

# Generation of Transport Correction Factor through the Comparison of Reactivity Coefficients Calculated by Transport and Diffusion Theory

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## 1. Introduction

The purpose of this research is to generate the transport correction factor to come close to the accuracy of the transport theory by using the result of diffusion theory calculation which mainly used in the core design of liquid metal reactor, KALIMER.

## 2. Methods and Results

The reactivity feedback coefficients that calculated for transport correction factor are as follows; fuel Doppler coefficient, steel Doppler coefficient, sodium density coefficient, steel density coefficient, fuel density coefficient, absorber worth, axial expansion coefficient, and radial expansion coefficient. And the objective cores of this research are the BN-600 reactor core proposed as IAEA CRP benchmark problem, the BFS-73-1 critical experiment in Russia IPPE, KALIMER-150 and KALIMER-600 breakeven cores.

### 2.1 Calculation method

The reactivity feedback coefficients were calculated by using the K-CORE code system based on transport and diffusion theory, on and after they were compared with each other.

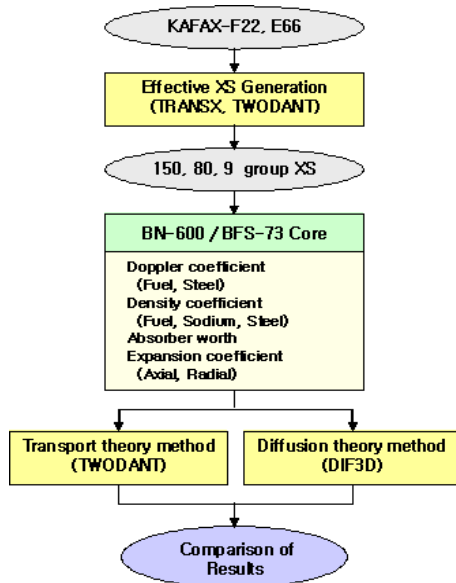


Fig. 1 K-CORE system

K-CORE is a core design and analysis computer code system constructed for KALIMER. Fig. 1 shows the calculation flow and the connection of codes in the K-CORE system.

### 2.2 BN-600 reactor

The calculation results of BN-600 reactor are presented in Table 1. The k-eff and the fuel Doppler coefficients of KAERI show a little bit higher than the other's values.

Table 1 BN-600 reactor calculation result

| Reactivity Coefficients | Participants<br>%Data<br>Energ/Group | KAERI<br>Korea |                  | ANL<br>USA          | CEVSA<br>France   | C/AE<br>China  | IGCAR<br>India | IPPE<br>Russia  | JNC<br>Japan       | ORNL<br>Russia  |
|-------------------------|--------------------------------------|----------------|------------------|---------------------|-------------------|----------------|----------------|-----------------|--------------------|-----------------|
|                         |                                      | JEF-2.2<br>80g | BNDFB-V1<br>150g | BNDFB-V2<br>202/230 | JEF-2.2<br>198/38 | UBVVM<br>46/12 | CAIM<br>26/26  | ABN-98<br>26/18 | JENDL-3.2<br>70/18 | ABN-98<br>26/26 |
| K-EFF                   | Transport                            | 1.0235         | 1.0210           | 1.0279              | 1.0230            | 1.0150         |                | 1.0268          | 1.0056             |                 |
|                         | Diffusion                            | 1.0146         | 1.0182           | 0.9969              | 1.0169            | 0.9961         | 1.0206         | 1.0114          | 1.0082             | 0.9980          |
| Fuel Doppler            | Transport                            | -0.008         | -0.0074          |                     | -0.0067           |                |                | -0.0063         | -0.0052            |                 |
|                         | Diffusion                            | -0.0079        | -0.0076          | -0.0065             | -0.0069           | -0.0050        | -0.0046        | -0.0052         | -0.0054            | -0.0066         |
| Steel Doppler           | Transport                            | -0.0019        | -0.0012          |                     | -0.0015           |                |                | -0.0012         | -0.0011            |                 |
|                         | Diffusion                            | -0.0019        | -0.0012          | -0.0011             | -0.0013           | -0.0005        |                | -0.0012         | -0.0012            | -0.0010         |
| Sodium Density          | Transport                            | 0.0060         | 0.0089           |                     | 0.0084            |                |                | 0.0021          | 0.0040             |                 |
|                         | Diffusion                            | 0.0078         | 0.0106           | 0.0175              | 0.0082            | 0.0021         | 0.0045         | 0.0080          | 0.0077             | 0.0107          |
| Steel Density           | Transport                            | -0.0118        | -0.0149          |                     | -0.0147           |                |                | -0.0088         | -0.0149            |                 |
|                         | Diffusion                            | -0.0099        | -0.0090          | -0.0084             | -0.0112           | -0.0056        | -0.0021        | -0.0053         | -0.0126            | -0.0114         |
| Fuel Density            | Transport                            | 0.3547         | 0.3682           |                     | 0.3682            |                |                | 0.3466          | 0.3481             |                 |
|                         | Diffusion                            | 0.3468         | 0.3683           | 0.3843              | 0.3423            | 0.3482         | 0.3410         | 0.3505          | 0.3481             | 0.3528          |
| Absorber Worth          | Transport                            | -0.0278        | -0.0277          |                     | -0.0263           |                |                | -0.0260         | -0.0270            |                 |
|                         | Diffusion                            | -0.0278        | -0.0282          | -0.0266             | -0.0273           | -0.0281        | -0.0269        | -0.0274         | -0.0265            | -0.0267         |
| Axial Expansion         | Transport                            | -0.1419        | -0.1486          |                     | -0.1378           | -0.1381        |                | -0.1267         | -0.1361            |                 |
|                         | Diffusion                            | -0.1378        | -0.1430          | -0.1227             | -0.1378           | -0.1482        | -0.1395        | -0.1297         | -0.1398            | -0.1415         |
| Radial Expansion        | Transport                            | -0.4882        | -0.4940          |                     | -0.4578           | -0.4603        |                | -0.4787         | -0.4687            |                 |
|                         | Diffusion                            | -0.4801        | -0.4988          | -0.4580             | -0.4650           | -0.4282        | -0.4940        | -0.4668         | -0.4812            | -0.4827         |

