# Covariance-based Recognition Using Machine Learning Model

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Abstract—We propose an on-line machine learning approach for object recognition, where new images are continuously added and the recognition decision is made without delay. Random forest (RF) classifier has been extensively used as a generative model for classification and regression applications. We extend this technique for the task of building incremental componentbased detector. First we employ object descriptor model based on bag of covariance matrices, to represent an object region then run our on-line RF learner to select object descriptors and to learn an object classifier. Experiments of the object recognition are provided to verify the effectiveness of the proposed approach. Results demonstrate that the propose model yields in object recognition performance comparable to the benchmark standard RF, AdaBoost, and SVM classifiers.

*Index Terms*—Random forests (RFs), object recognition, Histograms, covariance descriptor

## I. INTRODUCTION

Object recognition is one of the core problems in computer vision, and it turns out to be extremely difficult for reproducing in artificial devices, simulated or real. Specifically, an object recognition system must be able to detect the presence or absence of an object, under different illuminations, scales, pose, and under differing amounts of background clutter. In addition, the computational complexity is required to be kept minimum, in order for those algorithms to be applicable for real-life applications. Based on "strongly supervised" approach and "weakly supervised" method (without using any ground truth information or bounding box during the training), considerable progress has been made for detection of objects. Several studies also have shown that supervised componentbased approach is more robust to natural pose variations, than the traditional global holistic approach. However, supervised learning is usually carried out batch on the entire training set, often is not optimal in a dynamic recognition tasks. In this paper we consider instead how machine learning models for object recognition categories, can be build 'incrementally' or 'on-line' so that new images are continuously added and the recognition decision is made without delay. The process consists of two stages. First we employ object descriptor model based on bag of covariance matrices, to represent an image window then run our on-line random forest (RF) learning algorithm [5]. RF technique has been extend in this paper for the task of building incremental component-based detector, for attacking the problem of recognizing generic categories, such as bikes, cars or persons purely from object descriptors that combines histograms and appearance model. The rest of the paper is organized as follow. We briefly give an overview of the

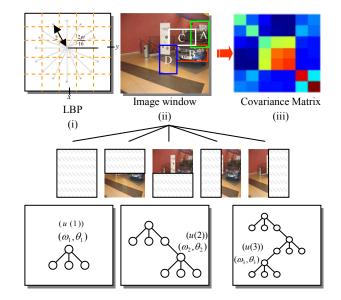


Fig. 1. (i) Points sampled to calculate the LBP around a point (x, y). (ii) Rectangles are examples of possible regions for histogram features. Stable appearance in Rectangles A, B and C are good candidates for a car classifier while regions D is not. (iii) Any region can be represented by A covariance matrix representation of object. Second row shows an object represented with five covariance matrices. The third row, an example of forest structure for a given object. Each node of the tree corresponds to a separator and the leaves correspond to a given object class. In our example, it can be seen that the tree adapts the decision at each intermediate node (nonterminal) from the response of the leaf nodes, which characterized by a vector  $(w_i, C_i)$  with  $||w_i|| = 1$ .

object descriptors in Section II. Then in Section III we describe our on-line RF. Section IV highlight on object recognition using our proposed approach. A description of datasets and experimental evaluation procedure is given in Section V. The paper concludes with experimental results and brief discussion in Section VI.

## **II. OBJECT DESCRIPTORS**

A variety of exiting representations to object recognition, range from aggregated statistics to appearance models, have been extensively used in computer vision literature. Histograms are among the most popular representations [7]–[12]. Histograms of Local Binary Patterns <sup>1</sup> (LBPs), although are most commonly used for recognizing textures, they are also

<sup>&</sup>lt;sup>1</sup>A LBP is a description of the intensity variation around the neighborhood of a particular point in the grey-scale (intensity) version of an image.

useful for capturing image statistics falling in an image region. In similar popularity the well known Scale invariant feature transform (SIFT) descriptor [9] and Shape Context [7] use position-dependent histograms of Gaussian weighted gradient orientations around scale invariant interest points. However, histograms require a finite neighborhood which limits the spatial resolution of features. Appearance models, on the other hand, are highly sensitive to noise and shape distortions. While many region-based descriptors were designed to achieve invariance to local geometric transformation, these descriptors are based on heuristic functions, they do not adapt to a changing situations.

