampling error is small being 1.1% in Kangwon Do and Kyonggi Do at the maximum tillering stage and at ear formation stage in Chungchong Nam Do. It is found considerably higher as compared to the other two provinces, while at harvesting stage they are in the following order; Kyongsang Nam Do, Chungchong Nam Do. Chulla Nam Do and Kangwon Do.

Percentages of true plot error at maximum tillering stage in Kyonggi Do and Kyongwon Do, northern part, are in same order, but that at earformation stage is higher in Kangwon Do as compared

to Kyonggi Do and Chungchong Nam Do mean while the percentages of true plot errors at harvesting stage are in same order of percentages of sampling error.

The minimum number of hills obtained accordingly by the help of the formulae above are given in Table 4. Large number of hills should be taken with p 3 and 5 in Kangwon Do and Chulla Nam Do, which seems to be due to considerably high sampling error in those provinces.

In Table 4, the number of hills to be included in the sample for tiller counts were found to be same at maximum tillering stage in Kangwon Do and Kyonggi Do, and were larger in Chungchong Nam Do and Kangwon Do at ear formation and harvesting stages, respectively. At these places the sampling errors were high.

Consequently, the number of samples to be taken are varying at different stages and depend upon the number of replications.

In this paper it has been found that about 2% sampling is necessary for about 50 to 60 percent of efficiency and about 75-85% of efficiency can obtained with 5% sampling, which are higher than what Abraham obtained.

On the basis of true plot error systematic sampling

may be examined whether or not it can be applied not only for estimating the yield components but also for simplification of field work with out disturbing precision.

4. Summary

The necessary number of hills for panicle counts have been obtained, and are more in Kangwon-Do and Chulla Nam-Do where the variability of sampling error is higher as compared to other provinces.

It seems that number of samples do not depend on the latitude but on the variabilities of yield components within the province and it is considered that about 5% sampling fraction gives about 75 to 85% of relative information on the average.

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