### 2.3 BFS-73-1 Critical Experiment

Table 2 shows the calculation result of BFS-73-1 critical experiment. As shown in Table 2, the result of transport calculation agrees well with the diffusion calculation.

Table 2 BFS-73-1 critical experiment calculation result

| Experimental value | TRANSPORT         |                 | DIFFUSION         |          |                  |          |               |
|--------------------|-------------------|-----------------|-------------------|----------|------------------|----------|---------------|
|                    | TWODANT (F-Z/80g) | DIF3D (F-Z/80g) | DIF3D (Hex-Z/80g) |          | DIF3D (Hex-Z/9g) |          |               |
| K-eff = 1.0008     | Value             | Value           | Val. Diff (%)     | Value    | Val. Diff (%)    | Value    | Val. Diff (%) |
| K-eff              | 1.00561           | 1.00065         | 0.49              | 0.99987  | 0.57             | 1.00324  | 0.24          |
| Doppler            | -0.00018          | -0.00019        | -5.83             | -0.00020 | -11.40           | -0.00019 | -5.83         |
| Sodium Density     | 0.02097           | 0.02257         | -7.63             | 0.02278  | -8.63            | 0.02236  | -6.63         |
| Steel Density      | 0.02077           | 0.02283         | -9.92             | 0.02272  | -9.39            | 0.02240  | -7.95         |
| Fuel Density       | 0.36867           | 0.40246         | -8.81             | 0.40178  | -8.63            | 0.39622  | -7.67         |
| Axial Expansion    | -0.44185          | -0.49037        | -1.93             | -0.44978 | -1.79            | -0.44703 | -1.17         |
| Radial Expansion   | -0.88467          | -0.90244        | -1.99             | -0.90146 | -1.87            | -0.89631 | -1.29         |

\*Relative Difference = (Transport - Diffusion) / Transport x 100 (%)

### 2.4 KALIMER-150 Breakeven Core

The calculation results of KALIMER-150 breakeven core are presented in Table 3. As shown in Table 3,

there were a lot of differences between the results of transport calculation and diffusion calculation.