## A. Our Approach

To overcome the above mentioned shortcomings in object descriptors, we have used bag of covariance<sup>2</sup> matrices, to represent an object region. Let I be an input color image. Let F be the dimensional feature image extracted from I

$$F(x,y) = \phi(I,x,y) \tag{1}$$

where the function  $\phi$  can be any feature maps (such as intensity, color, etc). For a given region  $R \subset F$ , let  $\{z_k\}_{k=1\dots n}$  be the *d* dimensional feature points inside *R*. We represent the region *R* with the  $d \times d$  covariance matrix  $C_R$  of feature points.

$$C_R = \frac{1}{n-1} \sum_{k=1}^n (z_k - \mu) (z_k - \mu)^T$$
(2)

where  $\mu$  is the mean of the point. Fig. 1 (i) depicts the points that must be sampled around a particular point (x, y) in order to calculate the LBP at (x, y). In our implementation, each sample point lies at a distance of 2 pixels from (x, y), instead of the traditional  $3 \times 3$  rectangular neighborhood, we sample neighborhood circularly with two different radii (1 and 3). The resulting operators are denoted by  $LBP_{8,1}$  and  $LBP_{8,1+8,3}$ , where subscripts tell the number of samples and the neighborhood radii. In Fig. 1 (ii), different regions of an object may have different descriptive power and hence, difference impact on the learning and recognition.

## B. Labeling the Image

We gradually build our knowledge of the image, from features to covariance matrix to a bag of covariance matrices. Our first step is to model each covariance matrix as a set of image features. Next, we group covariance matrices that are likely to share common label into a bag of covariance matrices. We follow [17] and represent an image objects with five covariance matrices  $C_{i=1...5}$  of the feature computed inside the object region, as shown in the second row of Fig.1. A bag of covariance which is necessary a combination of Ohta color space histogram ( $I_1 = R + G + B/3$ ,  $I_2 = R - B$ ,  $I_3 = (2G - R - B)/2$ ), LBP and appearance model of different features of an image window is presented in Fig.1 (iii). Then estimate the bag of covariance matrix likelihoods and the likelihood that each bag of covariance matrices is homogeneously

<sup>2</sup>Basically, covariance is a measure of how much two variables vary together.

labeled. We use this representation to automatically detect any target in images. We then apply on-line RF learner to select object descriptors and to learn an object classifier, as cab be seen in the last row of Fig.1.

#### **III. RANDOM FORESTS**

## A. RF Fundamentals

Details discussion of Breiman's random forest (RF) [1] learning algorithm is beyond the scope of this paper, however, in order to simplify the further discussion, we will need to define some fundamental terms:

**Random Forests.** Briefly, it is an ensemble of two sources of randomness to generate base decision trees; bootstrap replication of instances for each tree and sampling a random subset of features at each node. It is also enable different cues (such as appearance and shape) to be combined [14].

Feature importance estimation. RF measures feature importance by randomly permuting the values of the feature f for the out-of-bag<sup>3</sup> (OOB) cases for tree k, if feature f is important in the object detection, then the accuracy of the prediction should decrease. On the other hand, we can consider the accumulated reduction at nodes according to the criteria used at the splits, an idea from the original CART [2] formulation. Feature importance measures can be used to perform object descriptors selection.

**Decision tree.** For the k-th tree, a random vector  $C_k$  is generated, independent of the past random vectors  $C_1, \ldots, C_{k-1}$ , and a tree is grown using the training set of positive and negative image I and covariance feature  $C_k$ . The decision generated by a decision tree corresponds to a covariance feature selected by learning algorithm. Each tree casts a unit vote for a single matrix from the bag of covariance matrices. **Base classifier.** Given a set of M decision trees, a base classifier selects exactly one decision tree classifier from this set, resulting in a classifier  $h(I, C_k)$ .

**Forest** Given a set of N base classifiers, a forest is computed as ensemble of these tree-generated base classifiers  $h(I, C_k)$ , k = 1, ..., n. Finally, a forest detector is computed as a majority vote.

**Majority vote.** For M decision trees, the majority voting method will give a correct decision if at least floor(M/2) + 1 decision trees gives correct outputs. If each tree has probability p to make a correct decision, then the forest will have the following probability P to make a correction decision.

$$P = \sum_{i=\text{floor}(M/2)+1}^{b} \binom{M}{i} p(1-p)$$
(3)

## B. On-line Learning Random forest (RF)

To obtain an on-line algorithm, each of the steps described above must be on-line, where the current classifier is updated whenever a new sample arrives. In particular on-line RF [5]

<sup>&</sup>lt;sup>3</sup>There is on average  $I/e \approx 36.8$  of instances not taking part in construction of the tree, provides a good estimate of the generalization error.

