

**EUTROPHIC WATER BODY**

T. YUAN, J. C. LI and J. F. ZHOU, *Institute of Mechanics, CAS, China*, In eutrophic waters, phytoplankton or unicellular microalgae can grow rapidly to very high concentrations under favorable environmental conditions, occasionally resulting in harmful algal blooms. This kind of extreme environmental events have been worsening marine ecosystems and causing great economic loss. A dynamic eutrophication model is described to simulate algal growth and nutrient cycling during algal blooming in the present paper. It involves crucial influential factors including water temperature, nutrient supply and light density. Moreover, it takes non-predatory mortality, endogenous respiration and settling into consideration as controlling factors for alga decay. We have endeavored to elucidate the influence of some of these factors on algal blooming including temperature and the two crucial nutrient factors (P, N) by numerical results. In addition, nonlinear qualitative analysis is used to study the mechanism of the algal blooms occurrence. To begin with, we only focus on the examination of the most important nutrient element, phosphorus (P) effect. Based on numerical simulations, the threshold of phosphorus at different temperature may be delineated by the 3D isoquant contours of algal growth rate. It is apparently seen that the larger the phosphorus concentration, and the higher the water temperature, the greater the algal growth rate is, which may explain why alga blooming disasters are prone to occur in polluted water body in a fine summer day. Furthermore, the threshold is reduced when half-saturation constant  $K_{MP}$ , a parameter to indicate algae ability to digest nutrient, decreases. The result means that such kind of algae with smaller half-saturation constant grows faster and very probably becomes overwhelming species during algae blooms. The analysis on the phase plot clearly exhibits nonlinear behavior of the system during the process and further verifies the conclusions drawn by numerical simulation. Then, an additional nutrient element, namely nitrogen (N) is involved. Both nonlinear analysis and numerical simulation demonstrate the influence of the initial N/P ratio on the nutrient limitation. Three regions of nitrogen limitation, transitional and phosphorus limitation are identified as the ratio of N over P is rising. In the water body having higher ratio, phosphorus becomes a crucial factor and the algal growth is mainly limited by less supply of P. However, the role of N can't be neglected any more as this ratio drops. The fact means that P limitation is gradually replaced to N limitation, which is in accord with what was found by Sakamoto. In summary, we have investigated the effects of ambient water temperature and nutrients supply on algae blooming. In addition, half-saturation constant is also a decisive factor affecting algae blooming and selecting overwhelming species. Usually phosphorus is a decisive nutrient though, the role of nitrogen should be considered when the ratio of N over P drops to a certain amount in this kind of marine ecosystem disaster.

**W-4E-3. A NUMERICAL STUDY OF THE ROLE OF VERTICAL STRUCTURE OF VORTICITY DURING TROPICAL CYCLONE GENESIS**

T. N. VENKATESH, *National Aerospace Laboratories, Bangalore, India*, J. MATHEW, *Indian Institute of Science, Bangalore, India*, Understanding the processes leading to tropical cyclone genesis presents a challenge to fluid dynamicists. Of particular interest is the role of mid-level vorticity during early stages of cyclone genesis. An eight-level axisymmetric model with simple parameterizations for clouds and the atmospheric boundary layer was developed to examine the evolution of vortices that are precursors to tropical cyclones. The effect of vertical distributions of vorticity has been studied. To obtain a reasonable representation of the flow structure and physics, axisymmetry is assumed and hydrostatic and gradient wind balance approximations made. The effects of clouds, radiation, boundary layer and sea-surface are parameterized. The prognostic equations in the interior for the azimuthal velocity and the saturation equivalent potential temperature are solved. A Poisson equation is solved for the secondary flow. Non-linear terms are integrated using the second-order Adams-Bashforth scheme and the diffusion terms treated implicitly. The basic model has been validated with analytical results available for the spin-down of vortices. With the inclusion of the cloud and boundary layer parameterizations, the evolution of deep vortices into hurricanes and the subsequent decay is simulated quite well. The finite amplitude nature, dependence on various parameters, like sea surface temperature, Coriolis parameter, initial vortex strength etc. have been studied and these compare well with other simulations. The novel feature of this study is that the evolution of mid-level vortices has been studied. A new finding is the manner in which mid-level vortices decay and how, on simulated merger of these mid-level vortices, the resulting vortex amplifies to hurricane strength in a realistic time-frame. These results form an important part of the evidence in favour of the authors' model for tropical cyclone genesis.

