## Modeling of the Thermal Conductivity of Mo-ZrO<sub>2</sub> Composites for Inert Matrix Fuel

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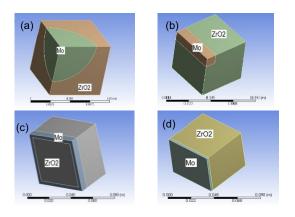
# 1. Introduction

Inert matrix fuel (IMF), in which the TRUs including Pu and minor actinides (MAs) are dispersed in a neutron transparent matrix, is one of the concepts developed for the management of radioactive spent fuel [1]. ZrO<sub>2</sub> is one of the candidate materials for the matrix of IMF owing to high melting point, low neutron absorption cross section, and good chemical and irradiation stability [2]. However, it has a low thermal conductivity that reduces its performance. The fabrication of Mo reinforced ZrO<sub>2</sub> composites with a low volume fraction of the reinforcement has been recently demonstrated and the effect of the reinforcement microstructure on the thermal conductivity of ZrO<sub>2</sub> has been measured [3]. The objective of this paper to investigate the effect of reinforcement microstructure on the thermal conductivity of ZrO<sub>2</sub> matrix using finite element method (FEM) and analytical modeling and to benchmark the theoretically predicted results with the experimentally measured ones.

#### 2. Thermal conductivity modeling

#### 2.1 Finite element method

Solid models of Mo-ZrO<sub>2</sub> composites with different structures were developed as shown in Fig. 1.



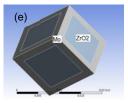


Fig. 1. Solid models of (a) Mo particle- (b) Mo fiber- (c) Mo mesh- (d) Mo sheet-, and (e) 3D interconnected Mo-ZrO<sub>2</sub> composites.

The thermal conductivities of Mo-ZrO<sub>2</sub> composites as function of temperature were calculated using the following equation:

$$K_{eff} = \frac{Q \times L}{A \times \Delta T}$$
(1)

where Q is the applied heat flux, L is the length along which the heat flows, A is the cross-sectional area, and  $\Delta T$  is the temperature difference between the two surfaces. The thermal conductivity was calculated by applying a constant heat flux at one surface and a constant temperature at the opposite surface.

## 2.2 Analytical modeling

Maxwell model [4] is one of the earliest models that have been developed based on the effective medium theory. The Maxwell model was developed for composites with dilute concentration of uniformly distributed spherical particles (Eq. 2):

$$K_{eff} = K_{m} \frac{(2 - 2V_{r})K_{m} + (1 + 2V_{r})K_{r}}{(2 + V_{r})K_{m} + (1 - V_{r})K_{r}}$$
(2)

where K<sub>r</sub>, K<sub>m</sub>, and K<sub>eff</sub> are the thermal conductivities of the reinforcement, matrix, and composite, respectively, and  $V_r$  is the volume fraction of the reinforcement.

#### 3. Results and discussions

FEM modeling of the thermal conductivity of Mo

fiber, mesh, sheet- $ZrO_2$  composites when the heat flux was applied parallel and perpendicular to the direction of the reinforcement is shown in Fig. 2 together with the Maxwell model predictions. When the heat flux was applied parallel to the direction of the reinforcement, the thermal conductivity increased from fiber, mesh, to sheet microstructure due to the increased degree of high thermal conductivity reinforcement. When the heat flux was perpendicular to the direction of the reinforcement, the thermal conductivity of the reinforced  $ZrO_2$  composites from mesh, fiber, to sheet due to the increased density of the reinforcement matrix interfaces.

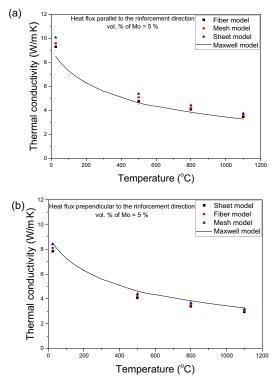


Fig. 2. FEM predicted thermal conductivity of Mo-ZrO<sub>2</sub> composites with different reinforcement structures and Maxwell model predictions.

Fig. 3 Shows a comparison between the experimentally measured thermal conductivity of Mo-ZrO<sub>2</sub> composited with dispersed particle and randomly distributed Mo wire mesh structures with the FEM and Maxwell model predictions. The thermal conductivity of Mo powder-ZrO<sub>2</sub> composites were corrected for the experimentally measured porosity of 99.0% using the modified Maxwell-Eucken correlation [5]. In general, the theoretically predicted thermal conductivity values are in good agreement with the experimentally measured ones.

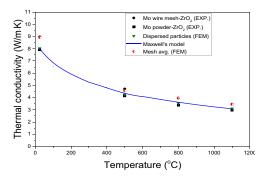


Fig. 3. Comparison between the theoretical predictions and the experimental measurements of Mo-ZrO<sub>2</sub> composites.

#### 4. Conclusion

The FEM modeling of the thermal conductivity of Mo-ZrO<sub>2</sub> composites showed that with increasing the interconnectivity of the reinforcement structure, the thermal conductivity significantly improved due to the higher degree of interconnectivity of high thermal conductivity pathways and the reduced intensity of reinforcement/matrix interfaces. The theoretically predicted thermal conductivities of Mo-ZrO<sub>2</sub> composites were compared with the experimentally results and a good agreement was found.

## Acknowledgments

This study was supported by the KUSTAR-KAIST institute at KAIST

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