## Algorithm 1 On-line Random Forests

- 1: Input: training set T, integer N (No. of bootstrap)
- 2: Use all available sample so far d to learn feature descriptors.
- 3: Estimate the importance of feature incrementally.
- 4: *Restrict* d to the relevant features.
- 5: Train RF based on the restricted data d as follows.
- 6: Initially select the number K of trees to be generated.
- 7: for  $k = 1, 2, \cdots, K$  do
- 8: T bootstrap sample from T initialize  $e = 0, t = 0, T_k = \phi$
- 9: **Do until**  $T_k = N_k$
- 10: Vector  $C_k$  that represent a bag of covariance is generate
- 11: Construct Tree  $h(I, C_k)$  using any decision tree algorithm
- 12: Each Tree makes its estimation based on a single matrix from the bag of covariance matrices at *I*.
- 13: Each Tree casts a vote for most popular covariance matrix at *I*
- 14: The popular covariance matrix at I at is predicted by selecting the matrix with max votes over  $h_1, h_2, \ldots, h_k$
- 15:  $= \arg \max_{y} \sum_{k=1}^{K} I(h_k(x) = y)$
- 16: Return a hypothesis  $h_l$
- 17: end for
- 18: Get the next sample set (x, y) in  $\hat{T}t \leftarrow t + 1$  t (is the number of sample sets examined in the process)
- 19: **Output:** Proximity measure, feature importance, a hypothesis *h*.

(see Algorithm.1) works as follows: First, the fixed set tree K is initialized. In contrast to off-line random forests, where the root node always represents the object class in on-line mode, for each training sample, the tree adapts the decision at each intermediate node (nonterminal) from the response of the leaf nodes, which characterized by a vector  $(w_i, C_i)$  with  $||w_i|| = 1$ . Root node numbered as 1, the activation of two child nodes 2i and 2i + 1 of node i is given as

$$u_{2i} = u_i f(w_i I + C_i)$$
(4)

$$u_{2i+1} = u_i f(-w_i' I + C_i)$$
(5)

where I is the input image,  $u_i$  represents the activation of node i, and f(.) is chosen as a sigmoidal function. Consider a sigmoidal activation function f(.), the sum of the activation of all leaf nodes is always unity provided that the root node has unit activation. The forest consist of fully grown trees of a certain depth l. The general performance of the on-line forests depends on the depth of the tree. However, we found that the number of trees one needs for good performance eventually tails off as new data vectors are considered. Since after a certain depth, the performance of on-line forest does not vary to a great extent, the user may choose K (the number of trees in forest) to be some fixed value or may allow it to grow up to the maximum possible which is at most  $|T|/N_k$ , where  $N_k$ 

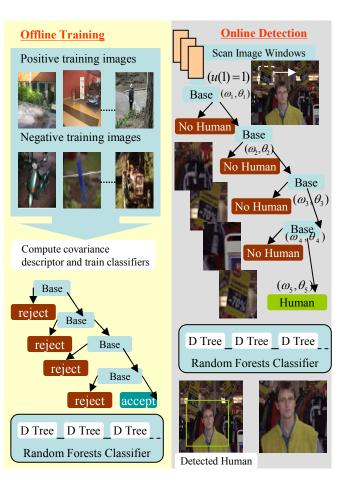


Fig. 2. A classifier is trained with positive (contains the object relevant to the class) and negative (does not contain the object) examples. Each decision tree makes its estimation based on a single matrix from the bag of covariance matrices.

the tree size chosen by the user. Next, when detecting a new instance, we first estimate the average margin of the trees on the instances most similar to the new instance and then, after discarding the trees with negative margin, weight the tree's votes with the margin. Then the set of classifiers is updated. For updating, any on-line learning algorithm may be used, but we employ a standard Karman filtering technique [6] to estimate the distribution of positive and negative samples similar way as we do in the off-line case.