**W-4E-4. IN WHAT SENSE IS A LOW-REYNOLDS MIXING LAYER STABLE?**

Roddam NARASIMHA, Pinaki BHATTACHARYA, Rama GOVINDARAJAN, *Engineering Mechanics Unit, JNCASR, Bangalore, India*, The Orr-Sommerfeld equation governs the evolution of linear disturbance modes in a strictly parallel flow. For the plane incompressible mixing-layer this equation yields a critical Reynolds number equal to zero [1]. This result has been difficult to understand for a long time, for 'energy' theories indicate that there must be a non-zero Reynolds number (however small), below which viscosity would damp out any disturbance. Recently, we have used a non-parallel analysis to show that the critical Reynolds number  $R_{cr}$  for the mixing-layer is not zero [2]. When expressed with the velocity difference  $D$  and vorticity thickness  $\delta$  as velocity and length scales respectively, it is found that  $R_{cr}$  is about 30. The analysis therein follows the minimal composite theory developed in [3]. We investigate here the physical behaviour of the disturbance kinetic energy in order to gain insight into the character of the stability of the flow. The mean flow in the incompressible mixing-layer we consider possesses a similarity solution. We simulate the flow as it might be observed in a wave-maker experiment. To this end a single disturbance mode, of dimensional frequency  $\omega_d$ , is introduced into the flow at an appropriate station. The local kinetic energy density of the disturbance, averaged over one period, is denoted by  $\langle kd \rangle$ , and fixing the amplitude level of the disturbance to be  $A_0$  at the location

$$\kappa \equiv \frac{\langle kd \rangle}{|A_0|^2 \Delta^2},$$

where it is introduced, we further define  $\bar{\kappa}$  as the non-dimensional disturbance kinetic energy. Two integral quantities are also defined as follows

$$K = \int_{-\infty}^{\infty} \kappa dy, \quad \bar{K} = \int_{-\infty}^{\infty} \kappa d\left(\frac{y_d \Delta}{\nu}\right), \quad \frac{1}{K} \frac{dK}{dx} = \frac{1}{K} \frac{dK}{dx} + \frac{p}{R},$$

where  $p$  is a constant depending on the velocity ratio parameter  $L = D/(2U_{-D})$ . As illustration we show the contours of  $\bar{\kappa}$  in the two extremes of  $L = 49/50$  and nearly shearless flow  $L = 1/39$  is shown in figures 1 and 2. It is apparent that upstream (/downstream) of the streamwise location corresponding to  $R \approx 39$ , there is hardly any streamline in the core of the flow along which energy decays (/grows) in the streamwise direction. Thus the picture is intuitively faithful to the concept of stability (/instability). For the same flows and the same frequency  $\omega_d$  considered above, the variation of the two integrated kinetic energies is shown in figures 3 and 4. We see that  $K$  decays upto  $R \approx 30$  and then amplifies, but at a relatively slow rate. On the other hand amplifies monotonically at all  $R$ . These results show that the integral over  $yd$  grows continuously from very low  $R$ , and hence points towards instability. On the other hand integral  $K$  over the similarity coordinate  $y$  shows stability upto  $R \approx 30$ . It is in this sense that the mixing-layer has a non-zero critical Reynolds number. Thus the maximum disturbance kinetic energy density  $\kappa_{max}$  may drop substantially over a given streamwise extent of the flow (figure 1), but its integral in  $yd$  may increase if the flow is rapidly thickening (see figure 3). Stability thus depends on how the norm is defined.

15:00 ~ 16:20 (Room106)

**Convection and Buoyancy – Driven Flows ( II )**

Session Chair : Prof. K. Mansour, Amirkabir Univ of Tech/Iran

**W-4F-1. OBERBECK CONVECTION IN CHIRAL FLUID THROUGH A VERTICAL CHANNEL IN THE PRESENCE OF TRANSVERSE MAGNETIC FIELD**

NAGARAJU, *Department of Mechanical Engineering, Siddaganga Institute of Technology, Tumkur, India* B. M. RAJPRAKASH, *Department of Mechanical Engineering, University Visveswaraya College of Engineering, Bangalore, India* N. RUDRAIAH, *National Research Institute for Applied Mathematics, Bangalore, India*, Conventionally, fans and regular fluids are used to improve the cooling process in mechanical, electrical and electronic devices but they increase the device weight, size and bulk. These days the industries are changed to find the miniature and portable devices for this purpose. Therefore, there is an urgent need of suitable materials to overcome these thermal problems. At present nano and smart materials are becoming popular for use in such cases. As an alternative to these materials we propose in this paper the use of chiral material. At present solid chiral materials have been used to manufacture devices like antennas, but much attention has not been given to chiral fluids like turpentine, sugarcane solution, body fluids and so on. By definition chiral material is one which cannot be brought into congruence by its mirror image by translation and rotation having the property of either left-handed