# Improved Analytic Crackling Core Model for the Description of UO<sub>2</sub> Sphere and Pellet Oxidation

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### 1. Introduction

The oxidation behavior of  $UO_2$  to  $U_3O_8$  is especially characterized by sigmoid behavior and mainly modeled by nuclear-growth model. Crackling core Model(CCM) proposed by Park and Levenspiel was found to exhibit sigmoid behavior [1] and applied to the modeling of  $UO_2$  oxidation [2]. However, the close description of the experimental data was not achieved. In this study, for the improved description of  $UO_2$  oxidation, we propose an analytic CCM accounting for area expansion effect and evaluate the applicability of the model toward the description of  $UO_2$  sphere and pellet oxidation.

#### 2. Model development

In CCM, the overall conversion is obtained from individual grain conversion by integration

$$1 - X(t) = \frac{\int_0^R [1 - X_g(r, t)] r^2 dr}{\int_0^R r^2 dr} = \frac{3}{R^3} \int_0^R [1 - X_g(r, t)] r^2 dr$$
(1)

where X(t) is overall conversion at give t time and R denotes the initial radius of UO<sub>2</sub> sphere or pellet.  $X_g(r,t)$  refers to the conversion of grain at position r. In this study, UO<sub>2</sub> particle and grain are assumed to follow Shrinking Core Model(SCM) considering reaction rate as rate limiting step. Then the radius of UO<sub>2</sub> particle is related to the following equation

$$-\frac{d}{dt}\left(\frac{4}{3}\pi r^{3}\rho_{B}\right) = 4\pi r^{2}k_{c}C_{A}$$
(2)

where  $\rho_B$  refers to the density of solid and  $k_c$  to reaction constant.  $C_A$  indicates the concentration of gaseous species A in bulk phase. The time required for complete reduction of *r* to zero,  $\tau_c$ , is defined by

$$\tau_c = \frac{\rho_B R}{k_c C_A} \tag{3}$$

Then the radius r is related to time by

$$\frac{r}{R} = Y = 1 - \frac{t_c}{\tau_c} \tag{4}$$

where  $t_c$  denotes the age of solid particle .

In original CCM, the non-porous surface of solid particle is considered to be transformed into porous surface through crackling of surface. This assumption implies that the reactive surface area becomes increased due to the newly formed porosity. In this study, the area expansion effect is included in eq (2) as follows

$$-\frac{d}{dt}\left(\frac{4}{3}\pi r^{3}\rho_{B}\right) = \frac{4\pi r^{2}k_{c}C_{A}}{\left(1-\beta\frac{t}{\tau_{c}^{*}}\right)^{2}}$$
(5)

where  $\beta$  is area expansion coefficient and  $\tau_c^*$  is related to  $\tau_c(1-\beta)$ . Then the radius *r* is newly obtained.

$$Y = \frac{1 - \frac{t_c}{\tau_c^*}}{1 - \beta \frac{t_c}{\tau_c^*}}$$
(6)

As grain reaction follows SCM, the conversion of grain is related to  $t_g$ , grain age, and  $\tau_g$ , the conversion time of grain

$$\frac{t_g(r)}{\tau_g} = 1 - \left[\frac{1 - X_g(r, t)}{1 - X_i}\right]^{1/3}$$
(7)

where  $X_i$  refers to the conversion of intermediate. If w is defined by  $\tau_c/\tau = \tau_c/(\tau_c+\tau_g)$  and  $t_g = t - t_c$ , the overall conversion in three steps is determined. Initiation step :  $t/\tau_c^* < 1-w$ 

$$1 - X(t) = Y_c^3 + 3 \int_{Y_c}^1 [1 - X_g(Y, t)] Y^2 dY$$
 (8)

Propagation step :  $1 - w < t/\tau_c^* < w$ 

$$1 - X(t) = Y_c^3 + 3 \int_{Y_c}^{Y_a} [1 - X_g(Y, t)] Y^2 dY$$
(9)

Termination step :  $w < t/\tau_c^* < 1$ 

$$1 - X(t) = 3 \int_0^{Y_a} [1 - X_g(Y, t)] Y^2 dY$$
 (10)

where  $Y_a$  and  $Y_c$  is defined by

$$Y_{c} = \frac{1 - \frac{t_{c}}{w\tau_{c}^{*}}}{1 - \beta \frac{t_{c}}{w\tau_{c}^{*}}} \qquad Y_{a} = \frac{\frac{1}{w} \left(1 - \frac{t_{c}}{\tau_{c}^{*}}\right)}{1 - \beta - \frac{\beta}{w} \left(\frac{t_{c}}{\tau_{c}^{*}} - 1\right)}$$
(11)

The unreacted conversion in eq (8)-(10) is formulated as follows-

$$1 - X_{g}(Y,t) = \left(1 - X_{i}\right) \left(1 - \frac{1}{1 - w} \left(\frac{t}{\tau} - \left(\frac{1 - Y}{1 - \beta Y}\right)w\right)\right)^{3}$$
(12)

 $X_i$  is assumed to 0.375 implying that UO<sub>2</sub> is oxidized to U<sub>3</sub>O<sub>8</sub> through the conversion to intermediate U<sub>4</sub>O<sub>9</sub>. As demonstrated in Fig. 1 and 2, the proposed model showed a good agreement with experimental conversion data of UO<sub>2</sub> sphere and pellet. The optimized parameters were  $\tau_c^* = 683$ , w =0.5 and  $\beta = 0.92$  for UO<sub>2</sub> sphere and  $\tau_c^* = 383$ , w =0.8 and  $\beta = 0.94$  for UO<sub>2</sub> pellet. The high value of  $\beta$ indicates that area expansion was significantly proceeded in the oxidation of both sphere and pellet.

#### 3. Conclusions

In spite of its simplicity formulation, the improved CCM accounting for area expansion effect was found to closely describe the experimental behavior of  $UO_2$  oxidation behavior. The overall performance of the model will be evaluated by correlating more experimental data.

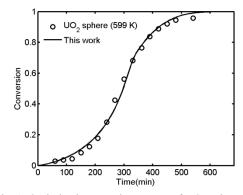


Fig. 1. Optimized conversion curves of UO<sub>2</sub> sphere in air atmosphere at 599 K.

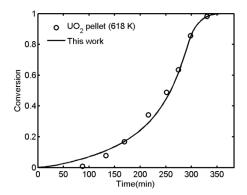


Fig. 2. Optimized conversion curves of UO<sub>2</sub> pellet in air atmosphere at 618 K.

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