#### IV. OBJECT RECOGNITION

Given a feature set and a sample set of positive (contains the object relevant to the class) and negative (does not contain the object) images, to detect a specific object, e.g. human, in a given image, the main difficulty is to train a classifier with relevant features toward accurate object recognition. The adoption of RF learner and its ability to measure feature importance relief us from this challenge. We train a random forests learner (detector) offline using covariance descriptors of positive and negative samples as shown in Fig. 2 (left column). We start by evaluation feature from input image I



Fig. 3. Examples from GRAZ02 dataset [3] for four different categories: bikes (1st pair), people (2nd pair), cars (3rd pair), and background (4th pair).

TABLE I NUMBER OF IMAGES AND OBJECTS IN EACH CLASS IN THE GRAZ02 DATASET

Dataset	Images	Objects
Bikes	373	511
Cars	420	770
Persons	460	785
Total	1253	2066

after the detector is scanned over it at multiple locations and scales. This has to be done for each object. Then for feature in I, we want to find corresponding covariance matrix for estimating a decision tree. Each decision tree learner may explore any feature f, we keep continuously accepting or rejecting potential covariance matrices. We then apply the on-line random forests at each candidate image window to determine whether the window depicts the target object or not as shown in Fig. 2 (right column). The on-line RF detector was defined as a 2 stage problem, with 2 possible outputs in each stage: In the first one, we build a detector that can decide if the image contains an object, and thus must be recognized, or if the image does not contain objects, and can be discarded, saving processing time. In the second stage, based on selected features the detector must decide which object descriptor should be used. There are two parameters controlling the learning recognition process: The depth of the tree, and the least node. It is not clear how to select the depth of the on-line forests. One alternative is to create a growing on-line forests where we first start with an on-line forest of depth one. Once it converges to a local optimum, we increase the depth. Thus, we create our on-line forest by iteratively increasing its depth.

## V. EXPERIMENTS AND EVALUATION

To evaluate and validate our approach, we designed our experiments in a way that we can answer the following questions:

- How does the performance of incrementally learning RF compare to one trained batch on the entire training set?
- 2) Does the recognition performance improve it uses covariance matrices rather than adapting Histograms?

# A. Dataset

To investigate the above questions we used data derived from the GRAZ02<sup>4</sup> dataset [3], a collection of  $640 \times 480$  24-

bit color images, run it against three state of the art classifiers (offline RF, AdaBoost, and SVM (a single threshold network)). As can be seen in Table I, GRAZ02 dataset has three object classes, bikes (373 images), cars (420 images) and persons (460 images), and a background class (270 images). Figure 3 illustrates the variability of this database with respect to scale and clutter. Objects of interest are often occluded, and they are not dominant in the image. According to [15] the average ratio of object size to image size counted in number of pixels is 0.22 for bikes, 0.17 for people, and 0.9 for cars. Obviously this dataset is more complex to learn detectors from, but of more interest because it better reflects the real world complexity.

## B. Experimental settings

For testing our framework we used the datasets described above and run it against three state of the art classifiers (offline RF, AdaBoost, and SVM). Each of the classifiers used in our experimentation were trained with varying amounts (10%, 50%)and 90% respectively) of randomly selected training data. All image not selected for the training split were put into the test split. For the 10% training data experiments, 10% of the image were selected randomly with the remainder used for testing. This was repeated 20 times. For the 50% training data experiments, stratified 5x2 fold cross validation was used. Each cross validation selected 50% of the dataset for training and tested the classifiers on the remaining 50%; the test and training sets were then exchanged and the classifiers retrained and retested. This process was repeated 5 times. Finally, for the 90% training data situation, stratified 1x10 fold cross validation was performed, with the dataset divided into ten randomly selected, equally sized subsets, with each subset being used in turn for testing after the classifiers were trained on the remaining nine subsets. For offline random forests, we train detectors for bikes, cars and persons on 100 positive and 100 negative images (of which 50 are drawn from the other object class and 50 from the background), and test on a similarly distributed set.

#### VI. EXPERIMENTAL RESULTS

GRAZ02 images contain only one object category per image so the recognition task can be seen as a binary classification problem: bikes vs. background, people vs. background, and car vs. background. The well known statistic measure; the Area Under the ROC Curve (AUC) is used to measure the classifiers performance in these object recognition experiments. The AUC is a measure of classifier performance that is

<sup>&</sup>lt;sup>4</sup>available at *htt://www.emt.tugraz.at/pinz/data/* 

TABLE II MEAN AUC PERFORMANCE OF FOUR CLASSIFIERS ON THE BIKES VS. BACKGROUND DATASET, BY AMOUNT OF TRAINING DATA. PERFORMANCE OF ON-LINE RF IS REPORTED FOR DIFFERENT DEPTHS

