



load characteristics for calculating the loss of load expectation. An hourly peak load variation model is used where its hourly peak load represents each hour.

$$LOLE_i = P_i(C_i < L_i) \quad (2)$$

Where

$C_i$  = available capacity on hour  $i$

$L_i$  = forecast peak load on hour  $i$

$P_i(C_i < L_i)$  = probability of loss of load on hour  $i$

$$LOLE = \sum_{k=1}^{nhs} LOLE_k \quad (3)$$

Where

LOLE = loss of load expectation for the period under study. The value of LOLE is in hours.

nhs = total number of hours under study

### 2.3 Loss of Load Expectation evaluation of Wind Energy Embedded Electric Power System

For reliability evaluation, the overall system is divided into two subsystems, containing the conventional and wind units respectively, and a generation system model is built using a Recursive Algorithm for each of these two subsystems. Each of the generation system models is described by two  $m$ -dimensional vectors as follows:

$C_i$  =  $i^{\text{th}}$  element of the Capacity vector  $C$

= one of the possible discrete capacity states

$P_i$  =  $i^{\text{th}}$  element of Probability vector  $P$

=  $P(C \geq C_i)$

= probability of capacity on outage being equal to or greater than  $C_i$

$m$  = number of generation states

These two generation system capacity models are represented by:

CC = capacity vector of conventional subsystem

PC = probability vector of conventional subsystem

CWIND = capacity vector of wind subsystem

PWIND = probability vector of wind subsystem

Now, for each hour under study, the power output of the wind subsystem is calculated and a vector containing the hourly outputs of the wind unit subsystem is created as:

POWIND $_k$  = power output of the wind system during the  $k^{\text{th}}$  hour of the period under study

Wind generation subsystem capacity model is modified to account for the effect of the fluctuating energy by creating an  $m$ -dimensional vector MWIND $_k$  such that:

$$MWIND_{k,i} = \frac{CWIND_i \cdot POWIND_k}{PRWIND} \quad (4)$$

where

MWIND $_{k,i}$  =  $i^{\text{th}}$  element of MWIND $_k$

CWIND $_i$  =  $i^{\text{th}}$  element of CWIND

PRWIND = rated power of wind subsystem

Each subsystem is treated as multi-state unit and these subsystems are combined to calculate the LOLE for the hour in question. The combination of these multi-state units results in states with capacities given by the equation:

$$C_{ij} = CC_i + CWIND_j \quad (5)$$

Where  $i$  and  $j$  refer to the states in the first and second subsystems respectively and  $C_{ij}$  represent an element in two-dimensional array  $C$  that constitutes all possible capacity states of the combined system. A Discrete State Algorithm is used for evaluating the LOLE of the system for the hour under study, which is as follows:

① Initialize by setting

$$LOLE_k = 0.0$$

where

LOLE $_k$  = loss of load expectation for  $k$  hour of study

②  $j = 1$

$$③ CT = CC_{nc} + CWIND_{nwind} \quad (6)$$

where

CT = total capacity

nc = number of states in conventional subsystem

nwind = number of states in wind subsystem

CC $_{nc}$  = total capacity in conventional subsystem

CWIND $_{nwind}$  = total capacity in wind subsystem

④  $i = 1$

$$⑤ C_y = CC_i + CWIND_j \quad (7)$$

If  $C_{ij}$  is equal to or more than (CT-load) for the hour, go to (8).

⑥  $i = i + 1$

If  $i$  is less than nc, go to (5).

⑦ If  $i$  is more than nc, go to (10)

⑧  $b = i$

where

$b$  = boundary state defining the loss of load.

$$⑨ LOLE_k = LOLE_k + PC_b (PWIND_j - PWIND_{j+1}) \quad (8)$$

⑩  $j = j + 1$

If  $j$  is less than or equal to nwind, go to (4).

The reliability index for the entire period is computed by the summation of all hourly values of LOLE.