Table 3 KALIMER-150 calculation result

|                  | TRANSPORT         |          | DIFFUSION       |          |                   |
|------------------|-------------------|----------|-----------------|----------|-------------------|
|                  | TWODANT (R-Z/80g) |          | DIF3D (R-Z/80g) |          | DIF3D (Hex-Z/80g) |
|                  | Value             | Value    | Rel. Diff (%)   | Value    | Rel. Diff (%)     |
| Fuel Doppler     | -0.00236          | -0.00265 | -12.29          | -0.00265 | -12.29            |
| Steel Doppler    | -0.00058          | -0.00059 | -1.72           | -0.00062 | -6.90             |
| Fuel Density     | 0.42380           | 0.41931  | 1.06            | 0.42671  | -0.69             |
| Sodium Density   | -0.00520          | 0.00040  | 107.69          | 0.0001   | 101.92            |
| Steel Density    | -0.02211          | -0.01390 | 37.13           | -0.0141  | 36.23             |
| Absorber Density | 0.14408           | -0.00170 | 101.18          | -0.0014  | 100.97            |
| Axial Expansion  | -0.25640          | -0.25570 | 0.27            | -0.2612  | -1.87             |
| Radial Expansion | -0.56210          | -0.57310 | -1.96           | -0.5672  | -0.91             |

\* Relative Difference = (Transport - Diffusion) / Transport x 100 (%)

## 2.5 KALIMER-600 Breakeven Core

Table 4 shows the calculation result of KALIMER-600 breakeven core. As shown in Table 4, we can see the good agreement between the result of transport calculation and diffusion calculation.

Table 4 KALIMER-600 calculation result

|                  | TRANSPORT         |          | DIFFUSION       |          |                   |
|------------------|-------------------|----------|-----------------|----------|-------------------|
|                  | TWODANT (R-Z/80g) |          | DIF3D (R-Z/80g) |          | DIF3D (Hex-Z/80g) |
|                  | Value             | Value    | Rel. Diff (%)   | Value    | Rel. Diff (%)     |
| Fuel Doppler     | -0.00272          | -0.00270 | 0.72            | -0.00274 | -0.63             |
| Steel Doppler    | -0.00112          | -0.00108 | 3.90            | -0.00111 | 1.15              |
| Fuel Density     | 0.38338           | 0.38190  | 0.39            | 0.382508 | 0.23              |
| Sodium Density   | -0.03153          | -0.03151 | 0.08            | -0.02983 | 5.39              |
| Steel Density    | -0.07004          | -0.07263 | -3.69           | -0.07018 | -0.19             |
| Absorber Density | -0.02839          | -0.02830 | 0.31            | -0.02733 | 3.73              |
| Axial Expansion  | -0.12199          | -0.12000 | 1.63            | -0.12553 | -2.90             |
| Radial Expansion | -0.48026          | -0.48229 | -0.42           | -0.48212 | -0.39             |

\* Relative Difference = (Transport - Diffusion) / Transport x 100 (%)

## 2.5 Transport Correction Factors

According to the differences between the results of transport and diffusion calculation, the transport correction factors are produced based on those results. Table 5 shows the transport correction factors in the average sense.

Table 5 Transport correction factors

|                  | JEF-2.2 |         | ENDF/B-VI |         |
|------------------|---------|---------|-----------|---------|
|                  |         | SD ±    |           | SD ±    |
| Fuel Doppler     | 1.02792 | 0.00303 | 0.98024   | 0.00231 |
| Steel Doppler    | 1.02400 | 0.00041 | 0.95082   | 0.00042 |
| Sodium Density   | 0.63918 | 0.00560 | 0.37311   | 0.00588 |
| Steel Density    | 1.20408 | 0.01297 | 1.86250   | 0.01371 |
| Fuel Density     | 1.01692 | 0.01643 | 0.99973   | 0.03220 |
| Absorber Worth   | 1.01832 | 0.00515 | 1.09921   | 0.00615 |
| Axial Expansion  | 1.02975 | 0.01177 | 1.02517   | 0.01748 |
| Radial Expansion | 1.01062 | 0.03916 | 0.99838   | 0.05344 |

## 3. Conclusion

In this work, the transport correction factor to come close to the accuracy of the transport theory was studied. According to the differences between the transport and diffusion calculation results, the values of the K-CORE code system show higher trends than those of other country participants and the measurement results. Through the update of nuclear data libraries and the comparison analysis of more numbers of experiments meaningful in statistical analysis, more accurate verification and improvement will be carried out. The result of this study will be utilized as the basic data for the development of reactivity coefficients analysis

system, and will improve the credit of reactivity coefficients calculation in conceptual core design.

But as we can see in Table 3 and Table 4, the calculation results by the diffusion and transport theory are different by the core size, loading pattern and composition etc. Thus we conclude that it is better to generate the transport correction factor according to the each core in the detailed design stage.

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