	On	On-line RF with different depth (Dth)						AdaB	SVM
	Dth=	:3 D	th=4	Dth=5	Dth=6	Dth=7	RF		
109	6 0.85	5 0	).86	0.81	0.85	0.85	0.86	0.81	0.82
50%	6 0.91	1 (	).90	0.89	0.91	0.92	0.90	0.89	0.90
90%	6 0.92	2 0	).90	0.91	0.92	0. 92	0.91	0.90	0.91

independent of the threshold: it summarizes not the accuracy, but how the true positive and false positive rate change as the threshold gradually increases from 0.0 to 1.0. An ideal, perfect, classifier has an AUC value 1.0 while a random classifier has an AUC of 0.5.

## A. Mean AUC Performance

Tables II, III, and IV give the mean AUC values across all runs to 2 decimal places for each of the classifier and training data amount combinations, for the bikes, cars ad people datasets respectively. For on-line RF we report the results for different depths of the tree. As can be seen, our algorithm always performs significantly better than the offline RF. We found that the differences in performance are (avg.  $= 1.2 \pm 15\%$ ), while our approach has achieved a number of desirable properties: (1) it is incremental, in a sense that we are able to add new categories incrementally making use of already acquired knowledge, the model will continuously improve by exploring more features and training data. If the process is running for a long time, a lot of features are processed and evaluated but still only a small number of features are sufficient for updating. (2) it is adaptable, in a sense that the selection of features and also the learning (we do not freeze the learning) can change over time. Note that this kind of adaptation is not possible in the standard random forests and the other batch learning classifiers. The improvement when we varying the tree depth are relatively small. This makes intuitive sense: when an image is characterized by high geometric variability, it is difficult to find useful global features.

# B. A bag of covariance vs. Histograms

Another objective of the experiments was to determine whether a bag of covariance matrices can improve the recognition performance of histogram methods. Covariance features are faster than the histogram since the dimensionality of the space is smaller. The search time of an object in 24-bit color image with size  $640 \times 480$  24-bit color image is 8.5 with C++ implementation which yield near real time performance. We noted that the standard deviation varies between  $\pm 2.0 \pm 3.2$ , which is considered quite high. The reason is the images in the dataset vary greatly in their level of difficulty, so the performance for any single run is dependent on the composition of the training set.

## VII. CONCLUSIONS

In this paper we have presented an on-line learning framework for object recognition categories that avoids hand labeling of training data. We have demonstrated that on-line

TABLE III MEAN AUC PERFORMANCE OF FOUR CLASSIFIERS ON THE CARS VS. BACKGROUND DATASET, BY AMOUNT OF TRAINING DATA. PERFORMANCE OF ON-LINE RF IS REPORTED FOR DIFFERENT DEPTHS

	On-lir	ne RF wi	Offline	AdaB	SVM			
	Dth=3	Dth=4	Dth=5	Dth=6	Dth=7	RF		
10%	0.77	0.79	0.75	0.78	0.73	0.79	0.75	0.73
50%	0.85	0.84	0.82	0.82	0.84	0.85	0.82	0.80
90%	0.86	0.82	0.83	0.85	0.86	0.85	0.83	0.82

TABLE IV MEAN AUC PERFORMANCE OF FOUR CLASSIFIERS ON THE PERSONS VS. BACKGROUND DATASET, BY AMOUNT OF TRAINING DATA. PERFORMANCE OF ON-LINE RF IS REPORTED FOR DIFFERENT DEPTHS

	On-lir	e RF wi	Offline	AdaB	SVM			
	Dth=3	Dth=4	Dth=5	Dth=6	Dth=7	RF		
10%	0.84	0.84	0.83	0.80	0.83	0.84	0.77	0.80
50%	0.88	0.86	0.88	0.88	0.88	0.88	0.84	0.86
90%	0.90	0.86	0.89	0.90	0.90	0.90	0.86	0.89

learning obtain comparable results to offline learning. Moreover, the proposed framework is quite general (i.e, it can be used to learn completely different objects) and can be extended in several ways. Although we assess the problem of producing accurate object recognition in images, without giving any prior information on object identities, orientation, positions and scales, but we still far behind than proposing a multi-general vision task algorithm but our hope is to design a simple algorithm for learning appropriate context for object recognition tasks in similar hierarchical and parallel processing of human brain.

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