### 3. ECONOMIC ANALYSIS OF WIND ENERGY EMBEDDED ELECTRIC POWER SYSTEM

The total energy generated by the wind units in entire period under study (nhs hours) is calculated by using the hourly modified wind generation capacity. Then the conventional fuel saving, achieved by replacing the conventional fuel units with wind power generation units, is assessed by using a formula:

$$\text{Quantity of Fuel saved} = \frac{1}{LCV} \sum_{i=1}^{nhs} \frac{3600000XY_i}{\eta} \text{ Kg} \quad (9)$$

$$\text{Cost of Fuel saved} = \frac{CF}{LCV} \sum_{i=1}^{nhs} \frac{3600000XY_i}{\eta} \text{ Won} \quad (10)$$

Where

X=power in MW which is replaced by wind units  
 $\eta$  = efficiency of conventional generation unit  
 $Y_i$ =percentage of full rated capacity that is generated by wind unit for a particular hour  
 LCV=lower calorific value of fuel used at the input of conventional unit: KJ/Kg  
 CF=cost of fuel used: Won/Kg

#### 4. SIMULATION RESULTS

The reliability and economic analysis methodology have been applied on a sample test system with a total capacity of 176 MW shown in table 1. The simulation study was done using the load characteristics of one province in India. The 12 MW conventional units were replaced one after one with wind units, which is represented as the penetration level of the wind power in the overall electric generation system. The details about the wind units are given in Appendix 1 [2]. For different penetration levels of the wind sources: reliability indices, energy generated and fuel & money saved by embedding the wind units have been simulated for four different months of the year. The results obtained are presented in table 2.

Table 1: Data for the test system used for simulation study

Unit capacity [MW]	No. of Unit	Total Capacity [MW]	Forced outage rate [FOR]
50	2	100	0.05
20	2	40	0.08
12	3	36	0.08

Table 2: LOLE, energy generated and fuel saved for four different months of a year

Penetration level[%]	March	June	September	December
LOLE(hours)				
6.8	68.70	10.87	17.34	65.92
13.6	80.54	12.24	30.81	79.21
20.5	94.61	21.94	59.02	107.13
Energy generated(KJ $\times 10^9$ )				
6.8	6.71	14.8	7.76	3.48
13.6	13.4	29.5	15.5	6.97
20.5	20.1	44.3	23.3	10.5
Fuel quantity saved (10 <sup>3</sup> Kg)				
6.8	629	1384	726.7	326.4
13.6	1258	2768	1453	652.7
20.5	1887	5142	2180	979.1
Money saved (Million Won)				
6.8	62.1	135	70.2	32.4
13.6	121.5	270	140.4	62.1
20.5	183.6	405	210.6	94.5

#### 5. CONCLUSIONS

A methodology for reliability evaluation for wind energy embedded electric power system has been presented in this paper. The probabilistic

capacity generation model of wind energy system is modified hourly to incorporate the fluctuating nature of the wind energy system and then the system reliability, which is represented as loss of load expectation (LOLE), is evaluated using the discrete state algorithm. Finally the energy generated by the wind energy system is calculated and the conventional fuel saving is assessed as an indication of economic saving in system operation due to the use of wind energy system. This methodology has been applied on an Indian test system and results obtained are presented for four different months of the year.

#### 6. ACKNOWLEDGEMENTS

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#### APPENDIX I

Wind turbine system units of 500 KW capacity with FOR = 0.03 were used in this paper and power output of these units was calculated using the following equations:

$$POW = \begin{cases} 0.0 & 0 < V < V_{ci} \\ A + BV + CV^2 & V_{ci} < V < V_r \\ PRW & V_r < V < V_{co} \\ 0.0 & V > V_{co} \end{cases} \quad (11)$$

$$A = \frac{1}{(V_{ci} - V_r)^2} \left[ V_{ci}(V_{ci} + V_r) - 4(V_{ci}V_r) \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 \right] \quad (12)$$

$$B = \frac{1}{(V_{ci} - V_r)^2} \left[ 4(V_{ci} + V_r) \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 - 3(V_{ci} + V_r) \right] \quad (13)$$

$$C = \frac{1}{(V_{ci} - V_r)^2} \left[ 2 - 4 \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 \right] \quad (14)$$

where

V = wind velocity for the hour in question

PRW = rated power of the unit

$V_{ci}$  = Cut-in velocity

$V_r$  = Rated velocity

$V_{co}$  = Cut-off velocity